Data Source and reference

- The data is collected from the source https://github.com/CSSEGISandData/COVID-19 (https://github.com/CSSEGISandData/COVID-19)
- This is the data repository for the 2019 Novel Coronavirus Visual Dashboard operated by the `Johns Hopkins University Center for Systems Science and Engineering (JHU CSSE)`. Also, Supported by `ESRI Living Atlas Team and the Johns Hopkins University Applied Physics Lab (JHU APL)`.
- You can view their dashboard at https://www.arcgis.com/apps/opsdashboard/index.html#/bda7594740fd40299423467b48e9ecf6 (https://www.arcgis.com/apps/opsdashboard/index.html#/bda7594740fd40299423467b48e9ecf6)

For SIR model fitting and analysis, we are taking help from the blogposts:

- https://towardsdatascience.com/infectious-disease-modelling-part-i-understanding-sir-28d60e29fdfc (https://towardsdatascience.com/infectious-disease-modelling-part-i-understanding-sir-28d60e29fdfc)
- https://towardsdatascience.com/infectious-disease-modelling-beyond-the-basic-sir-model-216369c584c4 (https://towardsdatascience.com/infectious-disease-modelling-beyond-the-basic-sir-model-216369c584c4)
- https://towardsdatascience.com/infectious-disease-modelling-fit-your-model-to-coronavirus-data-2568e672dbc7 (https://towardsdatascience.com/infectious-disease-modelling-fit-your-model-to-coronavirus-data-2568e672dbc7)

```python
In [1]:  import pandas as pd
         from IPython.display import Image
         import os
         import numpy as np
         import pandas as pd
         %matplotlib inline
         import warnings
         warnings.filterwarnings('ignore')

         COUNTRY = 'India'
```

```python
In [2]:  conf_case = pd.read_csv("https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19_time
         _series/time_series_covid19_confirmed_global.csv")
         conf_death = pd.read_csv("https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19_tim
         e_series/time_series_covid19_deaths_global.csv")
         conf_recovered = pd.read_csv("https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19
         _time_series/time_series_covid19_recovered_global.csv")
```

```python
In [3]:  cdf_conf_case = conf_case[conf_case['Country/Region']==COUNTRY].sum().drop(['Province/State','Country/Region','Lat','Long'])
         cdf_conf_death = conf_death[conf_death['Country/Region']==COUNTRY].sum().drop(['Province/State','Country/Region','Lat','Long'])
         cdf_conf_recovered = conf_recovered[conf_recovered['Country/Region']==COUNTRY].sum().drop(['Province/State','Country/Region','L
         at','Long'])
```

```python
In [4]:  def perDayCalc(totalList):
             pdf = []
             for idx, num in enumerate(totalList):
                 if idx == 0:
                     pdf.append(num)
                     prev = num
                 else:
                     pdf.append(num - prev)
                     prev = num
             return pdf

         def rateOfChange(totalList, interval=5):
             changeVal = []
             changePer = []
             for idx, num in enumerate(totalList):
                 if idx < interval:
                     changeVal.append(sum(totalList[:(idx+1)])/(idx+1))
                 else:
                     changeVal.append(sum(totalList[idx-interval+1:(idx+1)])/interval)
             for idx, newVal in enumerate(changeVal):
                 if idx == 0:
                     changePer.append(0)
                     prevVal = newVal
                 elif prevVal!=0:
                     changePer.append(100*(newVal-prevVal)/prevVal)
                     prevVal = newVal
                 else:
                     changePer.append(1)
                     prevVal = newVal
             #changePer = [i%35 for i in changePer]
             return changePer #changeVal

         def doublingRate(changePer):
             return [np.log(2)/np.log(1+(per/100)) for per in changePer]
```

```
In [5]:  cdf_case_list = cdf_conf_case.to_frame().T.sum().tolist()
         cdf_death_list = cdf_conf_death.to_frame().T.sum().tolist()
         cdf_recovered_list = cdf_conf_recovered.to_frame().T.sum().tolist()
         cdf_active_list = np.subtract(np.subtract(cdf_case_list, cdf_recovered_list).tolist(), cdf_death_list).tolist()

         pdf_case_list = perDayCalc(cdf_case_list)
         pdf_death_list = perDayCalc(cdf_death_list)
         pdf_recovered_list = perDayCalc(cdf_recovered_list)
         pdf_active_list = perDayCalc(cdf_active_list)
```

Cummulative visualization of COVID-19 cases in India since inception

```
In [6]:  data = {"Date": cdf_conf_case.to_frame().T.columns.to_list(),
                 "Total Case": cdf_case_list,
                 "Total Death": cdf_death_list,
                 "Total Recovered Case": cdf_recovered_list,
                 "Total Active Case": cdf_active_list}
         df = pd.DataFrame(data).set_index("Date")
         df.plot(figsize=(20, 10), title ="Total COVID-19 cases since inception", fontsize = 10, kind="line")
         plt.show()
```
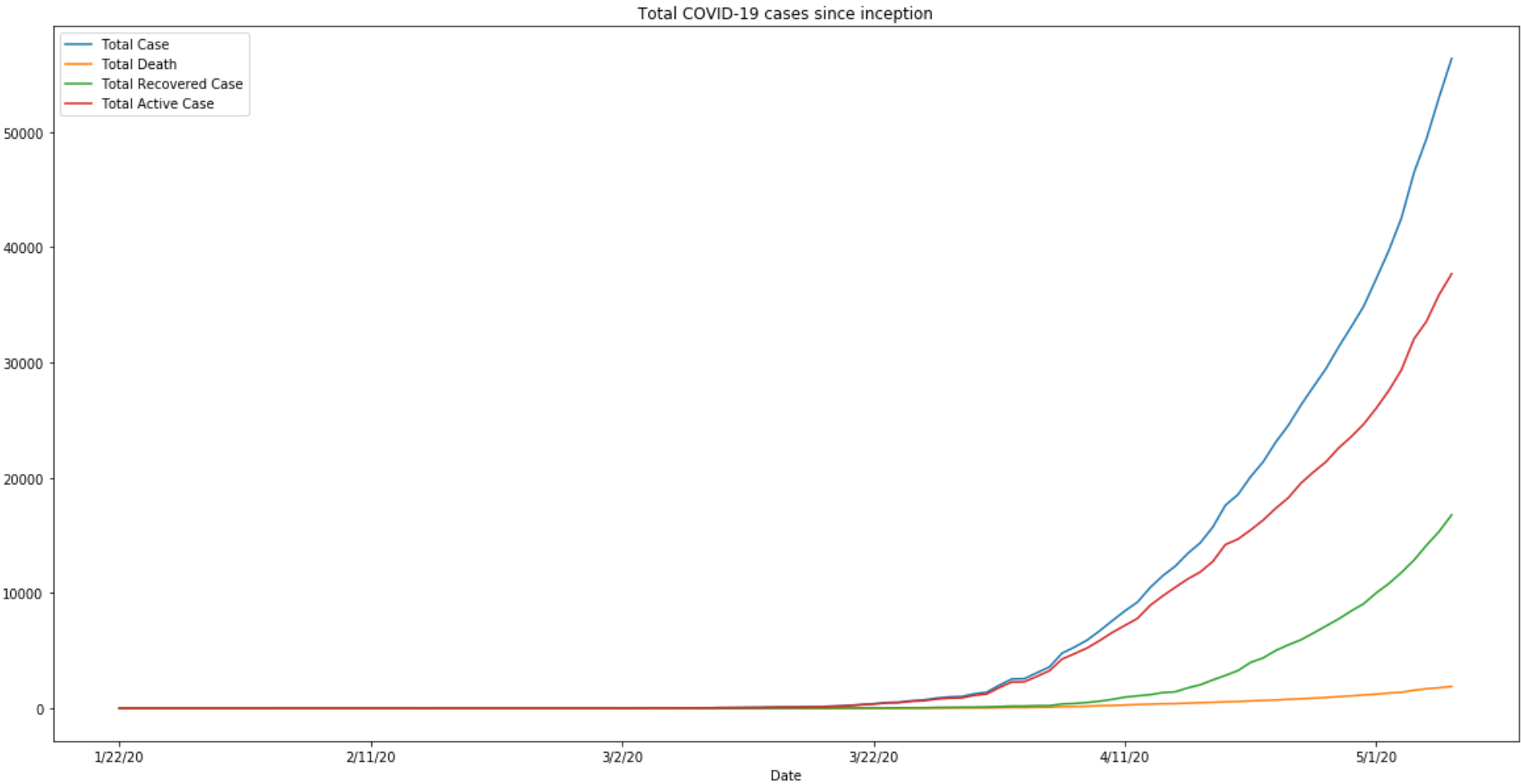

Daily basis newly added case visualization along with reecovered cases

```
In [7]: slice_1=-40
        data1 = {"Date": cdf_conf_case.to_frame().T.columns.to_list()[slice_1:],
                "Total Case": pdf_case_list[slice_1:],
                "Total Death": pdf_death_list[slice_1:],
                "Recovered Case": pdf_recovered_list[slice_1:],
                "Active Case": pdf_active_list[slice_1:]}
        dictfilt = lambda x, y: dict([ (i,x[i]) for i in x if i in set(y) ])
        data = dictfilt(data1, ("Total Case", "Recovered Case", 'Date'))
        df = pd.DataFrame(data).set_index("Date")
        df.plot(title="Day basis newly registerd cases and active cases",
                fontsize = 14, kind="bar", grid = True, figsize=(22,12))
        plt.xticks(rotation=90)
        plt.show()
```
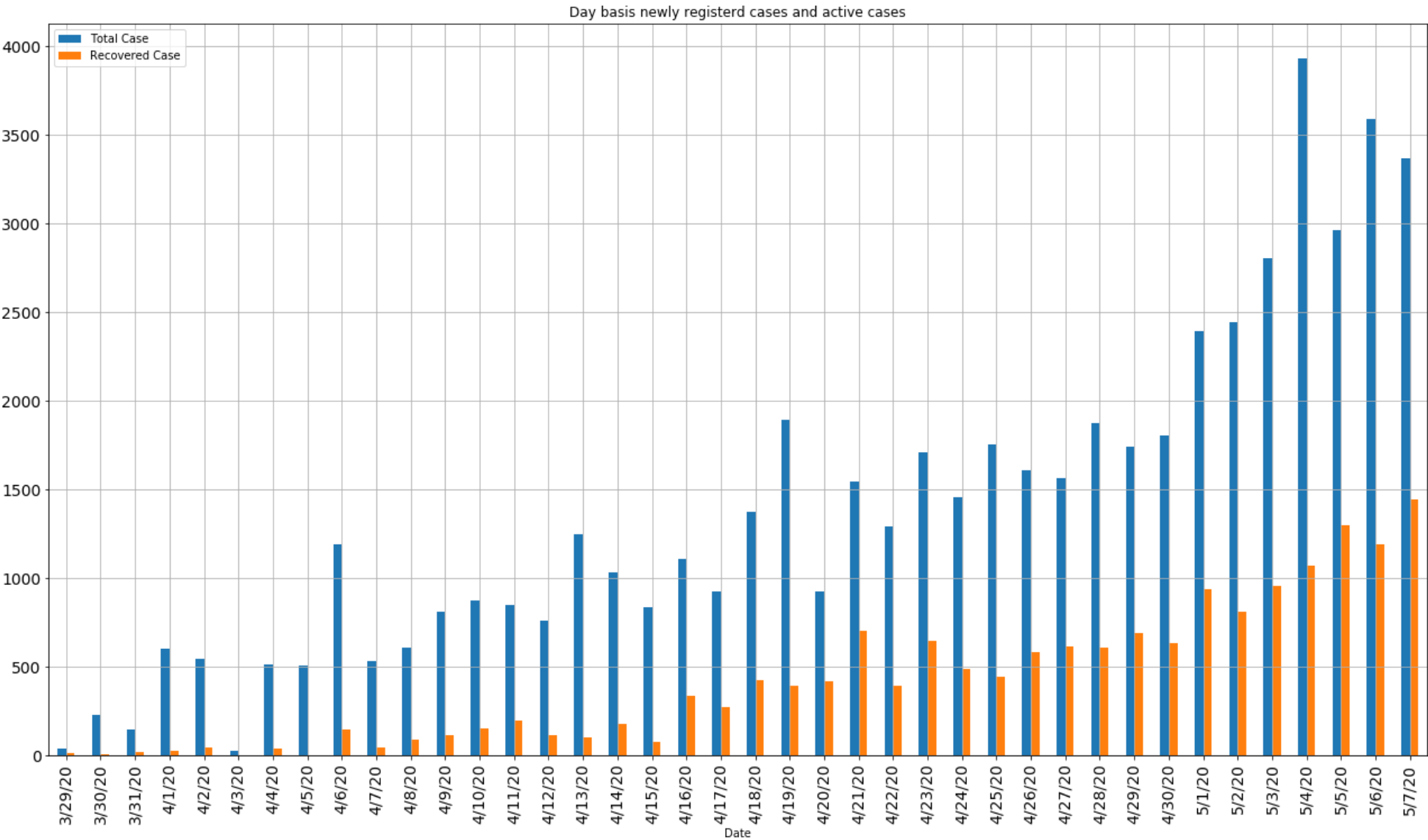


```
In [8]: df = pd.DataFrame.from_dict(data1)
        print(f"Total New cases added on last day: {np.round(df.iloc[-1].tolist()[1], 0)}")
        print(f"Total Death cases added on last day: {np.round(df.iloc[-1].tolist()[2], 0)}")
        print(f"Total Recovered cases added on last day: {np.round(df.iloc[-1].tolist()[3], 0)}")
        print(f"Changes/Added on Active cases on last day: {np.round(df.iloc[-1].tolist()[4], 0)}")
```

```
Total New cases added on last day: 3364.0
Total Death cases added on last day: 104.0
Total Recovered cases added on last day: 1445.0
Changes/Added on Active cases on last day: 1815.0
```

