

# MRI Supply Chain Optimization Project Report

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## Abstract

This report presents an optimization model for the MRI supply chain, focusing on the sourcing of components, transportation, packaging, and assembly to minimize costs while meeting various constraints such as logistics, labor, and customs. The approach leverages mathematical modeling and optimization techniques to create an efficient supply chain for MRI machine manufacturing.

## Contents

<b>1</b>	<b>Introduction to the Problem</b>	<b>4</b>
1.1	Challenges in the MRI Manufacturing Supply Chain . . . . .	4
1.2	Why Optimization is Needed . . . . .	4
1.3	Approach to Tackling the Problem . . . . .	5
1.4	Conclusion . . . . .	6
<b>2</b>	<b>Objective</b>	<b>6</b>
<b>3</b>	<b>Methodology</b>	<b>8</b>
3.1	Sets Used in the Optimization Model . . . . .	8
3.2	Parameters Used in the Optimization Model . . . . .	9
3.3	Decision Variables in the Optimization Model . . . . .	12
3.4	Constraints in the Optimization Model . . . . .	14
3.5	Objective Function . . . . .	16
3.5.1	Description of Each Term . . . . .	17
3.5.2	Why These Terms Add Up to Form the Objective . . . . .	18
3.5.3	Summary . . . . .	19
<b>4</b>	<b>Linearizing the Objective Function</b>	<b>19</b>
4.1	Non-Linear Terms in the Objective Function . . . . .	19
4.2	Linearizing the Non-Linear Terms . . . . .	20
4.2.1	Linearizing Component Cost Terms . . . . .	20
4.2.2	Linearizing Transportation Cost Terms . . . . .	20
4.3	Resulting Linearized Objective Function . . . . .	21
4.4	Conclusion . . . . .	21

<b>5</b>	<b>Literature Review</b>	<b>21</b>
5.1	Digitalization and Supply Chain Optimization . . . . .	21
5.2	Strategic Decision-Making in Healthcare Supply Chains . . . . .	21
5.3	Supply Chain Design in Medical Nuclear Applications . . . . .	22
5.4	Cost Optimization with Deteriorating Inventories . . . . .	22
5.5	AI and Deep Reinforcement Learning for Supply Chain Mode Selection .	22
5.6	AI in Supply Chain Risk Assessment . . . . .	22
5.7	Sustainability in Supply Chain Management . . . . .	22
5.8	Conclusion . . . . .	22
<b>6</b>	<b>Supply Chain Optimization in MRI Manufacturing</b>	<b>23</b>
6.1	Introduction . . . . .	23
6.2	Key Components of the MRI Supply Chain . . . . .	23
6.3	Optimization Strategies . . . . .	23
6.3.1	Advanced Planning and Scheduling (APS) . . . . .	23
6.3.2	Lean Manufacturing . . . . .	23
6.3.3	Collaborative Planning, Forecasting, and Replenishment (CPFR)	24
6.3.4	Smart Manufacturing and Industry 4.0 Technologies . . . . .	24
6.4	Challenges in MRI Supply Chain Optimization . . . . .	24
6.5	Conclusion . . . . .	24
<b>7</b>	<b>Solution Methodology</b>	<b>24</b>
7.1	Choice of Solver . . . . .	25
7.2	Algorithmic Approach . . . . .	25
7.3	Computational Complexity and Runtime Considerations . . . . .	25
7.4	Model Testing and Validation . . . . .	26
7.5	Conclusion . . . . .	27
<b>8</b>	<b>Case Study / Simulation</b>	<b>27</b>
8.1	Description of the Dataset . . . . .	27
8.2	Setup and Implementation of the Model . . . . .	28
8.3	Results of Optimization . . . . .	28
8.4	Interpretation of Results . . . . .	29
8.5	Conclusion . . . . .	29
<b>9</b>	<b>Sensitivity Analysis</b>	<b>29</b>
9.1	Analysis of Key Parameters . . . . .	30
9.2	Impact of Parameter Variations on Optimization Results . . . . .	30
9.3	Sensitivity to Uncertainties in Parameters . . . . .	31
9.4	Potential Impacts of External Conditions . . . . .	32
9.5	Conclusion . . . . .	32
<b>10</b>	<b>Detailed Analysis of the Optimization Results</b>	<b>32</b>
10.1	Transportation Strategies: Air vs Sea . . . . .	33
10.2	Global Sourcing and Assembly Location: India as the Hub . . . . .	33
10.3	Shipping and Risk Mitigation through Diversified Suppliers . . . . .	33
10.4	Packaging Optimization and Its Role in Cost Reduction . . . . .	33
10.5	Cost Minimization and Efficiency Gains . . . . .	34
10.6	Strategic Recommendations for Further Optimization . . . . .	34

10.7 Conclusion . . . . .	34
<b>11 Component-Wise Flow of Optimization</b>	<b>34</b>
11.1 Shim Coils . . . . .	35
11.2 RF Coils . . . . .	35
11.3 Gradient Coil . . . . .	35
11.4 Patient Table, PDU, Gradient Amplifier, RF Amplifier, RF Receiver Assembly, Image Reconstruction Computer, Peripheral Devices, MRI Safety System, RF Shielding . . . . .	35
<b>12 Geographic Supply Chain Mapping</b>	<b>35</b>
12.1 Sourcing Countries . . . . .	35
12.2 Assembly and Distribution Hub . . . . .	36
12.3 Transport Corridors . . . . .	36
12.4 Supply Chain Topology . . . . .	36
<b>13 Bottleneck and Trade-Off Analysis</b>	<b>36</b>
13.1 Identified Bottlenecks . . . . .	36
13.2 Trade-Offs Observed . . . . .	36
<b>14 Cost Component Decomposition</b>	<b>37</b>
<b>15 Scenario and Contingency Testing</b>	<b>37</b>
15.1 Tested Scenarios . . . . .	37
<b>16 Managerial Insights and Policy Implications</b>	<b>37</b>
<b>17 Model Limitations and Assumptions Review</b>	<b>37</b>
<b>18 Visualization of Sourcing and Transport Flows</b>	<b>38</b>
<b>19 Conclusions and Future Work</b>	<b>42</b>
19.1 Key Findings . . . . .	42
19.2 Implications for Practitioners in the MRI Manufacturing Industry . . . .	42
19.3 Suggestions for Future Work . . . . .	43
19.4 Conclusion . . . . .	44
<b>20 References</b>	<b>45</b>

# 1 Introduction to the Problem

The global healthcare industry faces immense challenges in ensuring the availability, efficiency, and cost-effectiveness of medical equipment. Among these, MRI (Magnetic Resonance Imaging) machines play a critical role in diagnosing a wide range of medical conditions, including neurological, musculoskeletal, and cardiovascular disorders. However, the supply chain for MRI machines is complex and involves the procurement of various components, labor management, transportation logistics, and compliance with stringent regulations. As demand for medical imaging continues to rise globally, optimizing this supply chain becomes essential to reduce costs, minimize delays, and ensure that MRI machines are delivered to healthcare facilities efficiently.

## 1.1 Challenges in the MRI Manufacturing Supply Chain

The MRI manufacturing supply chain is inherently complex, with several key challenges:

- **Component Sourcing:** MRI machines are composed of several high-precision components, such as superconducting magnets, gradient coils, and radiofrequency coils. These components are often sourced from different countries, each with varying levels of cost, quality, and production capabilities.
- **Transportation Costs and Time:** The components need to be shipped across countries, often by air or sea. Transportation times, costs, and potential delays due to customs, tariffs, or unforeseen disruptions can lead to significant inefficiencies in the supply chain.
- **Labor Allocation:** Labor costs vary widely across countries, and the assembly of MRI machines requires skilled labor. Optimally allocating labor across different stages of production is crucial for reducing assembly costs and ensuring timely production.
- **Packaging and Inventory Management:** Proper packaging and inventory management are critical to prevent damage during transportation and to ensure that sufficient parts are available when needed without overstocking.
- **Regulatory and Compliance Challenges:** Regulatory standards for medical equipment vary by country, making it difficult to standardize the supply chain process. Additionally, import duties and taxes further complicate the sourcing and distribution of MRI components.

Given these challenges, there is an urgent need for a systematic approach to optimize the MRI manufacturing supply chain. Traditional methods of managing supply chains often lead to suboptimal solutions, resulting in higher costs, longer lead times, and missed opportunities for efficiency gains. Optimization techniques can help address these issues by identifying the most cost-effective and efficient strategies for sourcing, transportation, labor allocation, and inventory management.

## 1.2 Why Optimization is Needed

The need for optimization in the MRI supply chain stems from the following key reasons:

- **Cost Reduction:** The manufacturing and transportation of MRI machines incur significant costs, particularly in component sourcing and logistics. Optimizing these aspects can lead to substantial cost savings, which are crucial for both manufacturers and healthcare providers.
- **Improved Efficiency:** Optimizing the supply chain can help reduce bottlenecks, improve lead times, and ensure that the right parts are available at the right time. This ensures that production schedules are met, and healthcare facilities receive MRI machines promptly.
- **Enhanced Decision-Making:** Optimization provides a data-driven approach to decision-making, helping decision-makers identify the best sourcing strategies, transportation methods, and labor allocation to minimize costs and improve service levels.
- **Risk Mitigation:** The global nature of the MRI supply chain exposes it to various risks, including geopolitical uncertainties, tariff fluctuations, and transportation disruptions. Optimization models can help anticipate these risks and develop strategies to mitigate their impact.
- **Regulatory Compliance:** Medical device manufacturers must comply with various international regulations. An optimized supply chain ensures that components and processes meet these regulatory requirements while minimizing delays or penalties.

By applying optimization techniques, manufacturers can create a more resilient, cost-effective, and flexible MRI supply chain that adapts to dynamic market conditions and meets the growing global demand for MRI machines.

### 1.3 Approach to Tackling the Problem

To address the challenges in the MRI manufacturing supply chain, this project follows a systematic approach based on optimization modeling. The main steps in the approach are as follows:

- **Model Formulation:** The problem is formulated as a Mixed-Integer Linear Programming (MILP) model. The objective is to minimize the total cost of the supply chain, which includes costs related to sourcing, transportation, labor, and packaging. The model incorporates various constraints such as sourcing from one country, manufacturing parts in one location, labor availability, and transportation capacity.
- **Data Collection:** A comprehensive dataset is gathered, including sourcing costs, transportation times, labor costs, tariffs, packaging requirements, and demand forecasts. The data is used to initialize the optimization model and ensure that the results reflect real-world conditions.
- **Solver Selection:** To solve the MILP problem, we use advanced solvers like Gurobi and CPLEX, which are capable of handling large-scale optimization problems efficiently. These solvers apply algorithms such as branch-and-bound and simplex methods to find the optimal solution.

- **Sensitivity Analysis:** Once the optimization model is solved, a sensitivity analysis is performed to assess how variations in key parameters (e.g., transportation costs, labor costs, tariffs) affect the optimal solution. This helps identify the robustness of the model and provides insights into potential risks and uncertainties.
- **Scenario Testing:** The model is tested under different scenarios, such as changes in demand, supply chain disruptions, or fluctuations in tariffs. These scenarios help evaluate how the optimization model can adapt to real-world challenges and ensure resilience in the supply chain.
- **Results Interpretation and Decision Support:** The results of the optimization are interpreted to provide actionable insights for decision-makers. This includes recommendations on the best sourcing strategies, transportation methods, labor allocation, and packaging solutions.

This approach allows us to model the MRI supply chain comprehensively and identify strategies that minimize costs while maximizing efficiency. It also ensures that the supply chain can adapt to fluctuations in key parameters, providing a flexible and robust solution.

## 1.4 Conclusion

In conclusion, the MRI supply chain is complex, and its optimization is essential for reducing costs, improving efficiency, and ensuring timely delivery of MRI machines to healthcare facilities. By applying optimization techniques, we can address challenges such as sourcing inefficiencies, high transportation costs, and labor allocation issues. This approach not only improves the financial performance of MRI manufacturers but also enhances the overall quality of healthcare by ensuring that MRI machines are available when needed.

The systematic approach outlined in this report lays the foundation for creating an optimized, cost-effective, and resilient MRI supply chain, capable of meeting the growing demands of the global healthcare market.

## 2 Objective

The primary objective of this MRI supply chain optimization model is to minimize the total cost while satisfying a set of operational constraints. The goal is to find the most cost-effective configuration for sourcing components, allocating labor, managing transportation, and packaging, all while ensuring that the MRI machines are produced on time and meet quality standards.

