Lecture 10

Data Aggregations on Multi-Indices ¶

We've previously seen that Pandas has built-in data aggregation methods, such as mean(), sum(), and max(). For hierarchically indexed data, these can be passed a level parameter that controls which subset of the data the aggregate is computed on.

For example, let's return to our health data:

In [58]:

health_data

Out[58]:

	subject	Bob		Guid	0	Sue	
	type	HR	Temp	HR	Temp	HR	Temp
year	visit						
2013	1	43.0	36.7	54.0	37.3	27.0	37.0
	2	26.0	37.6	46.0	35.0	22.0	36.7
2014	1	27.0	37.9	24.0	38.1	52.0	38.3
	2	42.0	35.5	43.0	35.9	45.0	37.9

Perhaps we'd like to average-out the measurements in the two visits each year. We can do this by naming the index level we'd like to explore, in this case the year:

In [59]:

```
data_mean = health_data.mean(level='year')
data_mean
```

Out[59]:

subject	Bob		Guide	o	Sue	
type	HR	Temp	HR	Temp	HR	Temp
year						
2013	34.5	37.15	50.0	36.15	24.5	36.85
2014	34.5	36.70	33.5	37.00	48.5	38.10

By further making use of the axis keyword, we can take the mean among levels on the columns as well:

In [61]:

```
data_mean.mean(axis=1, level='type')
```

Out[61]:

```
        type
        HR
        Temp

        year
        36.333333
        36.716667

        2014
        38.833333
        37.266667
```

In [62]:

```
# without levet it makes no sence
data_mean.mean(axis=1)
```

Out[62]:

year

2013 36.525 2014 38.050 dtype: float64

Thus in two lines, we've been able to find the average heart rate and temperature measured among all subjects in all visits each year.

Combining Datasets: Concat and Append

Some of the most interesting studies of data come from combining different data sources. These operations can involve anything from very straightforward concatenation of two different datasets, to more complicated database-style joins and merges that correctly handle any overlaps between the datasets. Series and DataFrame s are built with this type of operation in mind, and Pandas includes functions and methods that make this sort of data wrangling fast and straightforward.

Here we'll take a look at simple concatenation of Series and DataFrame s with the pd.concat function; later we'll dive into more sophisticated in-memory merges and joins implemented in Pandas.

For convenience, we'll define this function which creates a DataFrame of a particular form that will be useful below:

```
In [68]:
```

Out[68]:

```
        A
        B
        C

        0
        A0
        B0
        C0

        1
        A1
        B1
        C1

        2
        A2
        B2
        C2
```

In addition, we'll create a quick class that allows us to display multiple DataFrame s side by side. The code makes use of the special _repr_html_ method, which IPython uses to implement its rich object display:

```
In [69]:
```

```
eval("2 + 3 * len('hello')")
Out[69]:
17
```

In [168]:

The use of this will become clearer as we continue our discussion in the following section.

Recall: Concatenation of NumPy Arrays

Concatenation of Series and DataFrame objects is very similar to concatenation of Numpy arrays, which can be done via the np.concatenate function:

In [71]:

```
x = [1, 2, 3]
y = [4, 5, 6]
z = [7, 8, 9]
np.concatenate([x, y, z])
```

Out[71]:

```
array([1, 2, 3, 4, 5, 6, 7, 8, 9])
```

The first argument is a list or tuple of arrays to concatenate. Additionally, it takes an axis keyword that allows you to specify the axis along which the result will be concatenated:

```
In [72]:
```

```
x = [[1, 2],
      [3, 4]]
np.concatenate([x, x], axis=1)
```

```
Out[72]:
```

```
array([[1, 2, 1, 2], [3, 4, 3, 4]])
```

Simple Concatenation with pd.concat

Pandas has a function, pd.concat(), which has a similar syntax to np.concatenate but contains a number of options that we'll discuss momentarily:

pd.concat() can be used for a simple concatenation of Series or DataFrame objects, just as np.concatenate() can be used for simple concatenations of arrays:

```
In [75]:
```

```
ser1 = pd.Series(['A', 'B', 'C'], index=[1, 2, 3])
ser2 = pd.Series(['D', 'E', 'F'], index=[4, 5, 6])
pd.concat([ser1, ser2])
```