Rate of Increase of COVID-19 cases

Percentage wise increment of daily NEW cases as compared to previous day

```
In [9]: slice_1=-40
        data1 = {"Date": cdf_conf_case.to_frame().T.columns.to_list()[slice_1:],
                 "Total Case": rateOfChange(cdf_case_list)[slice_1:],
                 "Total Death": rateOfChange(cdf_death_list)[slice_1:],
                 "Recovered Case": rateOfChange(cdf_recovered_list)[slice_1:],
                 "Active Case": rateOfChange(cdf_active_list)[slice_1:],
                 "Doubling rate of Total Case": doublingRate(rateOfChange(cdf_case_list))[slice_1:]
                }
        dictfilt = lambda x, y: dict([ (i,x[i]) for i in x if i in set(y) ])
        data = dictfilt(data1, ("Total Case", 'Date'))
        df = pd.DataFrame(data).set_index("Date")
        df.plot(figsize=(22, 12), title ="Rate of percentage Increament of COVID-19 NEW case", fontsize = 10, kind="bar", grid = True)
        plt.show()
```


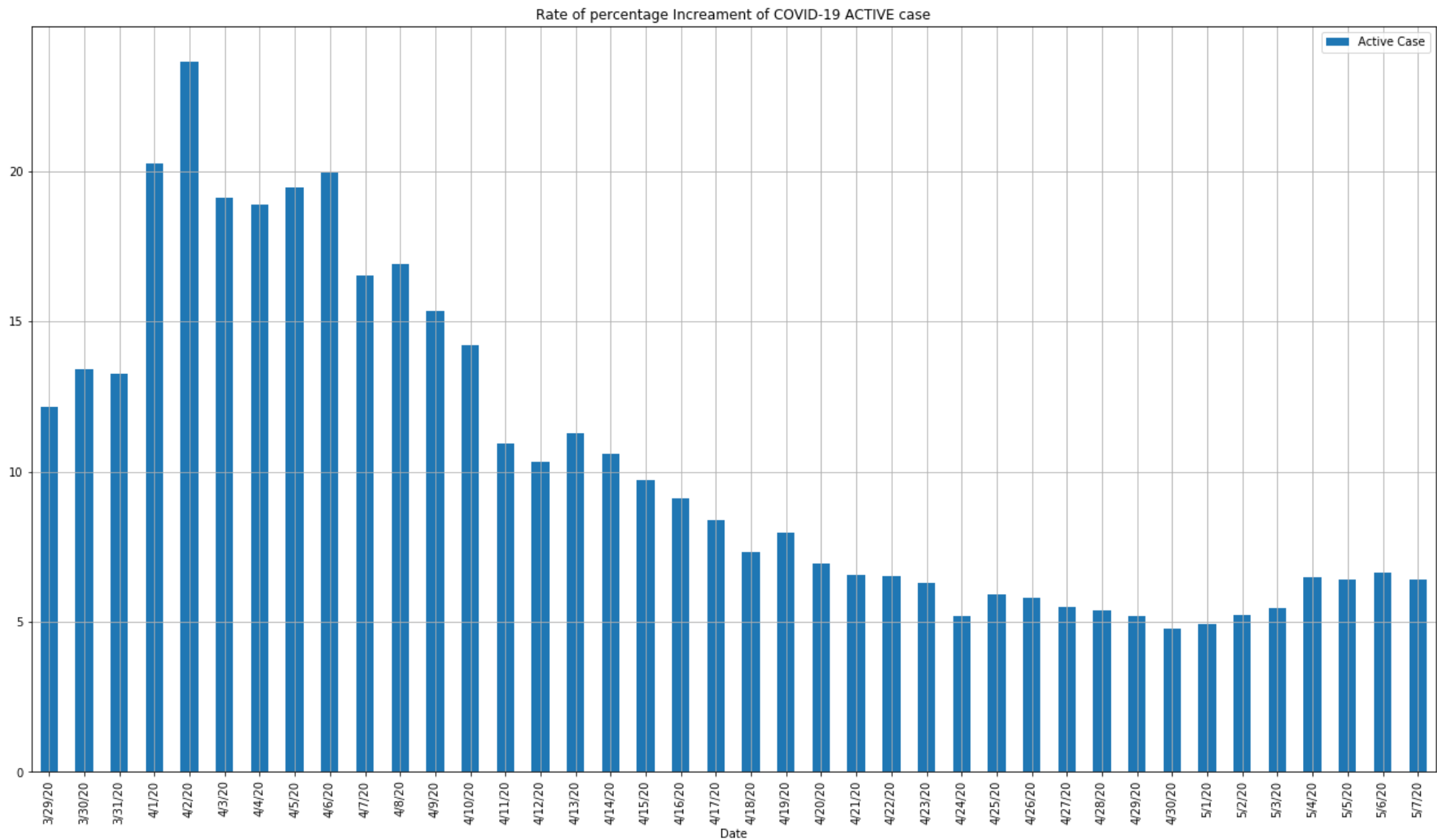Rate of percentage Increament of COVID-19 NEW case
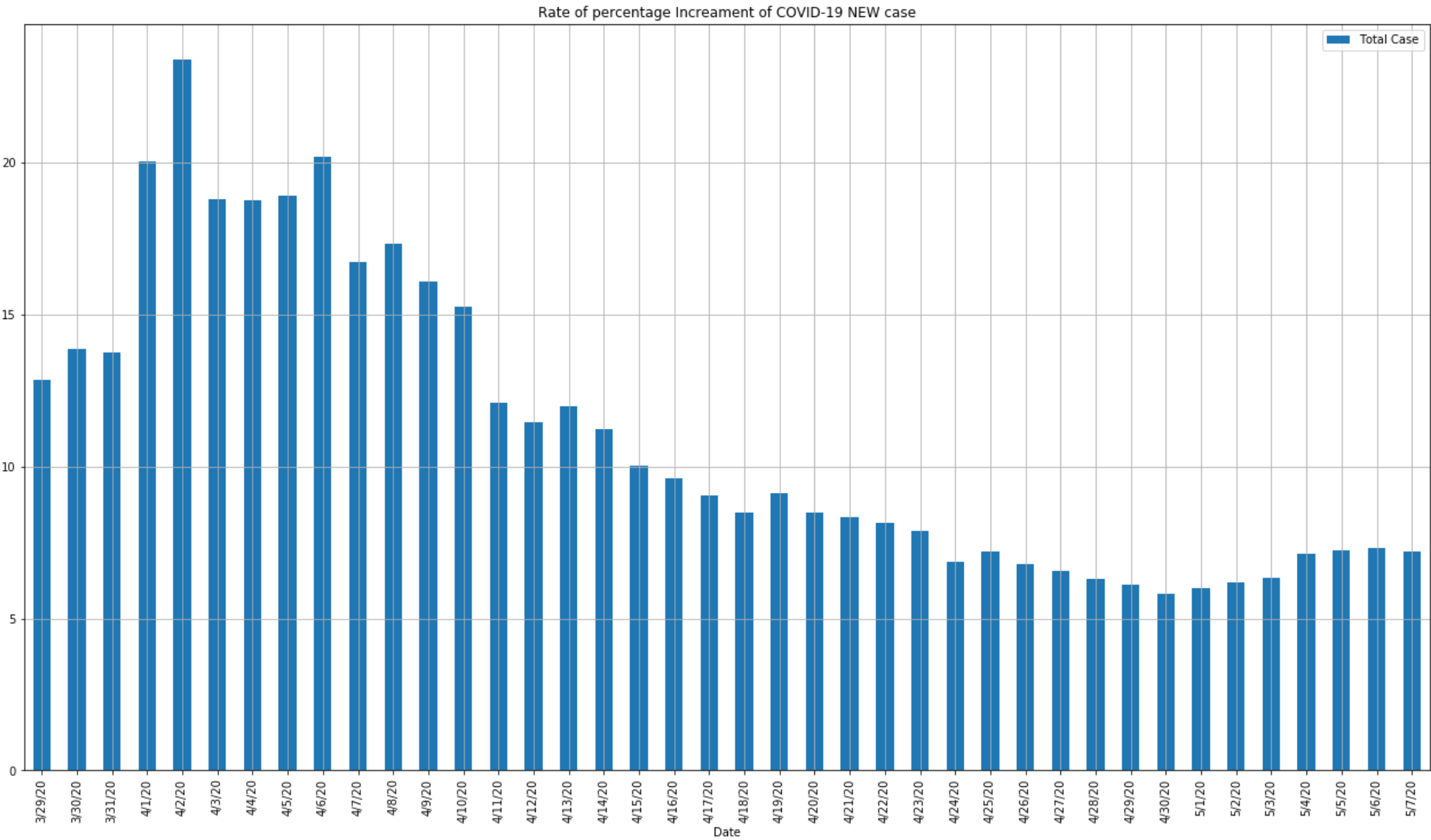
```
In [10]: present_case_rate = df.iloc[-1].tolist()[0]
         print(f"Percentage increment of total cases as compared to previous day: {np.round(df.iloc[-1].tolist()[0], 2)}%")
```

Percentage increment of total cases as compared to previous day: 7.21%

Percentage wise increment of daily ACTIVE cases as compared to previous day

```
In [11]: slice_1=-40
         data1 = {"Date": cdf_conf_case.to_frame().T.columns.to_list()[slice_1:],
                 "Total Case": rateOfChange(cdf_case_list)[slice_1:],
                 "Total Death": rateOfChange(cdf_death_list)[slice_1:],
                 "Recovered Case": rateOfChange(cdf_recovered_list)[slice_1:],
                 "Active Case": rateOfChange(cdf_active_list)[slice_1:],
                 "Doubling rate of Total Case": doublingRate(rateOfChange(cdf_case_list))[slice_1:]
                 }
         dictfilt = lambda x, y: dict([ (i,x[i]) for i in x if i in set(y) ])
         data = dictfilt(data1, ("Active Case", 'Date'))
         df = pd.DataFrame(data).set_index("Date")
         df.plot(figsize=(22, 12), title ="Rate of percentage Increament of COVID-19 ACTIVE case", fontsize = 10, kind="bar", grid = Tru
         e)
         plt.show()
```