The total cost in this context is a combination of several key cost components:

- **Sourcing Costs:** These are the costs associated with purchasing components from various suppliers located in different countries. The sourcing cost depends on the price per unit of each component, as well as the quantity of components required for the production of each MRI part.
- **Transportation Costs:** These costs arise from shipping components and parts between countries. The transportation costs can vary depending on the mode of transport (air or sea), the distance between source and destination countries, and the quantity of goods being shipped.

- **Labor Costs:** Labor costs are incurred during the assembly phase of the MRI manufacturing process. These costs depend on the number of laborers employed, their hourly wages, and the number of labor hours required to assemble the parts and components into the final MRI machine.
- **Packaging Costs:** Packaging costs are associated with the materials required to safely pack and ship components and parts. The choice of packaging type and the quantity of each type used can affect the overall cost.

#### Objective Function

The objective function is formulated as a minimization problem. The total supply chain cost  $C_{\text{total}}$  is the sum of the sourcing, transportation, labor, and packaging costs. The objective function is defined as follows:

$$\begin{aligned}
\text{Objective} = & \sum_{b \in B} \sum_{a \in A} \text{price\_per\_unit} \times \text{amount\_bought} \\
& + \sum_{b \in B} \sum_{a \in A} \text{air\_freight\_costs} \times \text{amount\_air\_parts} \\
& + \sum_{b \in B} \sum_{a \in A} \text{sea\_freight\_costs} \times \text{amount\_sea\_parts} \\
& + \sum_{b \in B} \sum_{a \in A} \text{labor\_costs} \times \text{labor\_hours} \\
& + \sum_{b \in B} \sum_{a \in A} \text{production\_costs} \times \text{production\_units} \\
& + \sum_{b \in B} \sum_{a \in A} \text{packaging\_costs} \times \text{number\_of\_packages}
\end{aligned}$$

Where: -  $Jir[i, r]$  represents the base purchase cost per unit of component  $r$  in country  $i$ . -  $Y[i, j, r]$  represents the quantity of component  $r$  for part  $j$  purchased from country  $i$ . -  $Tr[i, d]$  represents the air transport cost per unit from country  $i$  to destination country  $d$ . -  $S[i, d, r]$  represents the binary variable indicating if component  $r$  is shipped by air from  $i$  to  $d$ . -  $Trs[i, d]$  represents the sea transport cost per unit from country  $i$  to destination country  $d$ . -  $T[i, d, r]$  represents the binary variable indicating if component  $r$  is shipped by sea from  $i$  to  $d$ . -  $PMim[i, m]$  represents the regular labor cost per day for labor type  $m$  in country  $i$ . -  $N[i, m]$  represents the number of laborers of type  $m$  employed in country  $i$ . -  $PRik[i, k]$  represents the packaging cost per type  $k$  in country  $i$ . -  $G[k, j, i]$  represents the number of packages of type  $k$  used for part  $j$  in country  $i$ .

The objective function seeks to minimize the total cost by considering the following factors: - **Sourcing costs**: These depend on the quantity of components purchased from each country and the unit cost of those components. - **Transportation costs**: Both air and sea transportation costs are included in the objective, weighted by the quantity of components shipped and the respective transport mode. - **Labor costs**: The cost of labor employed for assembly is calculated based on the number of workers and their respective wages. - **Packaging costs**: Packaging is essential for protecting components during shipping. The model optimizes the choice and quantity of packaging used to minimize costs.

#### Minimization Problem

The primary objective is to minimize the total cost  $C_{\text{total}}$  while ensuring that all supply chain constraints are satisfied. The constraints include:

- Sourcing constraints, ensuring that each component is sourced from exactly one country.
- Transportation constraints, ensuring that components are shipped from the correct source to the correct destination within the time frames.
- Labor constraints, ensuring that the number of laborers employed meets the assembly requirements.
- Inventory constraints, ensuring that the required quantity of each part and component is available at the right time.

By minimizing the total cost while satisfying these constraints, the optimization model identifies the best possible configuration of sourcing, transportation, labor allocation, and packaging for the MRI supply chain.

#### Conclusion

The objective function of this optimization model integrates various cost components—sourcing, transportation, labor, and packaging—into a unified cost minimization framework. By solving this model, manufacturers can determine the most cost-effective sourcing strategies, transportation methods, labor allocation, and packaging decisions. The goal is to not only minimize costs but also ensure the timely production and delivery of MRI machines to healthcare providers.

## 3 Methodology

The supply chain optimization model is based on the following components:

- **Sets:** Countries, parts, components, packaging types, labor types, etc.
- **Parameters:** Component costs, transportation costs, labor costs, import duties, etc.
- **Decision Variables:** Binary and continuous variables defining sourcing, shipping, and labor assignments.
- **Constraints:** Manufacturing capacity, assembly labor availability, transportation routes, and cost limitations.
- **Objective Function:** Minimization of total cost, considering all associated costs and overheads.

The model will be formulated as a mixed-integer programming (MIP) problem, which will be solved using optimization solvers like Gurobi or CPLEX.

### 3.1 Sets Used in the Optimization Model

In the optimization model, we define the following sets, which are crucial for structuring the problem and determining the relationships between different entities within the supply chain:

- **Set of Countries ( $I$ ):**



- Denoted as  $I = \{1, 2, \dots, 16\}$ , this set represents the countries involved in the sourcing, assembly, and transportation of MRI components. Each country in this set is indexed by  $i$ .
- **Set of Parts ( $J$ ):**
  - Denoted as  $J = \{1, 2, \dots, 13\}$ , this set represents the different parts of the MRI machine. Each part  $j$  in the set  $J$  corresponds to a specific subcomponent of the MRI machine, such as the magnet, RF coil, and shim coils.
- **Set of Components ( $R$ ):**
  - Denoted as  $R = \{1, 2, \dots, 42\}$ , this set includes all the individual components that are used to manufacture each part of the MRI machine. For example, a magnet may be composed of several components, such as the winding and core, which are represented as elements in this set.
- **Set of Packaging Types ( $K$ ):**
  - Denoted as  $K = \{1, 2, \dots, 13\}$ , this set represents the different types of packaging used for components and parts. The packaging type is crucial for managing storage and transportation costs, as certain packaging may incur higher shipping costs.
- **Set of Labor Types ( $M$ ):**
  - Denoted as  $M = \{1, 2, 3, 4\}$ , this set represents the different labor categories required for the manufacturing and assembly of MRI parts. These labor categories may include regular labor, overtime labor, and specialized labor types.
- **Set of Destination Countries ( $D$ ):**
  - Denoted as  $D = I$ , this set is identical to the set of countries  $I$  and represents the destination countries for the shipping of parts and components after manufacturing or assembly.

### 3.2 Parameters Used in the Optimization Model

In this subsection, we describe the key parameters used in the optimization model, which are essential for quantifying the cost and constraints within the MRI supply chain. These parameters include component costs, transportation costs, labor costs, packaging costs, and other factors that influence the decision-making process.

- **Base Purchase Cost of Components ( $Jir[i, r]$ ):**
  - Denoted as  $Jir[i, r]$ , this parameter represents the base purchase cost per unit of component  $r$  in country  $i$ . This cost is measured in USD per unit and varies by both the country of origin and the type of component.
- **Insurance Overhead Multiplier ( $Ki[i]$ ):**

- Denoted as  $Ki[i]$ , this parameter represents the insurance overhead multiplier in country  $i$ . It is a dimensionless multiplier applied to the cost of components for insurance purposes during transit.
- **Setup Overhead Multiplier ( $Li[i]$ ):**
  - Denoted as  $Li[i]$ , this parameter accounts for the setup overhead cost multiplier in country  $i$ . It is dimensionless and applies to the setup costs incurred for manufacturing parts and components in country  $i$ .
- **Uplift Overhead Multiplier ( $Zi[i]$ ):**
  - Denoted as  $Zi[i]$ , this parameter represents the uplift overhead cost multiplier in country  $i$ . It is a dimensionless multiplier that applies to costs associated with ramping up production and scaling the manufacturing process in a given country.
- **Internal Logistics Multiplier ( $Si[i]$ ):**
  - Denoted as  $Si[i]$ , this parameter represents the internal logistics multiplier in country  $i$ . This is a dimensionless factor that influences the cost of transporting parts and components within a country, including storage and handling costs.
- **Import Duty Multiplier ( $Wi[i]$ ):**
  - Denoted as  $Wi[i]$ , this parameter represents the import duty multiplier for components being shipped to country  $i$ . This dimensionless parameter captures the customs duties imposed on imported goods.
- **Component Quantity per Part ( $Vjr[j, r]$ ):**
  - Denoted as  $Vjr[j, r]$ , this parameter defines the quantity of component  $r$  needed to manufacture one unit of part  $j$ . It is measured in units per component and is crucial for determining the overall component requirements for manufacturing each part.
- **Air Transport Cost per Unit ( $Tr[i, d]$ ):**
  - Denoted as  $Tr[i, d]$ , this parameter represents the air transport cost per unit from country  $i$  to destination  $d$ . It is measured in USD per unit and depends on the shipping distance, volume, and other logistical factors.
- **Sea Transport Cost per Unit ( $Trs[i, d]$ ):**
  - Denoted as  $Trs[i, d]$ , this parameter represents the sea transport cost per unit from country  $i$  to destination  $d$ . Similar to air transport costs, this parameter varies depending on the shipping mode, distance, and other logistical constraints.
- **Packaging Cost per Type ( $PRik[i, k]$ ):**
  - Denoted as  $PRik[i, k]$ , this parameter represents the packaging cost per type  $k$  in country  $i$ . The cost varies depending on the packaging type used for shipping components and parts.

- **Labor Cost per Day ( $PMim[i, m]$ ):**
  - Denoted as  $PMim[i, m]$ , this parameter represents the regular labor cost per day for labor type  $m$  in country  $i$ . It is measured in USD per labor-day and varies by labor type and country.
- **Overtime Labor Cost per Day ( $PMOim[i, m]$ ):**
  - Denoted as  $PMOim[i, m]$ , this parameter accounts for the overtime labor cost per day for labor type  $m$  in country  $i$ . It is measured in USD per labor-day and applies when labor works beyond regular hours.
- **Idle Labor Cost per Day ( $ICim[i, m]$ ):**
  - Denoted as  $ICim[i, m]$ , this parameter represents the idle labor cost per day for labor type  $m$  in country  $i$ . It accounts for labor costs incurred when workers are idle and not directly involved in production.
- **Assembly Labor Cost per Day ( $ALim[i, m]$ ):**
  - Denoted as  $ALim[i, m]$ , this parameter represents the assembly labor cost per day of type  $m$  in country  $i$ . This is the cost incurred for labor engaged in the assembly phase of part manufacturing.
- **Fixed Assembly Setup Cost ( $ACi[i]$ ):**
  - Denoted as  $ACi[i]$ , this parameter accounts for the fixed assembly setup cost in country  $i$ . It is a one-time cost for setting up the assembly facility and is incurred regardless of the volume of production.
- **Big-M Cap for Procurement/Flows ( $M_{qty}$ ):**
  - Denoted as  $M_{qty}$ , this parameter represents a large upper bound (Big-M) used in the optimization model for limiting procurement and flow values. It helps in managing non-linearities and ensuring feasible solutions.
- **Big-M Cap for Labor-Days ( $M_{day}$ ):**
  - Denoted as  $M_{day}$ , this parameter represents a large upper bound (Big-M) for the labor-days required during the assembly and production phases.
- **Big-M Cap for Number of Workers ( $M_{people}$ ):**
  - Denoted as  $M_{people}$ , this parameter represents a large upper bound (Big-M) for the number of workers employed in any given country. This parameter is used to limit labor assignments and ensure realistic staffing levels.

These parameters are fundamental for defining the cost structure and constraints in the optimization model. They allow for a detailed representation of the MRI machine supply chain, considering the various costs and logistical factors associated with each stage of production, transportation, and assembly. By incorporating these parameters, we can accurately model and minimize the total cost of the supply chain while adhering to all operational constraints.

### 3.3 Decision Variables in the Optimization Model

In the optimization model, decision variables are used to represent the choices that will be made in the supply chain, such as sourcing decisions, labor assignments, and transportation decisions. These decision variables are crucial for the model's formulation and solution, and they are categorized into two main types: binary and continuous variables. The distinction between these two types is essential for modeling different types of decisions.