Out[75]:

1 A
2 B
3 C
4 D
5 E
6 F

dtype: object

It also works to concatenate higher-dimensional objects, such as DataFrame s:

In [169]:

```
df1 = make_df('AB', [1, 2])
df2 = make_df('AB', [3, 4])
display('df1', 'df2', 'pd.concat([df1, df2])')
```

Out[169]:

df1 df2 pd.concat([df1, df2]) Α В Α В Α В **1** A1 B1 **3** A3 B3 **1** A1 B1 **2** A2 B2 4 A4 B4 2 A2 B2 **3** A3 B3 4 A4 B4

By default, the concatenation takes place row-wise within the DataFrame (i.e., axis=0). Like np.concatenate, pd.concat allows specification of an axis along which concatenation will take place. Consider the following example:

In [95]:

```
df3 = make_df('AB', [0, 1])
df4 = make_df('CD', [0, 1])
display('df3', 'df4', "pd.concat([df3, df4], axis='columns')")
```

Out[95]:

df3 df4 pd.concat([df3, df4], axis='columns')

	Α	В		С	D	_		Α	В	С	D
0	Α0	В0	0	C0	D0		0	Α0	В0	C0	D0
1	A1	B1	1	C1	D1		1	A1	В1	C1	D1

We could have equivalently specified axis=1; here we've used the more intuitive axis='columns.

Duplicate indices

One important difference between np.concatenate and pd.concat is that Pandas concatenation *preserves indices*, even if the result will have duplicate indices! Consider this simple example:

In [96]:

```
x = make_df('AB', [0, 1])
y = make_df('AB', [2, 3])
y.index = x.index # make duplicate indices!
display('x', 'y', 'pd.concat([x, y])')
```

Out[96]:

Notice the repeated indices in the result. While this is valid within DataFrame s, the outcome is often undesirable. pd.concat() gives us a few ways to handle it.

Catching the repeats as an error

If you'd like to simply verify that the indices in the result of pd.concat() do not overlap, you can specify the verify_integrity flag. With this set to True, the concatenation will raise an exception if there are duplicate indices. Here is an example, where for clarity we'll catch and print the error message:

In [97]:

```
try:
    pd.concat([x, y], verify_integrity=True)
except ValueError as e:
    print("ValueError:", e)
```

ValueError: Indexes have overlapping values: Int64Index([0, 1], dtype='int 64')

Ignoring the index

Sometimes the index itself does not matter, and you would prefer it to simply be ignored. This option can be specified using the <code>ignore_index</code> flag. With this set to true, the concatenation will create a new integer index for the resulting <code>Series</code>:

In [98]:

```
display('x', 'y', 'pd.concat([x, y], ignore_index=True)')
```

Out[98]:

Adding MultiIndex keys

Another option is to use the keys option to specify a label for the data sources; the result will be a hierarchically indexed series containing the data:

In [99]:

```
display('x', 'y', "pd.concat([x, y], keys=['x', 'y'])")
```

Out[99]:

The result is a multiply indexed DataFrame

Concatenation with joins

In the simple examples we just looked at, we were mainly concatenating <code>DataFrame</code> s with shared column names. In practice, data from different sources might have different sets of column names, and <code>pd.concat</code> offers several options in this case. Consider the concatenation of the following two <code>DataFrame</code> s, which have some (but not all!) columns in common:

In [100]:

```
df5 = make_df('ABC', [1, 2])
df6 = make_df('BCD', [3, 4])
display('df5', 'df6', 'pd.concat([df5, df6])')
```

Out[100]:

df5 df6 pd.concat([df5, df6]) С С C В D Α В D Α В **1** A1 B1 C1 **3** B3 C3 Α1 B1 C1 NaN D3 1 2 A2 B2 C2 A2 B2 C2 NaN **4** B4 C4 D4 2 B3 C3 D3 3 NaN 4 NaN B4 C4 D4

