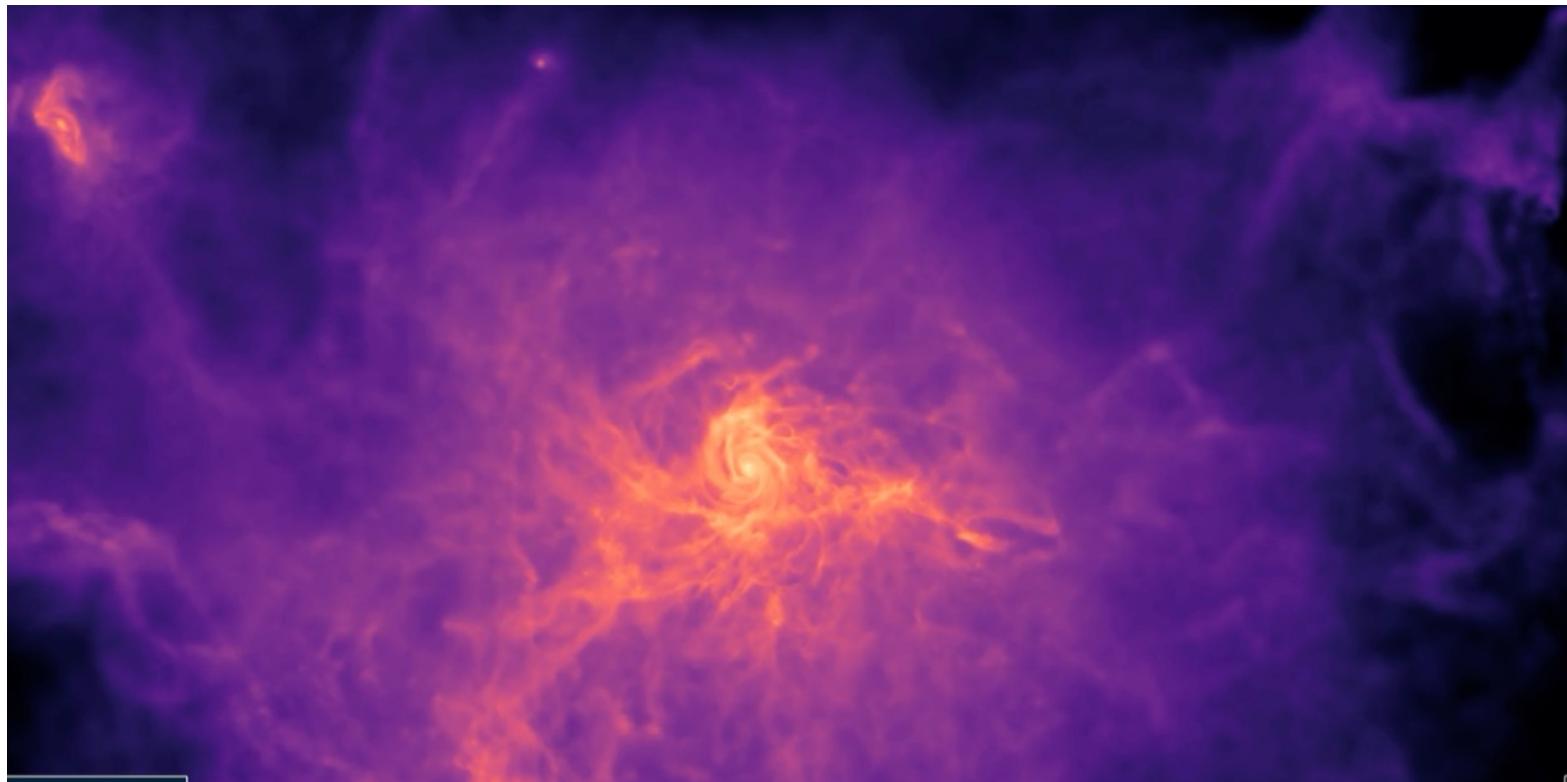
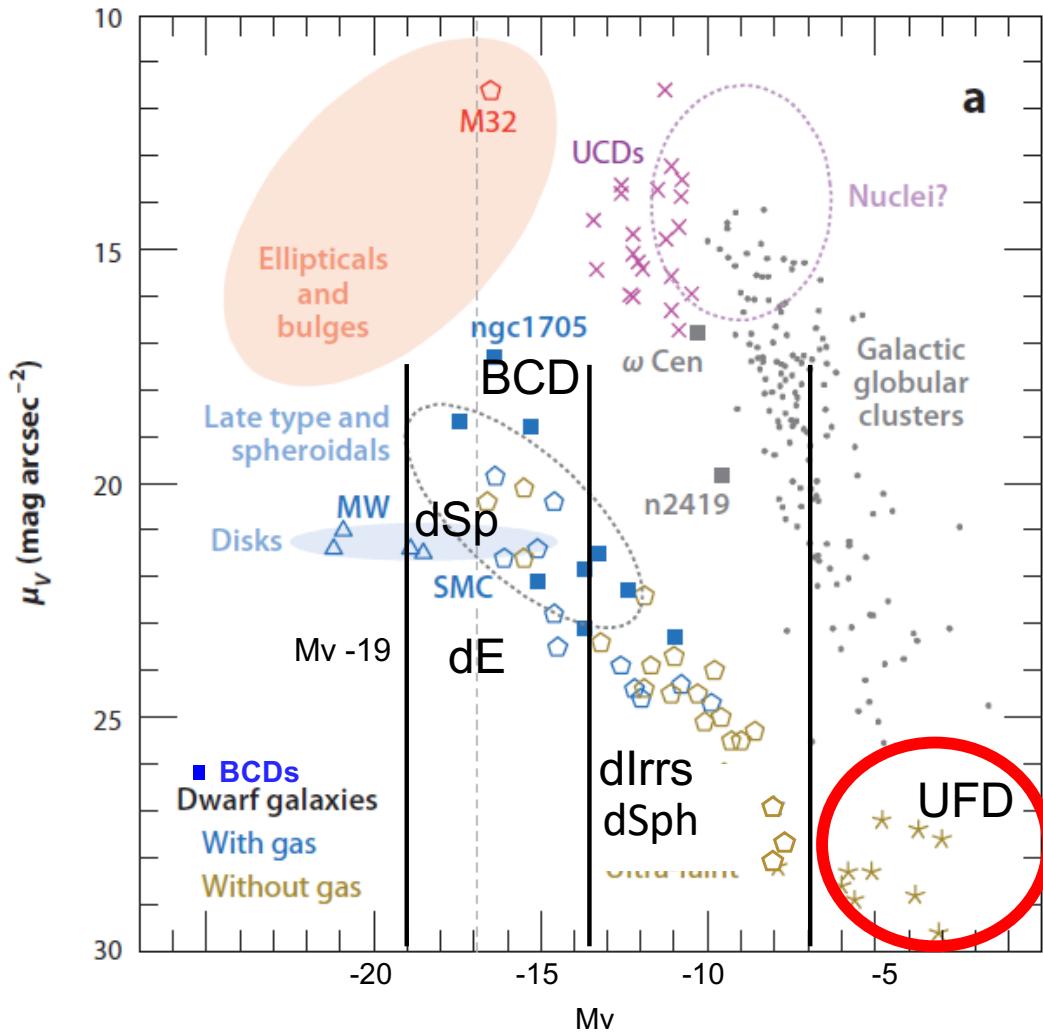


