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unit 3
ML

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(1) Training error & Generalization Error

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- error calculated in training phase
- error in known dataset

$$E = \frac{1}{n} \sum_{i=1}^n \text{error}(f_p(x_i), y_i)$$

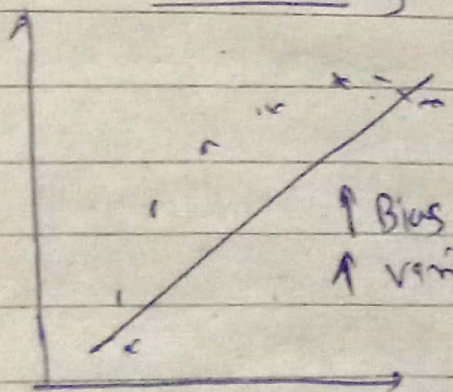
- error calculated in testing phase
- error in unknown or unseen dataset

Bias - algorithm error rate on the training set

variance - After getting low error in training, we apply for testing and got high error, this is variance.

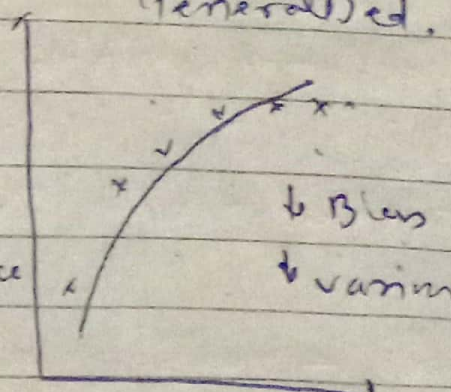
→ test set error.

underfitting



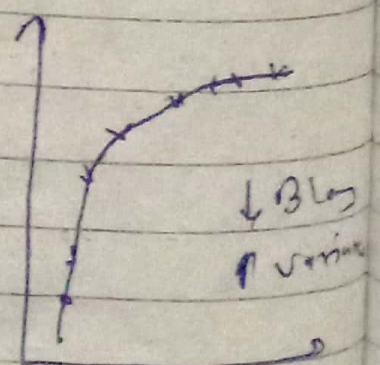
polynomial = 1 degree
Linear Regression

Generalized

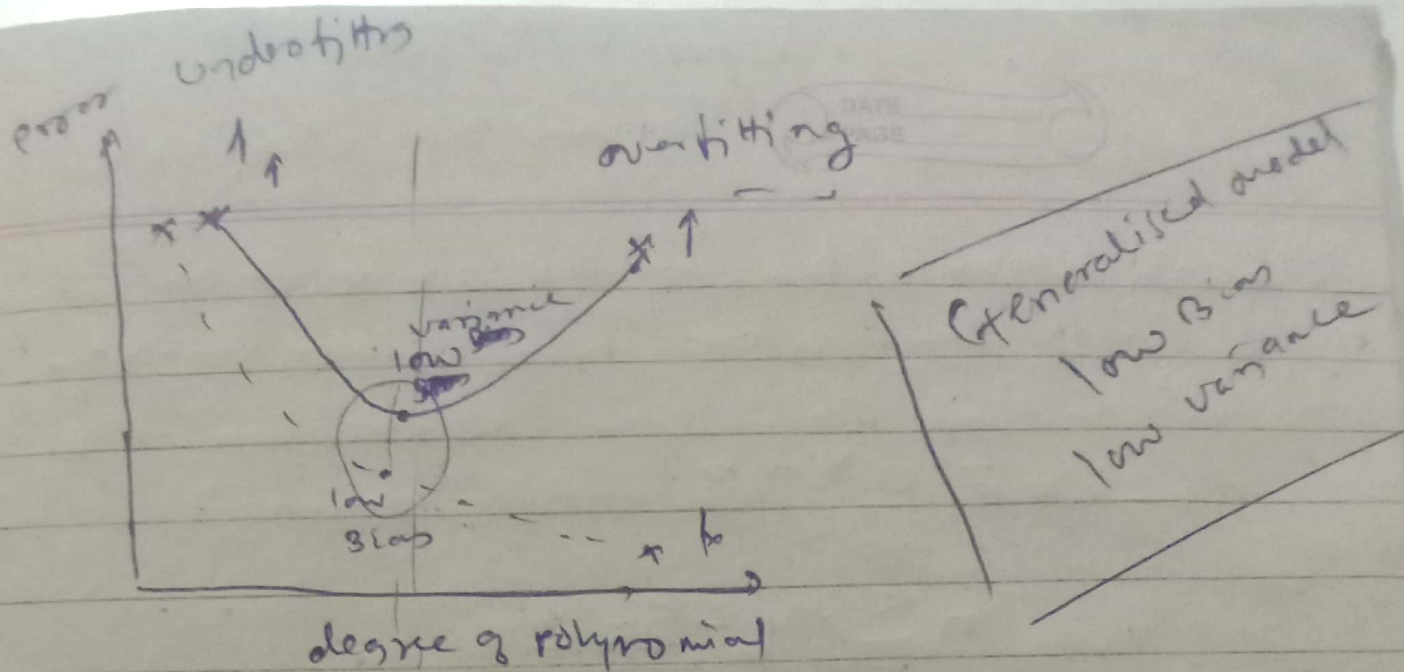


2 degree

overfitting



4 degree



Underfitting

- (1) Can't capture underlying pattern
- (2) does not fit well
- (3) less data to build an accurate model
- (4) \uparrow Bias, \uparrow variance

Reduce by

- (1) increase model complexity
- (2) increase no. of feature
- (3) Remove noise
- (4) increase the no. of epochs.