By default, the entries for which no data is available are filled with NA values. To change this, we can specify one of several options for the join parameters of the concatenate function. By default, the join is a union of the input columns (join='outer'), but we can change this to an intersection of the columns using join='inner':

In [101]:

Out[101]:

df5 df6 pd.concat([df5, df6], join='inner') Α В С В С D В С **1** A1 B1 C1 **3** B3 C3 D3 **1** B1 C1 2 A2 B2 C2 C4 **4** B4 D4 2 B2 C2 **3** B3 C3 4 B4 C4

The append() method

Because direct array concatenation is so common, Series and DataFrame objects have an append method that can accomplish the same thing in fewer keystrokes. For example, rather than calling pd.concat([df1, df2]), you can simply call df1.append(df2):

```
display('df1', 'df2', 'df1.append(df2)')
```

Out[103]:

Keep in mind that unlike the append() and extend() methods of Python lists, the append() method in Pandas does not modify the original object—instead it creates a new object with the combined data. It also is not a very efficient method, because it involves creation of a new index and data buffer. Thus, if you plan to do multiple append operations, it is generally better to build a list of DataFrame's and pass them all at once to the concat() function.

In the next section, we'll look at another more powerful approach to combining data from multiple sources, the database-style merges/joins implemented in <code>pd.merge</code>.

Combining Datasets: Merge and Join

One essential feature offered by Pandas is its high-performance, in-memory join and merge operations. If you have ever worked with databases, you should be familiar with this type of data interaction. The main interface for this is the pd.merge function, and we'll see few examples of how this can work in practice.

For convenience, we will start by redefining the display() functionality from the previous section:

Relational Algebra

The behavior implemented in pd.merge() is a subset of what is known as *relational algebra*, which is a formal set of rules for manipulating relational data, and forms the conceptual foundation of operations available in most databases. The strength of the relational algebra approach is that it proposes several primitive operations, which become the building blocks of more complicated operations on any dataset. With this lexicon of fundamental operations implemented efficiently in a database or other program, a wide range of fairly complicated composite operations can be performed.

Pandas implements several of these fundamental building-blocks in the pd.merge() function and the related join() method of Series and Dataframe s. As we will see, these let you efficiently link data from different sources.

Categories of Joins

The pd.merge() function implements a number of types of joins: the *one-to-one*, *many-to-one*, and *many-to-many* joins. All three types of joins are accessed via an identical call to the pd.merge() interface; the type of join performed depends on the form of the input data. Here we will show simple examples of the three types of merges, and discuss detailed options further below.

One-to-one joins

Perhaps the simplest type of merge expresion is the one-to-one join, which is in many ways very similar to the column-wise concatenation. As a concrete example, consider the following two DataFrames which contain information on several employees in a company:

In [104]:

Out[104]:

df1 df2

	employee	group			employee	hire_date
() Bob	Accounting		0	Lisa	2004
1	I Jake	Engineering		1	Bob	2008
2	2 Lisa	Engineering	:	2	Jake	2012
3	Sue	HR	;	3	Sue	2014

To combine this information into a single <code>DataFrame</code> , we can use the <code>pd.merge()</code> function:

In [105]:

```
df3 = pd.merge(df1, df2)
df3
```

Out[105]:

	employee	group	hire_date
0	Bob	Accounting	2008
1	Jake	Engineering	2012
2	Lisa	Engineering	2004
3	Sue	HR	2014

The pd.merge() function recognizes that each DataFrame has an "employee" column, and automatically joins using this column as a key. The result of the merge is a new DataFrame that combines the information from the two inputs. Notice that the order of entries in each column is not necessarily maintained: in this case, the order of the "employee" column differs between df1 and df2, and the pd.merge() function correctly accounts for this. Additionally, keep in mind that the merge in general discards the index, except in the special case of merges by index (see the left_index and right_index keywords).