# Structure Formation



# Ultra Faint Dwarfs $M^* < 10^5 M_\odot$

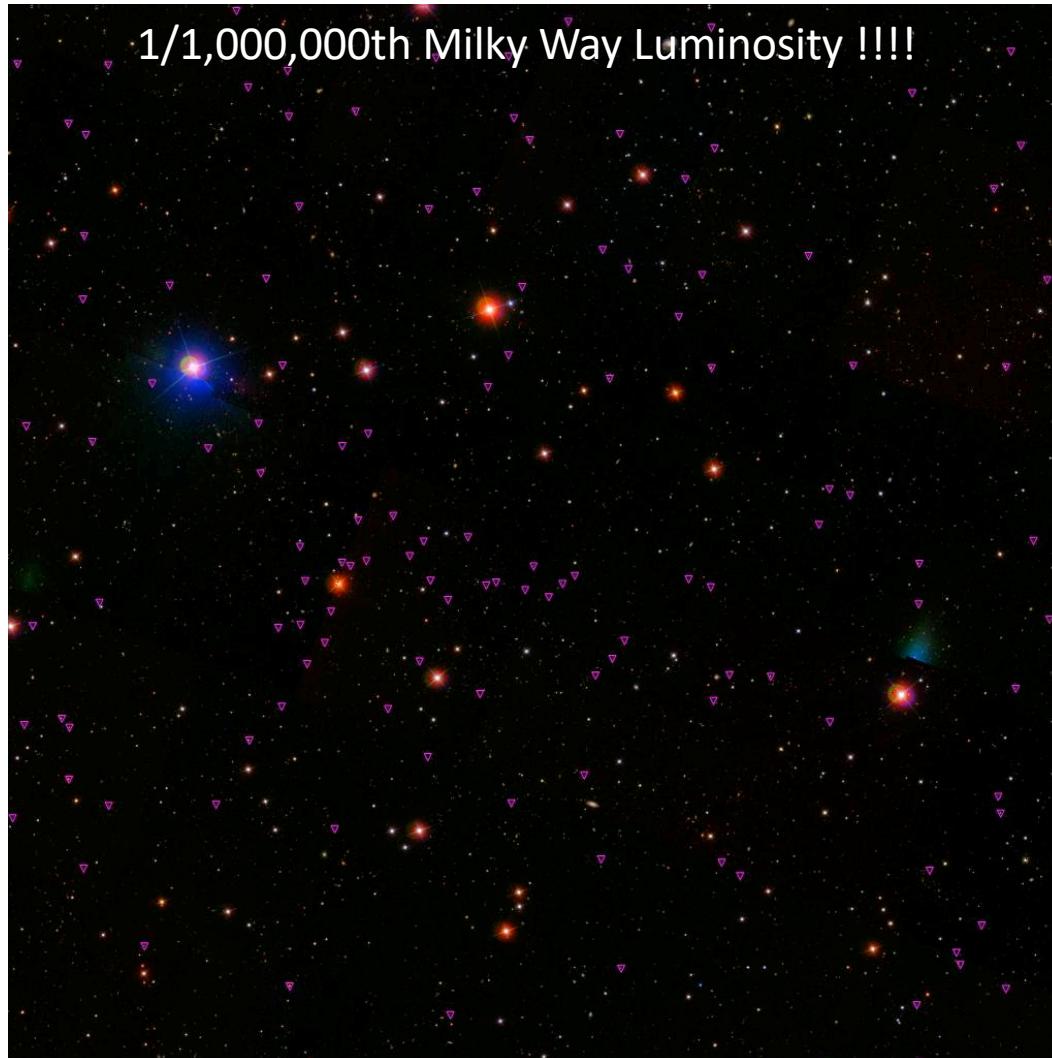
Tolstoy+ 2009

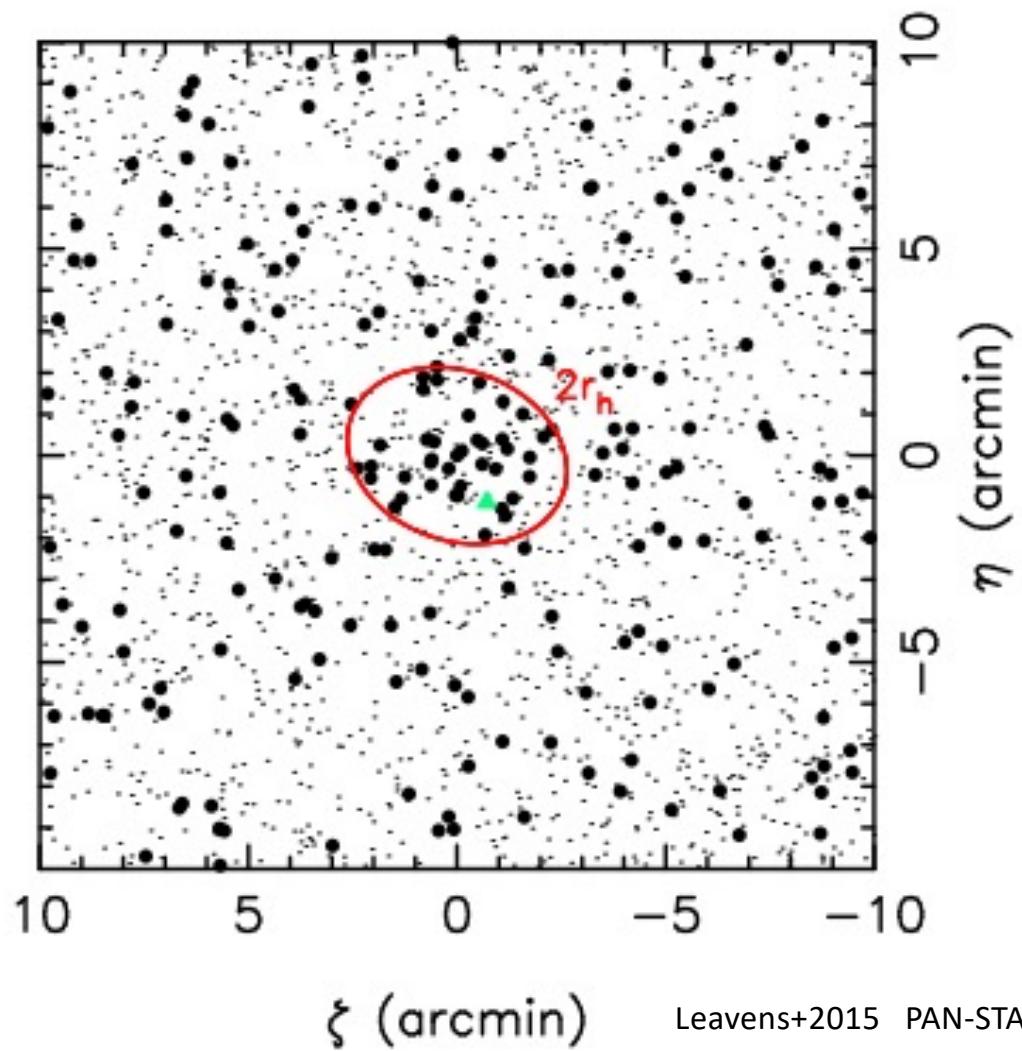


# Ursa Major I:

Willman + 2005

Diameter  
~ 13000 Ly

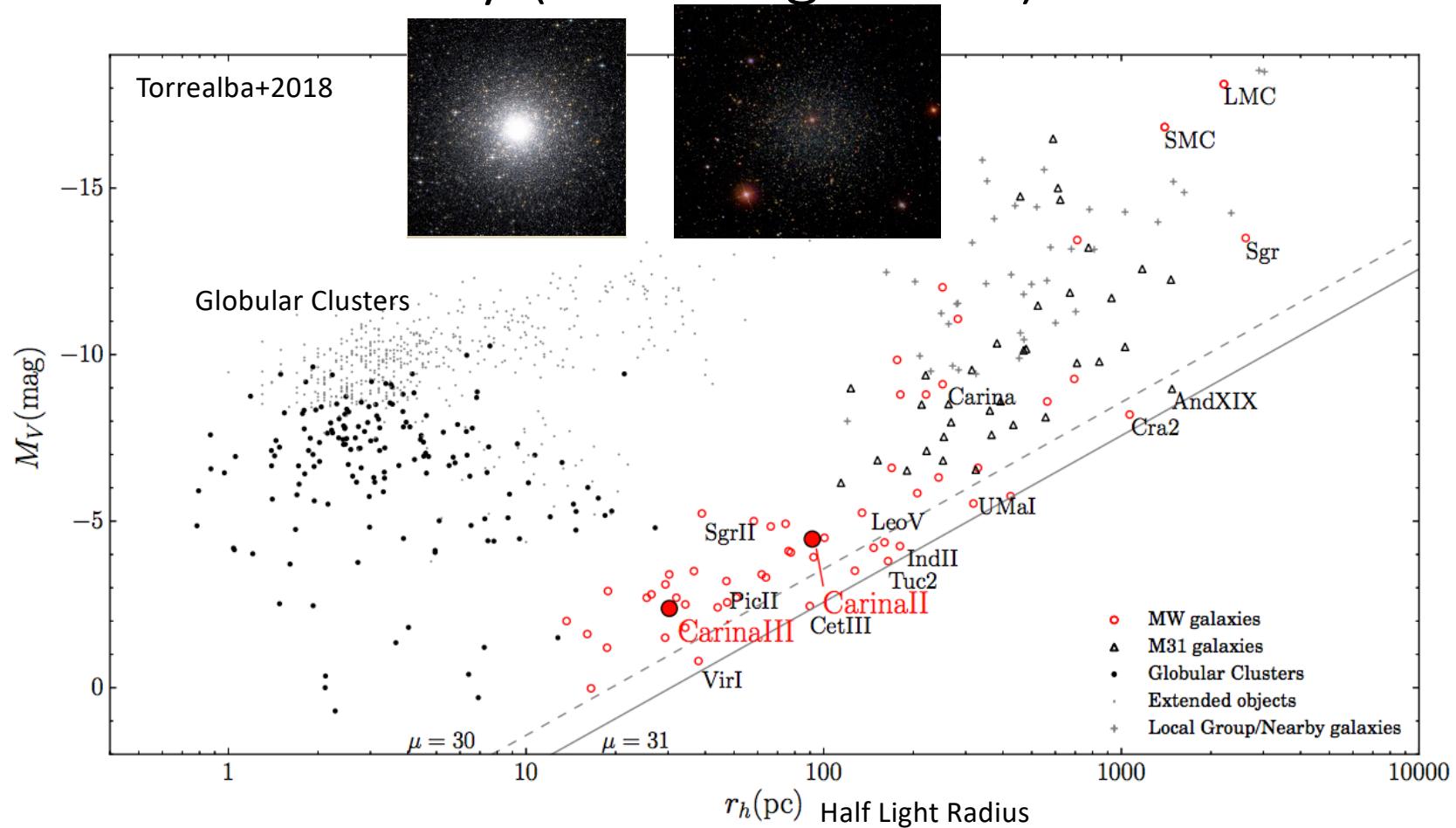




$\xi$  (arcmin)

Leavens+2015 PAN-STARRS discovery paper

# Size vs Luminosity (abs. magnitude)



## Recall: Definition of a “Galaxy”

- Willman & Strader 2012: “Galaxy” Defined

A galaxy is a gravitationally bound set of stars whose properties cannot be explained by a combination of baryons (gas & stars) and Newton’s laws of gravity.

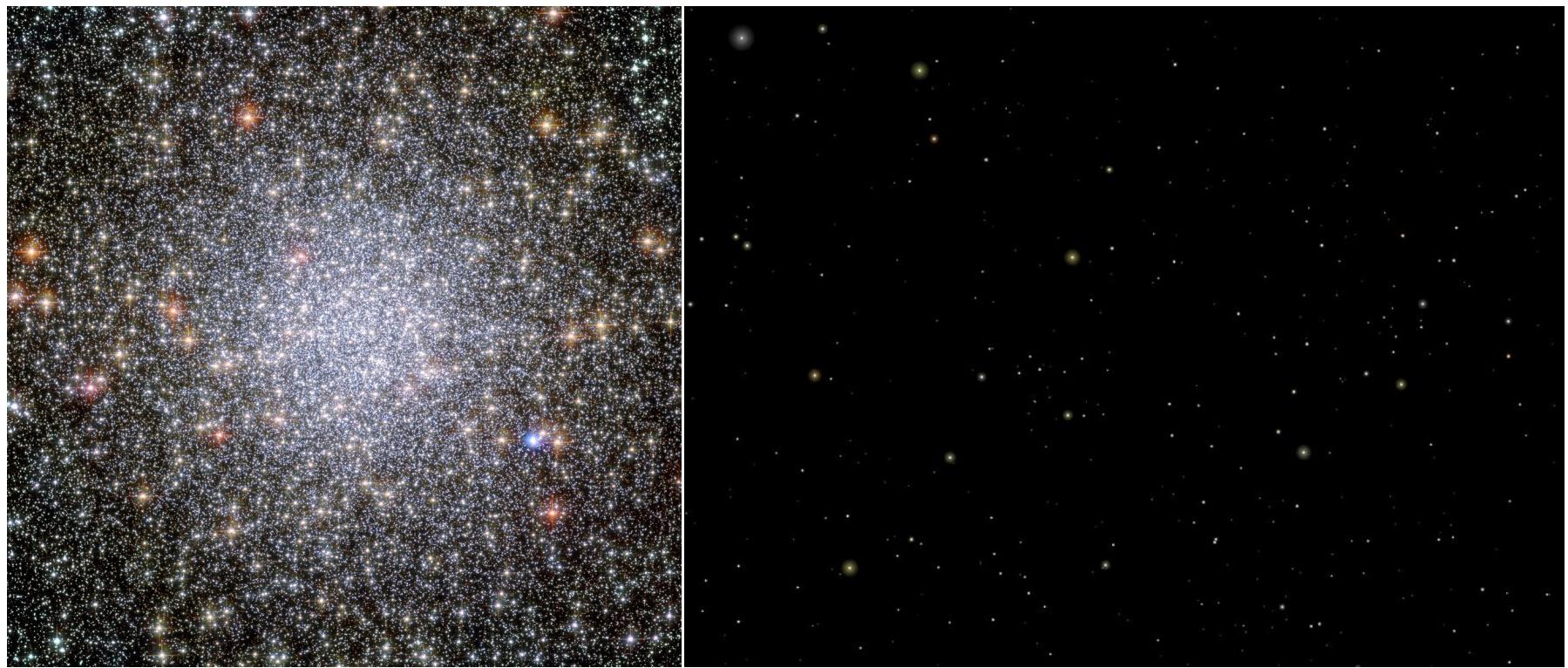
# Part 1 of Lab 5: Dynamical Mass Estimator

Wolf et al. 2010

$$\begin{aligned} M(< r_{1/2}) &= 3 G^{-1} \sigma_{\text{los}}^2 r_{1/2} \\ &= 4 G^{-1} \sigma_{\text{los}}^2 R_e . \end{aligned}$$

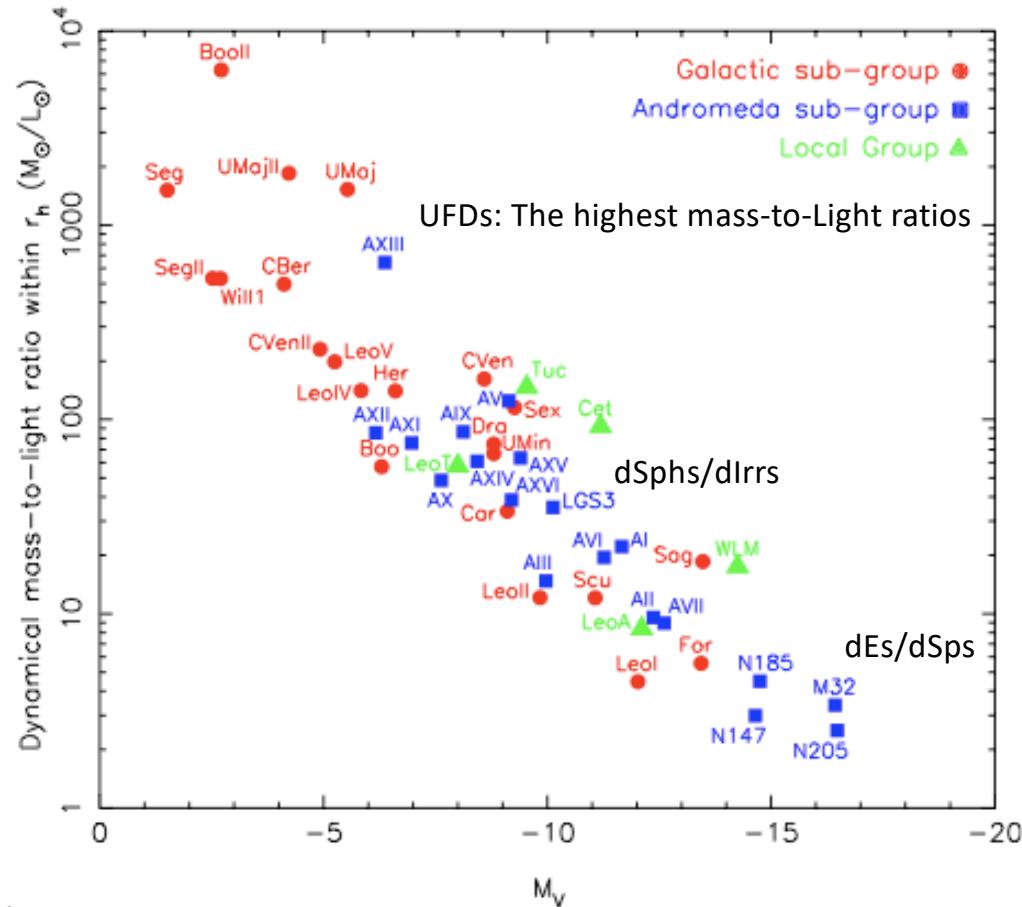
$$r_{1/2} \approx 4R_e/3,$$

$R_e$  = 2D radius that contains half the stellar mass (projection of  $r_{1/2}$ )