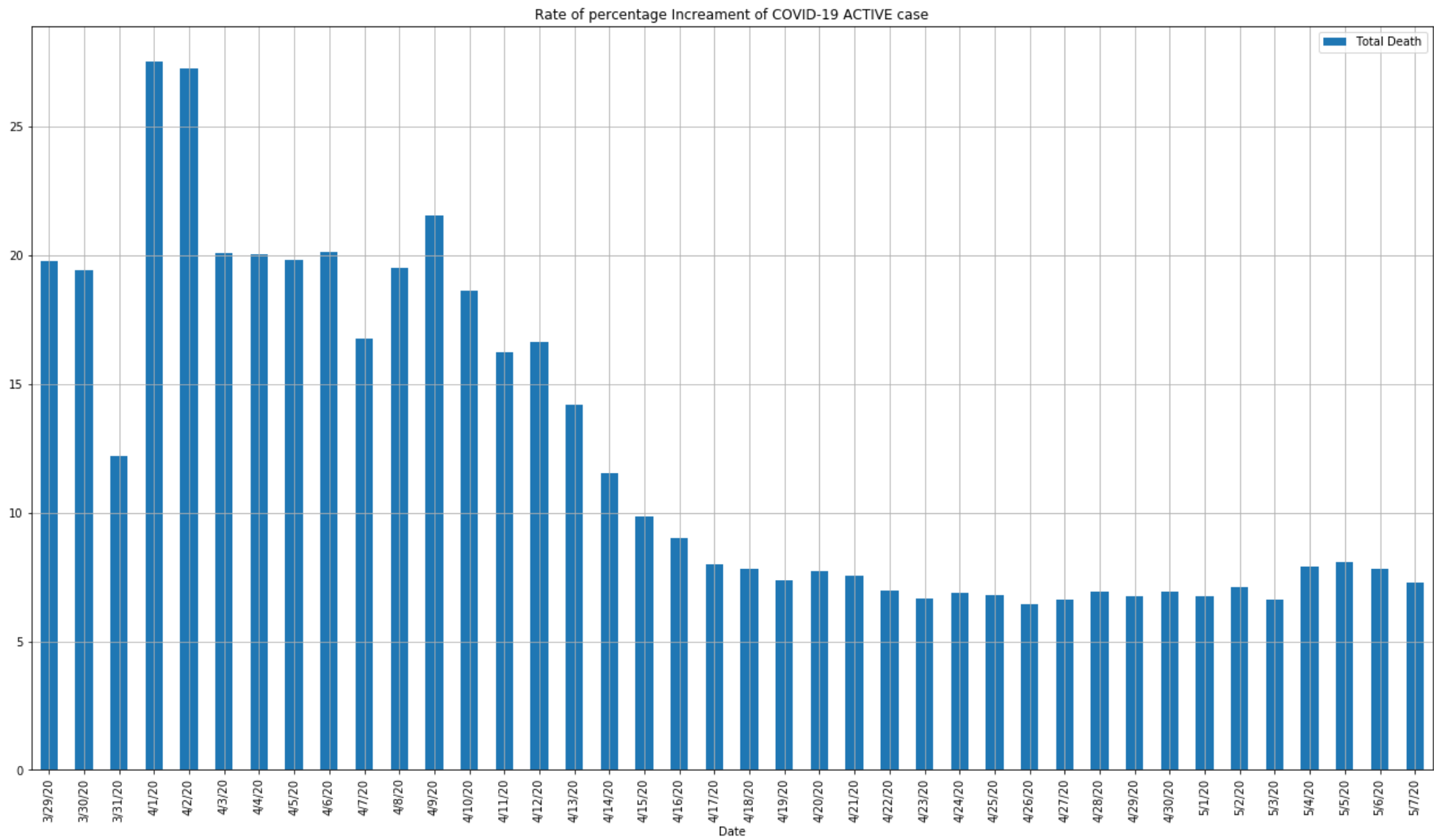Rate of percentage Increament of COVID-19 ACTIVE case

```
In [12]: print(f"Percentage increment of active cases as compared to previous day: {np.round(df.iloc[-1].tolist()[0], 2)}%")

         Percentage increment of active cases as compared to previous day: 6.4%
```

Percentage wise increment of daily DEATH cases as compared to previous day

```
In [13]: slice_1=-40
         data1 = {"Date": cdf_conf_case.to_frame().T.columns.to_list()[slice_1:],
                 "Total Case": rateOfChange(cdf_case_list)[slice_1:],
                 "Total Death": rateOfChange(cdf_death_list)[slice_1:],
                 "Recovered Case": rateOfChange(cdf_recovered_list)[slice_1:],
                 "Active Case": rateOfChange(cdf_active_list)[slice_1:],
                 "Doubling rate of Total Case": doublingRate(rateOfChange(cdf_case_list))[slice_1:]
                 }
         dictfilt = lambda x, y: dict([ (i,x[i]) for i in x if i in set(y) ])
         data = dictfilt(data1, ("Total Death", 'Date'))
         df = pd.DataFrame(data).set_index("Date")
         df.plot(figsize=(22, 12), title ="Rate of percentage Increament of COVID-19 ACTIVE case", fontsize = 10, kind="bar", grid = Tru
         e)
         plt.show()
```


Rate of percentage Increament of COVID-19 ACTIVE case

```
In [14]: present_death_rate = df.iloc[-1].tolist()[0]
         print(f"Percentage increment of DEATH cases as compared to previous day: {np.round(df.iloc[-1].tolist()[0], 2)}%")

         Percentage increment of DEATH cases as compared to previous day: 7.3%
```

Percentage wise increment of daily RECOVERED cases as compared to previous day

```
In [15]: slice_1=-40
         data1 = {"Date": cdf_conf_case.to_frame().T.columns.to_list()[slice_1:],
                  "Total Case": rateOfChange(cdf_case_list)[slice_1:],
                  "Total Death": rateOfChange(cdf_death_list)[slice_1:],
                  "Recovered Case": rateOfChange(cdf_recovered_list)[slice_1:],
                  "Active Case": rateOfChange(cdf_active_list)[slice_1:],
                  "Doubling rate of Total Case": doublingRate(rateOfChange(cdf_case_list))[slice_1:]
                 }
         dictfilt = lambda x, y: dict([ (i,x[i]) for i in x if i in set(y) ])
         data = dictfilt(data1, ("Recovered Case", 'Date'))
         df = pd.DataFrame(data).set_index("Date")
         df.plot(figsize=(22, 12), title ="Rate of percentage Increament of COVID-19 ACTIVE case", fontsize = 10, kind="bar", grid = Tru
         e)
         plt.show()
```


Rate of percentage Increament of COVID-19 ACTIVE case
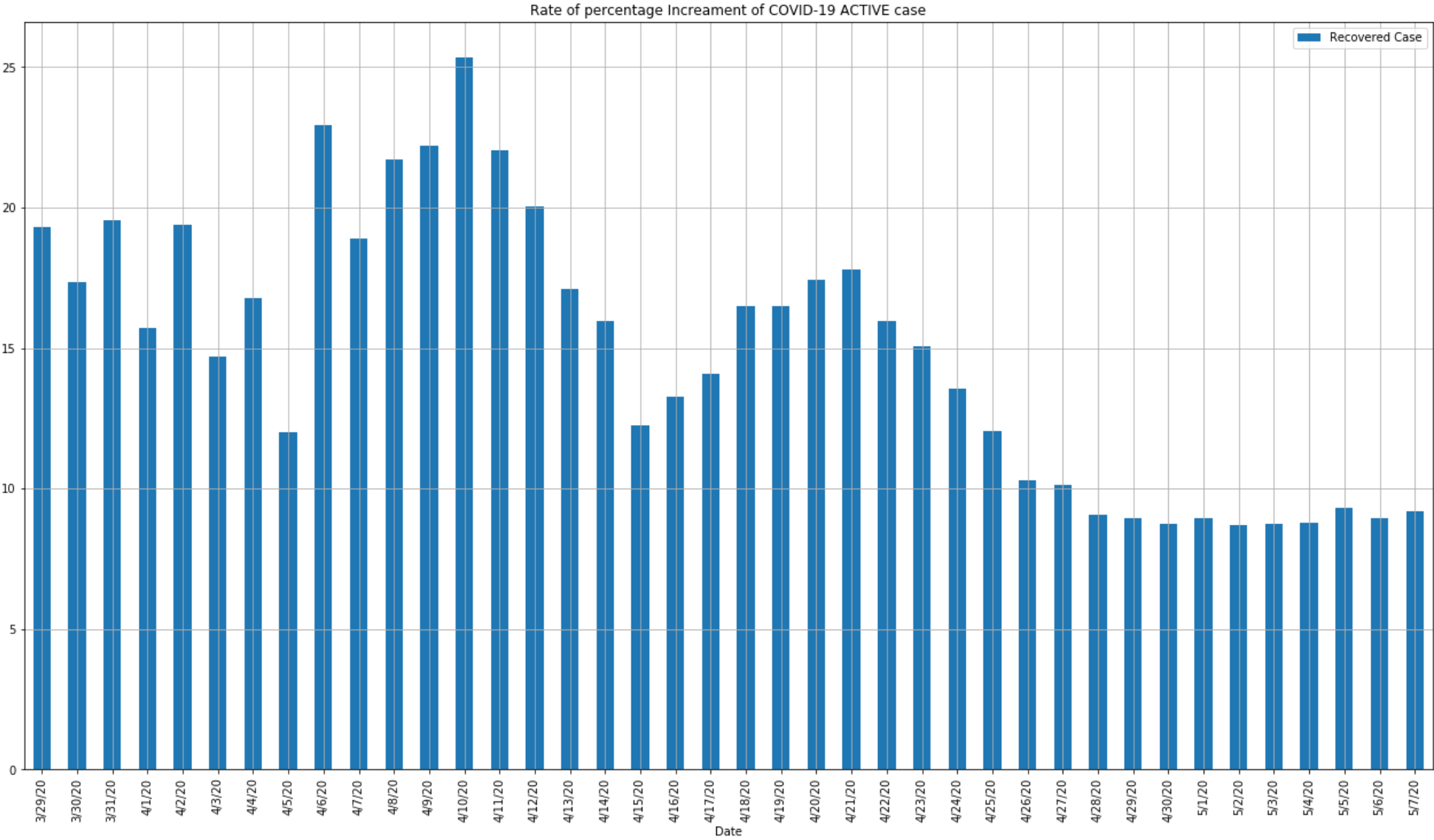
```
In [16]: print(f"Percentage increment of RECOVERED cases as compared to previous day: {np.round(df.iloc[-1].tolist()[0], 2)}%")

         Percentage increment of RECOVERED cases as compared to previous day: 9.18%
```