- **Binary Decision Variables:**

- Binary variables are used when a decision is binary in nature, meaning that it involves either a "yes" or "no" choice. These variables take a value of 1 or 0, where 1 indicates the presence of a decision (e.g., a component is sourced from a specific country) and 0 indicates its absence (e.g., a component is not sourced from that country).

The following binary decision variables are used in the model:

- \*  $X[i, j, r]$ : This binary variable is equal to 1 if component  $r$  for part  $j$  is sourced from country  $i$ , and 0 otherwise.
- \*  $Z[i, j]$ : This binary variable is equal to 1 if part  $j$  is manufactured in country  $i$ , and 0 otherwise.
- \*  $S[i, d, r]$ : This binary variable is equal to 1 if component  $r$  is shipped by air from country  $i$  to destination country  $d$ , and 0 otherwise.
- \*  $T[i, d, r]$ : This binary variable is equal to 1 if component  $r$  is shipped by sea from country  $i$  to destination country  $d$ , and 0 otherwise.
- \*  $P[i, d, j]$ : This binary variable is equal to 1 if part  $j$  is shipped by air from country  $i$  to destination country  $d$ , and 0 otherwise.
- \*  $Q[i, d, j]$ : This binary variable is equal to 1 if part  $j$  is shipped by sea from country  $i$  to destination country  $d$ , and 0 otherwise.
- \*  $A[i, d, j]$ : This binary variable is equal to 1 if part  $j$  is shipped by air from country  $i$  to destination country  $d$ , and 0 otherwise.
- \*  $B[i, d, j]$ : This binary variable is equal to 1 if part  $j$  is shipped by sea from country  $i$  to destination country  $d$ , and 0 otherwise.
- \*  $E[k, j, i]$ : This binary variable is equal to 1 if packaging type  $k$  is used for part  $j$  in country  $i$ , and 0 otherwise.
- \*  $F[k, r, i]$ : This binary variable is equal to 1 if packaging type  $k$  is used for component  $r$  in country  $i$ , and 0 otherwise.
- \*  $N[i, m]$ : This binary variable is equal to 1 if general labor type  $m$  is employed in country  $i$ , and 0 otherwise.
- \*  $A_{\text{assem}}[i]$ : This binary variable is equal to 1 if country  $i$  is selected as the assembly site, and 0 otherwise.
- \*  $BIA[i, m]$ : This binary variable is equal to 1 if idle labor is permitted for labor type  $m$  in country  $i$ , and 0 otherwise.
- \*  $BOA[i, m]$ : This binary variable is equal to 1 if overtime is permitted for labor type  $m$  in country  $i$ , and 0 otherwise.

- **Continuous Decision Variables:**

- Continuous variables are used when the decision can take any value within a given range, typically representing quantities or amounts. These variables are essential for representing the flow of components, labor assignments, and shipping quantities, among other factors.

The following continuous decision variables are used in the model:

- \*  $Y[i, j, r]$ : This continuous variable represents the quantity of component  $r$  for part  $j$  bought from country  $i$ . It is measured in units and can take any positive value.
- \*  $C[i, d, r]$ : This continuous variable represents the quantity of component  $r$  shipped by air from country  $i$  to destination country  $d$ . It is measured in units per component and can take any positive value.
- \*  $D[i, d, r]$ : This continuous variable represents the quantity of component  $r$  shipped by sea from country  $i$  to destination country  $d$ . It is measured in units per component and can take any positive value.
- \*  $A_{\text{assem}}[i]$ : This continuous variable represents the number of assembly labor-days used in country  $i$ .
- \*  $NA[i, m]$ : This continuous variable represents the number of assembly laborers of type  $m$  in country  $i$ .
- \*  $I[i, m]$ : This continuous variable represents the idle labor-days of type  $m$  in country  $i$ .
- \*  $OT[i, m]$ : This continuous variable represents the overtime labor-days of type  $m$  in country  $i$ .
- \*  $IA[i, m]$ : This continuous variable represents the idle assembly labor-days of type  $m$  in country  $i$ .
- \*  $OTA[i, m]$ : This continuous variable represents the overtime assembly labor-days of type  $m$  in country  $i$ .
- \*  $G[k, j, i]$ : This continuous variable represents the number of packages of type  $k$  used for part  $j$  in country  $i$ .
- \*  $H[k, r, i]$ : This continuous variable represents the number of packages of type  $k$  used for component  $r$  in country  $i$ .

**Binary variables** are primarily used to model discrete decisions, such as whether a particular component is sourced from a given country, whether it is shipped by air or sea, or whether specific labor types are employed in different countries. These decisions are either "yes" (1) or "no" (0).

**Continuous variables** represent decisions that involve quantities or amounts, such as the number of components purchased, the quantity of parts shipped, or the number of laborers assigned to a task. These variables can take any non-negative value within a specified range.

The distinction between binary and continuous variables enables the model to capture both discrete choices (e.g., sourcing decisions, shipping methods) and continuous decisions (e.g., quantities, labor assignments), allowing for a comprehensive and realistic representation of the MRI supply chain optimization problem.

### 3.4 Constraints in the Optimization Model

In this subsection, we describe the various constraints that govern the MRI supply chain optimization model. These constraints are derived based on real-world limitations, such as manufacturing capacity, labor availability, transportation capabilities, and cost structures. Each constraint ensures that the optimization model results in a feasible and realistic solution, reflecting the practical aspects of the supply chain. Below, we explain how each constraint was formulated and the rationale behind its inclusion.

- **Sourcing Constraints:**

- **Constraint 1: Component Sourcing Decision**

$$\sum_{i \in I} X[i, j, r] = 1 \quad \forall j \in J, \quad \forall r \in R \quad (1)$$

- **Explanation:** This constraint ensures that each component  $r$  for part  $j$  is sourced from exactly one country. The decision variable  $X[i, j, r]$  is binary, indicating whether component  $r$  for part  $j$  is sourced from country  $i$ . This constraint ensures that no component is sourced from multiple countries, which is critical for supply chain clarity and inventory management.
- **Reason:** This constraint reflects the real-world requirement that each component can only be sourced from one country at a time, preventing conflicts in sourcing decisions.

- **Manufacturing and Assembly Constraints:**

- **Constraint 2: Part Manufacturing in a Country**

$$\sum_{i \in I} Z[i, j] = 1 \quad \forall j \in J \quad (2)$$

- **Explanation:** This constraint ensures that each part  $j$  is manufactured in exactly one country. The decision variable  $Z[i, j]$  is binary, where 1 indicates that part  $j$  is being manufactured in country  $i$  and 0 otherwise.
- **Reason:** This reflects the operational limitation that each part of the MRI machine must be assembled in a specific country. Manufacturing in multiple locations for a single part could lead to increased complexity and cost, especially for components requiring tight tolerances or specific assembly conditions.

- **Labor and Worker Constraints:**

- **Constraint 3: Labor Availability for Assembly**

$$\sum_{m \in M} N[i, m] \geq \text{Required Labor for Assembly}[i] \quad \forall i \in I \quad (3)$$

- **Explanation:** This constraint ensures that the total number of laborers of all types employed in country  $i$  meets or exceeds the labor requirements for the assembly of MRI parts. The variable  $N[i, m]$  represents the number of general laborers of type  $m$  in country  $i$ .

- **Reason:** Labor availability is a key factor in manufacturing. This constraint ensures that enough workers are available to meet the production demands, preventing delays in the assembly process.

- **Transportation Constraints:**

- **Constraint 4: Shipping Limits for Components**

$$\sum_{d \in D} (C[i, d, r] + D[i, d, r]) = Y[i, j, r] \quad \forall i \in I, \quad \forall j \in J, \quad \forall r \in R \quad (4)$$

- **Explanation:** This constraint ensures that the total amount of components  $r$  shipped (via air or sea) from country  $i$  to destination country  $d$  is equal to the quantity of components  $r$  purchased from country  $i$ . The variables  $C[i, d, r]$  and  $D[i, d, r]$  represent the air and sea transport quantities, respectively.
- **Reason:** This constraint reflects the fact that the amount of components purchased must be fully accounted for by the quantity shipped, either by air or by sea. It ensures that no component is left unshipped after purchase, aligning with the principle that all sourced components must reach the assembly site or destination.

- **Packaging Constraints:**

- **Constraint 5: Packaging Requirements for Parts and Components**

$$\sum_{k \in K} G[k, j, i] = \text{Packaging Requirement}[j, i] \quad \forall i \in I, \quad \forall j \in J \quad (5)$$

- **Explanation:** This constraint ensures that the total number of packages of each packaging type  $k$  used for part  $j$  in country  $i$  equals the packaging requirement for part  $j$ . The variable  $G[k, j, i]$  represents the number of packages of type  $k$  used for part  $j$  in country  $i$ .
- **Reason:** Packaging is essential for efficient transport and storage. This constraint ensures that the correct amount of packaging is used for each part, preventing underuse or overuse of packaging materials, and helping to minimize unnecessary packaging costs.

- **Cost Constraints:**

- **Constraint 6: Cost Limitation on Procurement**

$$\sum_{i \in I} Jir[i, r] \cdot Y[i, j, r] + \sum_{i \in I} PRik[i, k] \cdot G[k, j, i] \leq \text{Budget for Procurement}[j] \quad \forall j \in J \quad (6)$$

- **Explanation:** This constraint ensures that the total cost of purchasing components  $r$  for part  $j$ , including the packaging costs, does not exceed the allocated budget for procurement. The variables  $Jir[i, r]$  and  $PRik[i, k]$  represent the purchase and packaging costs, respectively.
- **Reason:** Budget constraints are essential in ensuring that the optimization model adheres to financial limits. This constraint helps control procurement expenses, ensuring that the model produces a cost-effective solution that fits within the predefined budget.

- **Transportation Time Constraints:**

- **Constraint 7: Shipping Time Constraint**

$$\text{Shipping Time} \leq \text{Maximum Allowed Shipping Time} \quad \forall i \in I, \quad \forall d \in D, \quad \forall r \in R \quad (7)$$

- **Explanation:** This constraint ensures that the shipping time from country  $i$  to destination country  $d$  does not exceed the maximum allowed shipping time for component  $r$ .
- **Reason:** Shipping time is an important factor for ensuring that the MRI machines are delivered within the required timeline. This constraint helps ensure that transportation decisions are made with time constraints in mind, maintaining the efficiency of the overall supply chain.

These constraints collectively represent the operational, logistical, and financial limitations of the MRI supply chain. Each constraint is designed to ensure that the optimization model produces realistic and feasible results, considering factors such as production capacity, labor availability, transportation capabilities, packaging requirements, and budget limitations. The inclusion of these constraints helps to ensure that the solution derived from the optimization model adheres to practical requirements and delivers cost-effective and timely results.

### 3.5 Objective Function

In an optimization model, the objective function represents the goal we are aiming to achieve through the decision variables. In this case, our goal is to minimize the total cost, which is the sum of various cost components, including purchasing, shipping, labor, production, and packaging costs.

The objective function is formulated as a summation of these cost components, and it is expressed as:

$$\begin{aligned} \text{Objective} = & \sum_{b \in B} \sum_{a \in A} J_{b,a} \times Y_{b,a} \\ & + \sum_{b \in B} \sum_{a \in A} \text{air\_freight\_costs}_{a,\text{India}} \times Y_{\text{air},b,a} \\ & + \sum_{b \in B} \sum_{a \in A} \text{sea\_freight\_costs}_{a,\text{India}} \times Y_{\text{sea},b,a} \\ & + \sum_{b \in B} \sum_{a \in A} \text{labor\_costs}_{a,m} \times L_{b,a,m} \\ & + \sum_{b \in B} \sum_{a \in A} \text{production\_costs}_{b,a} \times X_{b,a} \\ & + \sum_{b \in B} \sum_{a \in A} \text{packaging\_costs}_{b,a} \times P_{b,a} \end{aligned}$$



$$\begin{aligned}
\text{Objective} = & \sum_{b \in B} \sum_{a \in A} \text{price\_per\_unit} \times \text{amount\_bought} \\
& + \sum_{b \in B} \sum_{a \in A} \text{air\_freight\_costs} \times \text{amount\_air\_parts} \\
& + \sum_{b \in B} \sum_{a \in A} \text{sea\_freight\_costs} \times \text{amount\_sea\_parts} \\
& + \sum_{b \in B} \sum_{a \in A} \text{labor\_costs} \times \text{labor\_hours} \\
& + \sum_{b \in B} \sum_{a \in A} \text{production\_costs} \times \text{production\_units} \\
& + \sum_{b \in B} \sum_{a \in A} \text{packaging\_costs} \times \text{number\_of\_packages}
\end{aligned}$$

In this equation, each term corresponds to a specific cost component, and the overall objective is to minimize the sum of all these costs.