Many-to-one joins

Many-to-one joins are joins in which one of the two key columns contains duplicate entries. For the many-to-one case, the resulting <code>DataFrame</code> will preserve those duplicate entries as appropriate. Consider the following example of a many-to-one join:

In [108]:

Out[108]:

df3 df4

	employee	group	hire_date
0	Bob	Accounting	2008
1	Jake	Engineering	2012
2	Lisa	Engineering	2004
3	Sue	HR	2014

	group	supervisor
0	Accounting	Carly
1	Engineering	Guido
2	HR	Steve

pd.merge(df3, df4)

	employee	group	hire_date	supervisor
0	Bob	Accounting	2008	Carly
1	Jake	Engineering	2012	Guido
2	Lisa	Engineering	2004	Guido
3	Sue	HR	2014	Steve

The resulting DataFrame has an aditional column with the "supervisor" information, where the information is repeated in one or more locations as required by the inputs.

Many-to-many joins

Many-to-many joins are a bit confusing conceptually, but are nevertheless well defined. If the key column in both the left and right array contains duplicates, then the result is a many-to-many merge. This will be perhaps most clear with a concrete example. Consider the following, where we have a <code>DataFrame</code> showing one or more skills associated with a particular group. By performing a many-to-many join, we can recover the skills associated with any individual person:

In [110]:

Out[110]:

df1 df5

skills	group		group	employee	
math	Accounting	0	Accounting	Bob	0
spreadsheets	Accounting	1	Engineering	Jake	1
coding	Engineering	2	Engineering	Lisa	2
linux	Engineering	3	HR	Sue	3
spreadsheets	HR	4			
organization	HR	5			

pd.merge(df1, df5)

	employee	group	skills
0	Bob	Accounting	math
1	Bob	Accounting	spreadsheets
2	Jake	Engineering	coding
3	Jake	Engineering	linux
4	Lisa	Engineering	coding
5	Lisa	Engineering	linux
6	Sue	HR	spreadsheets
7	Sue	HR	organization

These three types of joins can be used with other Pandas tools to implement a wide array of functionality. But in practice, datasets are rarely as clean as the one we're working with here. In the following section we'll consider some of the options provided by pd.merge() that enable you to tune how the join operations work.

Specification of the Merge Key

We've already seen the default behavior of pd.merge(): it looks for one or more matching column names between the two inputs, and uses this as the key. However, often the column names will not match so nicely, and pd.merge() provides a variety of options for handling this.

The on keyword

Most simply, you can explicitly specify the name of the key column using the on keyword, which takes a column name or a list of column names:

In [111]:

```
display('df1', 'df2', "pd.merge(df1, df2, on='employee')")
```

2014

Out[111]:

0

1

2

3

Sue

df1

employee hire_date employee group 2004 Bob Accounting 0 Lisa 2008 Jake Engineering 1 Bob Lisa Engineering 2 Jake 2012

df2

3

Sue

pd.merge(df1, df2, on='employee')

HR

	employee	group	hire_date
0	Bob	Accounting	2008
1	Jake	Engineering	2012
2	Lisa	Engineering	2004
3	Sue	HR	2014

This option works only if both the left and right DataFrame s have the specified column name.

The left_on and right_on keywords

At times you may wish to merge two datasets with different column names; for example, we may have a dataset in which the employee name is labeled as "name" rather than "employee". In this case, we can use the left_on and right_on keywords to specify the two column names:

In [114]:

Out[114]:

df1 df3

	employee	group		name	salary
0	Bob	Accounting	0	Bob	70000
1	Jake	Engineering	1	Jake	80000
2	Lisa	Engineering	2	Lisa	120000
3	Sue	HR	3	Sue	90000

pd.merge(df1, df3, left_on="employee", right_on="name")

	employee	group	name	salary
0	Bob	Accounting	Bob	70000
1	Jake	Engineering	Jake	80000
2	Lisa	Engineering	Lisa	120000
3	Sue	HR	Sue	90000

The result has a redundant column that we can drop if desired—for example, by using the <code>drop()</code> method of <code>DataFrame s</code>:

In [115]:

```
pd.merge(df1, df3, left_on="employee", right_on="name").drop('name', axis=1)
```