Doubling rate of the cases in last 5 days

```
In [17]: slice_1=-40
         data1 = {"Date": cdf_conf_case.to_frame().T.columns.to_list()[slice_1:],
                  "Total Case": rateOfChange(cdf_case_list)[slice_1:],
                  "Total Death": rateOfChange(cdf_death_list)[slice_1:],
                  "Recovered Case": rateOfChange(cdf_recovered_list)[slice_1:],
                  "Active Case": rateOfChange(cdf_active_list)[slice_1:],
                  "Doubling rate of Total Case": doublingRate(rateOfChange(cdf_case_list))[slice_1:]
                  }
         dictfilt = lambda x, y: dict([ (i,x[i]) for i in x if i in set(y) ])
         data = dictfilt(data1, ("Doubling rate of Total Case", 'Date'))
         df = pd.DataFrame(data).set_index("Date")
         df.plot(figsize=(20, 10), title ="Rate of doubling COVID-19 case", fontsize = 10, kind="bar", grid = True)
         plt.show()
```
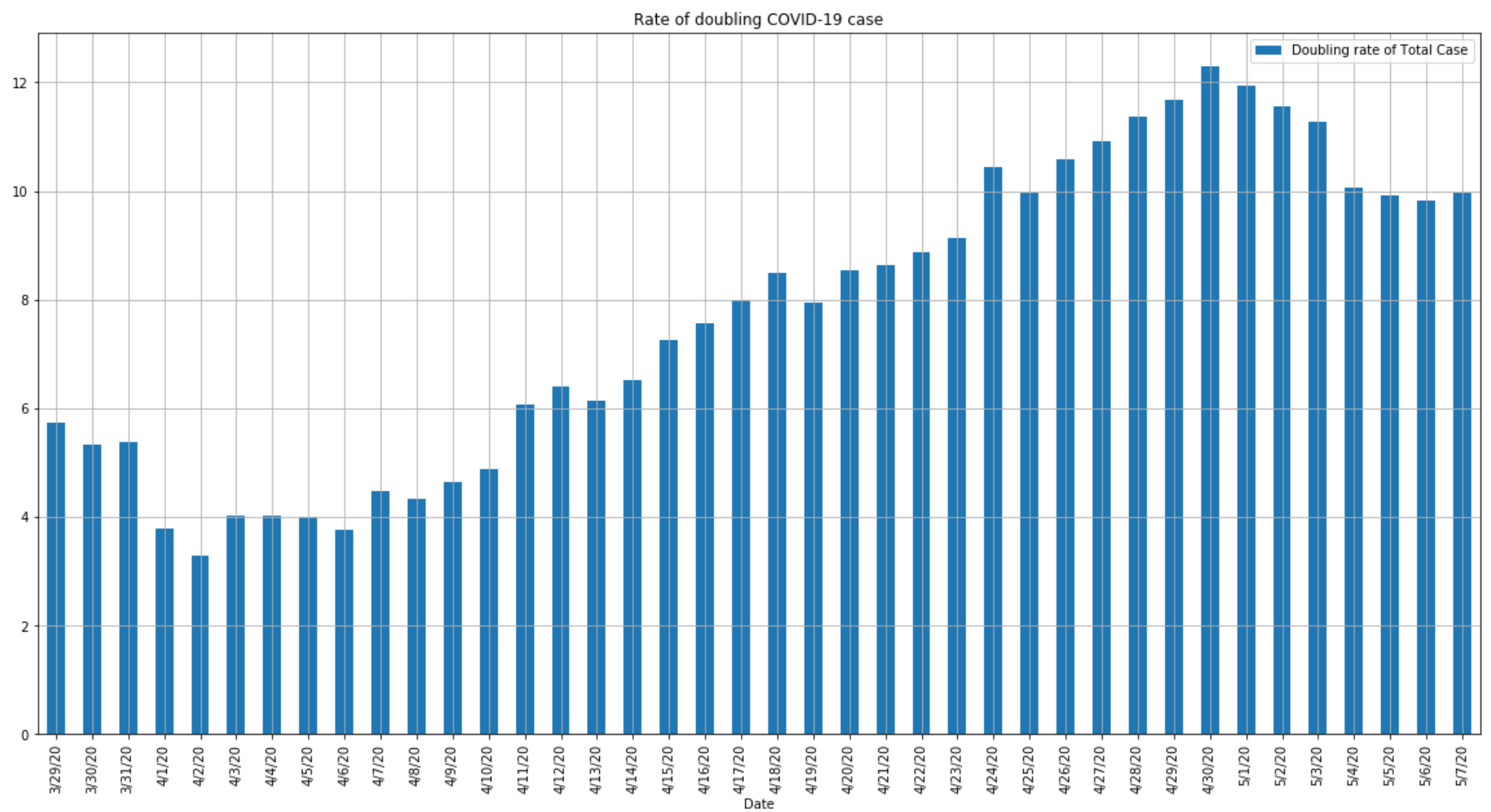


```
In [18]: print(f"Doubling rate of cases: {np.round(df.iloc[-1].tolist()[0], 2)} days")

         Doubling rate of cases: 9.96 days
```

Future number prediction with different rates

```
In [19]: total_case_till_date  = cdf_conf_case.tolist()[-1]
         total_death_till_date = cdf_conf_death.tolist()[-1]
         days=30
         starting_date=cdf_conf_case.to_frame().T.columns.to_list()[-1]
```

```
In [20]: def increment_list(initial_val, percentage_rate, number_count):
             final_list=[]
             for i in range(number_count):
                 if i ==0:
                     final_list.append(initial_val)
                     temp=initial_val
                 else:
                     temp = temp*(1+percentage_rate/100)
                     final_list.append(temp)
             return final_list
```

```
In [26]:  fig, ax = plt.subplots(1, 2, figsize=(25,12))

          ax[0].plot([i for i in range(days)], increment_list(initial_val=total_case_till_date,
                                                     percentage_rate=present_case_rate,
                                                     number_count=days), 'r',
                   label=f'Current Rate ({np.round(present_case_rate,2)}%)')
          ax[0].plot([i for i in range(days)], increment_list(initial_val=total_case_till_date,
                                                     percentage_rate=5,
                                                     number_count=days), 'g', label='5% Rate')
          ax[0].plot([i for i in range(days)], increment_list(initial_val=total_case_till_date,
                                                     percentage_rate=10,
                                                     number_count=days), 'b', label='10% Rate')
          ax[0].set_title("Total CASEs with different rete(%) of increment")
          ax[0].set_xlabel(f"Date strting from: {starting_date}")
          ax[0].set_ylabel("Total count")
          ax[0].grid()
          #ax[0].set_yscale('log')
          ax[0].xaxis.label.set_size(15)
          ax[0].yaxis.label.set_size(15)
          ax[0].legend()

          ax[1].plot([i for i in range(days)], increment_list(initial_val=total_death_till_date,
                                                     percentage_rate=present_death_rate,
                                                     number_count=days), 'r',
                   label=f'Current Rate ({np.round(present_death_rate, 2)}%)')
          ax[1].plot([i for i in range(days)], increment_list(initial_val=total_death_till_date,
                                                     percentage_rate=5,
                                                     number_count=days), 'g', label='5% Rate')
          ax[1].plot([i for i in range(days)], increment_list(initial_val=total_death_till_date,
                                                     percentage_rate=10,
                                                     number_count=days), 'b', label='10% Rate')
          ax[1].set_title("Total DEATHs with different rete(%) of increment")
          ax[1].set_xlabel(f"Date strting from: {starting_date}")
          ax[1].set_ylabel("Total count")
          ax[1].grid()
          ax[1].xaxis.label.set_size(15)
          ax[1].yaxis.label.set_size(15)
          ax[1].legend()

          fig.show()
```
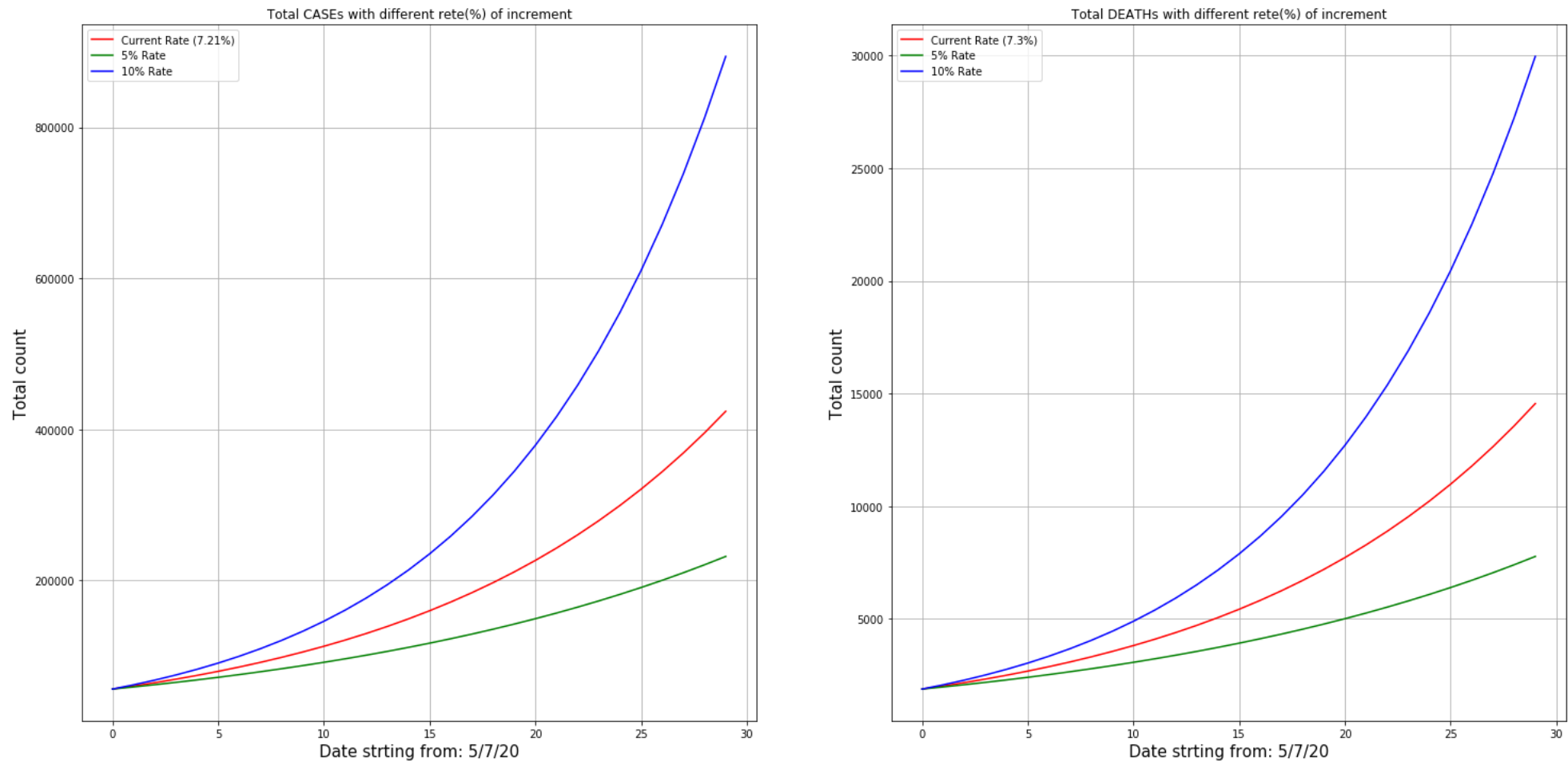

Epidemic modelling using Extended SIR and fitting it to COVID-19 data

Models are always simplifications of the real world. It is a way to put the real world scenarios in some mathemetical equation so that we can derive/infer information out of it. To model something, we have to assume some facts in the first place for the sake of simplicity and interpretability.

In Data Science terminology, these are some handcrafted features we are building to approximate the current COVID-19 scenarion. SIR(Susceptible, Infected, Recovered) is a very popular model for infectious diseases modelling. But the simple vanila SIR won't help us much in real life scenario. Thats why, here we are building a extended SIR model for COVID-19 India scenario.

Paramenters/Features

- N: total population
- S(t): number of people susceptible on day t
- E(t): number of people exposed on day t
- I(t): number of people infected on day t
- R(t): number of people recovered on day t
- D(t): number of people dead on day t
- β: expected amount of people an infected person infects per day
- D: number of days an infected person has and can spread the disease
- γ: the proportion of infected recovering per day (γ = 1/D)
- R₀: the total number of people an infected person infects (R₀ = β / γ)
- δ: length of incubation period
- α: fatality rate
- ρ: rate at which people die (= 1/days from infected until death)

```
In [27]:  ROOT_DIR = "D:/New folder/Covid19-India-finding-insight/data"
          Image(filename=os.path.join(ROOT_DIR, "relations.png"))
```

