# What are the Most Important Statistical Ideas of the Past 50 Years?

Faryal Fodderwala

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#### Introduction

- Overview of 8 significant statistical ideas from 1970 to 2021.
- Authors: Andrew Gelman and Aki Vehtari.
- ► Purpose: To provoke thought and discussion about modern statistical innovations and their impact on data science.

## Authors' Background



Andrew Gelman



Aki Vehtari

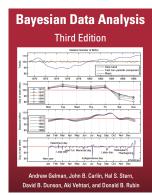
#### Andrew Gelman:

- Professor of Statistics and Political Science, Columbia University.
- Renowned for Bayesian statistics and multilevel modeling.

#### Aki Vehtari:

- Professor of Computational Probabilistic Modeling, Aalto University.
- Focused on Bayesian computation and model assessment.

# Authors' Background (cont.)



Bayesian Data Analysis

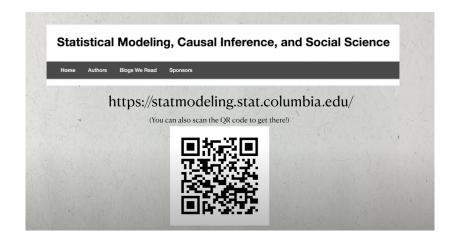
#### ► The Book: Bayesian Data Analysis

- Written by Andrew Gelman, Aki Vehtari, and others.
- Widely regarded as the foundational text ("the bible") for Bayesian practitioners.
- Covers theory, computation, and applied Bayesian methods.

#### ► Their Authority on the Topic

- Through this book, Gelman and Vehtari have shaped the modern understanding of Bayesian statistics.
- Their extensive research and contributions give them unique insights to answer: What are the most important statistical ideas of the past 50 years?

## Gelman's Blog



## Overview of the Paper

- ➤ Timeframe: 1970 to 2021, focusing on the development of modern statistics.
- ▶ 8 statistical ideas selected based on their influence on statistical theory, computation, and applications.
- Emphasis on integrating computation with statistical modeling.
- Designed as an essay, not a research manuscript.
- Meant to provoke thought, invite discussion, and reflect on statistical progress.
- Acknowledges that no definitive list can encompass all significant ideas.

### 01: Counterfactual Causal Inference

- Allows causal inference using observational data.
- Framework based on "potential outcomes" or "counterfactuals."

Causal Effect: 
$$Y(1) - Y(0)$$

- ▶ *Y*(1): Outcome if treated.
- $\triangleright$  Y(0): Outcome if untreated.
- Challenge: Only one outcome is observed.

#### Real-World Connection

NYC Open Data provides datasets on traffic accidents, enabling causal analysis of interventions like "Vision Zero."



## 02: Bootstrapping and Simulation-Based Inference

- Introduced by Bradley Efron (1979).
- Resampling technique to estimate sampling distributions without assumptions about data distribution.

#### Algorithm:

- 1. Resample the dataset with replacement.
- 2. Compute the statistic of interest (e.g., mean).
- 3. Repeat n times to estimate variability.

### Example: NYC 311 Calls Data

Use bootstrapping to estimate variability in the average response time for complaints across boroughs.

## 03: Overparameterized Models and Regularization

- ► High-dimensional models with more parameters than data points.
- Regularization prevents overfitting by adding penalties to the model:

LASSO: 
$$\min (||Y - X\beta||^2 + \lambda ||\beta||_1)$$

## Example

Neural networks for NYC Open Data crime prediction:

Regularization reduces noise and ensures generalizable predictions.

## 04: Bayesian Multilevel Models

- Models hierarchical data with varying parameters at different levels.
- Example: Modeling housing prices across NYC boroughs.

$$y_{ij} = \beta_0 + \beta_1 X_{ij} + u_j + \epsilon_{ij}$$

- $ightharpoonup u_j$ : Random effect for borough j.
- $ightharpoonup \epsilon_{ij}$ : Error term for observation i in borough j.

## Advantage

Combines individual-level and group-level variability for improved estimates.

## 05: Generic Computation Algorithms

- Advances in algorithms like MCMC, EM, and variational inference.
- Enabled complex models and large-scale Bayesian analysis.

## Connection to NYC Open Data

Use MCMC to model traffic flow patterns and predict congestion hotspots.

## 06: Adaptive Decision Analysis

- Framework for making decisions during experiments.
- ▶ Application: Stopping clinical trials early for ethical reasons.

## Real-World Example

In NYC public health studies, adaptive analysis helps evaluate the success of vaccination campaigns.

#### 07: Robust Inference

- ► Focuses on reliability under model misspecification.
- Example: Median-based estimators for income disparity in NYC.

## Key Insight

Robust inference allows valid results even when data deviates from assumptions.

# 08: Exploratory Data Analysis (EDA)

- ▶ Emphasizes visualization and insights over strict models.
- Examples: Trends in NYC Open Data on crime or health disparities.



## Connection to NYC Open Data

- Apply statistical methods to NYC datasets.
- Example: Visualize and analyze health disparities using robust inference and EDA.

#### Conclusions and Future Directions

- ► These statistical ideas are foundational to modern data analysis.
- ► Future: Integration of machine learning with causal inference.
- Importance of robust and interpretable models for real-world applications.

# The Importance of Human Oversight in Statistical Innovations

- As computational power advances, machine learning and statistical algorithms can model complex systems.
- ► However, these models are only as good as the assumptions and data they are based on.
- ► Example: Self-driving cars can use machine learning to navigate, but human oversight is needed to determine:
  - Are the outcomes (e.g., accident rates) statistically significant?
  - Are the algorithms operating ethically and equitably?
- ► **Key Point**: Computational tools are powerful, but without human observation and ethical guidance, they can lead to unintended consequences.

#### Reflection from Gelman

"On one hand, you have all these amazing things that machine learning can do, like self-driving cars, but you'll need a statistician to tell you if the number of people being killed by the self-driving cars is statistically significant." — Paraphrased from Andrew

## Questions?

Thank you! Any questions?

#### References

- Gelman, Andrew, and Aki Vehtari. 2021. "What are the Most Important Statistical Ideas of the Past 50 Years?" Journal of the American Statistical Association 116, no. 536: 2087–2097.
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