Out[115]:

	employee	group	salary
0	Bob	Accounting	70000
1	Jake	Engineering	80000
2	Lisa	Engineering	120000
3	Sue	HR	90000

The left_index and right_index keywords

Sometimes, rather than merging on a column, you would instead like to merge on an index. For example, your data might look like this:

In [116]:

```
df1a = df1.set_index('employee')
df2a = df2.set_index('employee')
display('df1a', 'df2a')
```

Out[116]:

df1a df2a

	group		hire_date
employee		employee	
Bob	Accounting	Lisa	2004
Jake	Engineering	Bob	2008
Lisa	Engineering	Jake	2012
Sue	HR	Sue	2014

You can use the index as the key for merging by specifying the left_index and/or right_index flags in pd.merge():

In [119]:

Out[119]:

df1a df2a

	group		hire_date
employee		employee	
Bob	Accounting	Lisa	2004
Jake	Engineering	Bob	2008
Lisa	Engineering	Jake	2012
Sue	HR	Sue	2014

pd.merge(df1a, df2a, left_index=True, right_index=True)

	group	hire_date		
employee				
Bob	Accounting	2008		
Jake	Engineering	2012		
Lisa	Engineering	2004		
Sue	HR	2014		

For convenience, DataFrame s implement the join() method, which performs a merge that defaults to joining on indices:

In [120]:

```
display('df1a', 'df2a', 'df1a.join(df2a)')
```

Out[120]:

dfla df2a df1a.join(df2a)

	group		hire_date	group	hire_date	
employee		employee		employee		
Bob	Accounting	Lisa	2004	Bob	Accounting	2008
Jake	Engineering	Bob	2008	Jake	Engineering	2012
Lisa	Engineering	Jake	2012	Lisa	Engineering	2004
Sue	HR	Sue	2014	Sue	HR	2014

If you'd like to mix indices and columns, you can combine left_index with right_on or left_on with right_index to get the desired behavior:

In [121]:

```
display('df1a', 'df3', "pd.merge(df1a, df3, left_index=True, right_on='name')")
```

Out[121]:

dfla df3

	group		name	salary
employee		0	Bob	70000
Bob	Accounting	1	Jake	80000
Jake	Engineering	2	Lisa	120000
Lisa	Engineering	3	Sue	90000
Sue	HR			

pd.merge(df1a, df3, left_index=True, right_on='name')

	group	name	salary
0	Accounting	Bob	70000
1	Engineering	Jake	80000
2	Engineering	Lisa	120000
3	HR	Sue	90000

All of these options also work with multiple indices and/or multiple columns; the interface for this behavior is very intuitive. For more information on this, see the "Merge, Join, and Concatenate" section (http://pandas.pydata.org/pandas-docs/stable/merging.html) of the Pandas documentation.

Specifying Set Arithmetic for Joins

In all the preceding examples we have glossed over one important consideration in performing a join: the type of set arithmetic used in the join. This comes up when a value appears in one key column but not the other. Consider this example:

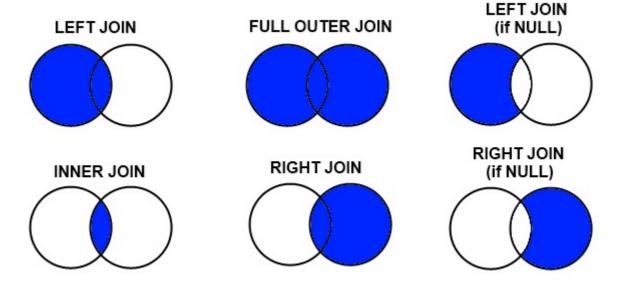
In [122]:

wine

Out[122]:

						_			
0	Peter	fish	0	Mary	wine	·-	0	Mary	bread
1	Paul	beans	1	Joseph	beer				

2 Mary bread



Here we have merged two datasets that have only a single "name" entry in common: Mary. By default, the result contains the *intersection* of the two sets of inputs; this is what is known as an *inner join*. We can specify this explicitly using the how keyword, which defaults to "inner":