Out[27]:
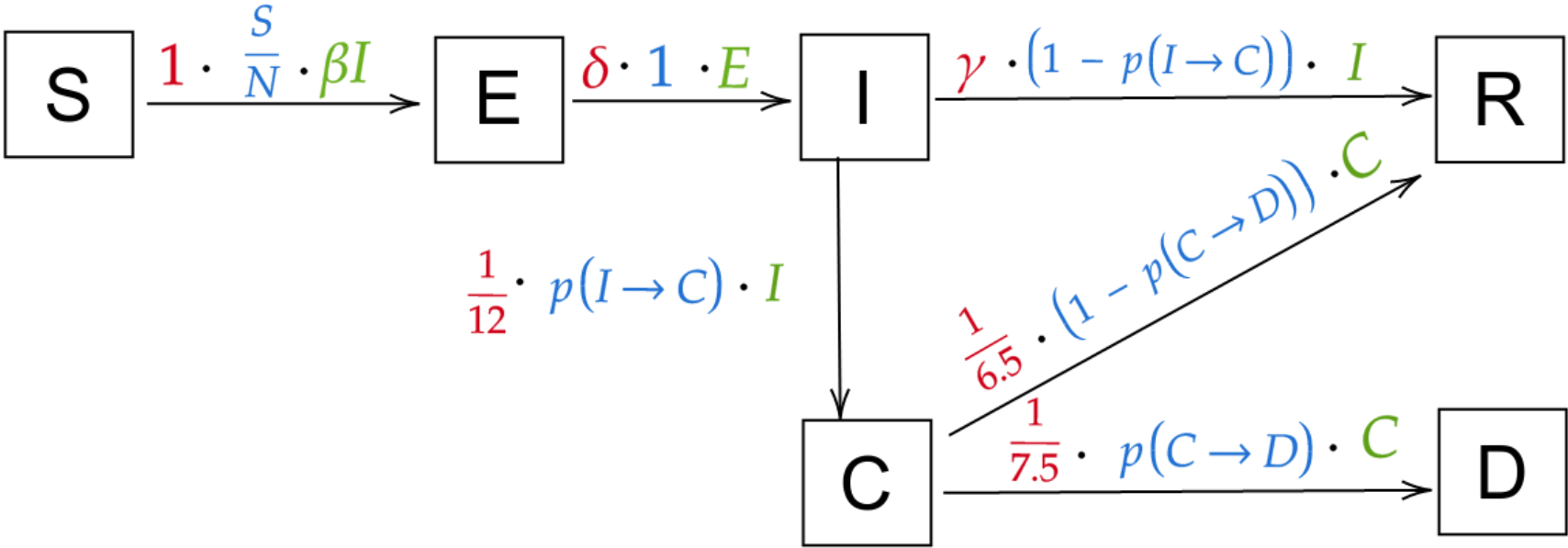
Below are the equations that go with it

```
In [28]:  Image(filename=os.path.join(ROOT_DIR, "equations.png"))
```

Out[28]:

$$\frac{dS}{dt} = -\beta(t) \cdot I \cdot \frac{S}{N}$$

$$\frac{dE}{dt} = \beta(t) \cdot I \cdot \frac{S}{N} - \delta \cdot E$$

$$\frac{dI}{dt} = \delta \cdot E - \frac{1}{12} \cdot p(I \to C) \cdot I - \gamma \cdot (1 - p(I \to C)) \cdot I$$

$$\frac{dC}{dt} = \frac{1}{12} \cdot p(I \to C) \cdot I - \frac{1}{7.5} \cdot p(C \to D) \cdot \min(Beds(t), C) - \max(0, C - Beds(t)) - \frac{1}{6.5} \cdot (1 - p(C \to D)) \cdot \min(Beds(t), C)$$

$$\frac{dR}{dt} = \gamma \cdot (1 - p(I \to C)) \cdot I + \frac{1}{6.5} \cdot (1 - p(C \to D)) \cdot \min(Beds(t), C)$$

$$\frac{dD}{dt} = \frac{1}{7.5} \cdot p(C \to D) \cdot \min(Beds(t), C) + \max(0, C - Beds(t))$$

```
In [29]:  pd.options.mode.chained_assignment = None  # default='warn'
          import matplotlib.pyplot as plt
          import matplotlib.dates as mdates
          %matplotlib inline
          import mpld3
          mpld3.enable_notebook()
          from scipy.integrate import odeint
          import lmfit
          from lmfit.lineshapes import gaussian, lorentzian
```

```
In [30]:   # Load the data
           ROOT_DIR = "D:/New folder/Covid19-India-finding-insight/data"
           beds = pd.read_csv(os.path.join(ROOT_DIR, "beds.csv"), header=0)
           agegroups = pd.read_csv(os.path.join(ROOT_DIR, "agegroups.csv"))
           probabilities = pd.read_csv(os.path.join(ROOT_DIR, "probabilities.csv"))

           covid_data = pd.read_csv("https://tinyurl.com/t59cgxn", parse_dates=["Date"], skiprows=[1])
           covid_data["Location"] = covid_data["Country/Region"]


           beds_lookup = dict(zip(beds["Country"], beds["ICU_Beds"]))
           agegroup_lookup = dict(zip(agegroups['Location'],
                                      agegroups[['0_9', '10_19', '20_29', '30_39', '40_49',
                                                 '50_59', '60_69', '70_79', '80_89', '90_100']].values))

           prob_I_to_C_1 = list(probabilities.prob_I_to_ICU_1.values)
           prob_I_to_C_2 = list(probabilities.prob_I_to_ICU_2.values)
           prob_C_to_Death_1 = list(probabilities.prob_ICU_to_Death_1.values)
           prob_C_to_Death_2 = list(probabilities.prob_ICU_to_Death_2.values)
```

```
In [31]:   covid_data.groupby("Date").sum()[["Value"]].plot(figsize=(12, 8), title="Covid-19 total fatalities (world)")
```

```
Out[31]:   <matplotlib.axes._subplots.AxesSubplot at 0x28afc25f0b8>
```
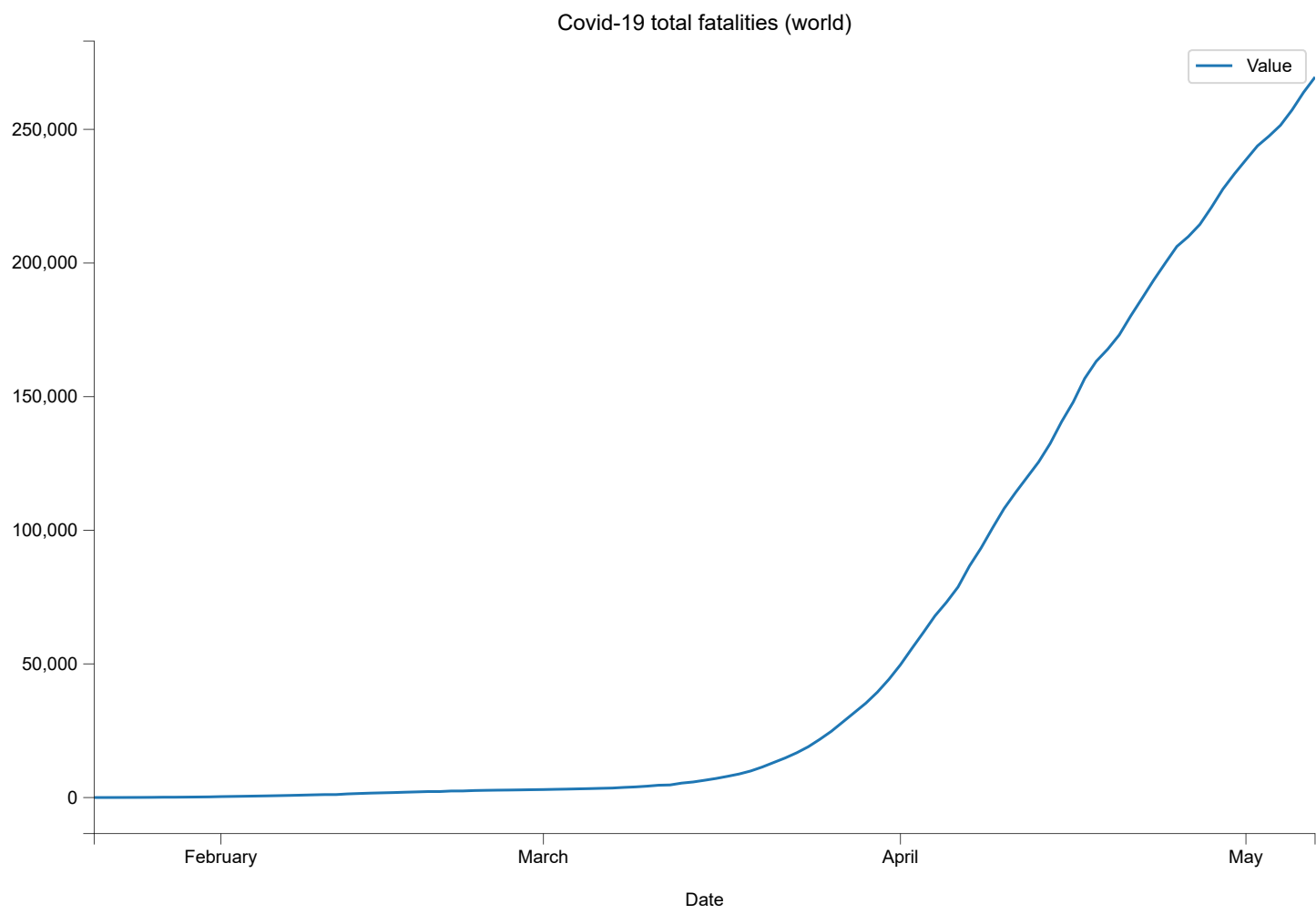