Overfitting

- (1) when we train we lot of data, and start learning noise & inaccurate data.
- (2) low training error But high testing error
- (3) low Bias & high variance.

Reduce By

- (1) increase training data
- (2) Reduce Complexity
- (3) Regularization.

Simple & Multiple Regression

one variable

more than 2 variables

Linear Regression — Linear function

Non Linear Regression — Non Linear function

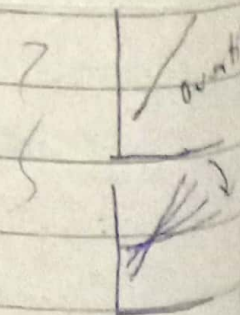
$$y' = ax + b$$

$$a = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{1}{n} (\sum y - a \sum x) = \bar{y} - a \bar{x}$$

LASSO Regression (L1 Regularization)

- Regularization technique
- overfitting issues solved
- feature selection. → → →
- used in multicollinearity.



Regularization → adding penalty to the best fit

penalty = absolute value of magnitude of the coefficient

Cost function →

Residual sum of squares + $\lambda \times$ (sum of the absolute value of the magnitude of coefficients)

we try to minimize this

$$\sum_{i=1}^n \left[y_i - \sum_{j=1}^p x_{ij} \beta_j \right]^2 + \lambda \sum_{j=1}^p |\beta_j|$$

λ = amount of shrinkage (Cross validation is used to find λ)

Ridge Regression (L2 regularization)

$$\frac{1}{2m} \sum_{i=1}^m \left(h(x^{(i)}) - y^{(i)} \right)^2$$

$$\left(h(x^{(i)}) - y^{(i)} \right)^2 + \lambda (\text{slope})^2 \quad \rightarrow \text{penalizing.}$$

$$= 0 + 1(2)^2$$

↓ ↓ ↓

① Overfitting Reduce

$$\sum_{i=1}^n \left[y_i - \sum_{j=1}^p x_{ij} \beta_j \right]^2 + \lambda \sum_{j=1}^p \beta_j^2$$

② Prevent multicollinearity.

Gradient Descent Algorithm

→ optimization algorithm - Minimizing the cost function by the model's parameter.

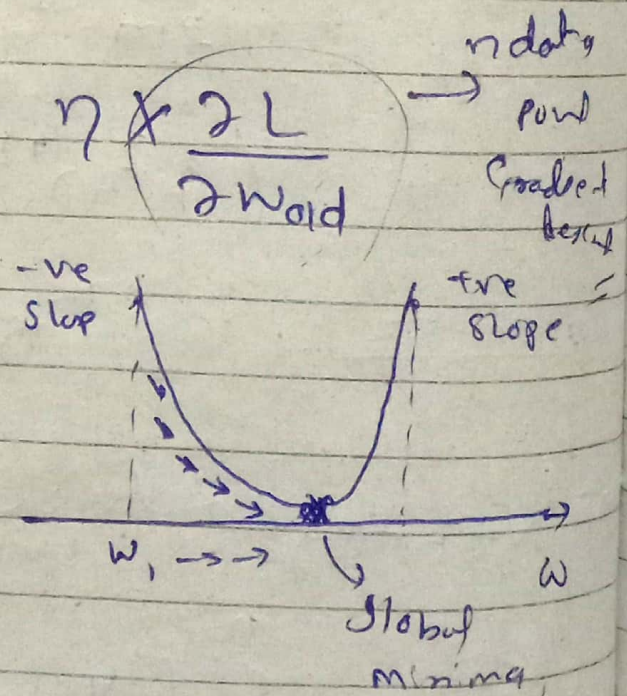
→ using iteration.

→ It helps in finding the local minimum of a function.

$$w_{\text{new}} = w_{\text{old}} - \eta \times \frac{2L}{2w_{\text{old}}}$$

$$\text{Loss} = \sum_{i=1}^n (y - \hat{y})^2$$

$$= \sum_{i=1}^n (y - \hat{y})^2$$



n data point - SGD

1 data point - Stochastic GD

1 data point - Minibatch GD

Evaluation Metrics. (cont function)

to Build and deploy a generalized Model we require to evaluate the Model on different Metrics which helps us

* Mean error \rightarrow average of the diff. b/w the actual value & predicted value

* Mean Squared error - (MSE)

\rightarrow Square average of Square of diff. b/w the actual value & predicted value

Mean Absolute error (MAE)

$$\rightarrow \frac{1}{N} \sum |y - \hat{y}|$$

Root Mean Squared error (RMSE)

$$RMSE = \sqrt{MSE}$$

$$RMSE = \sqrt{\frac{1}{N} \sum (y - \hat{y})^2}$$

R² (R Squared)

$$R^2 = 1 - \frac{SSr}{SSM}$$

SSr = Squared Sum
error of regression
line

SSM = Squared sum
error of Mean line

Q2. Show how well the data fit the regression
Model.