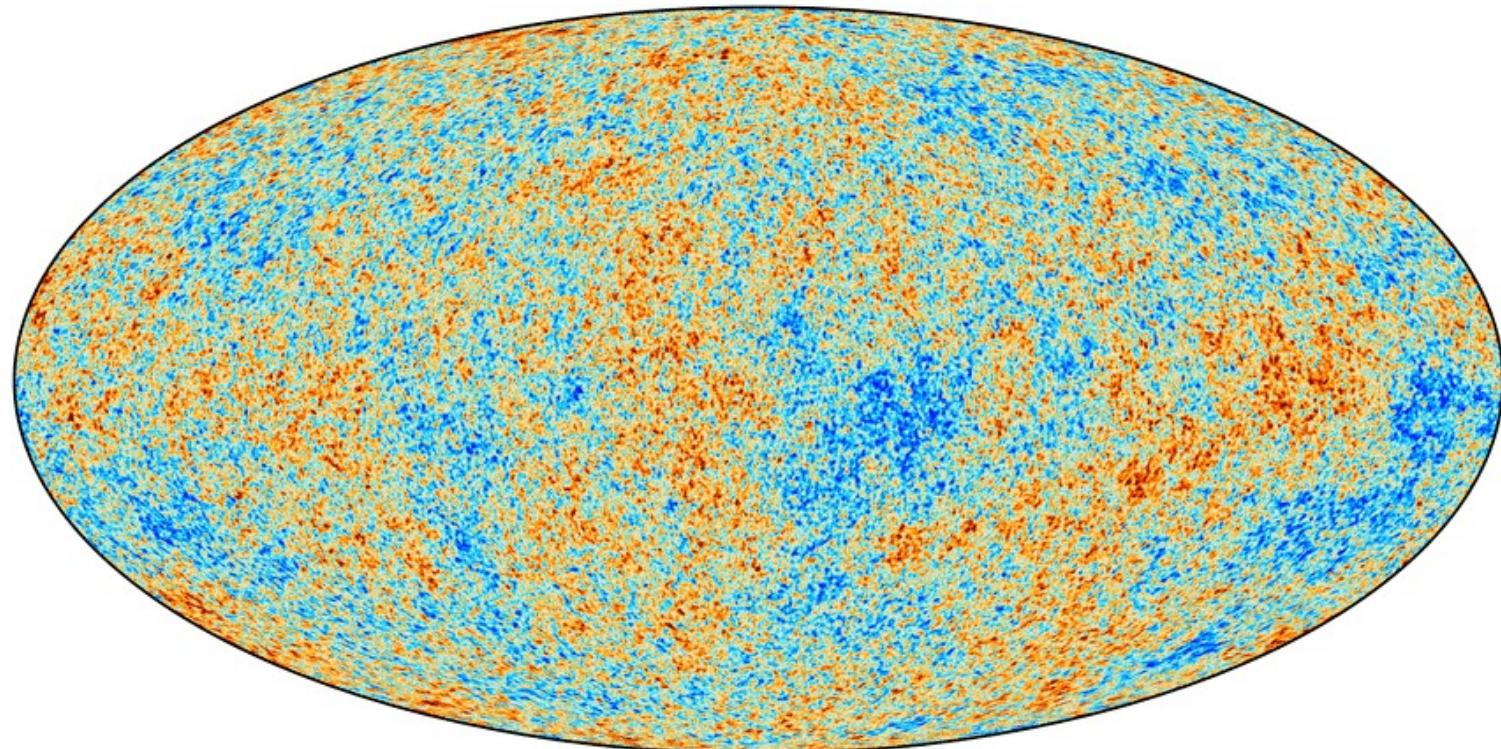
# $M_{\text{Dynamical}} / L$ Ratios

Segue (Seg) only has a stellar mass of 340 Msun!

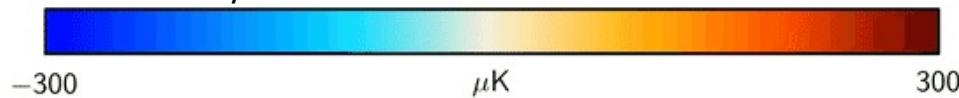


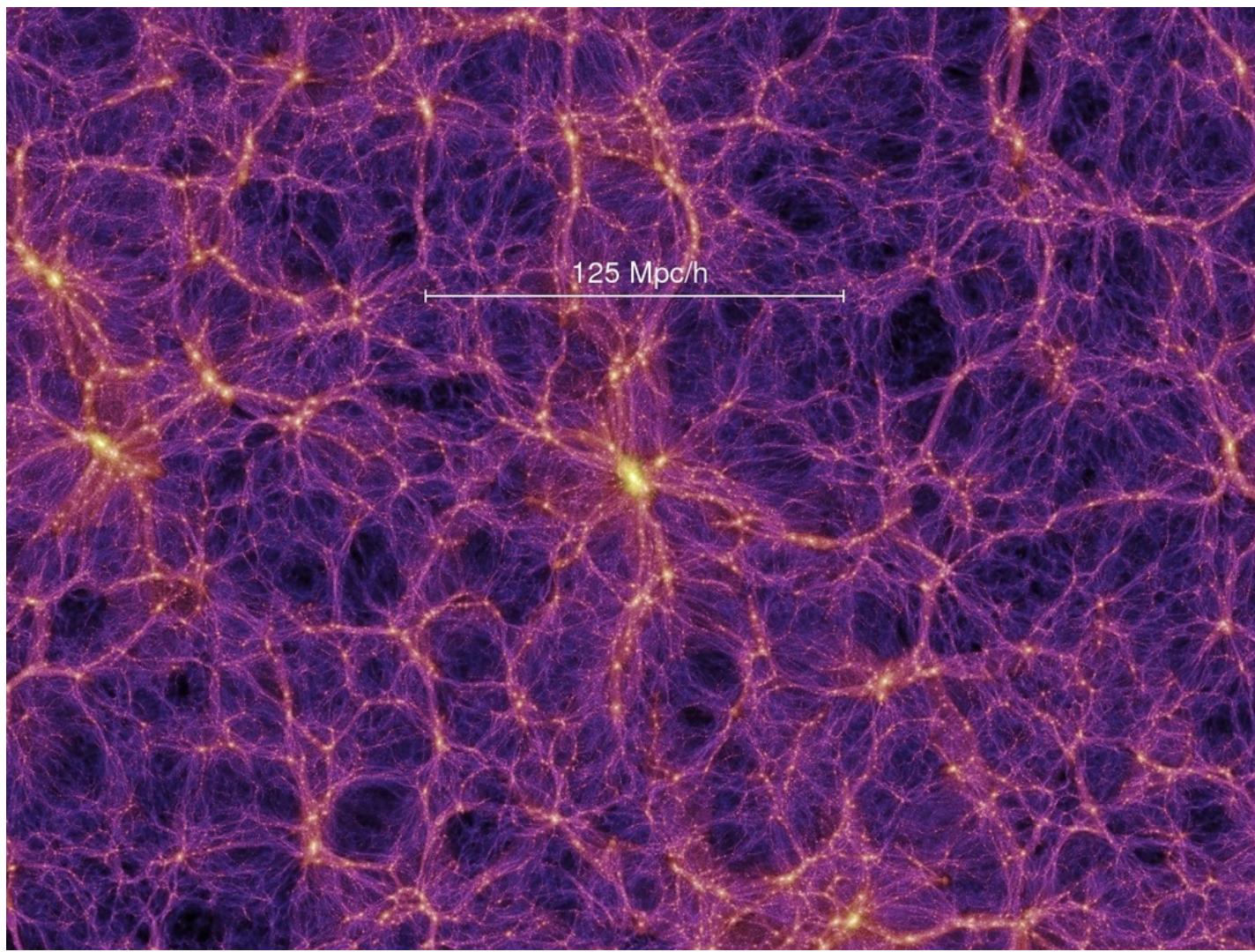
McConnachie 2012

Start with fluctuations in density after the Big Bang...



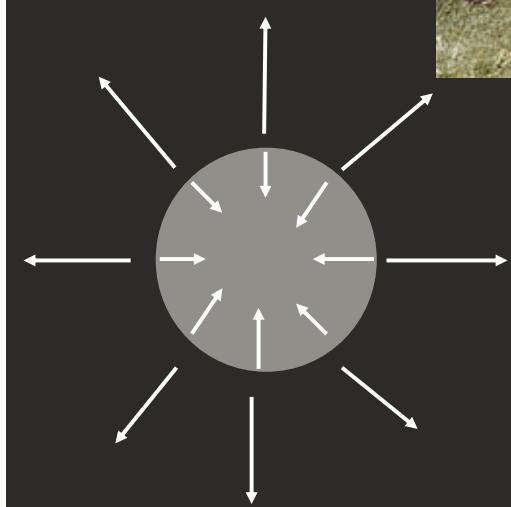
Planck measurement of the CMB -  $\Delta T/T \sim 10^{-6}$





# Formation of Structure: $\Lambda$ Cold Dark Matter Theory

Cosmological expansion



Gravity/dark matter

Overdensities (local regions of higher dark matter density than average) grow into gravitationally bound structures once they overcome expansion.

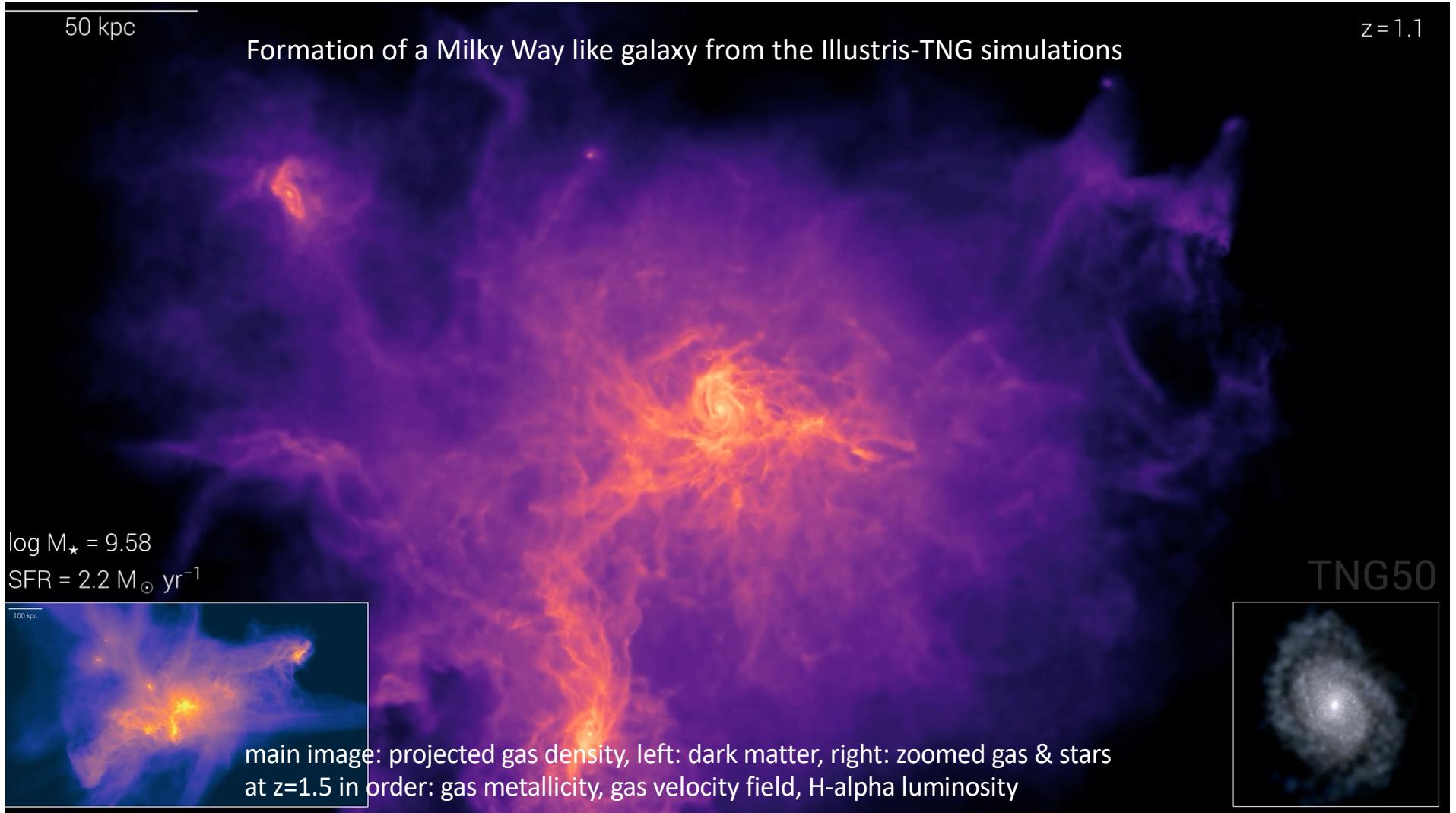
Space between bound overdensities expands.