Model definition

```
In [32]:   def deriv(y, t, beta, gamma, sigma, N, p_I_to_C, p_C_to_D, Beds):
               S, E, I, C, R, D = y

               dSdt = -beta(t) * I * S / N
               dEdt = beta(t) * I * S / N - sigma * E
               dIdt = sigma * E - 1/12.0 * p_I_to_C * I - gamma * (1 - p_I_to_C) * I
               dCdt = 1/12.0 * p_I_to_C * I - 1/7.5 * p_C_to_D * min(Beds(t), C) - max(0, C-Beds(t)) - (1 - p_C_to_D) * 1/6.5 * min(Beds(t
           ), C)
               dRdt = gamma * (1 - p_I_to_C) * I + (1 - p_C_to_D) * 1/6.5 * min(Beds(t), C)
               dDdt = 1/7.5 * p_C_to_D * min(Beds(t), C) + max(0, C-Beds(t))
               return dSdt, dEdt, dIdt, dCdt, dRdt, dDdt
```

```
In [33]: gamma = 1.0/9.0
         sigma = 1.0/3.0

         def logistic_R_0(t, R_0_start, k, x0, R_0_end):
             return (R_0_start-R_0_end) / (1 + np.exp(-k*(-t+x0))) + R_0_end

         def Model(days, agegroups, beds_per_100k, R_0_start, k, x0, R_0_end, prob_I_to_C, prob_C_to_D, s):

             def beta(t):
                 return logistic_R_0(t, R_0_start, k, x0, R_0_end) * gamma

             N = sum(agegroups)

             def Beds(t):
                 beds_0 = beds_per_100k / 100_000 * N
                 return beds_0 + s*beds_0*t    # 0.003

             y0 = N-1.0, 1.0, 0.0, 0.0, 0.0, 0.0
             t = np.linspace(0, days-1, days)
             ret = odeint(deriv, y0, t, args=(beta, gamma, sigma, N, prob_I_to_C, prob_C_to_D, Beds))
             S, E, I, C, R, D = ret.T
             R_0_over_time = [beta(i)/gamma for i in range(len(t))]

             return t, S, E, I, C, R, D, R_0_over_time, Beds, prob_I_to_C, prob_C_to_D
```

```
In [34]: def plotter(t, S, E, I, C, R, D, R_0, B, S_1=None, S_2=None, x_ticks=None):
             if S_1 is not None and S_2 is not None:
                 print(f"percentage going to ICU: {S_1*100}; percentage dying in ICU: {S_2 * 100}")

             f, ax = plt.subplots(1,1,figsize=(13,6))
             if x_ticks is None:
                 ax.plot(t, S, 'b', alpha=0.7, linewidth=2, label='Susceptible')
                 ax.plot(t, E, 'y', alpha=0.7, linewidth=2, label='Exposed')
                 ax.plot(t, I, 'r', alpha=0.7, linewidth=2, label='Infected')
                 ax.plot(t, C, 'r--', alpha=0.7, linewidth=2, label='Critical')
                 ax.plot(t, R, 'g', alpha=0.7, linewidth=2, label='Recovered')
                 ax.plot(t, D, 'k', alpha=0.7, linewidth=2, label='Dead')
             else:
                 ax.plot(x_ticks, S, 'b', alpha=0.7, linewidth=2, label='Susceptible')
                 ax.plot(x_ticks, E, 'y', alpha=0.7, linewidth=2, label='Exposed')
                 ax.plot(x_ticks, I, 'r', alpha=0.7, linewidth=2, label='Infected')
                 ax.plot(x_ticks, C, 'r--', alpha=0.7, linewidth=2, label='Critical')
                 ax.plot(x_ticks, R, 'g', alpha=0.7, linewidth=2, label='Recovered')
                 ax.plot(x_ticks, D, 'k', alpha=0.7, linewidth=2, label='Dead')

                 ax.xaxis.set_major_locator(mdates.YearLocator())
                 ax.xaxis.set_major_formatter(mdates.DateFormatter('%Y-%m-%d'))
                 ax.xaxis.set_minor_locator(mdates.MonthLocator())
                 f.autofmt_xdate()


             ax.title.set_text('extended SEIR-Model')

             ax.grid(b=True, which='major', c='w', lw=2, ls='-')
             legend = ax.legend()
             legend.get_frame().set_alpha(0.5)
             for spine in ('top', 'right', 'bottom', 'left'):
                 ax.spines[spine].set_visible(False)

             plt.show();

             f = plt.figure(figsize=(13,6))
             # sp1
             ax1 = f.add_subplot(131)
             if x_ticks is None:
                 ax1.plot(t, R_0, 'b--', alpha=0.7, linewidth=2, label='R_0')
             else:
                 ax1.plot(x_ticks, R_0, 'b--', alpha=0.7, linewidth=2, label='R_0')
                 ax1.xaxis.set_major_locator(mdates.YearLocator())
                 ax1.xaxis.set_major_formatter(mdates.DateFormatter('%Y-%m-%d'))
                 ax1.xaxis.set_minor_locator(mdates.MonthLocator())
                 f.autofmt_xdate()


             ax1.title.set_text('R_0 over time')
             ax1.grid(b=True, which='major', c='w', lw=2, ls='-')
             legend = ax1.legend()
             legend.get_frame().set_alpha(0.5)
             for spine in ('top', 'right', 'bottom', 'left'):
                 ax.spines[spine].set_visible(False)

             # sp2
             ax2 = f.add_subplot(132)
             total_CFR = [0] + [100 * D[i] / sum(sigma*E[:i]) if sum(sigma*E[:i])>0 else 0 for i in range(1, len(t))]
             daily_CFR = [0] + [100 * ((D[i]-D[i-1]) / ((R[i]-R[i-1]) + (D[i]-D[i-1]))) if max((R[i]-R[i-1]), (D[i]-D[i-1]))>10 else 0 f
         or i in range(1, len(t))]
             if x_ticks is None:
                 ax2.plot(t, total_CFR, 'r--', alpha=0.7, linewidth=2, label='total')
                 ax2.plot(t, daily_CFR, 'b--', alpha=0.7, linewidth=2, label='daily')
             else:
                 ax2.plot(x_ticks, total_CFR, 'r--', alpha=0.7, linewidth=2, label='total')
                 ax2.plot(x_ticks, daily_CFR, 'b--', alpha=0.7, linewidth=2, label='daily')
                 ax2.xaxis.set_major_locator(mdates.YearLocator())
                 ax2.xaxis.set_major_formatter(mdates.DateFormatter('%Y-%m-%d'))
                 ax2.xaxis.set_minor_locator(mdates.MonthLocator())
                 f.autofmt_xdate()

             ax2.title.set_text('Fatality Rate (%)')
             ax2.grid(b=True, which='major', c='w', lw=2, ls='-')
             legend = ax2.legend()
             legend.get_frame().set_alpha(0.5)
             for spine in ('top', 'right', 'bottom', 'left'):
                 ax.spines[spine].set_visible(False)

             # sp3
             ax3 = f.add_subplot(133)
             newDs = [0] + [D[i]-D[i-1] for i in range(1, len(t))]
             if x_ticks is None:
                 ax3.plot(t, newDs, 'r--', alpha=0.7, linewidth=2, label='total')
                 ax3.plot(t, [max(0, C[i]-B(i)) for i in range(len(t))], 'b--', alpha=0.7, linewidth=2, label="over capacity")
             else:
                 ax3.plot(x_ticks, newDs, 'r--', alpha=0.7, linewidth=2, label='total')
                 ax3.plot(x_ticks, [max(0, C[i]-B(i)) for i in range(len(t))], 'b--', alpha=0.7, linewidth=2, label="over capacity")
                 ax3.xaxis.set_major_locator(mdates.YearLocator())
                 ax3.xaxis.set_major_formatter(mdates.DateFormatter('%Y-%m-%d'))
                 ax3.xaxis.set_minor_locator(mdates.MonthLocator())
                 f.autofmt_xdate()
```

```
        ax3.title.set_text('Deaths per day')
        ax3.yaxis.set_tick_params(length=0)
        ax3.xaxis.set_tick_params(length=0)
        ax3.grid(b=True, which='major', c='w', lw=2, ls='-')
        legend = ax3.legend()
        legend.get_frame().set_alpha(0.5)
        for spine in ('top', 'right', 'bottom', 'left'):
            ax.spines[spine].set_visible(False)

        plt.show();
```

Fitting to available India's data

In [35]:
```
data = covid_data[covid_data["Location"] == "India"]["Value"].values[::-1]
agegroups = agegroup_lookup["India"]
beds_per_100k = beds_lookup["India"]
outbreak_shift = 0#14
# parameters to fit; form: {parameter: (initial guess, minimum value, max value)}
params_init_min_max = {"R_0_start": (3.0, 2.0, 5.0), "k": (2.5, 0.01, 5.0),
                       "x0": (90, 0, 120), "R_0_end": (0.9, 0.3, 3.5),
                       "prob_I_to_C": (0.05, 0.01, 0.1), "prob_C_to_D": (0.5, 0.05, 0.8),
                       "s": (0.003, 0.001, 0.01)}
```

In [36]:
```
days = outbreak_shift + len(data)
if outbreak_shift >= 0:
    y_data = np.concatenate((np.zeros(outbreak_shift), data))
else:
    y_data = y_data[-outbreak_shift:]

x_data = np.linspace(0, days - 1, days, dtype=int)  # x_data is just [0, 1, ..., max_days] array

def fitter(x, R_0_start, k, x0, R_0_end, prob_I_to_C, prob_C_to_D, s):
    ret = Model(days, agegroups, beds_per_100k, R_0_start, k, x0, R_0_end, prob_I_to_C, prob_C_to_D, s)
    return ret[6][x]
```

In [37]:
```
def fitter(x, R_0_start, k, x0, R_0_end, prob_I_to_C, prob_C_to_D, s):
    ret = Model(days, agegroups, beds_per_100k, R_0_start, k, x0, R_0_end, prob_I_to_C, prob_C_to_D, s)
    return ret[6][x]
```

In [38]:
```
mod = lmfit.Model(fitter)

for kwarg, (init, mini, maxi) in params_init_min_max.items():
    mod.set_param_hint(str(kwarg), value=init, min=mini, max=maxi, vary=True)

params = mod.make_params()
fit_method = "leastsq"
```

In [39]:
```
result = mod.fit(y_data, params, method="least_squares", x=x_data)
```

In [41]:
```
result.plot_fit(datafmt="-")
plt.show()
```
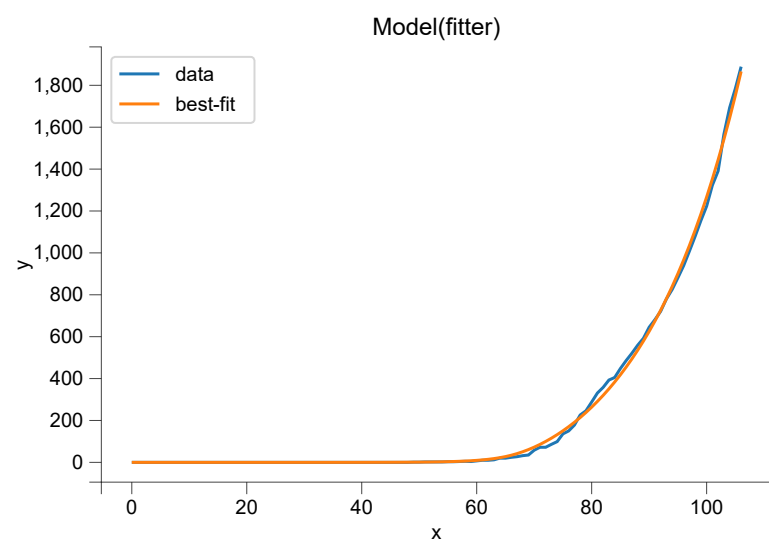

In [42]:
```
result.best_values
```

Out[42]:
```
{'R_0_start': 4.766901897821081,
 'k': 4.999999969774685,
 'x0': 64.24198527900687,
 'R_0_end': 1.7665303820055647,
 'prob_I_to_C': 0.010000000000000002,
 'prob_C_to_D': 0.05000000000000001,
 's': 0.003}
```

In [43]:
```
print(f"Current R0 value in India is:{result.best_values['R_0_end']}")
```

```
Current R0 value in India is:1.7665303820055647
```

```
In [44]: full_days = 365
         first_date = np.datetime64(covid_data.Date.min()) - np.timedelta64(outbreak_shift,'D')
         x_ticks = pd.date_range(start=first_date, periods=full_days, freq="D")
         print("Prediction for India")
         plotter(*Model(full_days, agegroup_lookup["India"], beds_lookup["India"], **result.best_values), x_ticks=x_ticks);
```