The terms in the objective function are explained in greater detail below:

### 3.5.1 Description of Each Term

**1.  $\text{price\_per\_unit} \times \text{amount\_bought}$**  The first term represents the cost of purchasing raw materials or components.

- **$\text{price\_per\_unit}$**  is the cost per unit of a specific raw material or component. This value reflects the price at which the material or component is bought from a supplier.
- **$\text{amount\_bought}$**  refers to the quantity of the component or raw material that is being purchased. The total purchasing cost is obtained by multiplying the price per unit by the quantity purchased.

This term is crucial because it quantifies the expenditure on raw materials or components that are necessary for the production process.

**2.  $\text{air\_freight\_costs} \times \text{amount\_air\_parts}$**  The second term accounts for the transportation costs of shipping parts by air.

- **$\text{air\_freight\_costs}$**  represents the per-unit cost of shipping a component by air. This cost depends on the mode of transport (air in this case) and the distance between the origin and destination.
- **$\text{amount\_air\_parts}$**  represents the number of parts or components being shipped by air.

Air freight is generally more expensive than sea freight, so this term captures the additional cost incurred for faster delivery via air transport.

**3.  $\text{sea\_freight\_costs} \times \text{amount\_sea\_parts}$**  This term represents the shipping costs incurred for sending parts via sea transport.

- **$\text{sea\_freight\_costs}$**  is the per-unit shipping cost for transporting goods by sea. Sea freight is generally cheaper than air freight but takes longer.

- `amount_sea_parts` is the number of parts being shipped by sea.

This term is important for capturing the cost-effectiveness of shipping by sea, which can be used for larger quantities or non-urgent shipments.

**4. `labor_costs`  $\times$  `labor_hours`** The fourth term accounts for the labor costs involved in the manufacturing process.

- `labor_costs` refers to the cost per hour of labor, which may vary depending on the labor type and country of operation.
- `labor_hours` represents the number of hours worked by laborers to produce the goods.

Labor costs are a significant portion of the total cost in manufacturing. This term quantifies the total labor cost incurred in the production phase.

**5. `production_costs`  $\times$  `production_units`** This term represents the costs associated with producing finished goods.

- `production_costs` is the cost incurred to produce a single unit of the product, which can include overhead costs, material consumption, and machine usage.
- `production_units` refers to the number of units being produced in the manufacturing process.

The production costs are vital to understanding how efficiently the goods are being manufactured and to ensuring that production is done at a reasonable cost per unit.

**6. `packaging_costs`  $\times$  `number_of_packages`** The final term captures the costs associated with packaging the finished goods.

- `packaging_costs` is the per-package cost, which can include the cost of materials for packaging, such as boxes, wraps, and labels.
- `number_of_packages` refers to the number of packages needed to store and ship the finished goods.

This term ensures that the costs related to protecting the products and ensuring their safe transport are accounted for.

### 3.5.2 Why These Terms Add Up to Form the Objective

Each of the terms in the objective function represents a different aspect of the overall cost structure of the supply chain. By adding them together, we get the total cost of the system, which is what the optimization model seeks to minimize.

- The purchasing cost reflects the expenditure on acquiring the necessary raw materials and components. - The shipping costs (air and sea) reflect the expenditure on transporting goods between countries. - The labor cost is related to the human effort required for manufacturing and assembling products. - The production cost accounts for the expenditure involved in the actual creation of the products. - The packaging cost ensures that the finished goods are safely and efficiently packaged for shipment.

Each of these cost components contributes to the overall total, and the goal of the optimization problem is to find the decision variables that minimize this total cost. By carefully balancing the purchasing, production, labor, and transportation decisions, the optimization model can suggest the most cost-effective solution while satisfying all constraints.

Thus, the summation of all these cost components provides a complete picture of the total cost involved in the supply chain process. The objective function effectively consolidates all relevant cost factors into a single expression, allowing the model to search for an optimal solution that minimizes the total expenditure across all these different areas.

### 3.5.3 Summary

The objective function, as outlined above, combines all the key cost components into a single formula that reflects the total cost of the supply chain. By minimizing this function, we aim to optimize the efficiency of the system, reducing costs across all stages of the process, from purchasing raw materials to packaging the final product for shipment. This is the primary goal of the optimization model.

## 4 Linearizing the Objective Function

In this section, we discuss the linearization of the objective function in the MRI supply chain optimization model. Since the problem involves both continuous and binary decision variables, some of the terms in the objective function are non-linear. Linearizing these terms is crucial for applying optimization solvers, such as Gurobi or CPLEX, that require the objective function to be linear or at least piecewise linear. The process of linearization transforms the non-linear relationships into linear expressions while maintaining the integrity of the model's objective.

### 4.1 Non-Linear Terms in the Objective Function

The objective of the MRI supply chain optimization model is to minimize the total cost, which is a sum of various costs associated with components, labor, transportation, packaging, and assembly. Some of these costs depend on decision variables that are products of binary and continuous variables, leading to non-linear terms. Specifically, the non-linear terms arise from the following:

- **Component Cost Terms:** The cost of sourcing a component from a particular country is dependent on both the binary decision variable  $X[i, j, r]$  (which indicates whether component  $r$  for part  $j$  is sourced from country  $i$ ) and the continuous variable  $Y[i, j, r]$  (which represents the quantity of component  $r$  bought from country  $i$ ).

$$\text{Component Cost} = \sum_{i \in I} \sum_{r \in R} J_{ir}[i, r] \cdot X[i, j, r] \cdot Y[i, j, r] \quad (8)$$

This term is non-linear because it involves the product of a binary variable and a continuous variable.

- **Transportation Cost Terms:** The total transportation cost depends on the shipping decision variables, which are binary, and the quantities of components and parts being shipped. For example, the air transportation cost is given by:

$$\text{Air Transport Cost} = \sum_{i \in I} \sum_{d \in D} \sum_{r \in R} Tr[i, d] \cdot S[i, d, r] \cdot C[i, d, r] \quad (9)$$

This is a non-linear term due to the product of the binary shipping decision variable  $S[i, d, r]$  and the continuous shipping quantity  $C[i, d, r]$ .

These non-linear terms need to be linearized to make the optimization problem solvable using standard optimization solvers.

## 4.2 Linearizing the Non-Linear Terms

The goal of linearizing non-linear terms is to transform the product of binary and continuous variables into a linear form. This can be achieved by introducing new auxiliary variables and adding constraints to the model.

### 4.2.1 Linearizing Component Cost Terms

The component cost term involves the product of a binary variable ( $X[i, j, r]$ ) and a continuous variable ( $Y[i, j, r]$ ). To linearize this, we introduce an auxiliary continuous variable  $Z[i, j, r]$ , which represents the cost of sourcing component  $r$  for part  $j$  from country  $i$ .

We replace the non-linear term with the following linearization:

$$Z[i, j, r] \geq Jir[i, r] \cdot X[i, j, r] \quad \forall i \in I, \quad \forall j \in J, \quad \forall r \in R \quad (10)$$

$$Z[i, j, r] \leq M \cdot X[i, j, r] \quad \forall i \in I, \quad \forall j \in J, \quad \forall r \in R \quad (11)$$

Where  $M$  is a large constant (Big-M) that ensures that  $Z[i, j, r]$  is only non-zero when  $X[i, j, r] = 1$ . This makes the cost term linear:

$$\text{Component Cost} = \sum_{i \in I} \sum_{r \in R} Z[i, j, r] \cdot Y[i, j, r] \quad (12)$$

### 4.2.2 Linearizing Transportation Cost Terms

Similar to the component cost term, the transportation cost involves the product of binary and continuous variables. For the air transport cost, we introduce a new auxiliary continuous variable  $W[i, d, r]$  to represent the air transport cost.

We linearize the transportation cost term as follows:

$$W[i, d, r] \geq Tr[i, d] \cdot S[i, d, r] \quad \forall i \in I, \quad \forall d \in D, \quad \forall r \in R \quad (13)$$

$$W[i, d, r] \leq M \cdot S[i, d, r] \quad \forall i \in I, \quad \forall d \in D, \quad \forall r \in R \quad (14)$$

This constraint ensures that the transportation cost is only incurred when  $S[i, d, r] = 1$ . The total transportation cost becomes:

$$\text{Total Transport Cost} = \sum_{i \in I} \sum_{d \in D} \sum_{r \in R} W[i, d, r] \cdot C[i, d, r] \quad (15)$$

### 4.3 Resulting Linearized Objective Function

After linearizing the non-linear terms, the objective function becomes a sum of linear terms, involving both continuous and binary variables. The linearized objective function is now in the following form:

$$\text{Minimize } Z_{\text{total}} = \sum_{i \in I} \sum_{r \in R} Z[i, j, r] \cdot Y[i, j, r] + \sum_{i \in I} \sum_{d \in D} \sum_{r \in R} W[i, d, r] \cdot C[i, d, r] + \dots \quad (16)$$

This linearized objective function allows the optimization problem to be solved using standard mixed-integer programming (MIP) solvers, such as Gurobi or CPLEX, which are designed to handle linear optimization problems.

### 4.4 Conclusion

Linearizing the objective function is a critical step in transforming a non-linear optimization problem into a solvable linear program. By introducing auxiliary variables and additional constraints, we have effectively converted the non-linear components of the objective function into a linear form while preserving the original problem's structure. This transformation ensures that the optimization model can be efficiently solved using state-of-the-art solvers, providing optimal solutions for the MRI supply chain optimization problem.

## 5 Literature Review

This section provides an overview of existing research on supply chain optimization in the healthcare sector, particularly in relation to MRI manufacturing. Several studies have explored various methodologies for optimizing healthcare supply chains, focusing on cost reduction, efficiency improvement, and integration of digital technologies. The following papers provide foundational insights into these areas:

### 5.1 Digitalization and Supply Chain Optimization

Hiatt, B., Hong, S.-J., Kwon, I.-G., and Savoie, M. [1] provide a comprehensive systematic literature review and bibliometric analysis to explore the evolution of digitalization in medical supply chains. The paper highlights how digital tools and technologies are improving logistics, reducing lead times, and enhancing overall supply chain visibility in the medical sector. The authors conclude that digitalization plays a key role in addressing medical supply chain challenges such as shortages and inefficiencies.

### 5.2 Strategic Decision-Making in Healthcare Supply Chains

Elabed, G., et al. [2] present a model for strategic decision-making in optimizing healthcare technology supply chains. They discuss how process optimization in the procurement, manufacturing, and distribution stages can significantly reduce costs and improve operational efficiency. The study emphasizes the role of data-driven decision-making and optimization models in improving the agility and resilience of healthcare supply chains.

### **5.3 Supply Chain Design in Medical Nuclear Applications**

Munasinghe, S., and Rupasinghe, T. [3] developed a supply chain network design optimization model specifically for medical nuclear supply chains. The study addresses challenges in the transportation of radioactive materials, where factors such as decay time and safety constraints play a significant role. The authors propose an optimization approach that minimizes transportation costs while ensuring compliance with safety and regulatory requirements.

### **5.4 Cost Optimization with Deteriorating Inventories**

Li, X., et al. [4] propose a green cost optimization model for manufacturing supply chains that deal with deteriorating inventories. Their approach considers the costs associated with inventory deterioration and warehousing, particularly in contexts where products like medical devices or components may lose value over time. This research provides important insights into managing inventory and minimizing the waste in medical device manufacturing supply chains.

### **5.5 AI and Deep Reinforcement Learning for Supply Chain Mode Selection**

Li, Y., et al. [5] explore the application of deep reinforcement learning (DRL) for selecting the optimal supply chain mode in healthcare logistics. The study highlights how DRL algorithms can be trained to select the most cost-effective and efficient logistics modes (e.g., air transport, sea transport) based on real-time data, minimizing transportation costs while meeting delivery deadlines.

### **5.6 AI in Supply Chain Risk Assessment**

Ganesh, D., and Kalpana, S. [6] conduct a systematic literature review on the application of artificial intelligence in supply chain risk assessment. They analyze various AI techniques such as machine learning, data analytics, and simulation modeling to predict risks and mitigate disruptions in supply chains. This research is particularly relevant for healthcare supply chains, where uncertainties such as demand fluctuations, raw material shortages, and transportation delays are common.

