Les 01

homework assignments

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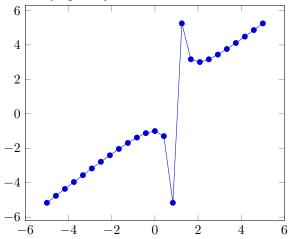
Artificial intelligence, Universiteit van Amsterdam, the Netherlands

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1 2.3.19

A function y = f(x) with a vertical asymptote at x = 1 and a slanting asymptote y = x + 1 when $x \to \pm \infty$.



$$f(x) = x + \frac{1}{x - 1} \tag{1}$$

$2 \quad 2.3.21$

$$\lim_{x \to \infty} \frac{x^2}{x - 1} - x \Rightarrow \lim_{x \to \infty} \frac{x}{x - 1} = 1 \tag{2}$$

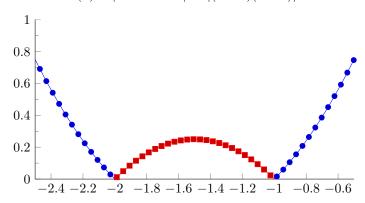
3 2.3.23

$$\lim_{x \to \infty} x \ln(1 + \frac{1}{x}) \Leftrightarrow \lim_{x \to \infty} \ln((1 + \frac{1}{x})^x) = 1$$
 (3)

 $\lim_{x\to\infty}(1+\frac{1}{x})^x$ gives us the Euler constant e. And $\log_a(a)=1.$

4 5.8.13

$$h(x) = |x^2 + 3x + 2| \Leftrightarrow |(1+x)(x+2)| \tag{4}$$



We find the points -2 and -1 to be **non-differentiable**.

5 5.8.15

Using the derivatives table, $f(x) = \sin(x^2)$ gives us $f(x)' = 2x\cos(x^2)$, from which we get to $f(x)'' = 2\cos(x^2) - 4x^2\sin(x^2)$.