









$I(x, y, t)$



$I(x + \delta x, y + \delta y, t + \delta t)$

## Assumption #2:

Displacement  $(\delta x, \delta y)$  and time step  $\delta t$  are small

$$I(x + \delta x, y + \delta y, t + \delta t) = I(x, y, t) + \frac{\partial I}{\partial x} \delta x + \frac{\partial I}{\partial y} \delta y + \frac{\partial I}{\partial t} \delta t$$

# Optical Flow Constraint Equation

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$$I(x + \delta x, y + \delta y, t + \delta t) = I(x, y, t) \quad \text{----- (1)}$$

$$I(x + \delta x, y + \delta y, t + \delta t) = I(x, y, t) + I_x \delta x + I_y \delta y + I_t \delta t \quad \text{----- (2)}$$

Subtract (1) from (2):  $I_x \delta x + I_y \delta y + I_t \delta t = 0$

Divide by  $\delta t$  and take limit as  $\delta t \rightarrow 0$ :  $I_x \frac{\partial x}{\partial t} + I_y \frac{\partial y}{\partial t} + I_t = 0$

Constraint Equation:  $I_x u + I_y v + I_t = 0$   $(u, v)$ : Optical Flow