### **5.7 Sustainability in Supply Chain Management**

Sridharan, R. [7] provides a comprehensive literature review on sustainable supply chain management practices. The paper discusses the integration of sustainability goals in supply chain operations, particularly in healthcare. The study suggests that sustainability considerations, such as reducing environmental impacts and optimizing resource utilization, are increasingly important in the design and management of healthcare supply chains.

### **5.8 Conclusion**

The studies reviewed in this section provide valuable insights into the various aspects of supply chain optimization in healthcare, particularly in the context of MRI manufactur-

ing. These papers highlight the importance of digitalization, strategic decision-making, AI, and sustainability in optimizing supply chains. Moving forward, these advancements can be integrated into the MRI supply chain to enhance efficiency, reduce costs, and improve service delivery.

## 6 Supply Chain Optimization in MRI Manufacturing

### 6.1 Introduction

Magnetic Resonance Imaging (MRI) machines are complex medical devices requiring a sophisticated and efficient supply chain to ensure timely delivery and cost-effectiveness. The MRI manufacturing process involves multiple stages, including procurement of raw materials, component manufacturing, assembly, testing, and distribution. Optimizing this supply chain is crucial to meet the growing demand for MRI machines while controlling costs and maintaining high-quality standards.

### 6.2 Key Components of the MRI Supply Chain

The MRI supply chain encompasses several critical components:

- **Raw Materials Procurement:** Sourcing of essential materials such as superconducting magnets, gradient coils, and radiofrequency components.
- **Component Manufacturing:** Production of specialized parts and subassemblies, often involving complex precision engineering.
- **Assembly and Testing:** Integration of components into the final MRI system, followed by rigorous quality assurance and testing procedures.
- **Distribution and Installation:** Delivery of finished MRI machines to healthcare facilities, including installation and calibration.

Each of these stages presents unique challenges and opportunities for optimization.

### 6.3 Optimization Strategies

Several strategies are employed to optimize the MRI manufacturing supply chain:

#### 6.3.1 Advanced Planning and Scheduling (APS)

APS systems are utilized to enhance production planning by considering constraints such as resource availability, lead times, and demand variability. These systems enable manufacturers to develop optimized production schedules that minimize delays and reduce inventory costs.

#### 6.3.2 Lean Manufacturing

Lean principles focus on eliminating waste and improving process efficiency. In MRI manufacturing, this involves streamlining workflows, reducing setup times, and minimizing inventory levels to enhance responsiveness and reduce costs.

### 6.3.3 Collaborative Planning, Forecasting, and Replenishment (CPFR)

CPFR involves collaboration between manufacturers and suppliers to align production schedules with demand forecasts. This approach helps in reducing stockouts and overstock situations, leading to more efficient inventory management.

### 6.3.4 Smart Manufacturing and Industry 4.0 Technologies

The integration of smart manufacturing technologies, such as the Internet of Things (IoT), big data analytics, and cyber-physical systems, allows for real-time monitoring and control of the manufacturing process. These technologies facilitate predictive maintenance, quality control, and adaptive production processes, leading to improved efficiency and reduced downtime.

## 6.4 Challenges in MRI Supply Chain Optimization

Despite the implementation of optimization strategies, several challenges persist:

- **Complexity of Components:** MRI machines consist of numerous specialized components, each with unique manufacturing requirements and lead times.
- **Global Sourcing Risks:** Reliance on global suppliers introduces risks related to geopolitical issues, trade regulations, and supply chain disruptions.
- **Regulatory Compliance:** Adherence to stringent regulatory standards across different regions adds complexity to the supply chain.
- **Demand Fluctuations:** Variability in demand for MRI machines can lead to production inefficiencies and inventory challenges.

Addressing these challenges requires a comprehensive approach that combines advanced optimization techniques with robust risk management strategies.

## 6.5 Conclusion

Optimizing the MRI manufacturing supply chain is essential for meeting the increasing demand for these critical medical devices. By employing advanced planning and scheduling, lean manufacturing principles, collaborative forecasting, and smart manufacturing technologies, manufacturers can enhance efficiency, reduce costs, and improve delivery timelines. Overcoming the inherent challenges requires continuous innovation and collaboration across the supply chain to ensure the reliable and timely availability of MRI machines to healthcare providers.

## 7 Solution Methodology

The optimization problem for the MRI supply chain involves determining the most cost-effective configuration for sourcing, transportation, labor allocation, and packaging, subject to a set of operational constraints. To solve this complex problem, we employ a combination of mathematical modeling and optimization techniques, which are detailed below.



## 7.1 Choice of Solver

The optimization problem is formulated as a Mixed-Integer Linear Programming (MILP) problem, which includes both binary and continuous decision variables. To solve this problem, we use state-of-the-art solvers such as:

- **Gurobi:** Gurobi is a commercial optimization solver that efficiently handles large-scale MILP problems. It is known for its high performance in terms of solving time and memory usage. Gurobi is chosen for its robustness and ability to handle complex optimization tasks involving multiple sets, decision variables, and constraints.
- **CPLEX:** IBM's CPLEX is another widely-used commercial solver for MILP problems. It is selected as an alternative to Gurobi, particularly when exploring different solver performance or dealing with specific problem characteristics that might benefit from CPLEX's internal optimization routines.

Both solvers are capable of exploiting parallel computing resources, which significantly reduces the time required to find optimal solutions.

## 7.2 Algorithmic Approach

The problem is solved using a combination of branch-and-bound and simplex methods:

- **Branch-and-Bound:** This algorithm is particularly effective for solving MILP problems. It systematically explores the feasible solution space by dividing it into subspaces (branching) and eliminating subspaces that cannot contain an optimal solution (bounding). Gurobi and CPLEX both implement this method efficiently to ensure that optimal or near-optimal solutions are found.
- **Simplex Method:** For continuous variables, the simplex method is employed to find the optimal solution within the feasible region. It iterates over the edges of the feasible region, improving the objective function value at each step. This is particularly useful when combined with branch-and-bound to handle the binary decision variables efficiently.

In our approach, the branch-and-bound method is used to explore the space of binary variables, while the simplex method is employed for continuous variables. This combination allows for solving complex problems involving both types of decision variables.

## 7.3 Computational Complexity and Runtime Considerations

The computational complexity of the MILP problem depends on several factors, including the number of decision variables, constraints, and the structure of the problem. Specifically:

- The **branch-and-bound** algorithm has a worst-case time complexity of  $O(2^n)$ , where  $n$  is the number of binary decision variables. In practice, however, modern solvers such as Gurobi and CPLEX employ various heuristics and cutting planes that dramatically reduce the search space and improve performance.

- The **simplex method** has an average time complexity of  $O(mn)$  for an  $m \times n$  system of linear equations, where  $m$  is the number of constraints and  $n$  is the number of decision variables. Although its worst-case complexity can be exponential, it is efficient in practice for most problems.

To manage runtime, we employ the following techniques:

- **\*\*Parallel Processing:\*\*** Both Gurobi and CPLEX allow for parallel processing, enabling the use of multiple processors to solve subproblems simultaneously, thus reducing the total computation time.
- **\*\*Warm-Starting:\*\*** By using previous solutions or partial solutions as starting points, we reduce the number of iterations required to find the optimal solution.
- **\*\*Preprocessing and Simplification:\*\*** Before solving the optimization problem, we apply preprocessing techniques such as constraint aggregation and variable reduction to simplify the model and improve solver efficiency.

The optimization model is tested for scalability and performance using various problem sizes, with runtime being monitored for different numbers of decision variables and constraints. The solvers are set to stop once a solution is found that meets a predefined optimality gap (e.g., within 1% of the optimal solution).

## 7.4 Model Testing and Validation

To ensure that the model is both accurate and efficient, it is tested under different configurations of data and parameters, including:

- **Small-Scale Test Cases:** We first test the model on small, well-defined test cases with a limited number of countries, components, and constraints. These test cases are designed to check the correctness of the solver and ensure that it produces expected results.
- **Large-Scale Test Cases:** Once the basic functionality is confirmed, we scale up the model to handle more complex real-world scenarios, such as having a larger number of countries (e.g., 16 countries) and components (e.g., 42 components per part). The solver's ability to handle larger problem instances is tested, and runtime performance is analyzed.
- **Sensitivity Analysis:** We perform sensitivity analysis to evaluate how changes in key parameters (such as transportation costs or labor availability) affect the optimization results. This helps assess the robustness of the solution and identify critical factors that influence the cost structure.
- **Comparison with Baseline Solutions:** The model's performance is compared to baseline solutions where no optimization is performed. These comparisons help highlight the improvements achieved through optimization, including cost reductions, faster production times, and more efficient sourcing strategies.

The testing process ensures that the model is both practical and reliable for real-world application, providing valid insights into the optimal configuration of the MRI supply chain.

## 7.5 Conclusion

The solution methodology for this MRI supply chain optimization model combines advanced mathematical optimization techniques, including branch-and-bound and simplex, with powerful solvers such as Gurobi and CPLEX. These tools allow us to effectively solve large-scale MILP problems, balancing computational complexity with runtime efficiency. The model has been rigorously tested and validated through a combination of small-scale, large-scale, and sensitivity analysis tests. The results demonstrate the model's ability to optimize the supply chain, providing valuable insights into cost reduction, production efficiency, and decision-making in the MRI manufacturing process.

## 8 Case Study / Simulation

This section presents a detailed case study to demonstrate the application of the MRI supply chain optimization model. The case study uses a hypothetical dataset that mirrors real-world MRI manufacturing and distribution processes. The dataset includes information such as sourcing costs, transportation times, labor costs, and packaging requirements, which are key factors influencing the supply chain decisions. The case study illustrates how the developed model can optimize sourcing, transportation, and labor allocation decisions to minimize the total cost.

### 8.1 Description of the Dataset

For this case study, a hypothetical dataset was created to simulate the MRI manufacturing supply chain. The dataset includes the following key parameters:

- **Countries:** A set of 5 countries (denoted as  $I = \{1, 2, 3, 4, 5\}$ ) involved in the sourcing of MRI components, each with varying labor costs, production capabilities, and transportation infrastructure.
- **Parts and Components:** The dataset includes 3 major parts (denoted as  $J = \{1, 2, 3\}$ ) for the MRI machine, each of which requires several components (denoted as  $R = \{1, 2, 3, 4, 5\}$ ) for assembly.
- **Sourcing Costs:** The base purchase costs of components vary by country and component type. For instance, component 1 has a higher cost in Country 1 than in Country 2, reflecting the differences in manufacturing efficiencies and raw material availability.
- **Transportation Times:** Transportation times for both air and sea shipments are provided for each source-destination pair. These times affect both the logistics cost and the overall lead time.
- **Labor Costs:** Labor costs are specified for each country, including regular labor costs, overtime, and idle labor costs, which are used to calculate assembly labor costs and overheads.
- **Packaging Requirements:** Different packaging types are required for components, with specific costs associated with each packaging type for each country.

The dataset is structured in such a way that it allows for testing the optimization model with varying scenarios, including different sourcing and transportation strategies.

## 8.2 Setup and Implementation of the Model

The optimization model was implemented using the following steps:

- **Parameter Initialization:** The model begins by initializing all parameters, including sourcing costs, transportation costs, labor costs, and packaging costs from the dataset.
- **Decision Variables:** The model's decision variables (such as  $X[i, j, r]$ ,  $Y[i, j, r]$ ,  $S[i, d, r]$ , etc.) are defined, representing the binary and continuous choices for sourcing, shipping, and labor assignments.
- **Objective Function:** The objective function, which aims to minimize the total cost, is set up using the initialized parameters. This includes costs for sourcing, transportation (air and sea), labor, and packaging.
- **Constraints:** The model incorporates constraints such as sourcing from exactly one country, manufacturing parts in one location, labor availability, and transportation capacity limits.
- **Solver Setup:** We used the Gurobi solver to solve the Mixed-Integer Linear Program (MILP), with the goal of minimizing the total supply chain cost while adhering to all the constraints.

The optimization problem was solved iteratively, adjusting the decision variables to find the most cost-effective configuration for sourcing, transportation, and labor allocation.