In [123]:

```
pd.merge(df6, df7, how='inner')
```

Out[123]:

```
name food drink

Mary bread wine
```

Other options for the how keyword are 'outer', 'left', and 'right'. An *outer join* returns a join over the union of the input columns, and fills in all missing values with NAs:

In [124]:

```
display('df6', 'df7', "pd.merge(df6, df7, how='outer')")
```

Out[124]:

df6 df7 pd.merge(df6, df7, how='outer') food name drink name food drink name **0** Peter fish Peter NaN Mary wine fish Paul beans NaN 1 Joseph 1 Paul beans beer 2 2 Mary bread Mary bread wine 3 Joseph NaN beer

The *left join* and *right join* return joins over the left entries and right entries, respectively. For example:

In [125]:

df6

```
display('df6', 'df7', "pd.merge(df6, df7, how='left')")
Out[125]:
```

pd.merge(df6, df7, how='left')

	name	food			name	drink			name	food	drink
0	Peter	fish	_	0	Mary	wine	-'	0	Peter	fish	NaN
1	Paul	beans		1	Joseph	beer		1	Paul	beans	NaN
2	Mary	bread						2	Mary	bread	wine

df7

The output rows now correspond to the entries in the left input. Using how='right' works in a similar manner.

All of these options can be applied straightforwardly to any of the preceding join types.

In [126]:

```
display('df6', 'df7', "pd.merge(df6, df7, how='right')")
```

Out[126]:

2 Mary bread

df6 df7					pd	.merge	how='right')			
	name	food		name	drink		name	food	drink	
0	Peter	fish	0	Mary	wine	0	Mary	bread	wine	-
1	Paul	beans	1	Joseph	beer	1	Joseph	NaN	beer	

Overlapping Column Names: The suffixes Keyword

Finally, you may end up in a case where your two input DataFrame s have conflicting column names. Consider this example:

In [127]:

Out[127]:

df8 df9 pd.merge(df8, df9, on="name")

	name	rank		name	rank			name	rank_x	rank_y
0	Bob	1	0	Bob	3	-	0	Bob	1	3
1	Jake	2	1	Jake	1		1	Jake	2	1
2	Lisa	3	2	Lisa	4		2	Lisa	3	4
3	Sue	4	3	Sue	2		3	Sue	4	2

Because the output would have two conflicting column names, the merge function automatically appends a suffix _x or _y to make the output columns unique. If these defaults are inappropriate, it is possible to specify a custom suffix using the suffixes keyword:

In [128]:

```
display('df8', 'df9', 'pd.merge(df8, df9, on="name", suffixes=["_L", "_R"])')
```

Out[128]:

df8 df9

	name	rank		name	rank
0	Bob	1	0	Bob	3
1	Jake	2	1	Jake	1
2	Lisa	3	2	Lisa	4
3	Sue	4	3	Sue	2

pd.merge(df8, df9, on="name", suffixes=[" L", " R"])

	name	rank_L	rank_R
0	Bob	1	3
1	Jake	2	1
2	Lisa	3	4
3	Sue	4	2

These suffixes work in any of the possible join patterns, and work also if there are multiple overlapping columns.

Also see the <u>Pandas "Merge, Join and Concatenate" documentation (http://pandas.pydata.org/pandas-docs/stable/merging.html</u>) for further discussion of these topics.

Example: US States Data

Merge and join operations come up most often when combining data from different sources. Here we will consider an example of some data about US states and their populations.

