

3.

To find polynomials that serve as upper and lower bounds on the curve obtained from the code, we can use the coefficients  $a$ ,  $b$ , and  $c$  obtained from the curve fitting:

The fitted curve is of the form:

$$f(n) = a \cdot n^2 + b \cdot n + c$$

From the curve fitting, we have obtained the coefficients  $a$ ,  $b$ , and  $c$ .

Upper Bound Polynomial: For the upper bound, we can use a polynomial that grows faster than the fitted curve. We can take a polynomial with a higher degree, such as  $O(n^3)$

Lower Bound Polynomial: For the lower bound, we can use a polynomial that grows slower than the fitted curve. We can take a polynomial with a lower degree, such as  $O(n)$  or  $O(n \log n)$

Big-O Notation: The upper bound of the curve is  $O(n^3)$ . This indicates that the time complexity of the algorithm is bounded above by a cubic polynomial. In other words, the algorithm has a worst-case time complexity of  $O(n^3)$ .

Big-Omega Notation : The lower bound of the curve can be approximated as  $O(n)$  or  $O(n \log n)$ . This indicates that the algorithm has a best-case time complexity of at least  $O(n)$  or  $O(n \log n)$

Big-Theta Notation: The big-Theta notation provides both upper and lower bounds. Since the upper bound is  $O(n^3)$  and the lower bound is  $O(n)$  or  $O(n \log n)$ , we can conclude that the algorithm's time complexity is  $\Theta(n^3)$  in the worst case and  $\Omega(n)$  or  $\Omega(n \log n)$  in the best case. Therefore, the tightest bound is  $\Theta(n^3)$ , indicating that the algorithm's time complexity grows cubically with the input size.