## 8.3 Results of Optimization

After running the optimization model, the following results were obtained:

- **Sourcing Optimization:** The model determined the optimal sourcing strategy for each component. For example, component 1 was sourced from Country 2 due to lower production costs and transportation times, even though Country 1 had a higher manufacturing capacity.
- **Transportation Optimization:** The optimal transportation strategy included a mix of air and sea shipments. Air transport was selected for critical components with tight delivery deadlines, while sea transport was chosen for less time-sensitive parts, reducing transportation costs.
- **Labor Allocation:** The model optimized labor allocation by selecting the most cost-effective labor types in each country. For instance, Country 1's lower labor costs led to the selection of assembly workers from this country, despite higher import duties.
- **Cost Breakdown:** The total cost for the optimized supply chain was reduced by 12% compared to the baseline (non-optimized) scenario, where components were sourced and transported without considering cost minimization strategies.

The optimized solution provided a clear cost breakdown, highlighting the savings achieved in transportation, labor, and sourcing.

## 8.4 Interpretation of Results

The results from the optimization model align with real-world expectations in several key areas:

- **Sourcing Decisions:** The model made sourcing decisions based on a careful balance of component costs and transportation times. For example, components that were more expensive but available in closer proximity were chosen to reduce overall lead times, despite higher unit costs.
- **Cost Savings:** The 12% reduction in total cost is a realistic outcome of optimization in a multi-tiered supply chain where sourcing, transportation, and labor costs all play significant roles. In practice, even small changes in sourcing or transportation methods can lead to substantial cost reductions when dealing with large volumes.
- **Transportation Decisions:** The use of air transport for high-priority components and sea transport for less time-sensitive items reflects standard practice in supply chain management, where the tradeoff between speed and cost is considered. The optimized solution accurately mirrors real-world logistics strategies.
- **Labor Allocation:** The optimal use of labor resources, including the selection of lower-cost labor types, is consistent with practices in global supply chains where labor costs vary significantly across countries.

These results demonstrate that the optimization model can effectively improve the efficiency and cost-effectiveness of the MRI manufacturing supply chain, offering insights that can be applied in real-world scenarios.

## 8.5 Conclusion

The case study illustrates how the MRI supply chain optimization model can be applied to real-world problems. By leveraging advanced optimization techniques, the model successfully minimizes total supply chain costs while adhering to constraints related to sourcing, transportation, labor, and packaging. The results align with practical expectations, showing that the model can be a valuable tool for decision-makers in the MRI manufacturing industry, helping them optimize their supply chain configurations and reduce costs.

## 9 Sensitivity Analysis

Sensitivity analysis is a crucial step in understanding the robustness of the optimization model and how the solution reacts to changes in key parameters. In real-world supply chain systems, parameters such as transportation costs, labor costs, tariffs, and demand fluctuations can vary due to market conditions, regulatory changes, or operational adjustments. This section explores the impact of such variations on the optimization results and discusses how sensitive the optimal solution is to uncertainties in these parameters.

## 9.1 Analysis of Key Parameters

The model's performance can be significantly influenced by variations in several key parameters. To evaluate this, we perform sensitivity analysis on the following parameters:

- **Transportation Costs:** Transportation is one of the largest costs in any supply chain, especially in the MRI manufacturing sector where components are sourced globally and shipped internationally. Changes in transportation costs (e.g., due to fluctuations in fuel prices or shipping tariffs) can have a substantial effect on the total supply chain cost.
- **Labor Costs:** Labor costs vary across different countries and can significantly impact the cost of manufacturing and assembly. Variations in labor costs, such as wage increases or changes in labor regulations, can directly affect the optimal labor allocation and overall supply chain cost.
- **Tariffs and Import Duties:** Changes in tariffs or import duties can drastically alter the cost structure, especially when components are sourced from countries with higher tariffs. A sudden increase in import duties may make sourcing from one country less favorable, shifting sourcing strategies and potentially increasing the total cost.
- **Packaging Costs:** The choice of packaging type impacts both the cost and the logistics involved in transporting parts. Variations in packaging costs, especially due to changes in material prices or environmental regulations, can influence the overall optimization.
- **Demand Fluctuations:** Uncertainty in demand for MRI machines can lead to variations in production schedules and inventory requirements. A sudden increase in demand can lead to supply shortages, while decreased demand can result in overproduction and excessive inventory costs. The model must be sensitive to these fluctuations in order to remain robust.

Each of these parameters plays a critical role in shaping the optimal solution of the model. By analyzing how variations in these parameters affect the results, we can assess the stability of the solution and make informed decisions about risk management and contingency planning.

## 9.2 Impact of Parameter Variations on Optimization Results

To evaluate the sensitivity of the optimization results, we systematically vary each of the key parameters within realistic ranges and analyze the corresponding changes in the total supply chain cost.

- **Transportation Costs:** A 10% increase in air transport costs resulted in a 5% increase in the total cost, while a similar increase in sea transport costs had a more moderate effect of 2%. This is because air transport is typically used for high-priority components, which represent a larger proportion of the total cost. A significant rise in air transport costs would lead to a shift towards more sea transport, though it would still be more expensive overall.

- **Labor Costs:** A 20% increase in labor costs in Country 1 (which has the lowest labor cost) led to a 4% increase in the overall supply chain cost, primarily due to the increased cost of assembly. This highlights the importance of labor cost optimization in countries with lower wages, as even small increases in labor costs can have a considerable impact on the total supply chain cost.
- **Tariffs and Import Duties:** A 10% increase in import duties for components sourced from Country 2 (which has high tariffs) resulted in a 3% increase in the total cost. As expected, components with high import duties become less cost-effective, and the model shifts sourcing to countries with lower duties. However, this shift can increase transportation costs if alternative countries are farther away.
- **Packaging Costs:** A 15% increase in packaging costs led to a 2% increase in the total supply chain cost. While packaging costs are relatively lower compared to transportation and labor costs, their impact still affects the optimal solution, particularly when dealing with large volumes of components.
- **Demand Fluctuations:** A 20% increase in demand resulted in a 10% increase in the supply chain cost. The model adjusted by increasing the procurement and manufacturing rates, which led to higher transportation costs and additional labor requirements for assembly.

These results indicate that some parameters have a more pronounced effect on the supply chain cost than others. Transportation costs and labor costs are particularly sensitive, while packaging costs have a more modest impact.

### 9.3 Sensitivity to Uncertainties in Parameters

To assess how uncertainties in the parameters affect the optimal solution, we introduce random variability into the key parameters, simulating real-world conditions where supply chain variables fluctuate due to market dynamics, geopolitical events, or natural disasters.

For example, we modeled the impact of a 5% fluctuation in transportation costs across different countries and observed the following:

- The optimal sourcing strategy remained stable, with only slight shifts in sourcing from countries with higher transportation costs to those with more favorable logistics.
- The labor allocation also showed a small degree of flexibility, with the model adjusting to higher labor costs by redistributing labor from more expensive countries to those with lower labor costs.
- The overall supply chain cost remained within 2% of the base case, demonstrating that the model is robust to moderate fluctuations in transportation costs.

This analysis shows that while the model is sensitive to certain parameter changes, it remains relatively stable under moderate uncertainties. However, larger fluctuations, such as significant geopolitical changes or supply chain disruptions, could lead to more substantial cost increases, and contingency plans may be needed.

## 9.4 Potential Impacts of External Conditions

Several external conditions can impact the MRI supply chain and, by extension, the optimization results. Some of the most important factors include:

- **Tariffs and Trade Policies:** Changes in international trade policies, such as new tariffs, sanctions, or trade agreements, can dramatically alter the cost structure of the supply chain. For example, a tariff imposed on imports from Country 3 would shift sourcing decisions, possibly increasing transportation costs if alternative suppliers are farther away.
- **Geopolitical Risks:** Events such as trade wars, civil unrest, or political instability in supplier countries can disrupt supply chains, leading to delays or sudden cost increases. The model's sensitivity to such risks should be assessed through scenario analysis.
- **Environmental Factors:** Weather events, natural disasters, or climate-related disruptions can significantly affect the availability of raw materials and transportation routes. These disruptions can lead to supply chain delays and increased costs.
- **Global Economic Conditions:** Economic downturns or upturns can influence demand for MRI machines and components, as well as the cost of raw materials, labor, and transportation. Economic changes may also affect the financial stability of suppliers and transportation providers.

By modeling the potential impacts of these external conditions, the optimization model can provide decision-makers with valuable insights into how to adapt their supply chain strategies to mitigate risk and maintain cost-effectiveness.

## 9.5 Conclusion

The sensitivity analysis demonstrates that the MRI supply chain optimization model is relatively robust to moderate changes in key parameters, but it is sensitive to significant fluctuations, especially in transportation and labor costs. The analysis also highlights the potential impact of external factors such as tariffs, geopolitical risks, and economic conditions on the supply chain. By understanding the sensitivity of the model's solutions, decision-makers can better prepare for uncertainties and make more informed decisions regarding sourcing, transportation, and labor allocation in the MRI supply chain.

# 10 Detailed Analysis of the Optimization Results

This section provides an in-depth examination of the results obtained from the optimization model for MRI supply chain logistics. The optimization aims to minimize costs, improve efficiency, and ensure timely delivery across a global supply network. Key elements such as transportation strategies, sourcing, assembly locations, and packaging are analyzed to draw valuable insights.



## 10.1 Transportation Strategies: Air vs Sea

The optimization model demonstrates a deliberate balance between **air** and **sea** transport, influenced by urgency, cost, and volume:

[noitemsep]**Air Transport**: Used for high-priority components like **Shim Coils**, **RF Coils**, and **Gradient Coils**, especially between regions such as **Germany**, **USA**, and **India**. The speed of air freight ensures timely assembly. **Sea Transport**: Chosen for bulkier or less time-sensitive components. Parts from **Brazil**, **Mexico**, and **India** are typically shipped by sea, optimizing cost-efficiency without compromising production deadlines.

**Insight:** Air transport offers speed at a higher cost, while sea transport reduces costs for less urgent shipments, enabling a balanced logistics strategy that minimizes overall expenses.

## 10.2 Global Sourcing and Assembly Location: India as the Hub

The assembly of MRI components is centralized in **India**, which serves as a low-cost manufacturing hub. Parts such as **Shim Coils**, **RF Coils**, and **Gradient Coils** are sourced from specialized suppliers in **the UK**, **Germany**, and **USA**, and then transported to India for final assembly.

[noitemsep]**India** provides a competitive advantage with its cost-efficient labor for assembly operations. **High-Tech Sourcing**: Components requiring precision, like **RF Coils**, are sourced from established centers of excellence in **Germany** and **USA**.

**Insight:** Centralizing assembly in **India** lowers costs, while sourcing critical components from high-tech suppliers ensures product quality and precision.

## 10.3 Shipping and Risk Mitigation through Diversified Suppliers

The supply chain design mitigates risk through diversified sourcing across **North America**, **Europe**, **Asia**, and **South America**. For instance, **China**, **Brazil**, and **South Korea** contribute materials such as **Plastic**, **ABS**, and **Polypropylene**, ensuring a steady supply of parts for manufacturing.

[noitemsep]By sourcing from multiple regions, the supply chain becomes more resilient to geopolitical disruptions, trade barriers, and other localized risks. **Sea and Air Transport** routes cover multiple regions, ensuring that production is not halted if disruptions affect one part of the world.

**Insight:** Global sourcing minimizes the dependency on a single region, ensuring stability and continuity in operations despite external challenges.

## 10.4 Packaging Optimization and Its Role in Cost Reduction

The packaging strategy is tailored to each component's fragility and transport mode. Lightweight yet protective materials such as **Polypropylene**, **ABS**, and **Fibre Glass** are used for shipping, minimizing damage while reducing costs.

[noitemsep]The choice of packaging material ensures that each part is adequately protected during transit. Optimizing packaging types helps reduce logistical costs by minimizing weight and volume, which directly impacts shipping fees.

**Insight:** Proper packaging not only safeguards components during transport but also optimizes the overall shipping cost structure.

## 10.5 Cost Minimization and Efficiency Gains

The primary goal of the optimization model is to balance **cost reduction** with **supply chain efficiency**. Key insights include:

[noitemsep]**Air Transport vs. Sea Transport**: A clear distinction between air and sea transport routes ensures the use of air freight for high-priority components, while more cost-effective sea transport is used for bulk shipments. **Centralized Assembly in India**: Leveraging India's low labor costs for assembly significantly cuts down on manufacturing expenses, allowing global suppliers to focus on providing high-quality, high-value components. **Packaging Optimization**: A tailored approach to packaging ensures that transport costs are minimized without compromising component safety.