In []:

```
# Following are shell commands to download the data
# !curl -0 https://raw.githubusercontent.com/jakevdp/data-USstates/master/state-populat
ion.csv
# !curl -0 https://raw.githubusercontent.com/jakevdp/data-USstates/master/state-areas.c
sv
# !curl -0 https://raw.githubusercontent.com/jakevdp/data-USstates/master/state-abbrev
s.csv
```

Let's take a look at the three datasets, using the Pandas read_csv() function:

In [129]:

```
pop = pd.read_csv('D:\Cвeтa\Фреймворки пайтон\Лекции\lect_10\state-population.csv')
areas = pd.read_csv('D:\Cвeтa\Фреймворки пайтон\Лекции\lect_10\state-areas.csv')
abbrevs = pd.read_csv('D:\Cвeтa\Фреймворки пайтон\Лекции\lect_10\state-abbrevs.csv')
display('pop.head()', 'areas.head()', 'abbrevs.head()')
```

Out[129]:

pop.head()

areas.head()

	state/region	ages	year	population	state		area (sq. mi)
0	AL	under18	2012	1117489.0	0	Alabama	52423
1	AL	total	2012	4817528.0	1	Alaska	656425
2	AL	under18	2010	1130966.0	2	Arizona	114006
3	AL	total	2010	4785570.0	3	Arkansas	53182
4	AL	under18	2011	1125763.0	4	California	163707

abbrevs.head()

	state	abbreviation
0	Alabama	AL
1	Alaska	AK
2	Arizona	AZ
3	Arkansas	AR
4	California	CA

Given this information, say we want to compute a relatively straightforward result: rank US states and territories by their 2010 population density. We clearly have the data here to find this result, but we'll have to combine the datasets to find the result.

We'll start with a many-to-one merge that will give us the full state name within the population <code>DataFrame</code> . We want to merge based on the <code>state/region</code> column of pop , and the abbreviation column of abbrevs . We'll use <code>how='outer'</code> to make sure no data is thrown away due to mismatched labels.

In [132]:

```
merged = pd.merge(pop, abbrevs, how='outer',
                  left_on='state/region', right_on='abbreviation')
merged.head()
```

Out[132]:

	state/region	ages	year	population	state	abbreviation
0	AL	under18	2012	1117489.0	Alabama	AL
1	AL	total	2012	4817528.0	Alabama	AL
2	AL	under18	2010	1130966.0	Alabama	AL
3	AL	total	2010	4785570.0	Alabama	AL
4	AL	under18	2011	1125763.0	Alabama	AL

In [134]:

```
merged = merged.drop('abbreviation',1) # drop duplicate info, 1 is an axis
merged.head()
```

Out[134]:

	state/region	ages	year	population	state
0	AL	under18	2012	1117489.0	Alabama
1	AL	total	2012	4817528.0	Alabama
2	AL	under18	2010	1130966.0	Alabama
3	AL	total	2010	4785570.0	Alabama
4	AL	under18	2011	1125763.0	Alabama

Let's double-check whether there were any mismatches here, which we can do by looking for rows with nulls:

In [136]:

```
merged.isna().any()
```

Out[136]:

state/region False False ages year False True population True state

dtype: bool

Some of the population info is null; let's figure out which these are!

In [137]:

```
merged[merged['population'].isna()].head()
```

Out[137]:

	state/region	ages	year	population	state
2448	PR	under18	1990	NaN	NaN
2449	PR	total	1990	NaN	NaN
2450	PR	total	1991	NaN	NaN
2451	PR	under18	1991	NaN	NaN
2452	PR	total	1993	NaN	NaN

It appears that all the null population values are from Puerto Rico prior to the year 2000; this is likely due to this data not being available from the original source.

More importantly, we see also that some of the new state entries are also null, which means that there was no corresponding entry in the abbrevs key! Let's figure out which regions lack this match:

In [138]:

```
merged.loc[merged['state'].isnull(), 'state/region'].unique()
Out[138]:
array(['PR', 'USA'], dtype=object)
```

We can quickly infer the issue: our population data includes entries for Puerto Rico (PR) and the United States as a whole (USA), while these entries do not appear in the state abbreviation key. We can fix these quickly by filling in appropriate entries:

In [139]:

```
merged.loc[merged['state/region'] == 'PR', 'state'] = 'Puerto Rico'
merged.loc[merged['state/region'] == 'USA', 'state'] = 'United States'
merged.isnull().any()
```

Out[139]:

```
state/region False
ages False
year False
population True
state False
dtype: bool
```

No more nulls in the state column: we're all set!