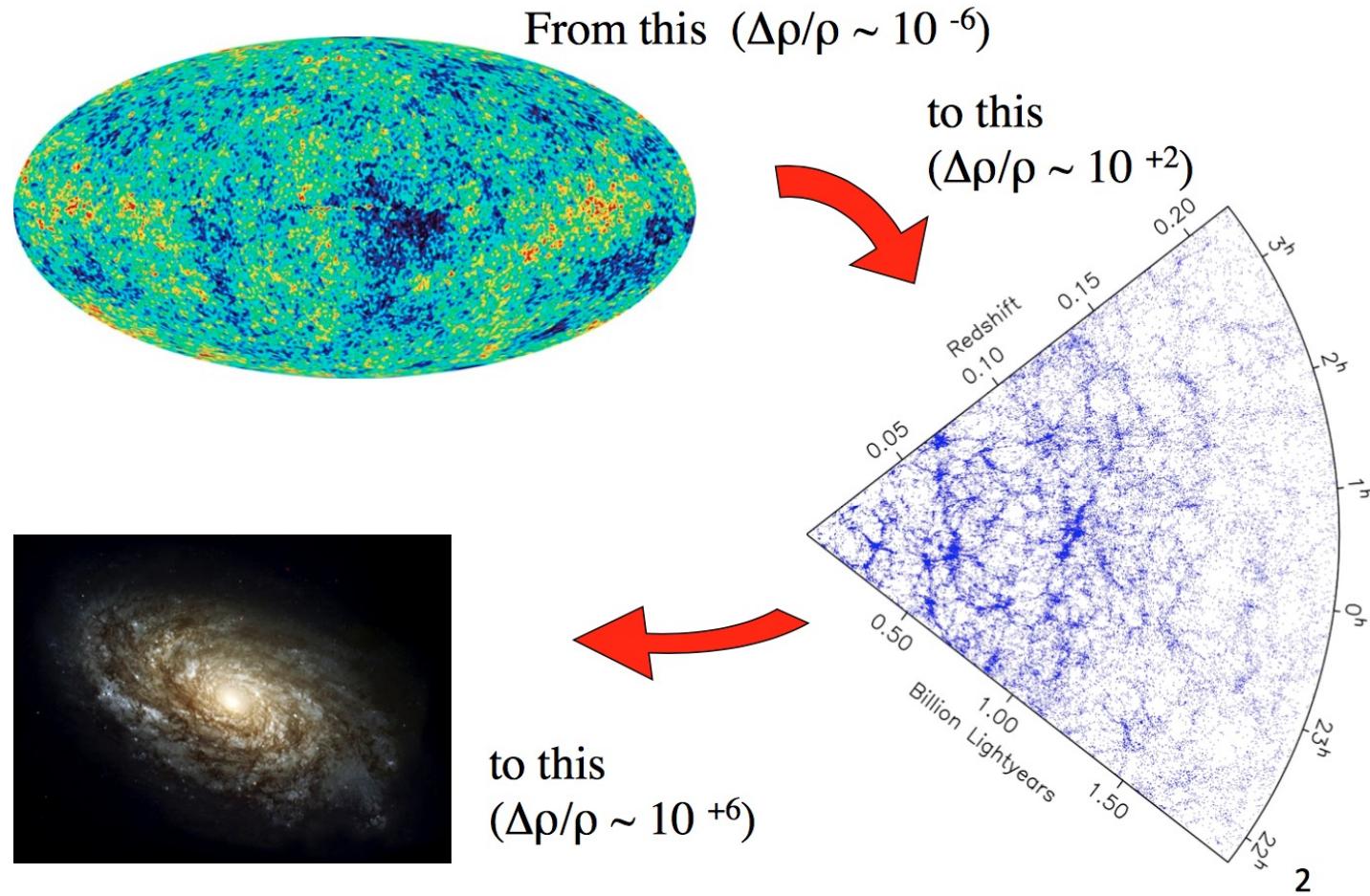
50 kpc

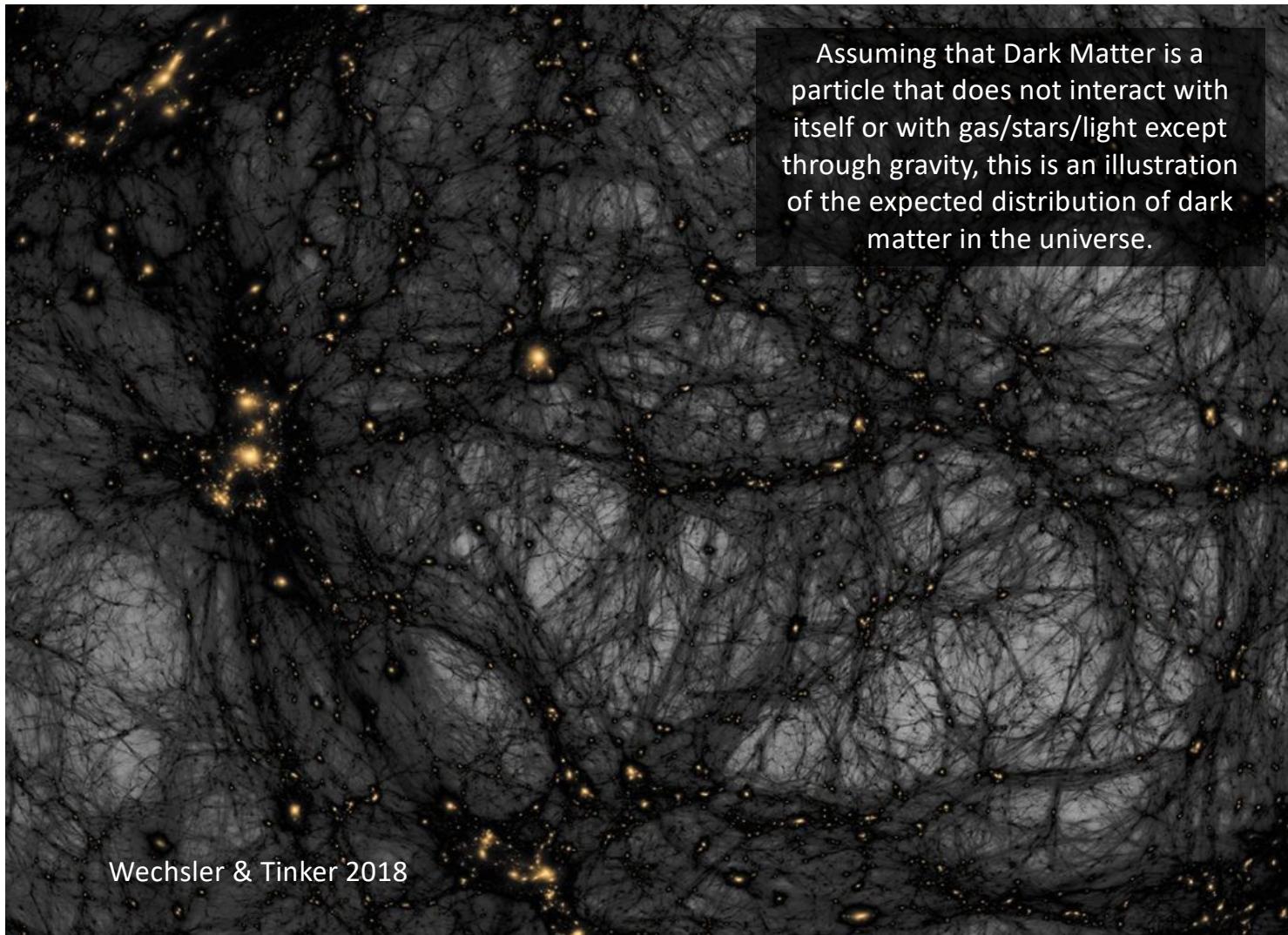
$z = 1.1$

### Formation of a Milky Way like galaxy from the Illustris-TNG simulations



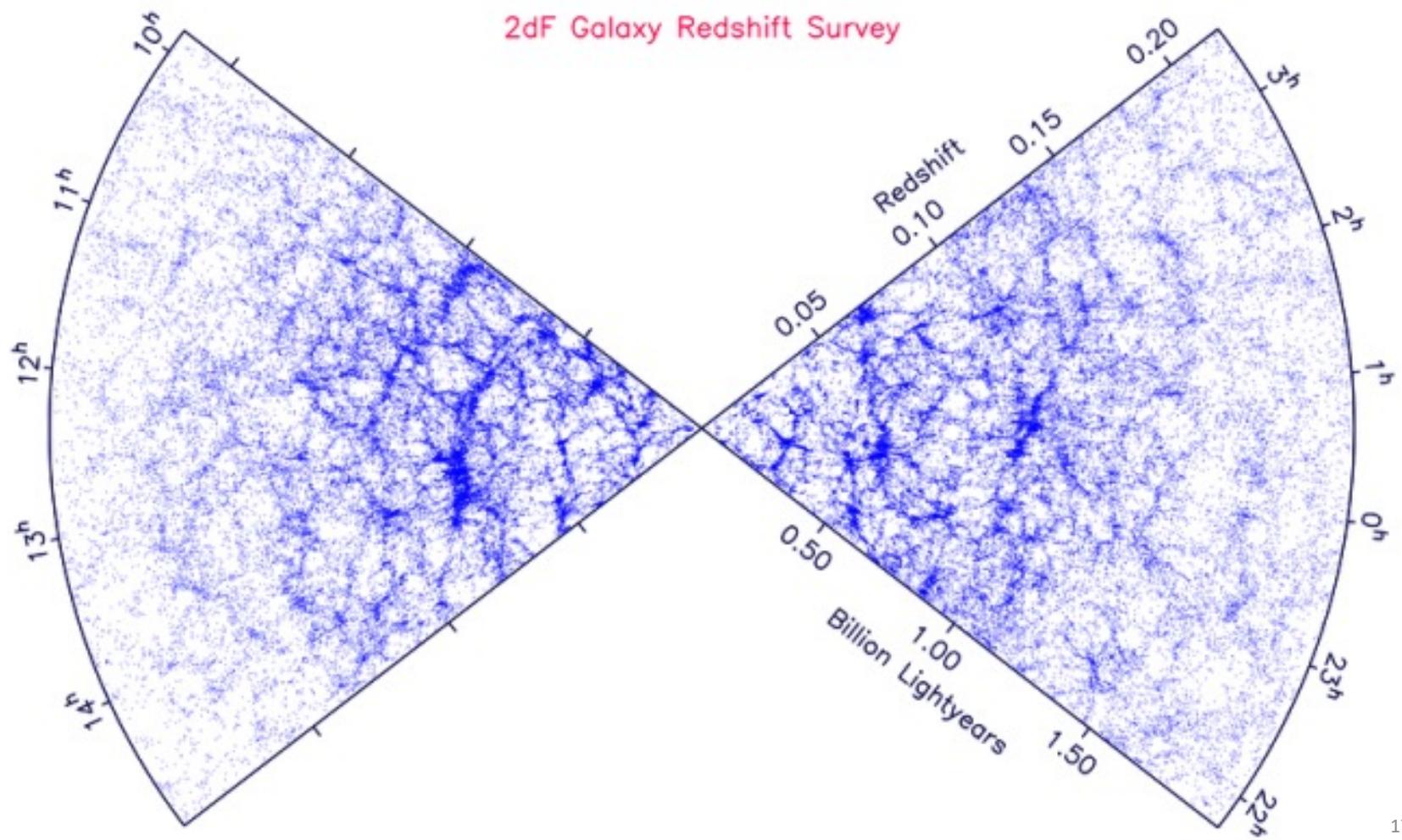
# Structure Formation and Evolution



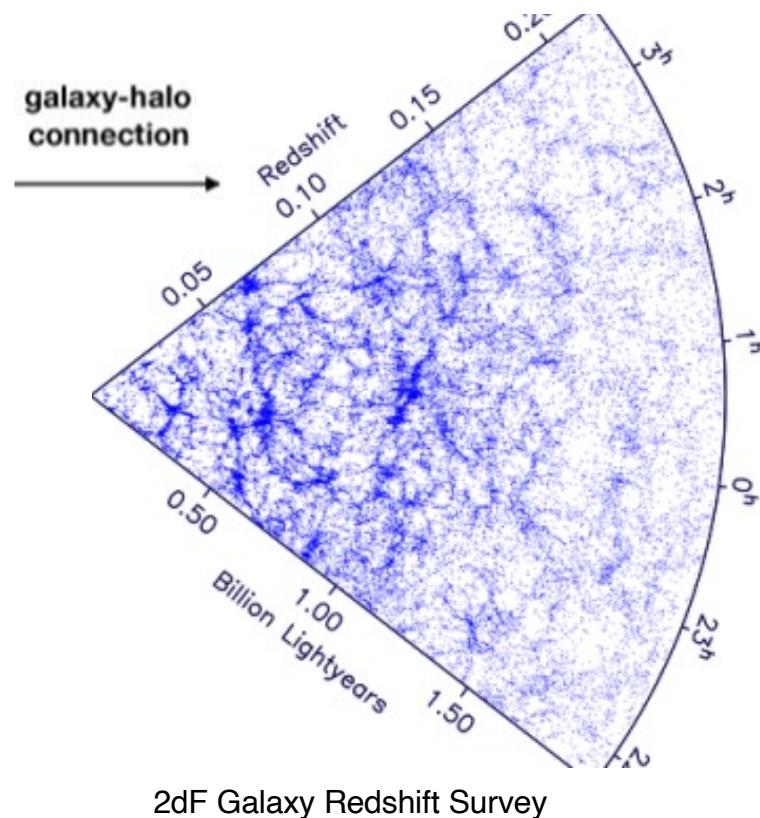
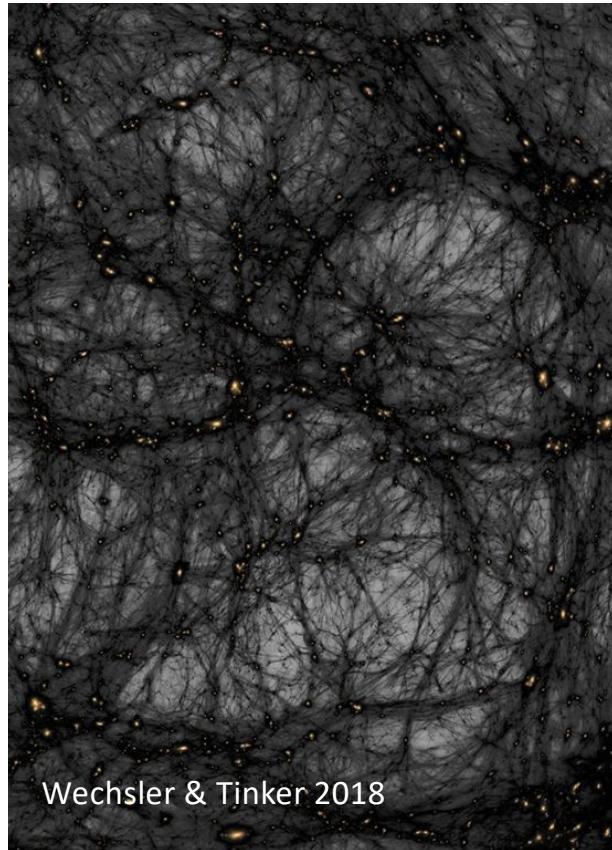


Assuming that Dark Matter is a particle that does not interact with itself or with gas/stars/light except through gravity, this is an illustration of the expected distribution of dark matter in the universe.