Prediction for India
percentage going to ICU: 1.0000000000000002; percentage dying in ICU: 5.000000000000001
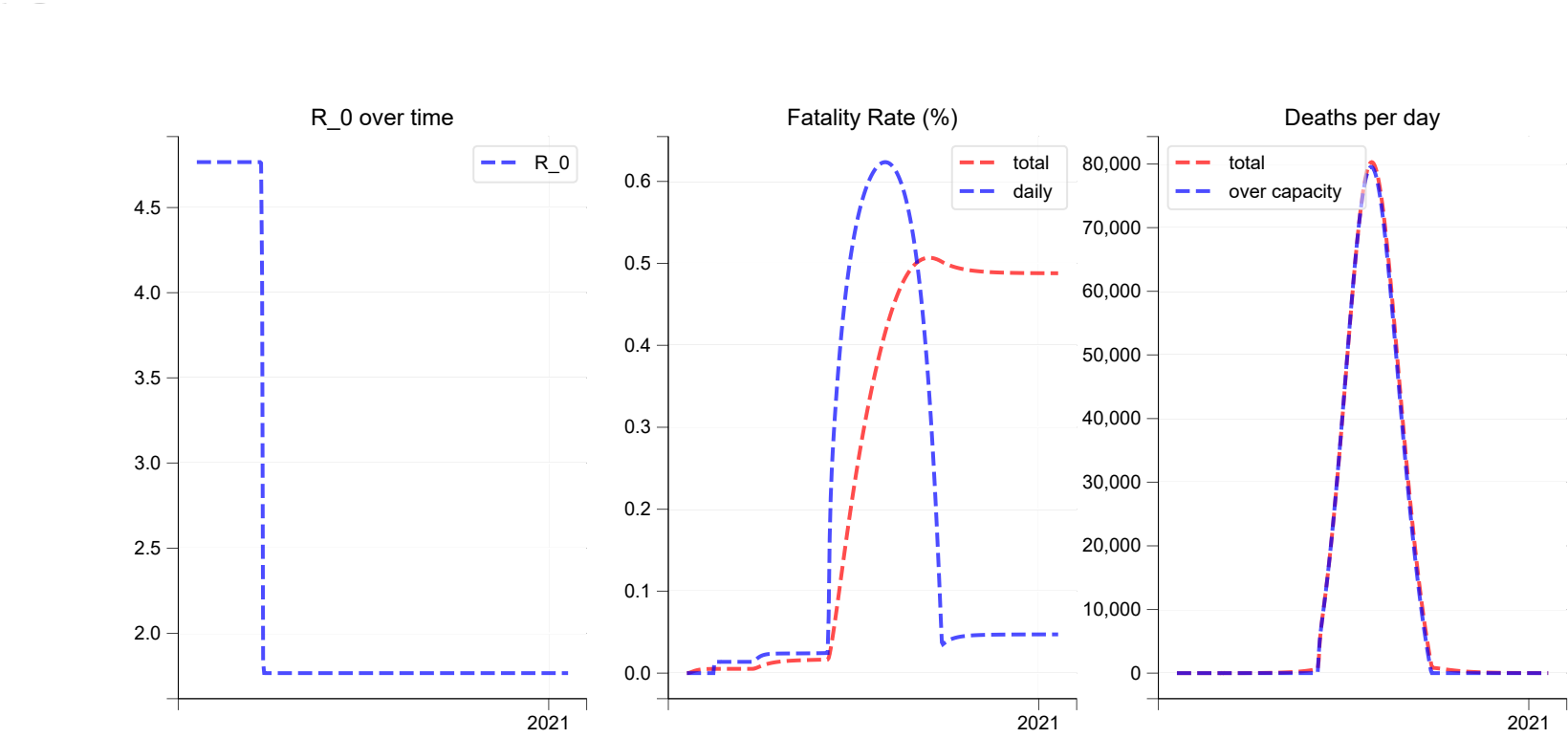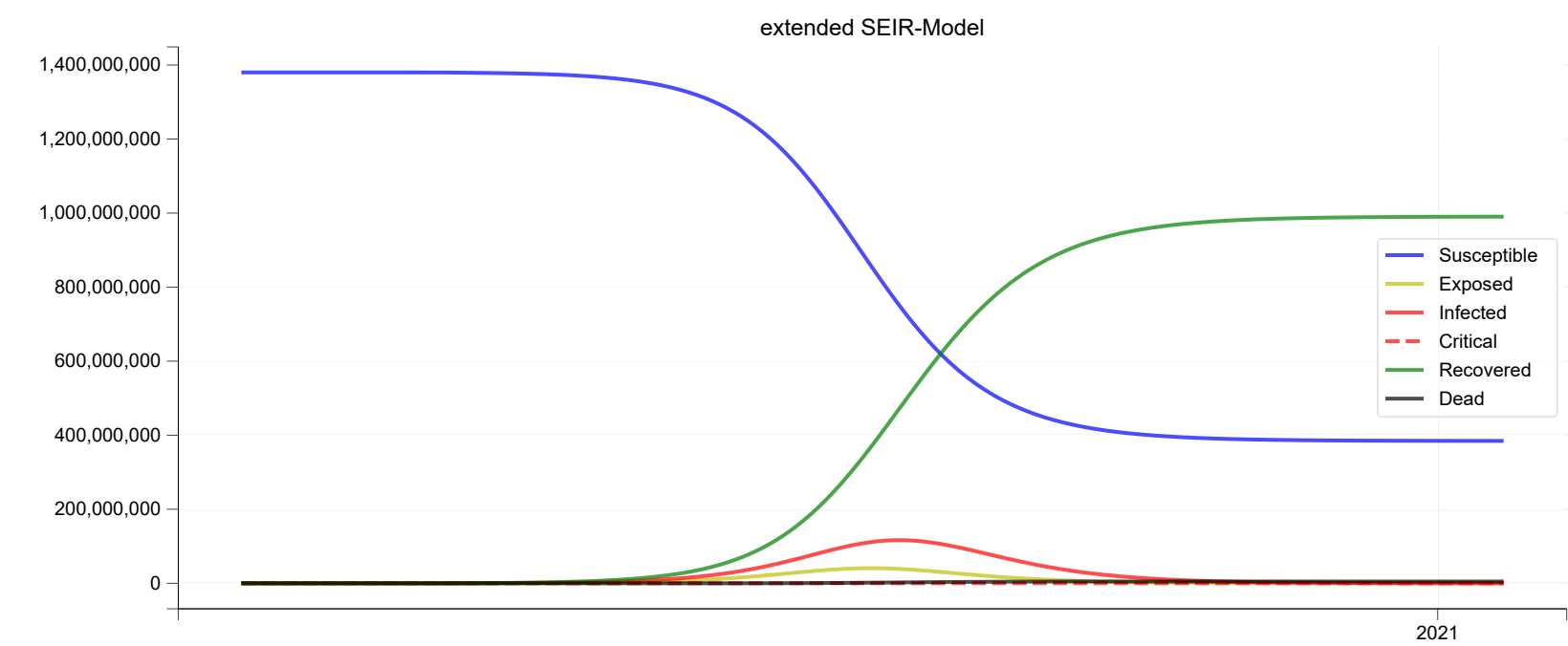
More interpretation

```
In [45]: def dayToDate(days):
             dayToDate=[]
             for day in days:
                 if 0 <= day < 10:
                     dayToDate.append(f"{int(day+22)} Jan")
                 elif 10 <= day < 39:
                     dayToDate.append(f"{int(day-9)} Feb")
                 elif 39 <= day < 70:
                     dayToDate.append(f"{int(day-38)} Mar")
                 elif 70 <= day < 100:
                     dayToDate.append(f"{int(day-69)} Apr")
                 elif 100 <= day < 131:
                     dayToDate.append(f"{int(day-99)} May")
                 elif 131 <= day < 161:
                     dayToDate.append(f"{int(day-130)} Jun")
                 elif 161 <= day < 192:
                     dayToDate.append(f"{int(day-160)} Jul")
                 elif 192 <= day < 223:
                     dayToDate.append(f"{int(day-191)} Aug")
                 elif 223 <= day < 253:
                     dayToDate.append(f"{int(day-222)} Sep")
                 elif 253 <= day < 284:
                     dayToDate.append(f"{int(day-252)} Oct")
                 elif 284 <= day < 314:
                     dayToDate.append(f"{int(day-283)} Nov")
                 elif 314 <= day < 345:
                     dayToDate.append(f"{int(day-313)} Dec")
                 elif 345 <= day:
                     dayToDate.append(f"{int(day-344)} Jan")
             return dayToDate

         modelParams = Model(full_days, agegroup_lookup["India"], beds_lookup["India"], **result.best_values)
         #t, S, E, I, C, R, D, R_0_over_time, Beds, prob_I_to_C, prob_C_to_D
         fig1, ax = plt.subplots(1,2, figsize=(12,6))

         ax[0].plot(modelParams[0], perDayCalc(modelParams[6]), 'r')
         ax[0].set_title("Daily death")
         ax[0].set_xlabel("Days")
         ax[0].set_ylabel("Death Count")

         ax[1].plot(modelParams[0], (modelParams[4]), 'm')
         ax[1].set_title("Daily critical cases")

         '''
         ax[2].plot(modelParams[0], (modelParams[3]), 'y')
         ax[2].set_title("Daily infected cases")

         ax[3].plot(modelParams[0], perDayCalc(modelParams[5]), 'g')
         ax[3].set_title("Daily recovered cases")
         '''

         fig1.tight_layout()
         plt.show()
```
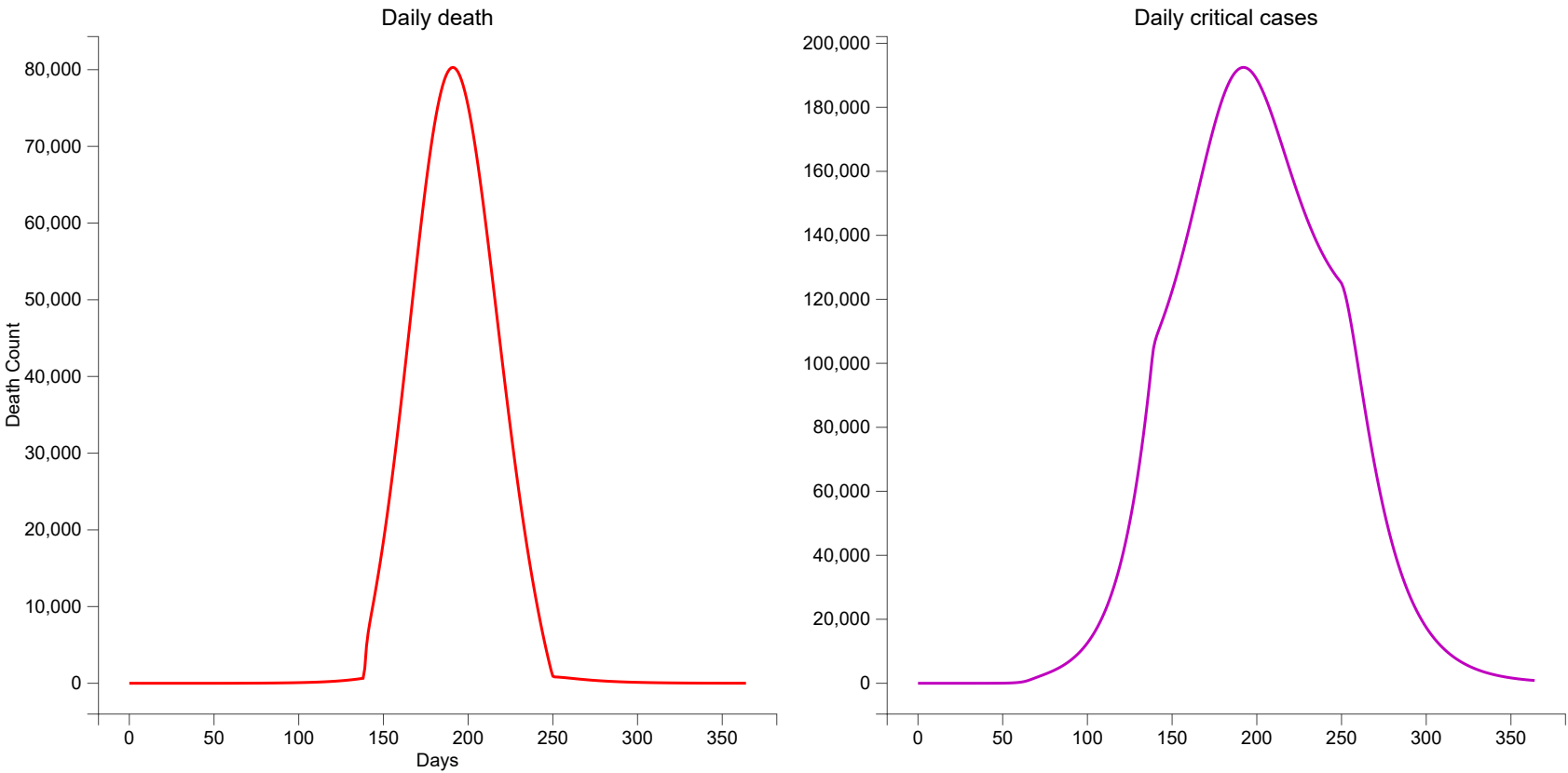
```
In [46]: date1 = dayToDate(days=modelParams[0])

         print(f"DAY(starting from 21st Jan)+    DATE      +    DEATH")
         print(f"++++++++++++++++++++++++++++++++++++++++++++++++++++++++")
         for day in modelParams[0]:
             if day%10 == 0:
                 day=np.int64(day)
                 print(f"{day:>25}  |    {date1[day]:<10}  |   {int(perDayCalc(modelParams[6])[day]):<10}")
```

```
DAY(starting from 21st Jan)+    DATE      +    DEATH
++++++++++++++++++++++++++++++++++++++++++++++++++++++++
                        0  |    22 Jan     |   0
                       10  |    1 Feb      |   0
                       20  |    11 Feb     |   0
                       30  |    21 Feb     |   0
                       40  |    2 Mar      |   0
                       50  |    12 Mar     |   0
                       60  |    22 Mar     |   1
                       70  |    1 Apr      |   11
                       80  |    11 Apr     |   25
                       90  |    21 Apr     |   46
                      100  |    1 May      |   81
                      110  |    11 May     |   143
                      120  |    21 May     |   248
                      130  |    31 May     |   428
                      140  |    10 Jun     |   4821
                      150  |    20 Jun     |   18518
                      160  |    30 Jun     |   35747
                      170  |    10 Jul     |   55608
                      180  |    20 Jul     |   72665
                      190  |    30 Jul     |   80235
                      200  |    9 Aug      |   75258
                      210  |    19 Aug     |   60622
                      220  |    29 Aug     |   42235
                      230  |    8 Sep      |   24944
                      240  |    18 Sep     |   11025
                      250  |    28 Sep     |   923
                      260  |    8 Oct      |   666
                      270  |    18 Oct     |   455
                      280  |    28 Oct     |   296
                      290  |    7 Nov      |   188
                      300  |    17 Nov     |   119
                      310  |    27 Nov     |   74
                      320  |    7 Dec      |   46
                      330  |    17 Dec     |   29
                      340  |    27 Dec     |   18
                      350  |    6 Jan      |   11
                      360  |    16 Jan     |   7
```

```
In [47]: d1=108
         print(f"Total predicted death on {date1[d1]} 2020, is:  {int(perDayCalc(modelParams[6])[d1])} ")
```

```
Total predicted death on 9 May 2020, is:  127
```

Finding R-naught value using over simplified method(Not so correct)

The `R-Naught` of a disease, or the `contagiousness` , represents how transmissible the disease is. An R-Naught of 2 means that for every one person with the disease, two more people are infected. A fractional R-Naught means that the epidemic is dying down. Hepatitis C and Ebola have an R-Naught of 2, HIV and SARS 4, and Measles 18, to give a few examples.

The `R-Naught (R0)` of a disease is usually publicly declared by the World Health Organization after careful and lengthy analysis of various factor such as the infectious period, contact rate, mode of transmission, etc. In this article, we'll handwrite a program that optimizes an exponential model to the data to find the R0 of the coronavirus in Python. While this is in no means a substitute for the WHO and other health agencies' findings, it is a good way to gauge just how contagious the coronavirus is with the current lack of information.

In this notebook, we'll handwrite a program that optimizes an exponential model to the data to find the R0 of the coronavirus in Python. While this is in no means a substitute for the WHO and other health agencies' findings, it is a good way to gauge just how contagious the coronavirus is with the current lack of information.

R-naught Model

```
In [48]: Image(filename=os.path.join(ROOT_DIR, "eq1.png"))
Out[48]:
```

$$y = a^{(x-b)}$$

Our model will have a very simple equation stated above:

…where y is the forecasted number of cases and x is the number of days since the first confirmed case. a and b are the only two parameters that will allow changing.

a controls how steep the curve will be. A smaller a value represents a less steep curve, and a higher a value represents a steeper curve.

a is also the R0 value. For each number of days x after the epidemic begins, the number of new cases multiplies by a factor of a — for every one person infected on day x, a more people will be infected on day x + 1. This also provides another representation of what different quantities of R0 values mean.

Fitting the Model

```
In [49]:    '''
            learning_rate = 0.001
            a = 1
            b = 4
            y = conf_case[conf_case['Country/Region']=='India'].sum().drop(['Province/State','Country/Region','Lat','Long']).tolist()
            x = range(len(y))

            def cost_function(a, b, x, y):
                error = 0
                for index in x:
                    error += abs((a**(x[index]-b)) - (y[index]))#**2
                return error / len(x)

            def training(a, b, x, y, learning_rate):
                print(f"Initial a: {a}")
                print(f"Initial b: {b}")
                print(f"Learning Rate: {learning_rate}")
                print(f"Initial Cost Function: {cost_function(a, b, x, y)}\n")
                from math import log
                for index in x:
                    if 0.9*x[index] < b+1 < 1.1*x[index]:
                        #pass
                        continue
                    a_old = a
                    a = a - ( learning_rate * 2 * ((a**(x[index]-b)) - (y[index])) * (x[index] - b) * (a**(x[index]-b-1)) )
                    if a < 0 or a == float("inf") or a == float("-inf"):
                        a = a_old
                        continue
                    b_old = b
                    b = b - ( learning_rate * 2 * ((a**(x[index]-b)) - (y[index])) * (a**(x[index]-b)) * log(a) )
                    if b == float("inf") or b == float("-inf"):
                        b = b_old
                        continue
                    if False:#index % 5 == 0:
                        print(f"ITERATION {index+1}:")
                        print(f"New a: {a}")
                        print(f"New b: {b}")
                        print(f'Cost Function:  {cost_function(a, b, x, y)}\n')
                print(f"ITERATION {index+1}:")
                print(f"Final a: {a}, \nFinal b: {b}")
                print(f'Cost Function:  {cost_function(a, b, x, y)}\n')
                return a, b

            def multiple_train(a, b, x, y, learning_rate, epoch):
                for e in range(epoch):
                    a, b = training(a=a, b=b, x=x, y=y, learning_rate=learning_rate)
                    print(f"\n\n\n\nEPOCH: {e}")
                    print("{'A':"+str(a)+", 'B':"+str(b)+"}")
                    print(f"ERROR: {cost_function(a, b, x, y)}")
                return a, b


            multiple_train(a=1.2, b=4, x=x, y=y, learning_rate=0.00001, epoch=2)
            '''
```

```
Out[49]:   '\nlearning_rate = 0.001\na = 1\nb = 4\ny = conf_case[conf_case[\'Country/Region\']==\'India\'].sum().drop([\'Province/State
           \',\'Country/Region\',\'Lat\',\'Long\']).tolist()\nx = range(len(y))\n\ndef cost_function(a, b, x, y):\n    error = 0\n    for
           index in x:\n        error += abs((a**(x[index]-b)) - (y[index]))#**2\n    return error / len(x)\n\ndef training(a, b, x, y, le
           arning_rate):\n    print(f"Initial a: {a}")\n    print(f"Initial b: {b}")\n    print(f"Learning Rate: {learning_rate}")\n    pr
           int(f"Initial Cost Function: {cost_function(a, b, x, y)}\n")\n    from math import log\n    for index in x:\n        if 0.9*x[i
           ndex] < b+1 < 1.1*x[index]:\n            #pass\n            continue\n        a_old = a\n        a = a - ( learning_rate * 2 *
           ((a**(x[index]-b)) - (y[index])) * (x[index] - b) * (a**(x[index]-b-1)) )\n        if a < 0 or a == float("inf") or a == float
           ("-inf"):\n        a = a_old\n            continue\n        b_old = b\n        b = b - ( learning_rate * 2 * ((a**(x[index]
           -b)) - (y[index])) * (a**(x[index]-b)) * log(a) )\n        if b == float("inf") or b == float("-inf"):\n            b = b_old\n
           continue\n        if False:#index % 5 == 0:\n            print(f"ITERATION {index+1}:")\n            print(f"New a: {a}")\n
           print(f"New b: {b}")\n            print(f\'Cost Function:  {cost_function(a, b, x, y)}\n\')\n    print(f"ITERATION {index+1}:")
           \n    print(f"Final a: {a}, \nFinal b: {b}")\n    print(f\'Cost Function:  {cost_function(a, b, x, y)}\n\')\n    return a, b\n
           \ndef multiple_train(a, b, x, y, learning_rate, epoch):\n    for e in range(epoch):\n        a, b = training(a=a, b=b, x=x, y=
           y, learning_rate=learning_rate)\n        print(f"\n\n\n\nEPOCH: {e}")\n        print("{\'A\':"+str(a)+", \'B\':"+str(b)+"}")\n
           print(f"ERROR: {cost_function(a, b, x, y)}")\n    return a, b\n\n\nmultiple_train(a=1.2, b=4, x=x, y=y, learning_rate=0.00001,
           epoch=2)\n'
```

```
In [50]:    y = np.array(cdf_case_list)
            #y = np.array(cdf_active_list)
            x = np.array(range(len(y)))
```

## Curve fitting using LMFIT

```python
In [51]: from scipy.optimize import leastsq
         from lmfit import minimize, Parameters
         params = Parameters()
         params.add('a', value=1.0)
         params.add('b', value=5.0)

         def get_residual(params, x, data):
             a = params['a'].value
             b = params['b'].value
             model = a**(x-b)
             return data - model
```

```python
In [52]: out = minimize(fcn=get_residual, params=params, method='leastsq', args=(x, y))
         a, b = out.__dict__['params']['a'].value, out.__dict__['params']['b'].value
```

```python
In [53]: best_set = {'A':a, 'B':b}
         def function(x):
             return best_set['A']**(x-best_set['B'])

         plt.figure(figsize=(10,8))
         plt.plot(x,y,label='Real Data')
         plt.plot(x,[function(i) for i in x],label='Exponential Model')
         plt.legend()
         plt.show()
```
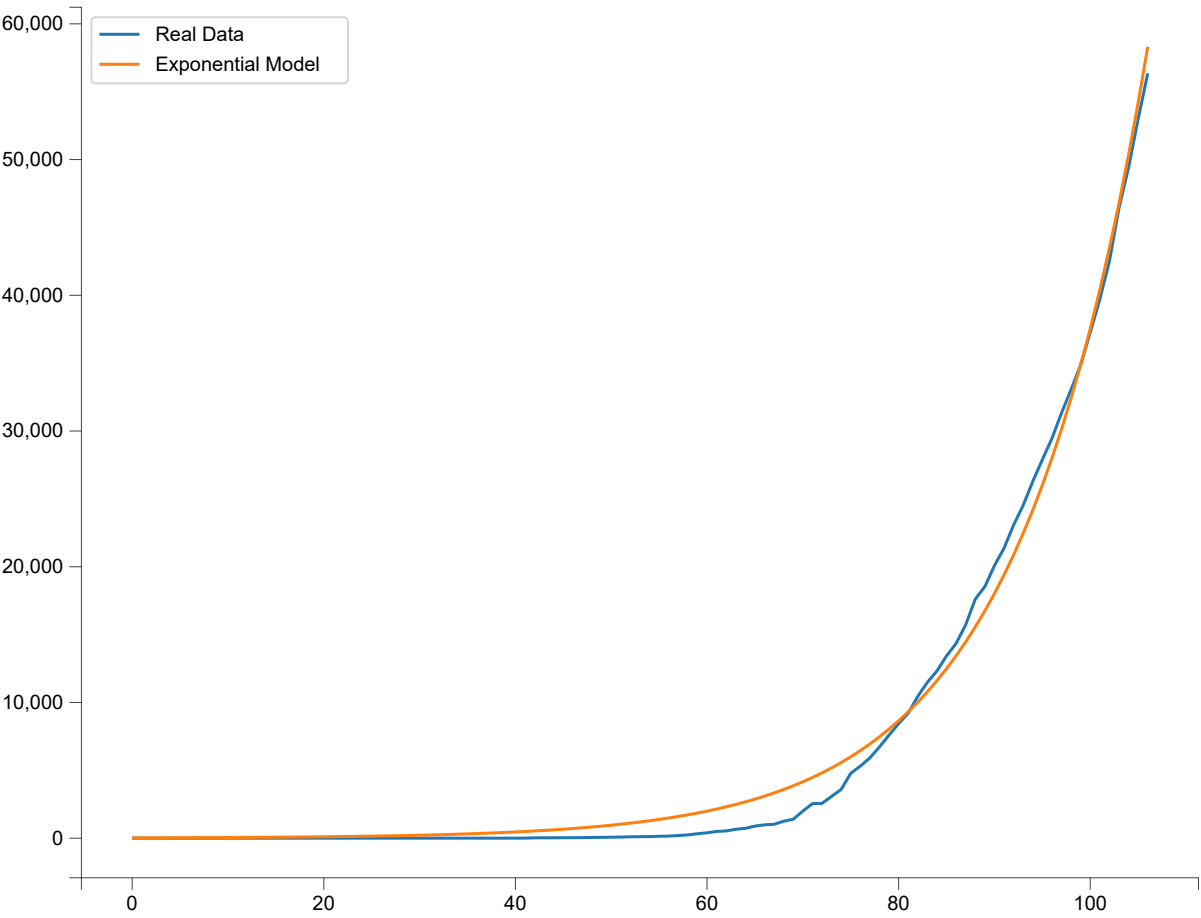

Results

```python
In [54]: print(f"The R0 value on today is: {np.round(a, 2)}")
         print(f"For initial \'a\': 1.00 and \'b\': 5.00,  MEAN ABSOLUTE ERROR was: \
             {np.round(sum(abs(get_residual(params=params, x=x, data=y)))/len(x), 2)}")

         params1 = Parameters()
         params1.add('a', value=a)
         params1.add('b', value=b)
         print(f"For final \'a\': {np.round(a, 2)} and \'b\': {np.round(b, 2)}, MEAN ABSOLUTE ERROR is:   \
             {np.round(sum(abs(get_residual(params=params1, x=x, data=y)))/len(x), 2)}")
```

```
The R0 value on today is: 1.08
For initial 'a': 1.00 and 'b': 5.00,  MEAN ABSOLUTE ERROR was:     7312.99
For final 'a': 1.08 and 'b': -43.55, MEAN ABSOLUTE ERROR is:      841.43
```