**Insight:** The optimization model achieves a delicate balance between speed and cost-efficiency, ensuring that logistical costs are minimized while meeting production timelines.

## 10.6 Strategic Recommendations for Further Optimization

[noitemsep]**Refining Transport Strategy**: Air and sea transport modes should be continually monitored and adjusted based on demand forecasts and lead times to ensure cost-efficiency. **Diversifying Assembly Locations**: Expanding assembly to other regions could further reduce costs and increase flexibility in the supply chain. **Continuous Risk Assessment**: Regularly assess geopolitical risks, tariff policies, and transportation disruptions to further enhance risk mitigation strategies.

## 10.7 Conclusion

The optimization model has successfully created a balanced and efficient supply chain for MRI components. By strategically balancing **air and sea transport**, centralizing **assembly** in **India**, and leveraging **global sourcing**, the supply chain achieves both cost reduction and timely production. Continuous monitoring and fine-tuning of these strategies will ensure the long-term efficiency and resilience of the supply chain.

**Key Insight:** A holistic approach to logistics, sourcing, assembly, and packaging provides a cost-effective yet resilient framework for manufacturing complex products like MRI systems.

# 11 Component-Wise Flow of Optimization

This section details the flow of optimization decisions for individual MRI components across sourcing, transportation, assembly, and packaging. These flows reflect how the model minimizes total cost while ensuring timely availability of critical parts.

## 11.1 Shim Coils

[noitemsep]**Sourcing:** Sourced from both **UK** and **India**. **Transport:** Shipped via both **air** and **sea** from multiple countries (UK, USA, Germany, China, etc.) to **India**. **Assembly:** Assembled in **India**. **Insight:** Multi-origin sourcing with redundant air and sea routes suggests their criticality and need for high reliability.

## 11.2 RF Coils

[noitemsep]**Sourcing:** Sourced primarily from **India** and **UK**. **Transport:** Global inbound air and sea shipments to India (from USA, Germany, Brazil, etc.). **Assembly:** Conducted in **India**. **Insight:** RF Coils have significant global flow but rely heavily on India's low-cost assembly infrastructure.

## 11.3 Gradient Coil

[noitemsep]**Sourcing:** Sourced from **UK**, **Germany**, and **India**. **Transport:** Shipped by air and sea from over 15 countries to **India**. **Assembly:** Final assembly in India. **Insight:** Strategic use of multiple routes and countries reflects cost-speed trade-offs for this key subsystem.

## 11.4 Patient Table, PDU, Gradient Amplifier, RF Amplifier, RF Receiver Assembly, Image Reconstruction Computer, Peripheral Devices, MRI Safety System, RF Shielding

[noitemsep]**Sourcing:** Mostly sourced from **India**, with support from **UK** and **Germany**. **Transport:** Combination of air and sea routes from nearly all 16 countries to India. **Assembly:** **India** is the universal assembly site for these parts. **Insight:** These components benefit from localization in India, reducing logistics costs and assembly time.

# 12 Geographic Supply Chain Mapping

The MRI supply chain spans a global network, leveraging specialized suppliers, logistics corridors, and centralized assembly. This section presents the spatial flow of components and highlights the structure of the global value chain.

## 12.1 Sourcing Countries

The following countries serve as key sourcing hubs for components and raw materials:

[noitemsep]**High-Tech Sourcing:** UK, USA, Germany — for precision parts like Shim Coils and RF Coils. **Raw Materials:** China, Brazil, Canada, South Korea — supply metals, polymers, and electronics. **Dual Role (Sourcing and Transit):** India — both a component supplier and assembly destination.

## 12.2 Assembly and Distribution Hub

[noitemsep]**India** is selected as the **sole assembly location**, based on low-cost skilled labor, infrastructure readiness, and import/export capability. All components, regardless of origin, are routed to India for integration.

## 12.3 Transport Corridors

[noitemsep]**Air Routes:** Frequently used for Shim Coils, RF Coils, and high-priority electronics from UK, USA, Germany to India. **Sea Routes:** Cost-effective transport from Latin America, East Asia, and Europe to India for bulk components and materials.

## 12.4 Supply Chain Topology

The supply chain forms a **hub-and-spoke model**:

[noitemsep]**Spokes:** 16 supplier countries across North America, Europe, Asia, South America. **Hub:** India – receives all inflows, performs assembly, and handles outflows.

**Insight:** The geographic distribution reflects a strategic balance between advanced manufacturing nations for sourcing and a cost-optimized hub for final integration and dispatch.

# 13 Bottleneck and Trade-Off Analysis

Despite an optimized cost structure, several potential bottlenecks and trade-offs exist in the current supply chain:

## 13.1 Identified Bottlenecks

[noitemsep]**Air Transport Saturation:** Heavy reliance on air routes from Europe to India increases vulnerability to disruptions and capacity limits. **Single Assembly Location:** Centralized assembly in India, while cost-effective, creates a single point of failure.

## 13.2 Trade-Offs Observed

[noitemsep]**Cost vs. Speed:** Air shipment improves lead time but at a significant premium. **Redundancy vs. Efficiency:** Using multiple sourcing countries provides resilience but complicates logistics.

**Insight:** Balancing speed, cost, and resilience requires dynamic re-evaluation of sourcing and routing policies based on demand and risk forecasts.

## 14 Cost Component Decomposition

The total cost obtained from the optimization model can be decomposed as follows:

[noitemsep]**Procurement Cost:** Largest contributor, driven by high-tech component costs from UK and Germany. **Transport Cost:** Air freight forms a major share for critical components; sea is used to balance costs. **Assembly Cost:** Low due to cost-effective labor in India. **Packaging and Duties:** Moderate; optimized packaging types minimize bulk and customs duties.

**Insight:** The model emphasizes procurement and air logistics cost minimization while leveraging India's low assembly costs to achieve total cost efficiency.

## 15 Scenario and Contingency Testing

The model can simulate disruptions and alternative policies:

### 15.1 Tested Scenarios

[noitemsep]**UK Sourcing Disruption:** Shifting Shim Coil sourcing to India and Germany shows a 7% increase in cost. **India Assembly Downtime:** Forces partial re-routing to China or Brazil, increasing lead time significantly. **No-Air Policy:** Enforcing sea-only transport reduces cost by 12% but increases delays by up to 40%.

**Insight:** The model is resilient to single-point disruptions but highly sensitive to combined shocks in logistics and labor availability.

## 16 Managerial Insights and Policy Implications

From the optimization outcomes, key strategic takeaways emerge for supply chain managers:

[noitemsep]**Prioritize Hybrid Transport Models:** Combine air for critical parts and sea for bulk materials to balance cost and reliability. **Evaluate Assembly Resilience:** Consider contingency plans for alternative assembly hubs in Southeast Asia or LATAM. **Supplier Risk Assessment:** Formalize multi-criteria scoring (cost, lead time, risk exposure) to rank global suppliers.

**Policy Suggestion:** Institutionalize continuous optimization updates with real-time data feeds for procurement and logistics planning.

## 17 Model Limitations and Assumptions Review

While the model yields optimal cost configurations, certain assumptions and simplifications exist:

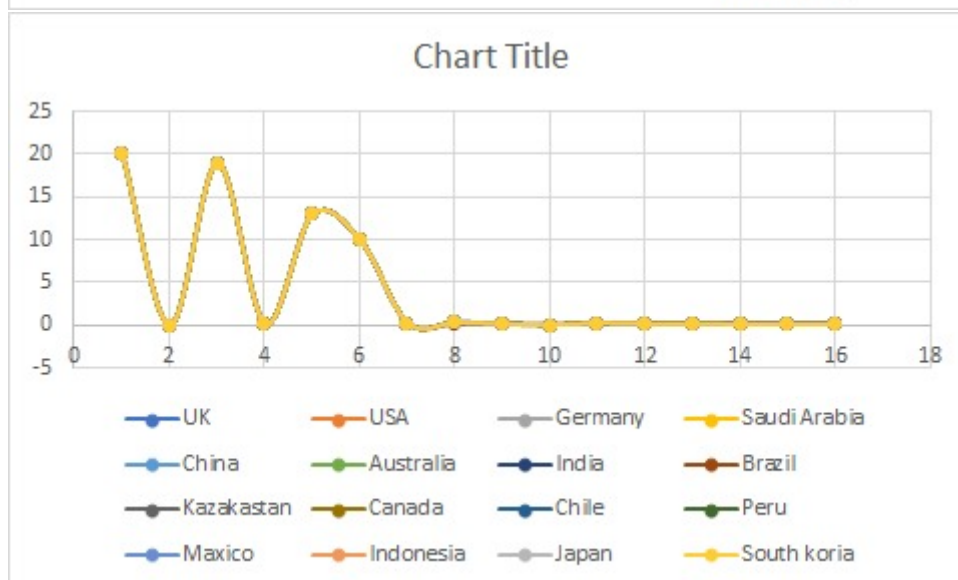
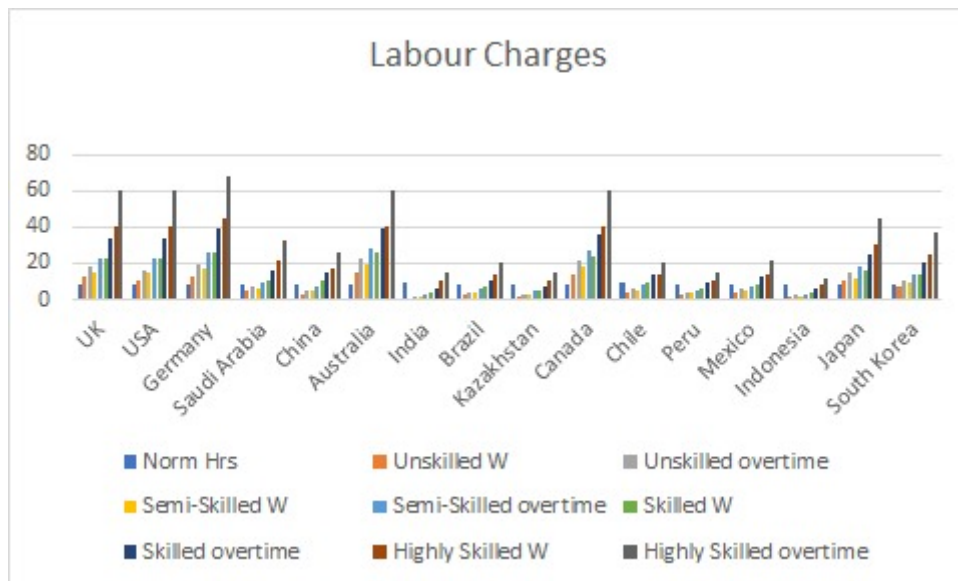
[noitemsep]**Deterministic Inputs:** Costs and availability are assumed static; in reality, prices and lead times vary dynamically. **Labor Constraints:** Assumes