Now we can merge the result with the area data using a similar procedure. Examining our results, we will want to join on the state column in both:

In [156]:

```
final = pd.merge(merged, areas, on='state', how='left')
final.head()
```

Out[156]:

	state/region	ages	year	population	state	area (sq. mi)
0	AL	under18	2012	1117489.0	Alabama	52423.0
1	AL	total	2012	4817528.0	Alabama	52423.0
2	AL	under18	2010	1130966.0	Alabama	52423.0
3	AL	total	2010	4785570.0	Alabama	52423.0
4	AL	under18	2011	1125763.0	Alabama	52423.0

Again, let's check for nulls to see if there were any mismatches:

In [157]:

```
final.isnull().any()
```

Out[157]:

state/region False
ages False
year False
population True
state False
area (sq. mi) True
dtype: bool

There are nulls in the area column; we can take a look to see which regions were ignored here:

In [158]:

```
final['state'][final['area (sq. mi)'].isnull()].unique()
Out[158]:
```

```
array(['United States'], dtype=object)
```

We see that our areas DataFrame does not contain the area of the United States as a whole. We could insert the appropriate value (using the sum of all state areas, for instance), but in this case we'll just drop the null values because the population density of the entire United States is not relevant to our current discussion:

In [159]:

```
final.dropna(inplace=True)
final.head()
```

Out[159]:

	state/region	ages	year	population	state	area (sq. mi)
0	AL	under18	2012	1117489.0	Alabama	52423.0
1	AL	total	2012	4817528.0	Alabama	52423.0
2	AL	under18	2010	1130966.0	Alabama	52423.0
3	AL	total	2010	4785570.0	Alabama	52423.0
4	AL	under18	2011	1125763.0	Alabama	52423.0

Now we have all the data we need. To answer the question of interest, let's first select the portion of the data corresponding with the year 2000, and the total population. We'll use the <code>query()</code> function to do this quickly:

In [160]:

```
data2010 = final.query("year == 2010 & ages == 'total'")
data2010.head()
```

Out[160]:

	state/region	ages	year	population	state	area (sq. mi)
3	AL	total	2010	4785570.0	Alabama	52423.0
91	AK	total	2010	713868.0	Alaska	656425.0
101	AZ	total	2010	6408790.0	Arizona	114006.0
189	AR	total	2010	2922280.0	Arkansas	53182.0
197	CA	total	2010	37333601.0	California	163707.0

Now let's compute the population density and display it in order. We'll start by re-indexing our data on the state, and then compute the result:

In [162]:

```
data2010.set_index('state', inplace=True)
data2010.head()
```

Out[162]:

state/region ages year population area (sq. mi)

state					
Alabama	AL	total	2010	4785570.0	52423.0
Alaska	AK	total	2010	713868.0	656425.0
Arizona	AZ	total	2010	6408790.0	114006.0
Arkansas	AR	total	2010	2922280.0	53182.0
California	CA	total	2010	37333601.0	163707.0

In [163]:

```
density = data2010['population'] / data2010['area (sq. mi)']
```

In [164]:

```
density.sort_values(ascending=False, inplace=True)
density.head()
```

Out[164]:

state

District of Columbia 8898.897059
Puerto Rico 1058.665149
New Jersey 1009.253268
Rhode Island 681.339159
Connecticut 645.600649

dtype: float64

The result is a ranking of US states plus Washington, DC, and Puerto Rico in order of their 2010 population density, in residents per square mile. We can see that by far the densest region in this dataset is Washington, DC (i.e., the District of Columbia); among states, the densest is New Jersey.

We can also check the end of the list:

In [165]:

density.tail()

Out[165]:

state

 South Dakota
 10.583512

 North Dakota
 9.537565

 Montana
 6.736171

 Wyoming
 5.768079

 Alaska
 1.087509

dtype: float64

We see that the least dense state, by far, is Alaska, averaging slightly over one resident per square mile.

This type of messy data merging is a common task when trying to answer questions using real-world data sources. I hope that this example has given you an idea of the ways you can combine tools we've covered in order to gain insight from your data!

In []: