

10 | Friday

8 am

Hashing

what is good Hashfunction →

- quick to compute
- Uniform distribution

10

How to deal with non-integer key?

Birthday paradox?

There always be collision.

12

hash code map key → integer
compression map integer → $[0, N-1]$

1 pm

Every time location must match.

3

Popular Hash code map

- Integer Cast [32 bit interpretation]

- For more than 32 bit add them up to get 32 bit

- Polynomial accumulation

$a_0 + a_1x + \dots + x^{n-1}a_{n-1}$
 $x = 33, 37, 39 \text{ or } 41$ gives

at most 6 collision on
50,000 english word.

Compression map

$h(k) = k \bmod m$

Note: m -prime good not power of 2.

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$0 \dots k_{max} \rightarrow [0 \dots k_{max}] A$

Take fractional part (mod 1)
map to into $0 \dots m-1$

choice of m is not critical.
critical.

11

Multiple, add, Divide

$h(k) = |ak + b| \bmod N$

k - key, N - size of hash.

1 pm a should not multiple of N .

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Universal Hashing:-

Randomly pick Hash function.

more on collisions:-

- Linear probing & open
- Double Hashing Addressing

Go on different location till find empty location.

No. of element \leq size of Table

Linear Probing Example.

$h(k) = k \bmod 13$

18, 41, 22, 44, 59, 32, 31, 7, 3

Note:

44 → 32
18 → 44
59 → 32
22 → 31
73 → 7

fill → go to next.

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8 am Double Hash function.

$h_1(k)$ & $h_2(k)$

9 \rightarrow position in table we
1st check for key

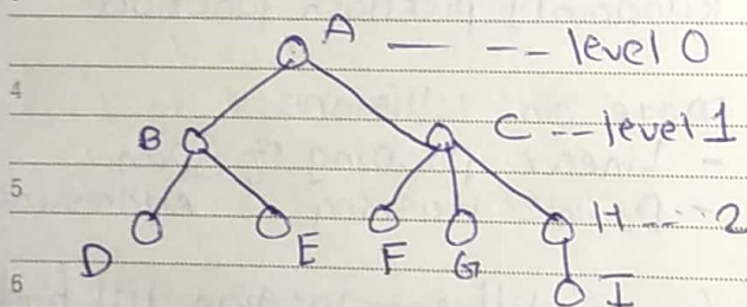
10 $h_2(k) \rightarrow$ determine offset
we use when searching
11 key k .

12 e.g.

$$h_1(k) = k \bmod 13$$

1 pm $h_2(k) = 8 - (k \bmod 8)$

Trees



A \rightarrow root

B, C, H \rightarrow Internal nodes

D, E, F, G, I \rightarrow leaves

9 Ordered tree - Tree in which
the children of each node
are ordered.

Note: Binary tree - At most 2
children, ordered.

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8 am Complete Binary tree :-

9 level i has 2^i nodes.

$$\text{Total nodes} = 2^{h+1} - 1 = n$$

10 $\text{internal nodes} = 2^n - 1$

11 $\text{Height} = \log_2(\text{no. of leaves})$

$$\text{No. of leaves} = (n+1)/2$$

12 Min. height of Binary tree
with n nodes

1 pm $n \leq 2^{h+1} - 1$

$$h \geq \log_2(n+1) - 1$$

2 max. height - $(n-1)$ with n

3 no. of leaves - 1 \leq no. of
internal nodes.

4 ADT for trees :-

5 $\text{size}()$, isEmpty , elements

6 $\text{positions}()$, $\text{isRoot}()$,

7 $\text{root}()$, $\text{parent}()$,

8 $\text{leftchild}()$, $\text{rightchild}()$.

Tree walks

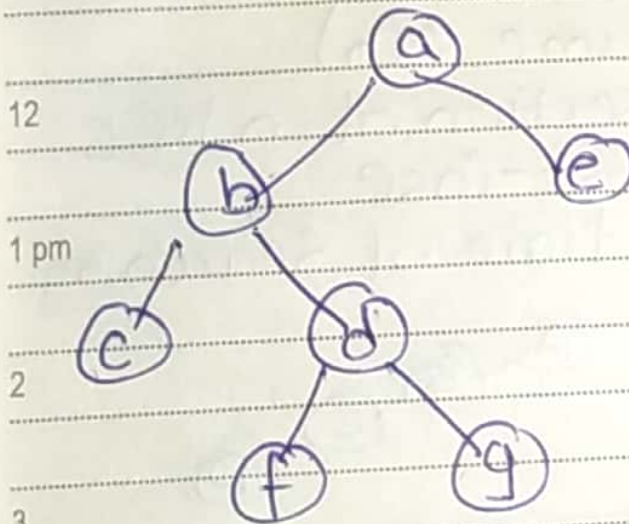
8 Preorder(v)

9 if ($v == \text{null}$) then return
else visit(v)

Note: $\text{Preorder}(v.\text{leftchild}())$
 $\text{Preorder}(v.\text{rightchild}())$

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Postorder(v)
 if (v == null) then return
 else postorder(v.leftchild())
 postorder(v.rightchild())
 visit(v)



preorder - abcdfge
 postorder - cfgdbea
 Inorder - cbfdgae

* Given the preorder & Inorder traversals of binary tree we can uniquely determine tree. // same with post & inorder But can not build with pre-postorder

Note :

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Ordered Dictionaries

In addition to dictionary function we want additional function:

Min()

Max()

Predecessor(S, k)

Successor(S, k)

* Unordered list

34 - 14 - 12 - 22 - 18

Searching $O(n)$

inserting $O(1)$

Ordered

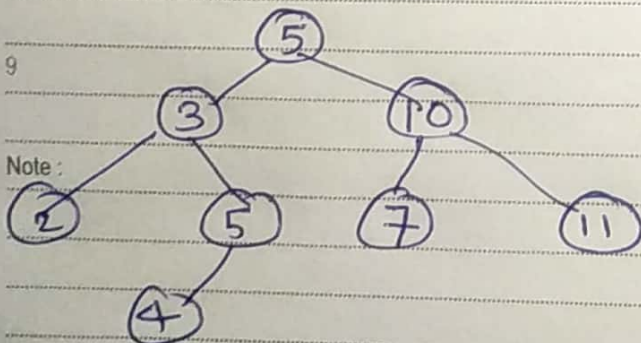
12 - 14 - 18 - 22 - 34

Searching $O(n)$

insertion $O(n)$

Binary Search runs in $O(\log n)$

Searching in Bst



Note:

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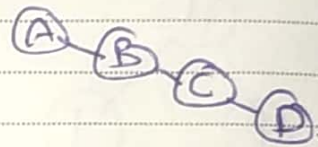
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- 1) Compare 'k' with root-key
- 2) if $k < \text{root-key}$, search k in left of root
- 3) Otherwise in right of root

* Running time $O(h)$

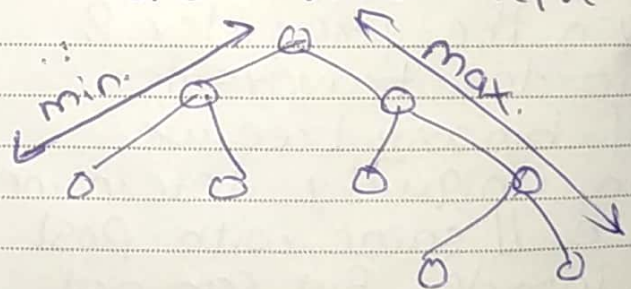
* After insertion of n keys the worst-case running time of Searching is $O(n)$

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BST minimum

while left(root) \neq NULL
do root \leftarrow left(root)



* Successor

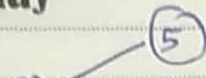
If have right node than leftmost of right

Note:



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← If not have right node than parent right

Deletion from tree

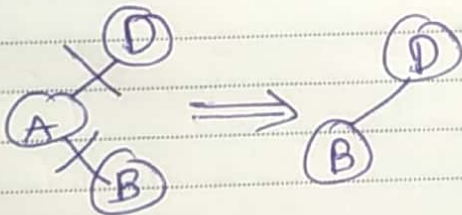
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Delete node X from tree we can have 3 cases

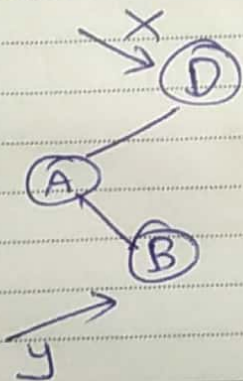
- X has no children
- X has one children
- X has two children

Case 1 -
Just remove X

Case 2 -



Case 3 -



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For removing X find successor of X i.e. y & replace X with y (successor or predecessor)

Note y has at most one child (beac it has right child than that becomes successor)

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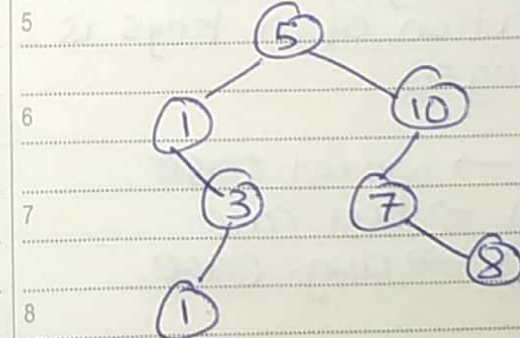
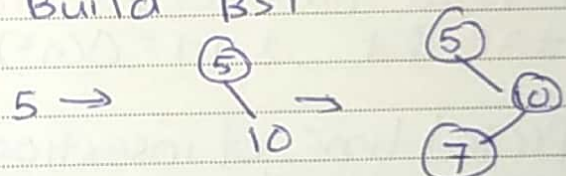
BST Sorting

1 pm

Sort the following no.

5 10 7 1 8 1 8

Build BST



Call Inorder walk
1 3 5 7 8 10

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In what order should we insert?

o We want to sort numbers $\{1, 2, 3, \dots, n\}$

o Total time taken to insert these no. equals the sum of level no. of nodes

o Thus if no. inserted in ascending order we would get tree of $(n-1)$ height

o So total time for insertion $1 + 2 + 3 + \dots + n-1 = O(n^2)$

* Expected time of insertion of a randomly chosen permutation of n keys is $O(n \log n)$

$\therefore O(n^2) \rightarrow$ worst case

$O(n \log n) \rightarrow$ Best case

$O(n \log n) \rightarrow$ avg. case

9

Note :