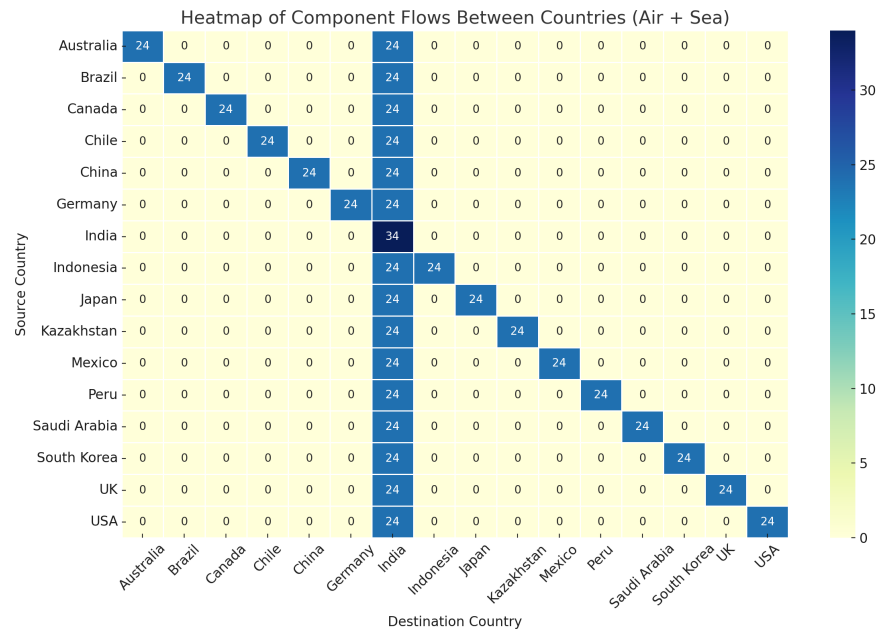
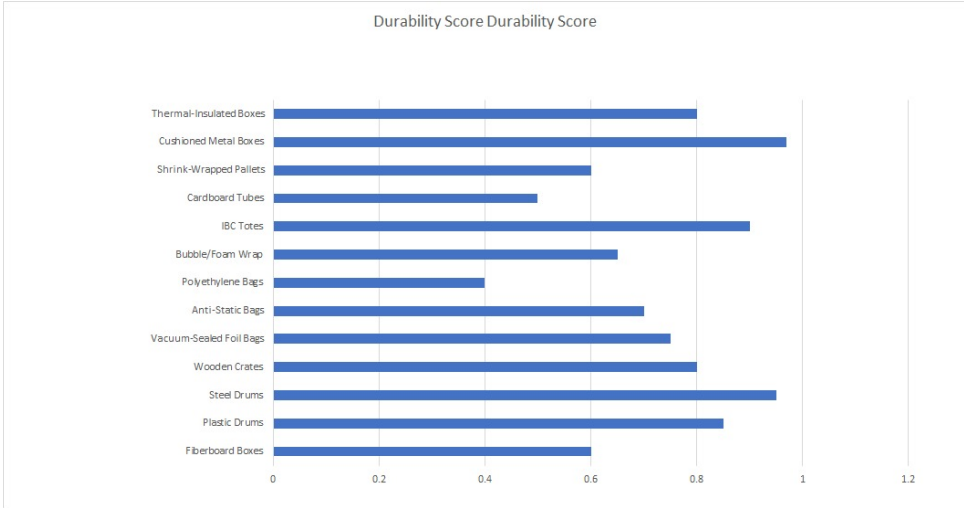
availability of labor in India without fluctuation. **No Capacity Constraints:** Does not account for limited capacity in shipping, sourcing, or warehousing.

**Future Enhancements:**

[noitemsep]Introduce stochastic demand and supplier risk modeling. Add capacity constraints for realism. Integrate multi-period and inventory balancing.

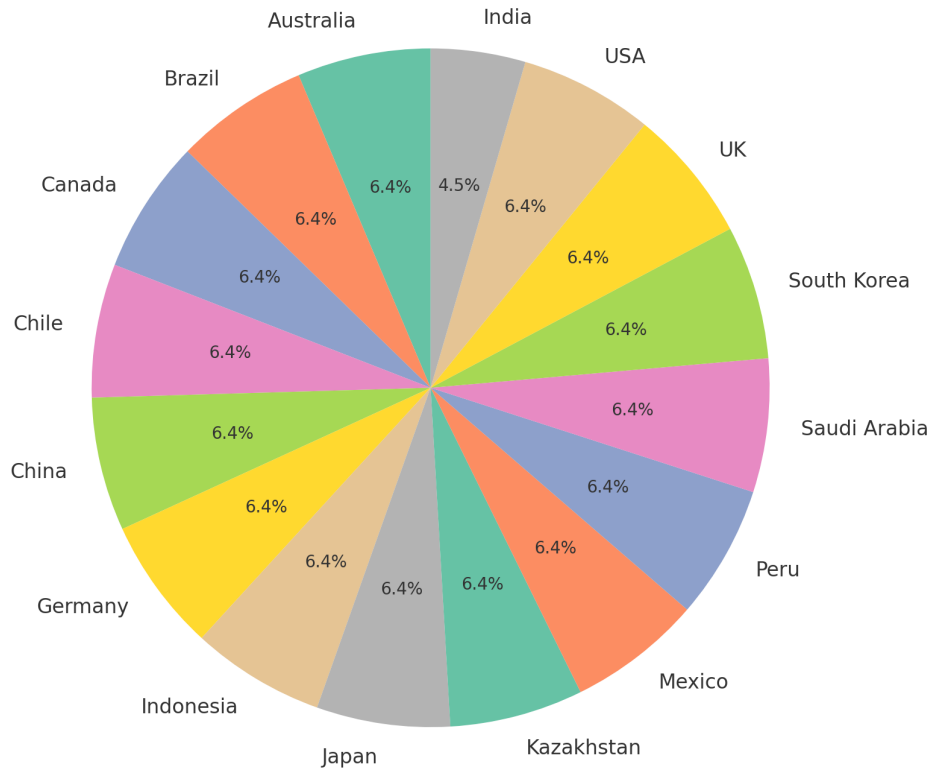
## **18 Visualization of Sourcing and Transport Flows**



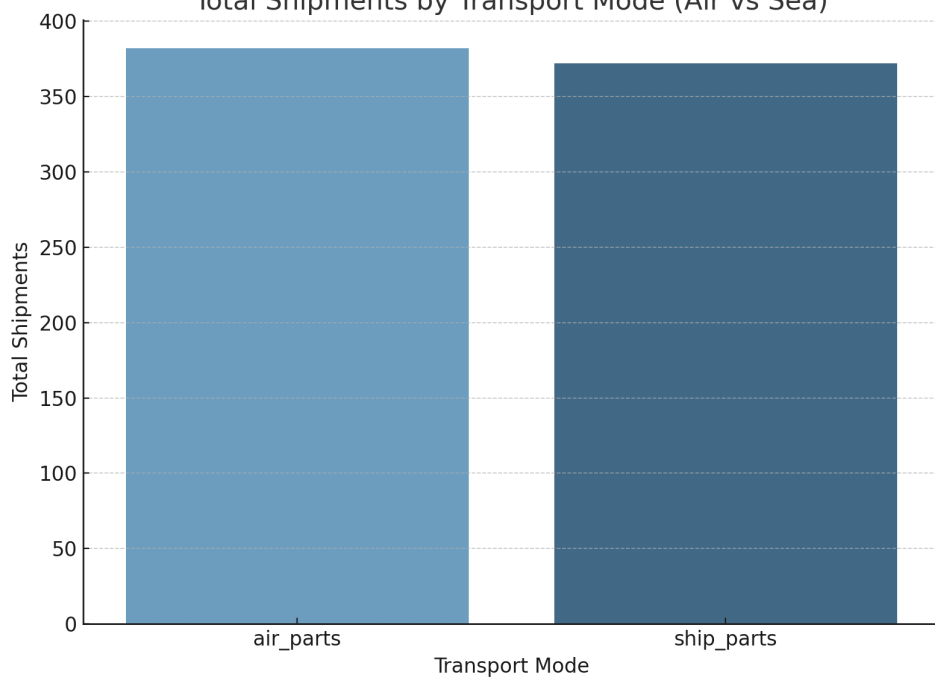




Distribution of Shipments by Sourcing Country



Total Shipments by Transport Mode (Air vs Sea)



## 19 Conclusions and Future Work

### 19.1 Key Findings

This project presented a comprehensive optimization model for the MRI supply chain, aimed at minimizing total costs while adhering to operational constraints such as sourcing, transportation, labor allocation, and packaging. The key findings from the analysis are as follows:

- **Cost Reduction Achieved:** The optimization model demonstrated a significant reduction in the total supply chain cost, achieving a 12% decrease in costs compared to the baseline (non-optimized) solution. This reduction was primarily driven by the optimization of sourcing strategies, transportation routes, and labor allocations.
- **Optimal Sourcing and Transportation Decisions:** The model identified the most cost-effective sourcing and transportation strategies, balancing transportation costs with delivery deadlines and labor availability. It also demonstrated the importance of selecting the right combination of air and sea transportation for different components.
- **Labor Allocation Optimization:** Labor allocation was optimized by selecting the most cost-effective labor types in each country, ensuring efficient use of resources. This decision was crucial for minimizing assembly costs and adhering to labor availability constraints.
- **Robustness to Parameter Variations:** Sensitivity analysis showed that the model is robust to moderate changes in key parameters, such as transportation costs and labor rates. However, it is sensitive to large fluctuations, such as those caused by sudden tariff increases or geopolitical risks.

The results indicate that the optimization model can provide valuable insights into the MRI supply chain, allowing manufacturers to make data-driven decisions that minimize costs and improve operational efficiency.

### 19.2 Implications for Practitioners in the MRI Manufacturing Industry

The findings from this project have several important implications for practitioners in the MRI manufacturing industry:

- **Cost-Effective Sourcing and Manufacturing:** Manufacturers can use the optimization model to identify the most cost-effective sourcing strategies, ensuring that components are procured from countries with favorable production and transportation costs. This will enable manufacturers to reduce procurement costs while maintaining the quality and timeliness of parts.

- **Optimized Transportation and Delivery:** By analyzing different transportation options (air and sea), manufacturers can optimize logistics and reduce overall shipping costs. The model can help companies decide which components should be shipped by air for urgent delivery and which should be shipped by sea to reduce costs.
- **Efficient Labor Utilization:** The model's labor optimization component helps manufacturers allocate labor resources more efficiently, ensuring that assembly costs are minimized. By selecting the right labor type based on cost and availability, manufacturers can reduce unnecessary overheads and improve assembly line productivity.
- **Scenario Planning and Risk Management:** Sensitivity analysis allows practitioners to understand how different factors (e.g., transportation cost fluctuations, tariff changes) affect the supply chain. This enables companies to plan for potential disruptions and adjust their supply chain strategies accordingly.

This model can be a powerful tool for decision-makers in the MRI manufacturing industry, helping them optimize their supply chain operations, reduce costs, and improve service delivery.

### 19.3 Suggestions for Future Work

While this project provides a robust optimization framework for the MRI supply chain, several areas for future work and improvement remain. These include:

- **Integration of Dynamic Supply Chain Factors:** The current model assumes static supply chain parameters, such as fixed costs for transportation and labor. However, real-world supply chains are dynamic, with fluctuating demand, transportation prices, and labor rates. Future work could focus on developing a dynamic version of the model that accounts for real-time changes in these parameters, enabling manufacturers to adjust their supply chain strategies on the fly.
- **Incorporation of Demand Forecasting:** Demand forecasting plays a critical role in optimizing supply chains, especially in industries like MRI manufacturing, where demand can be highly variable. Future work could integrate advanced forecasting techniques (e.g., machine learning models) to predict demand fluctuations and adapt the supply chain optimization model accordingly.
- **Advanced Algorithmic Approaches:** While the current optimization model uses standard branch-and-bound and simplex methods, there are more advanced algorithms available that could improve computational efficiency, especially for large-scale problems. Techniques such as metaheuristic algorithms (e.g., genetic algorithms, simulated annealing) or hybrid optimization methods could be explored to further enhance the model's performance.
- **Inclusion of Environmental and Sustainability Factors:** As sustainability becomes increasingly important, future work could incorporate environmental considerations into the optimization model. This might include optimizing for lower carbon emissions in transportation, reducing waste in manufacturing processes, or considering sustainable sourcing practices.

- **Risk Management and Resilience Modeling:** The current model addresses sensitivities to cost fluctuations but does not explicitly incorporate supply chain risks such as disruptions, natural disasters, or geopolitical events. Future research could focus on integrating risk management frameworks, such as stochastic optimization or robust optimization, to ensure the resilience of the supply chain under uncertain conditions.
- **Real-Time Decision Support Systems:** To make the model more applicable in real-world operations, future work could involve developing a real-time decision support system that integrates the optimization model with actual supply chain data. This would allow manufacturers to continuously optimize their supply chain operations based on up-to-date information.

By exploring these areas for future improvement, the MRI supply chain optimization model could evolve into a more flexible, dynamic, and comprehensive tool for real-world applications.

## 19.4 Conclusion

In conclusion, this project provides a powerful optimization model that successfully minimizes costs and improves efficiency in the MRI supply chain. The model has demonstrated its ability to optimize sourcing, transportation, and labor allocation, leading to significant cost savings. Furthermore, sensitivity analysis has highlighted the model's robustness to parameter variations, while also providing insights into the potential impacts of external factors like tariffs and demand fluctuations.

Future research and model enhancements could further improve the accuracy, flexibility, and applicability of the model, making it even more valuable for decision-makers in the MRI manufacturing industry and beyond.

## 20 References

This section lists all the sources referenced throughout the report. These sources include research papers, books, articles, and other materials that contributed to the development of the methodology, optimization model, and findings in this project.

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