

Understanding Recursion

A Step-by-Step Approach

Programming Fundamentals

December 4, 2024

What is Recursion?

- A method where a function calls itself
- Solves problems by breaking them into smaller subproblems
- Two main components:
 - Base case(s)
 - Recursive case(s)

- **Base Case**
 - Condition where recursion stops
 - Returns value directly without recursion
- **Recursive Case**
 - Problem broken into smaller subproblems
 - Function calls itself with modified parameters

Example 1: Factorial

- Definition: $n! = n \times (n-1)!$
- Base case: $0! = 1! = 1$

```
function fact = factorial_recursive(n)
    if n == 0 || n == 1
        fact = 1;
    else
        fact = n * factorial_recursive(n-1);
    end
end
```

5! calculation:

1. $\text{factorial}(5) \rightarrow 5 \times \text{factorial}(4)$
2. $\text{factorial}(4) \rightarrow 4 \times \text{factorial}(3)$
3. $\text{factorial}(3) \rightarrow 3 \times \text{factorial}(2)$
4. $\text{factorial}(2) \rightarrow 2 \times \text{factorial}(1)$
5. $\text{factorial}(1) \rightarrow 1$

Then unwind: $1 \rightarrow 2 \rightarrow 6 \rightarrow 24 \rightarrow 120$

Example 2: Fibonacci Sequence

- Each number is sum of previous two
- Base cases: $F(1) = F(2) = 1$

```
function fib = fibonacci_recursive(n)
    if n <= 2
        fib = 1;
    else
        fib = fibonacci_recursive(n-1) +
            fibonacci_recursive(n-2);
    end
end
```

Recursion vs Iteration

Recursion

- Elegant and clear
- Memory intensive
- Natural for tree structures

Iteration

- More efficient
- Less memory usage
- Better for linear problems

Example 3: Binary Search

```
function index = binary_search_recursive(arr, target, left, right)
    if left > right
        index = -1;
        return;
    end

    mid = floor((left + right)/2);
    if arr(mid) == target
        index = mid;
    elseif arr(mid) > target
        index = binary_search_recursive(arr, target, left, mid-1);
    else
        index = binary_search_recursive(arr, target, mid+1, right);
    end
end
```


Classic Example: Tower of Hanoi

- Problem:
 - Move n disks from source to target
 - Using auxiliary pole
 - Larger disk cannot be on smaller disk
- Recursive solution:
 1. Move $n-1$ disks to auxiliary
 2. Move largest disk to target
 3. Move $n-1$ disks to target

Tower of Hanoi Implementation

```
function tower_of_hanoi(n, source, auxiliary, target)
    if n == 1
        fprintf( 'Move disk 1 from %s to %s\n',
                  source, target );
        return;
    end

    tower_of_hanoi(n-1, source, target, auxiliary);
    fprintf( 'Move disk %d from %s to %s\n',
              n, source, target );
    tower_of_hanoi(n-1, auxiliary, source, target);
end
```