Wechsler & Tinker 2018

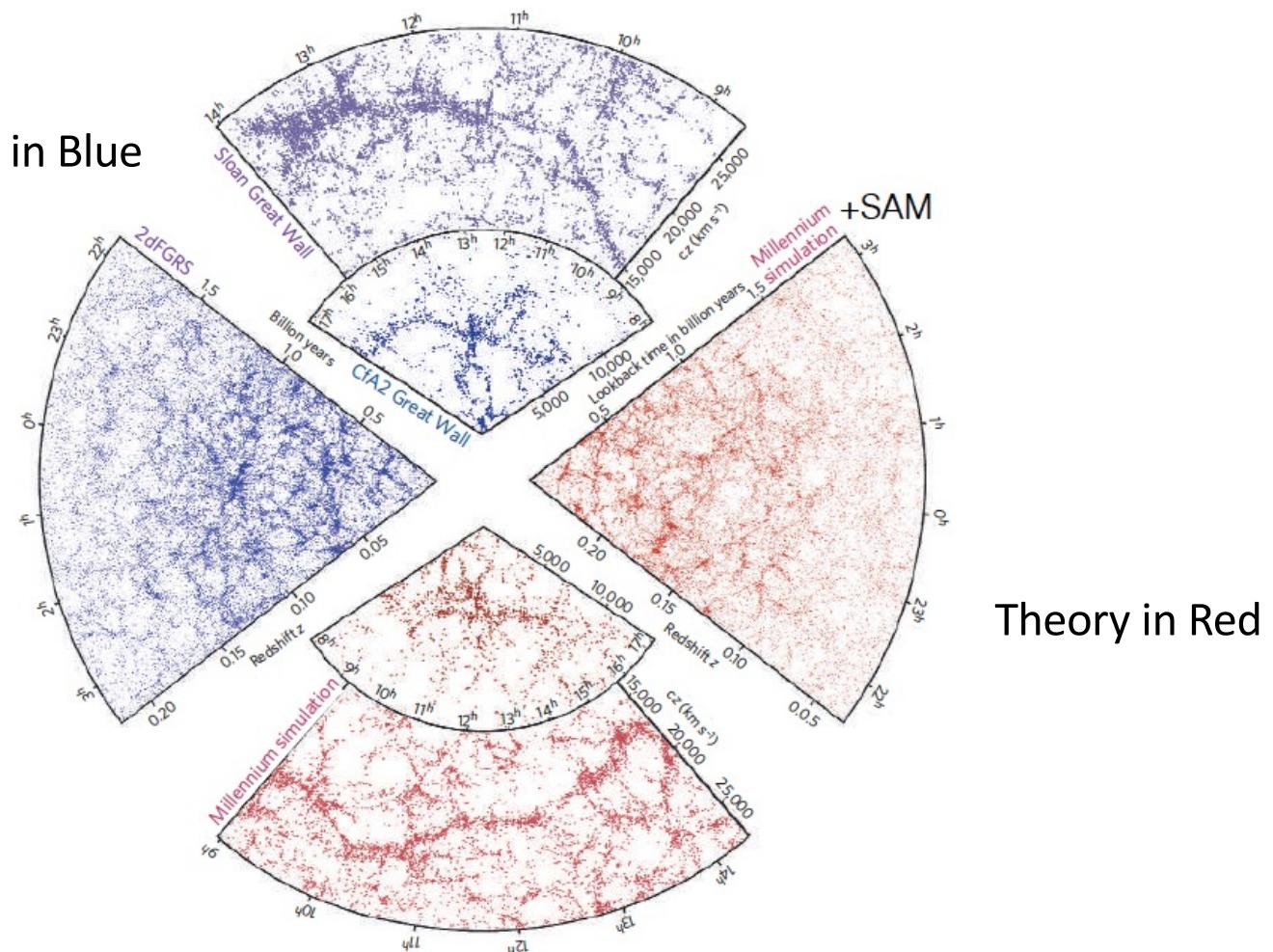


Simulated “web” matches the observed distribution of galaxies



## Observations in Blue

The successful reproduction of the large scale structure of the universe (Filaments and Voids) is one of the greatest successes of LCDM theory.

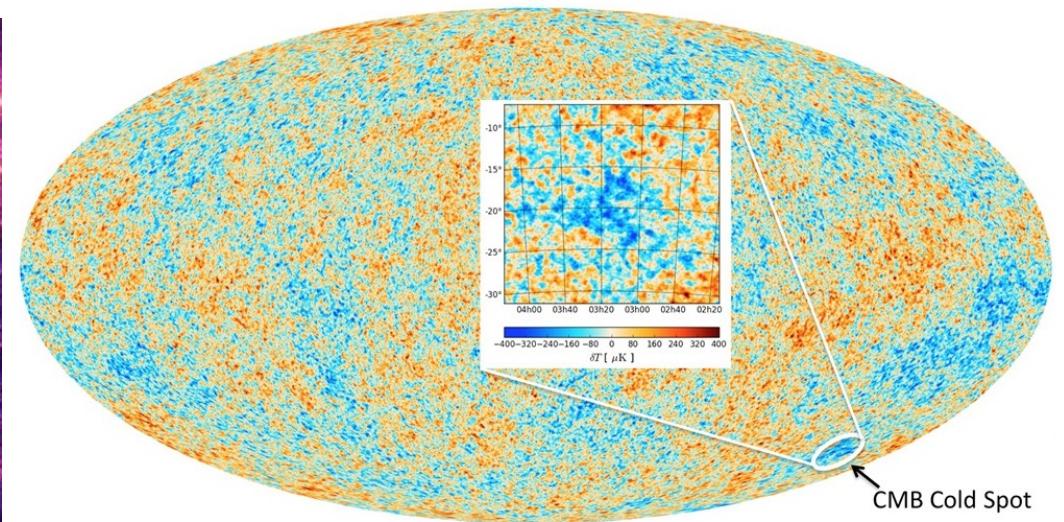
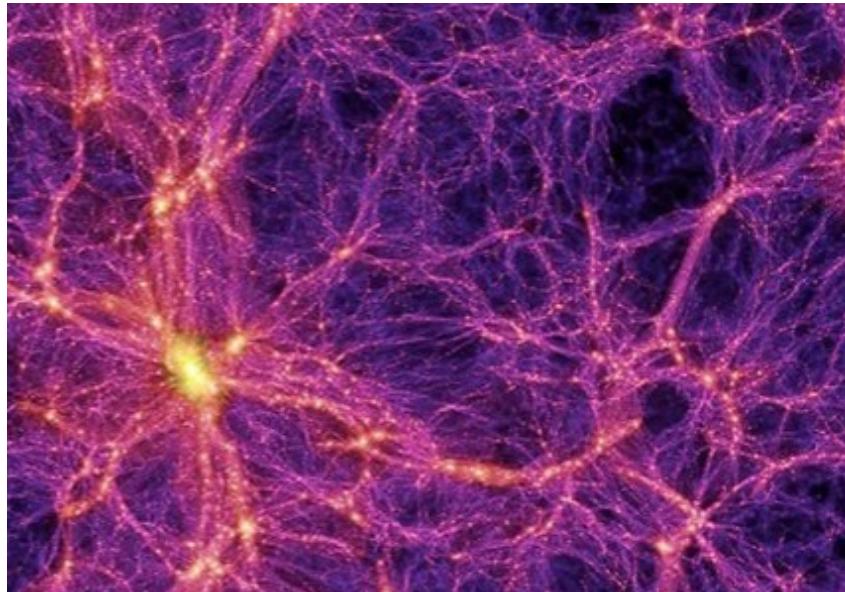


Theory in Red

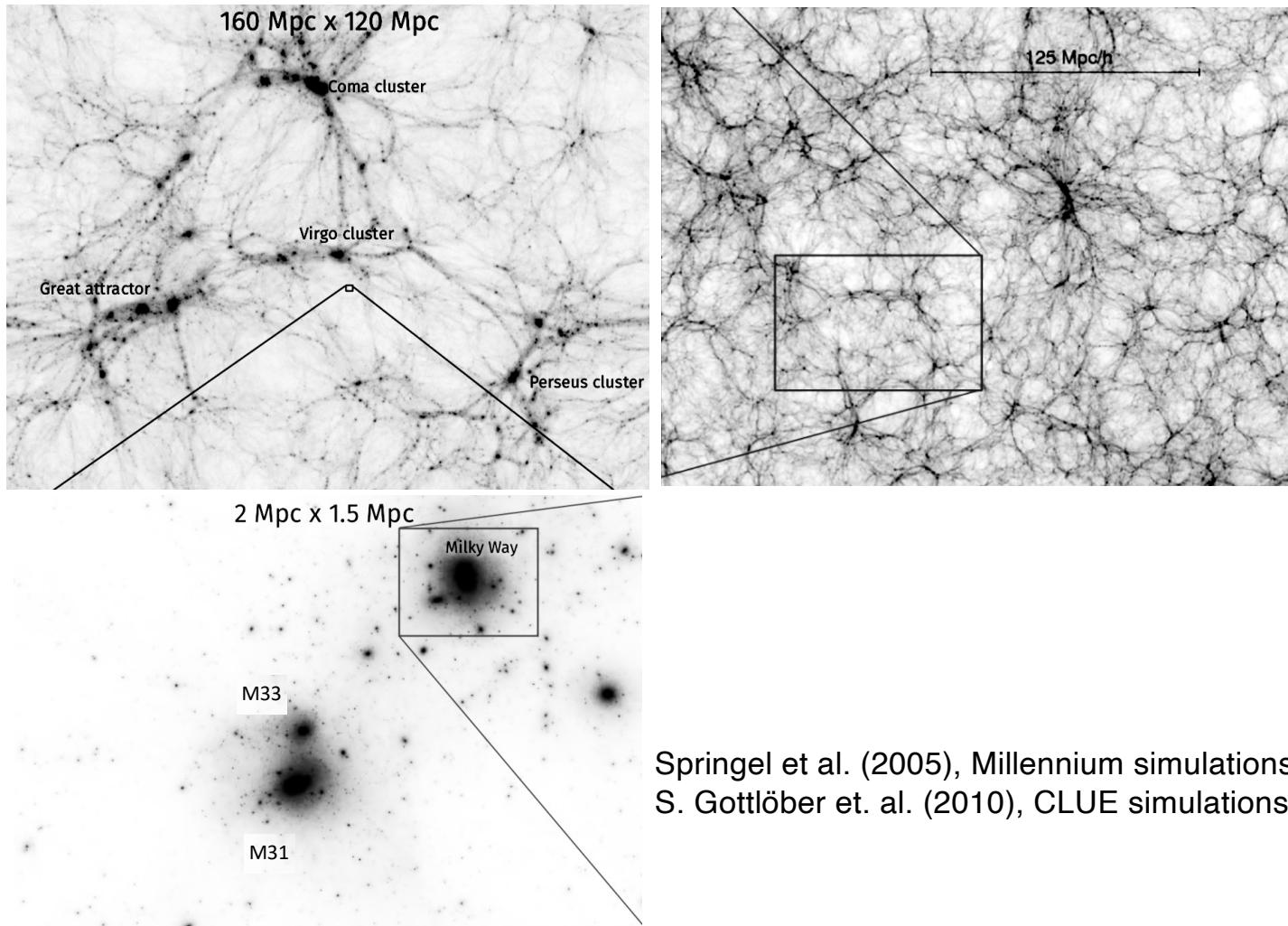
Springel, Frenk, White 06

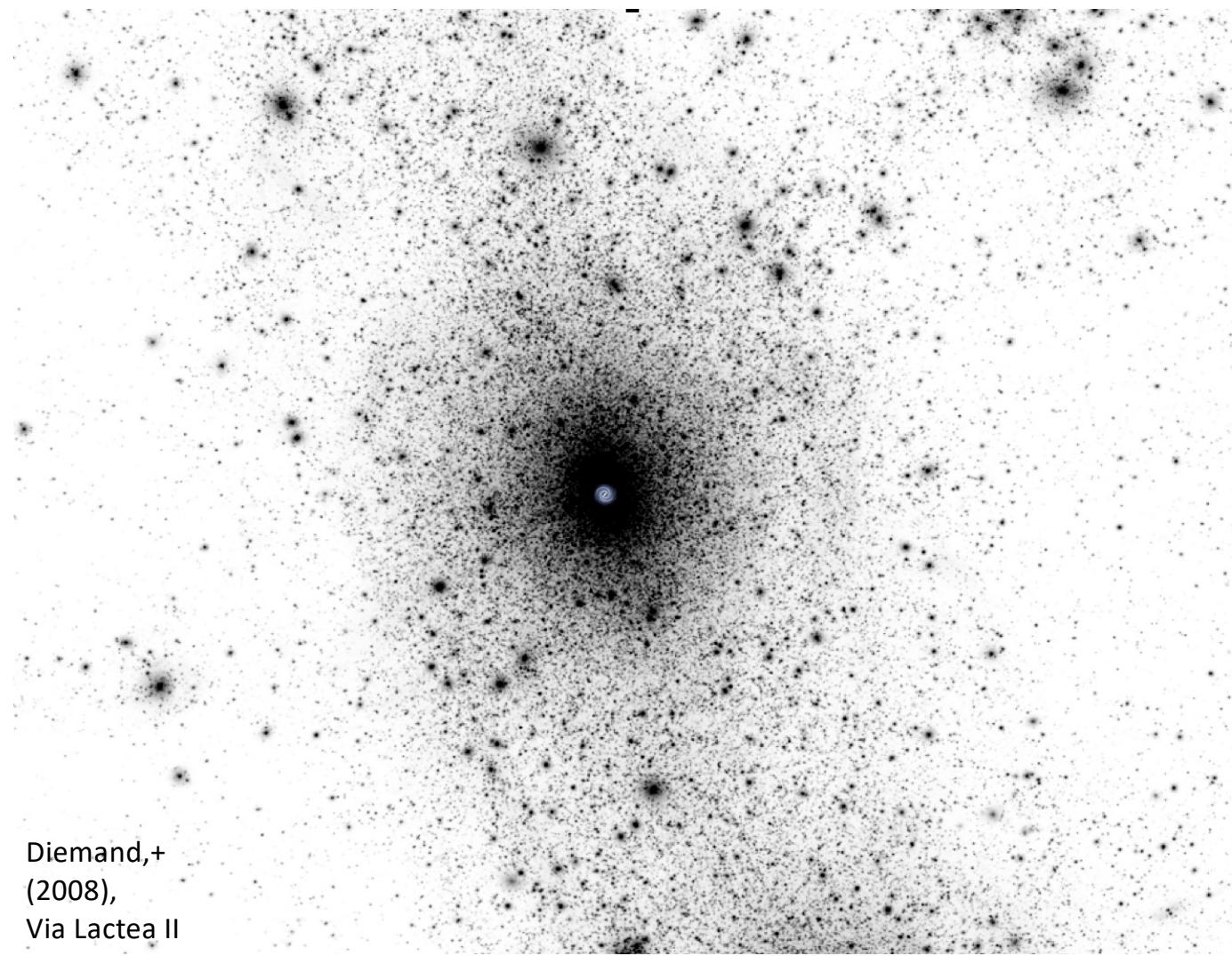
# Cosmic Voids:

- Large spaces (10-100 Mpc) between filaments that contain very few galaxies.
- Average density of dark matter in a void is  $\sim 1/10^{\text{th}}$  the mean density of the universe



The Cold Spot is an area of the cosmic microwave background with a lower temperature than its surroundings. On this map created by the Planck satellite, warmer CMB temperatures appear redder and cooler temperatures appear bluer.  
ESA and Durham University





Diemand,+  
(2008),  
Via Lactea II

# Dark Matter Halo

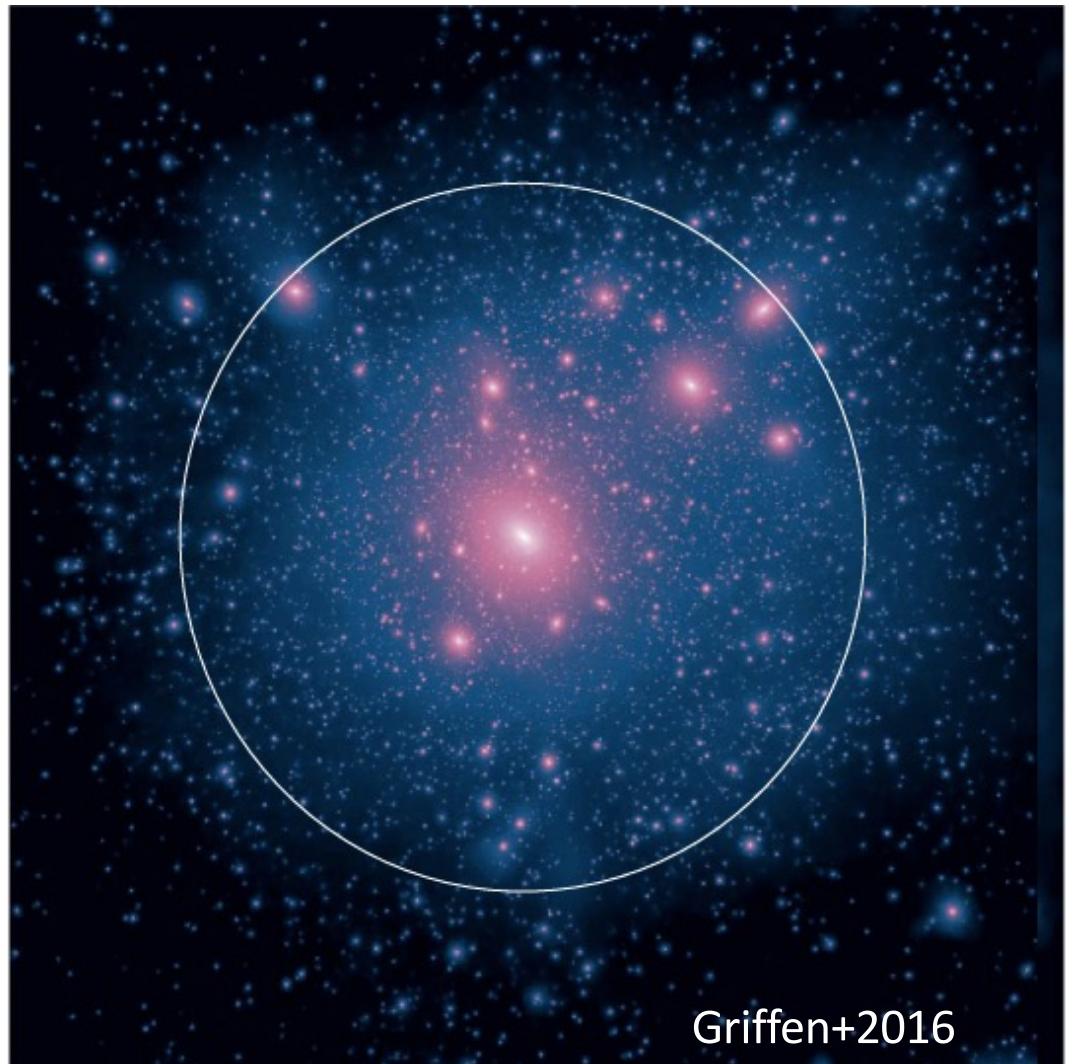
What is the size of the halo?

$R_{\text{vir}}$  = Virial Radius: where the dark matter density is 360x the average dm density of the universe.  
(assuming Planck cosmology)

$R_{200}$  = where the dark matter density is 200x the critical density needed to close the universe.

$R_{\text{vir}} > R_{200}$

For MW:  $R_{\text{vir}}$  is  $\sim 17 \times$  size of disk  
 $= \sim 260 \text{ kpc}$  (if halo =  $1\text{e}12 \text{ M}_{\odot}$ )



Griffen+2016

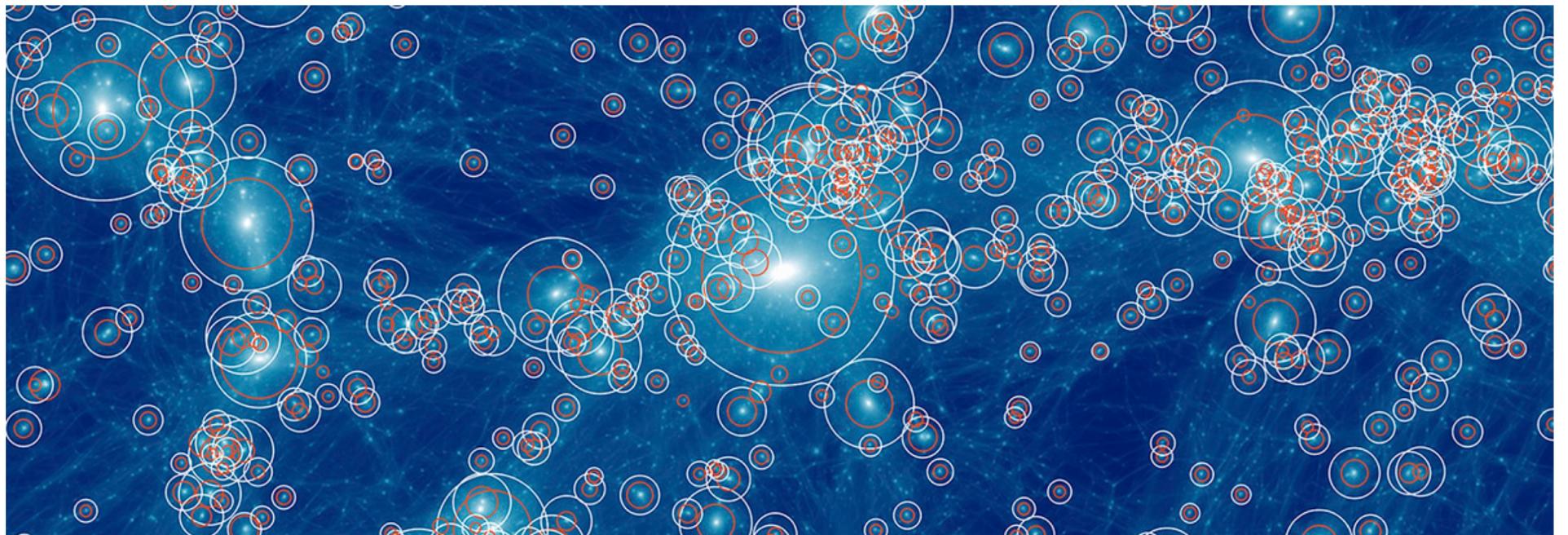


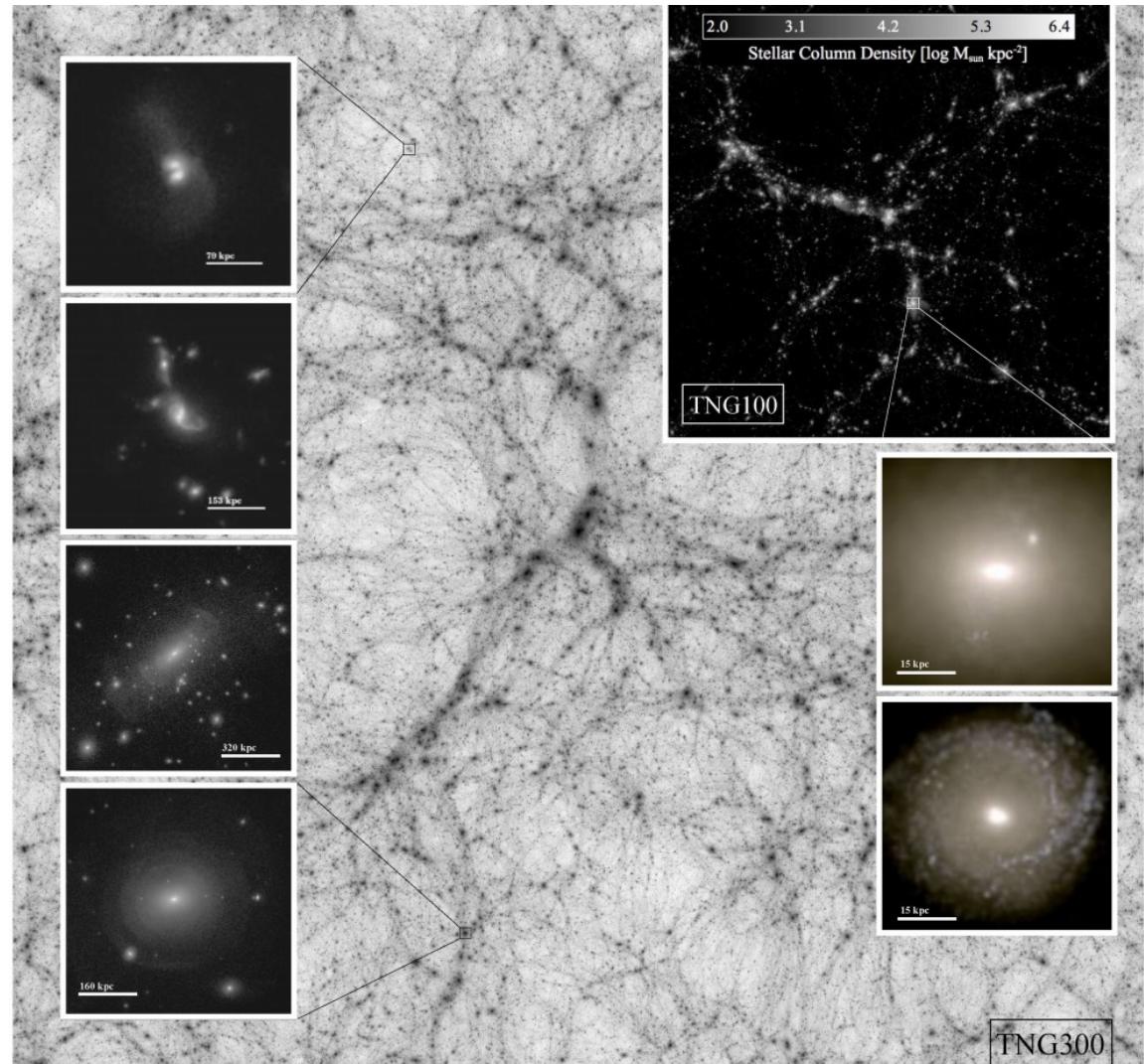
Image: Benedikt Diemer

Splash back radius (white), where particles reach the apocenter of their first orbit, is larger than  $R_{\text{vir}}$  (orange)

See also More, Diemer & Kravtsov 2015

How do we  
put the right  
stellar mass  
galaxy into the  
the halo with  
the right dark  
matter mass ?

