

Assignment No. 6.

Title - Linear probing with & without replacement.

Aim - To learn & implement the hashing with linear probing with & without replacement.

Problem Statement:- Implement all the functions of dictionary using hashing. Data: set of (key, value) pairs. Keys are mapped to values. Key must be comparable, keys must be unique. Standard operation: insert(key), Find(key), Delete(key) (use linear probing with & without replacement calculate average search cost for both.)

Objective =

- i) To learn & implement the hashing data structure.
- ii) To understand the use of hashing & advantage of hashing over tree
- iii) To understand different hashing functions with different collision resolution strategies.

Theory:-

Hashing:- Hashing is an important data structure is designed to use a special function called hash function which is used to map a given value with a particular key for faster access of elements. The efficiency of hashing mapping depends on the efficiency of hash function used.

Let hash function $H(x)$ maps the value at index $x \times 10$ in an array. for e.g. the values $\{11, 12, 13, 14, 15\}$ will be stored at position $\{1, 2, 3, 4, 5\}$ in hash table.

• Collision in hashing -

- In hashing, hash function used to compute hash value for a key.
- Hash value is then used as an index to store the key.
- Hash function may return same hash value for two or more keys. It means the collision occurs.
- A collision occurs when two non-identical identifiers are hashed to same bucket.

• Collision resolution strategy -

i) Linear probing -

In linear probing, when collision occurs we linearly search for next bucket. we keep probing until an empty bucket is found.

• With replacement -

In this we linearly search for next bucket if collision occurs.

e.g. 10, 15, 14, 20, 40

hash function = $h(x) = x \% 5$

0	10	$10 \% 5 = 0$
1	15	$15 \% 5 = 0$
2	20	$20 \% 5 = 0$
3	40	$40 \% 5 = 0$
4	14	$14 \% 5 = 4$

• Linear probing with replacement:-

In this type of strategy, if collision occur then we linearly search for next available bucket & store the value in it. If hash value is calculated & the incorrect value is stored in the bucket then correct value is stored in appropriate bucket & previous value is stored in next available bucket.

e.g. 13, 23, 20, 14, 10

0	20	$20 \% 5 = 0$
1	23	$23 \% 5 = 3$
2	10	$10 \% 5 = 0$
3	13	$13 \% 5 = 3$
4	14	$14 \% 5 = 4$

Operations :

i) Insert (key, value) :

First hash value of key is calculated & then data is inserted at that hash address in hash table.

0	10
1	
2	12
3	23

$$h(x) = x \% 10$$

$$h(x) = 31 \% 10$$

1

0	10
1	31
2	12
3	23

Before
inserting 31

After inserting
31

ii) Deletion :

Deletion of key from hash table required to calculate hash address & value to be deleted & making that bucket empty.

0	10
1	31
2	22
3	43

$$h(x) = x \% 10$$

$$h(22) = 22 \% 10$$

$$= 2$$

0	10
1	31
2	
3	43

Before deleting
22

After deleting
22

ii) Search (key)

Searching is very simple process in hashing. It is very fast as compared to other DS.

0	10
1	31
2	22
3	43

$$h(x) = x \% 10$$

$$h(43) = 43 \% 10$$

3

43 Found at 3

Calculate the hash Value

Searching 43

• Pseudocode / Algorithm

i) Insertion =

Step 1:) Read the key & value to be inserted, key & value.

Step 2:) Calculate hash address using hash function
say hashaddr

Step 3:) IF (hashTable[hashaddr] is empty) then
store the key & value at hashaddr

else

3.1) Set one pointer to next index of hashaddr
 $i = \text{hashaddr} + 1$

3.2) Set flag to 0

while $((i < n) \&\& (\text{flag} == 0))$
{

```

if (hashTable[i] is empty) then
    insert key & value at i & set flag to 1
else
    increment i
}

```

```

3.3) set i = 0
while ((i < hashAddr) && (flag == 0))
{
    if (hashTable[i] is empty)
    {
        insert key & value at i
        & set flag to 1
    }
    else
    {
        increment i
    }
}

```

4) END

2) Searching :

Step 1.) Read the key to be search

Step 2.) Calculate hash value of key, say hashAddr

Step 3.) if ($[\text{hashAddr}] == \text{key}$)
return (hashAddr && key)

else

for $i = \text{hashAddr} + 1$ to $(i \% n) \neq \text{hashAddr}$


```
if (hashTable[i.v.n] → key == key)
    return (i.v.n)
```

```
end if
```

```
i++
```

```
end for
```

```
end if
```

step 4.) Return -1

step 5.) Stop

3) Deleting =

step 1:] Read the key to be deleted.

step 2:] Search the key to be deleted & store its position, say k

step 3:] If (k != empty)

make the hashTable[k] as empty.

else

print "key not found"

step 4:] stop.

Conclusion:-

- i) hash tables are faster in most cases but general problem with hash tables there $O(1)$ complexity is not guaranteed.
- ii) For addition there is a point when table becomes full, then table needs to be enlarged which requires moving all of its elements.
- iii) Hash put the operation & get the operation of time complexity $O(1)$ with assumption that key-value pairs are well distributed across the buckets.

iv) Time complexity :-

	Average case	Worst case
Search	$O(1)$	$O(n)$
Insert	$O(1)$	$O(n)$
Delete	$O(1)$	$O(n)$