

1.

The outer and inner loops run from 1 to n .

The no. of iterations that occur:

for $i=1$, inner loop runs n times

for $i=2$, inner loop runs n times

...

for $i=n$, inner loop runs n times

Total no. of iterations can be calculated by adding the no. of iterations of the inner loop for each value of i from 1 to n .

Mathematically,

$$\sum_{i=1}^n \sum_{j=1}^n 1$$

From the above, the inner sum denotes the no. of times the inner loop runs for a specific value of i , and the outer sum denotes the no. of times the outer loop runs.

\therefore Multiplying the terms,

$$\sum_{i=1}^n \sum_{j=1}^n 1 = \sum_{i=1}^n (n)$$

Simplifying the expression,

$$\sum_{i=1}^n (n) = n \cdot \sum_{i=1}^n 1$$

$$n \cdot \sum_{i=1}^n 1 = n \cdot n = n^2$$

\therefore Runtime of the algorithm is $O(n^2)$.