Pillepich+  
MNRAS 475, 2018



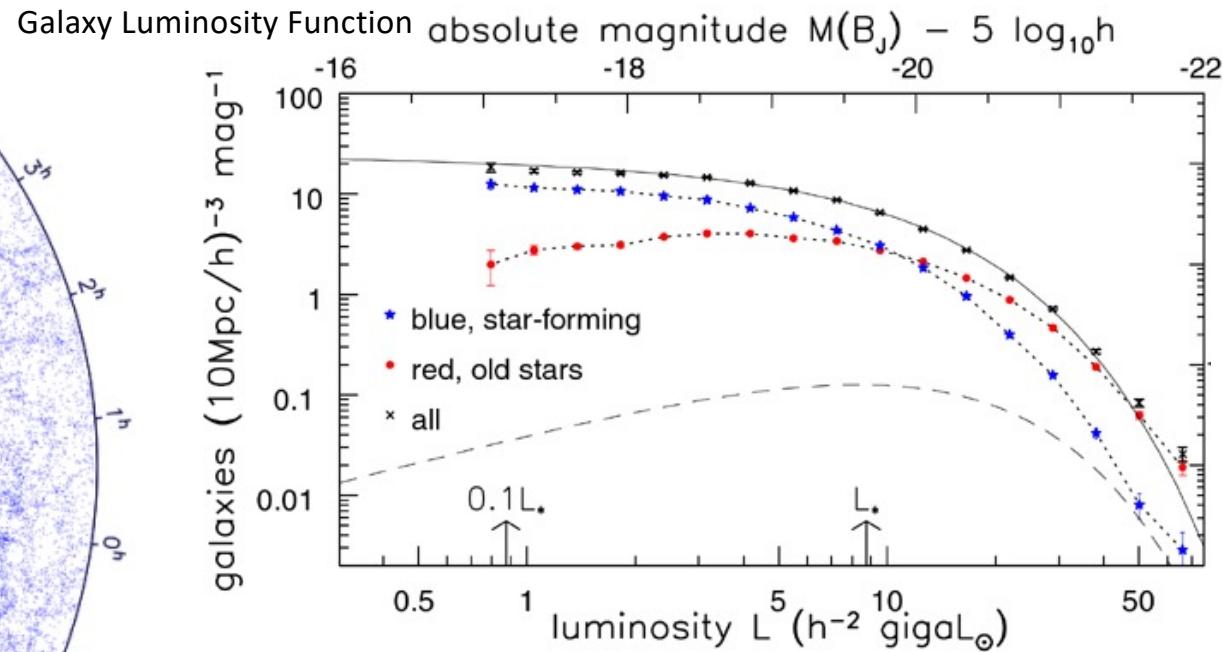
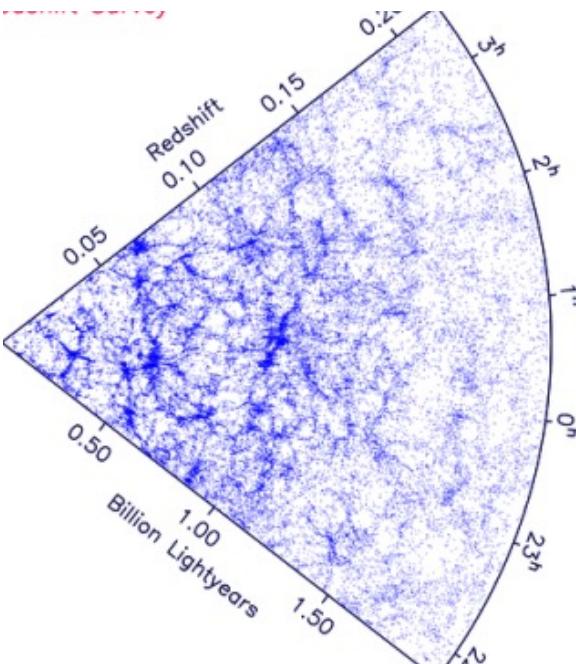


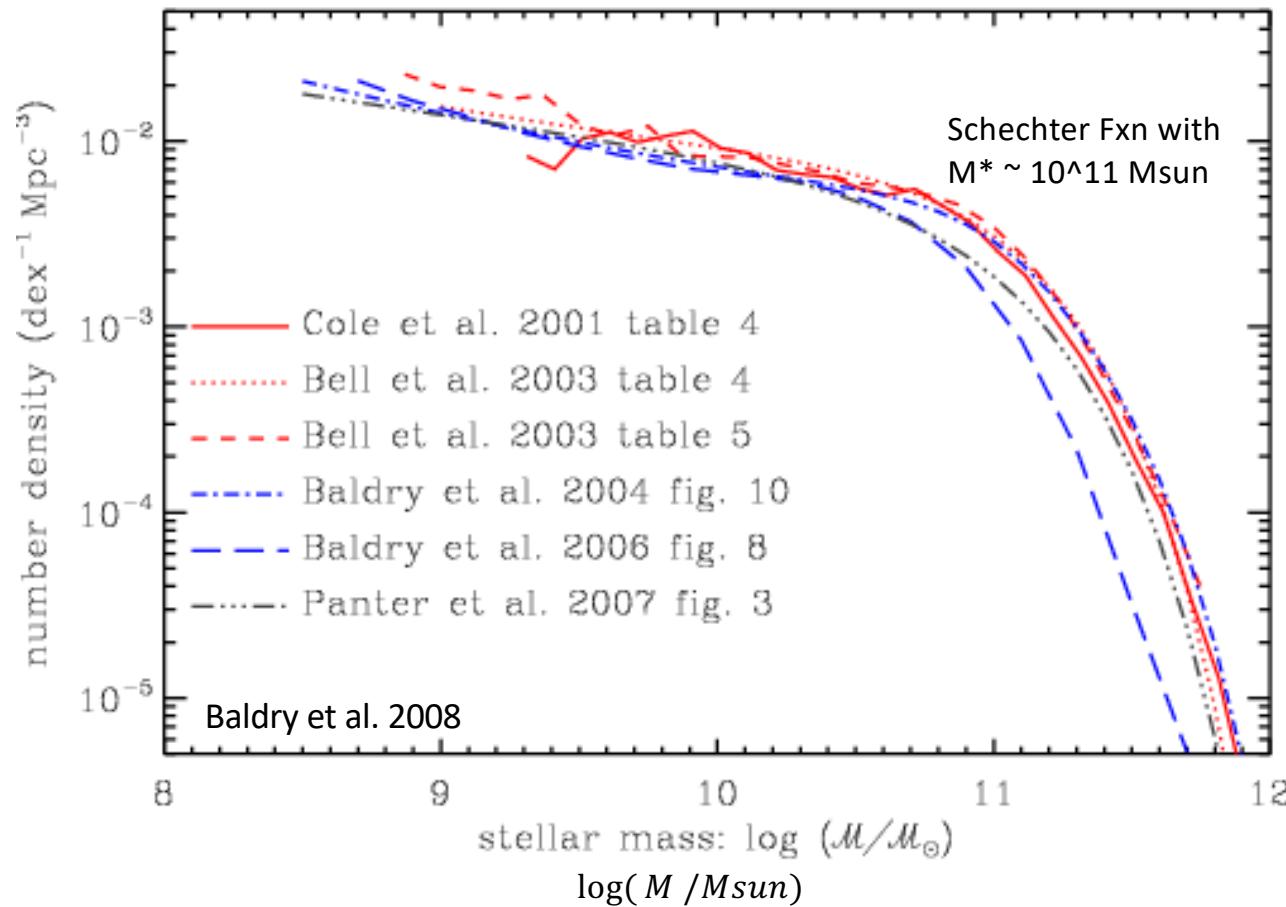
Fig 1.16 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

**Fig. 1.16.** Number of galaxies per  $10 \text{ Mpc}$  cube between absolute magnitude  $M(B_J)$  and  $M(B_J) + 1$  (crosses). Dotted lines show numbers of blue (stars) and red (filled dots) galaxies making up this total; vertical bars indicate errors. The solid line shows the luminosity function of Equation 1.24; the dashed line gives  $\Phi(M) \times L/L_*$ , the light from galaxies in each interval of absolute magnitude. The blue bandpass  $B_J$  is matched to the photographic plates used to select the galaxies – 2dF survey, D. Croton.

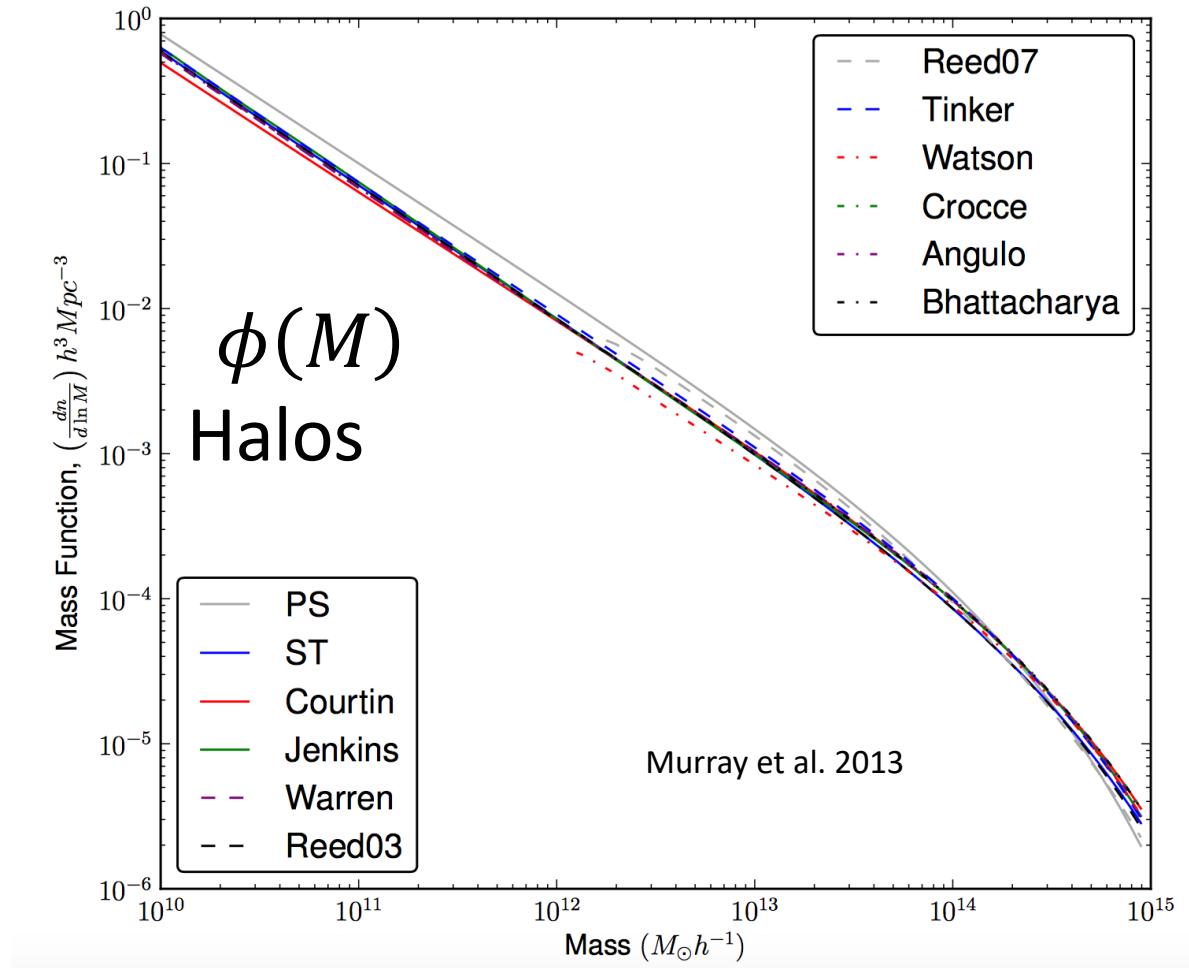
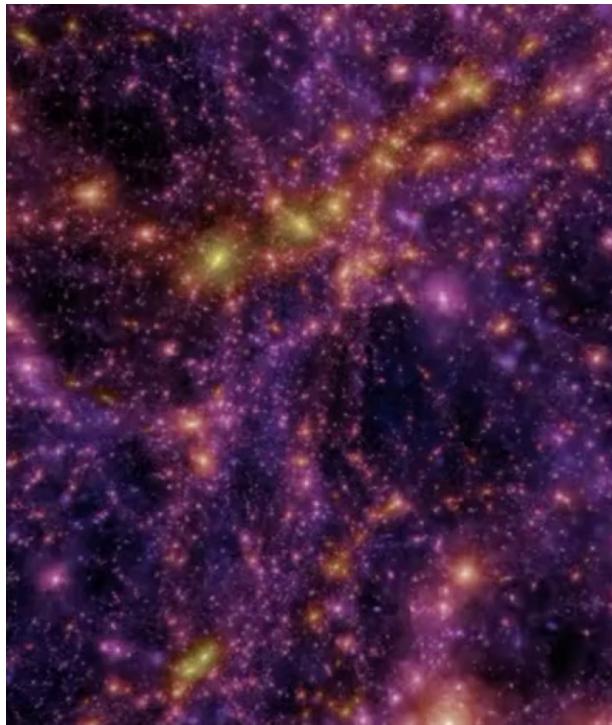
Sparke & Gallagher Ch 1

$\phi(M)$   
Galaxy

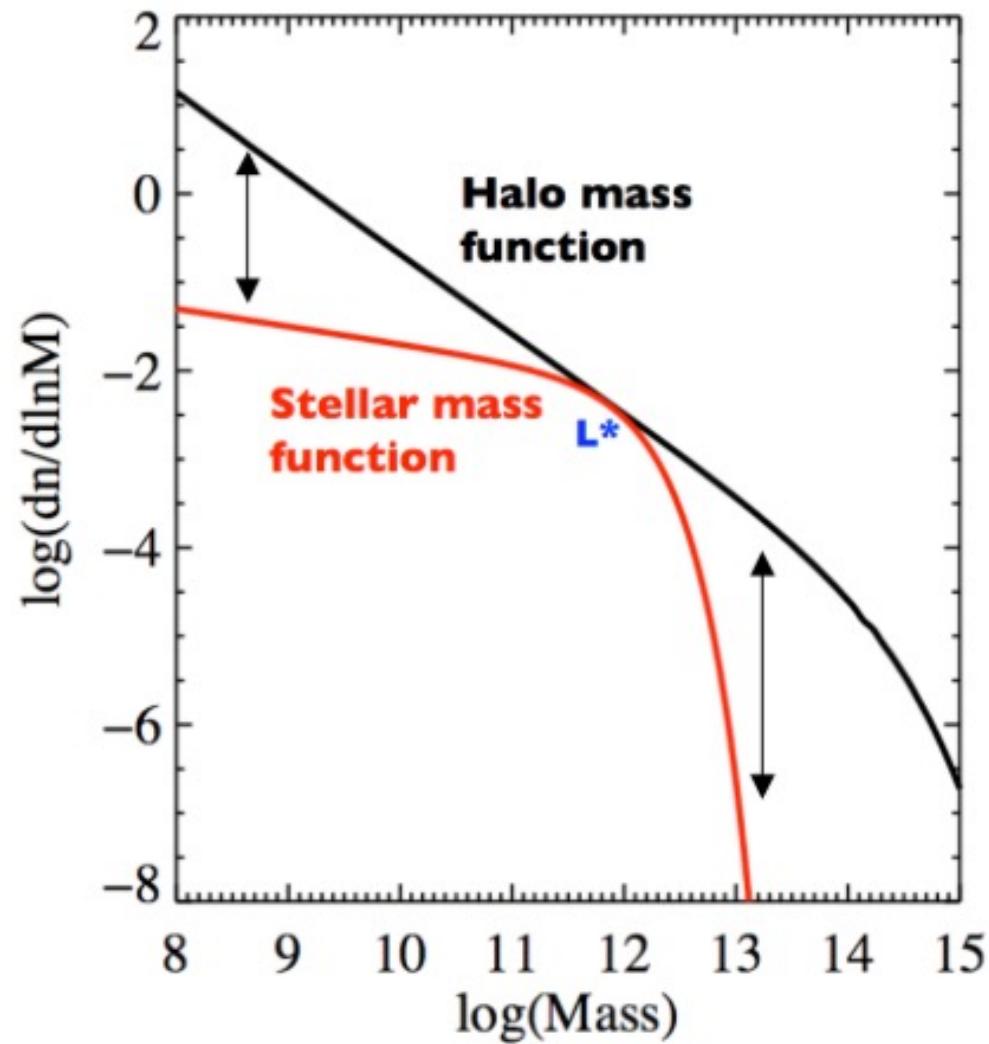
If we can determine each galaxy's mass-to-light ratio (M/L) we can construct a **galaxy stellar mass function**



From dark matter-only simulations, we can find the mass function of dark matter halos.



Need a relationship to connect  
the number of halos per dark matter halo mass bin  
to  
the number of galaxies per galaxy stellar mass bin

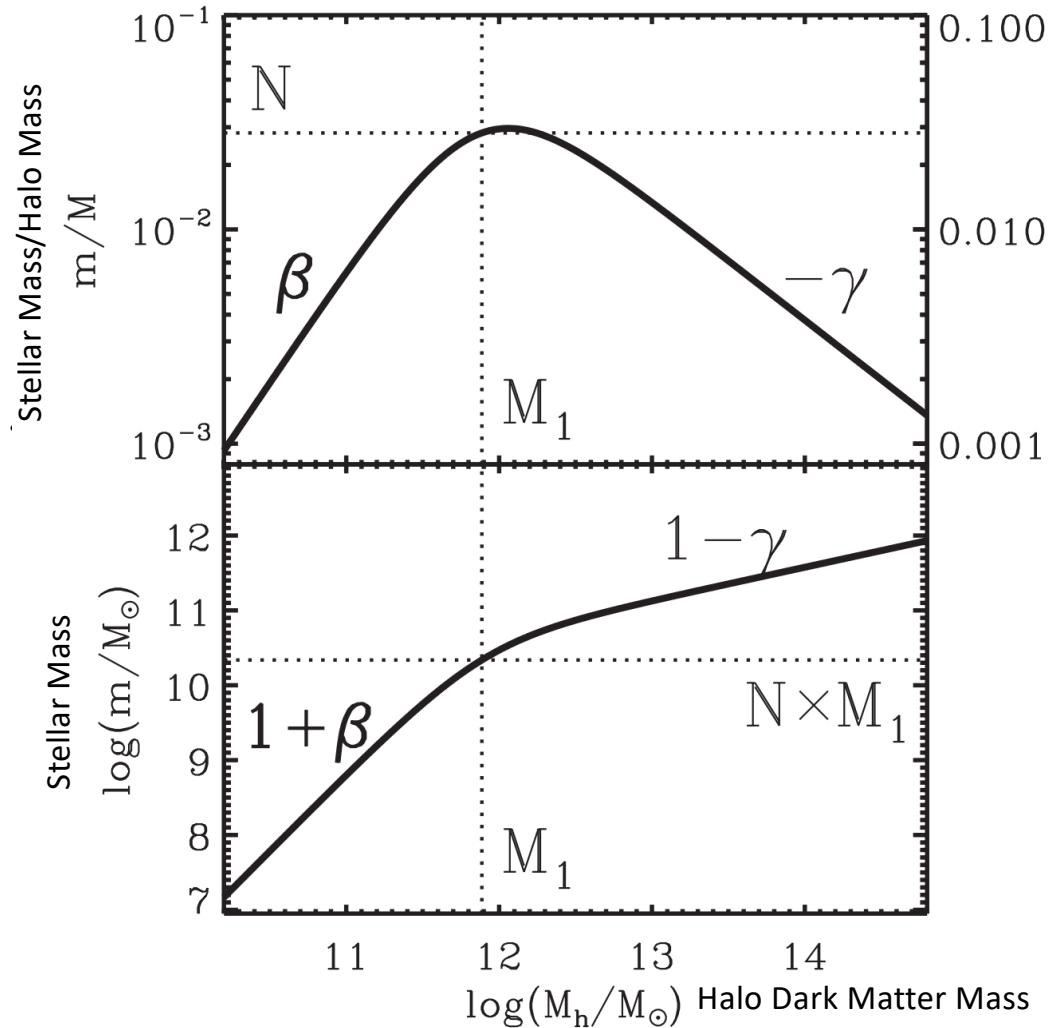


# Halo Mass to Stellar Mass Relation

$$\frac{m}{M} = 2N \left[ \left( \frac{M}{M_1} \right)^{-\beta} + \left( \frac{M}{M_1} \right)^\gamma \right]^{-1}$$

Moster + 2013 MNRAS 428, 3121

See also Behroozi+2013



# Moster+2013 eqns 11-14, Table 1 : Lab 5 part B

$$\log M_1(z) = M_{10} + M_{11}(1 - a) = M_{10} + M_{11} \frac{z}{z + 1}$$

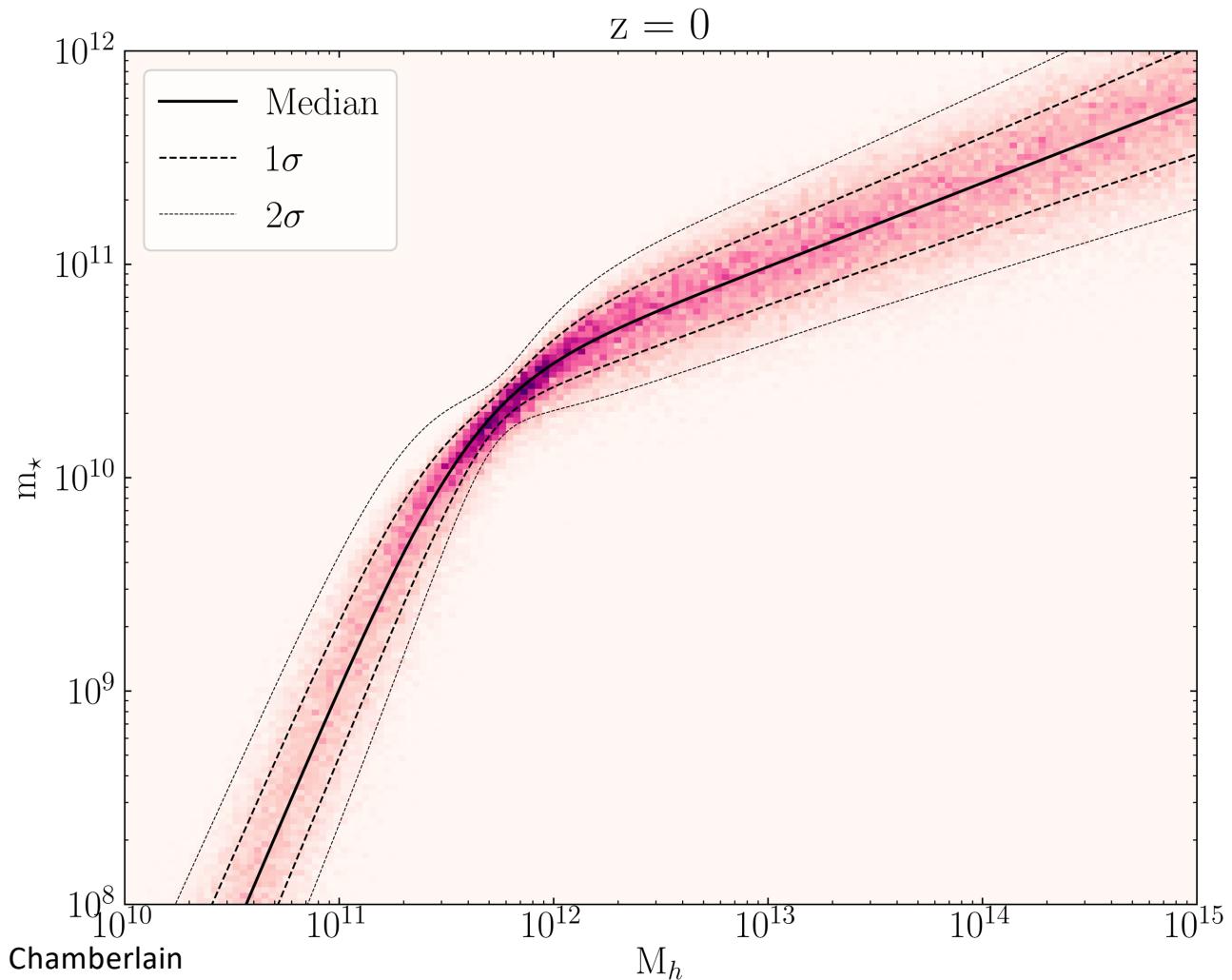
$$N(z) = N_{10} + N_{11}(1 - a) = N_{10} + N_{11} \frac{z}{z + 1}, \quad \gamma(z) = \gamma_{10} + \gamma_{11}(1 - a) = \gamma_{10} + \gamma_{11} \frac{z}{z + 1}.$$

$$\beta(z) = \beta_{10} + \beta_{11}(1 - a) = \beta_{10} + \beta_{11} \frac{z}{z + 1},$$

**Table 1.** Fitting results for the redshift-dependent SHM relationship.

	$M_{10}$	$M_{11}$	$N_{10}$	$N_{11}$	$\beta_{10}$	$\beta_{11}$	$\gamma_{10}$	$\gamma_{11}$
Best fit	11.590	1.195	0.0351	-0.0247	1.376	-0.826	0.608	0.329
Range $\pm$	0.236	0.353	0.0058	0.0069	0.153	0.225	0.059	0.173

Notes. All masses are in units of  $M_\odot$ .



Courtesy: Dr Katie Chamberlain