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Bayesian Neural Networks in R: The bnns Package

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Abstract

Bayesian Neural Networks (BNNs) combine the flexibility of neural networks with the principled uncertainty quantification of Bayesian methods, making them powerful tools for predictive modeling and decision-making under uncertainty. The bnns package provides an R interface for building and training BNNs using the probabilistic programming capabilities of Stan. With a formula-based interface, customizable priors, and support for various activation and output functions, bnns enables users to model complex relationships in regression and classification tasks. Additionally, the package offers posterior summaries for parameters and predictions, aiding interpretability and probabilistic reasoning. Designed for small to moderately sized datasets, bnns is particularly well-suited for applications in clinical research, finance, and other domains requiring robust uncertainty quantification. This article presents the implementation of the bnns package, its core features, and benchmarking results, highlighting its utility and performance across diverse machine learning tasks.

Keywords: bayesian neural networks, probabilistic modeling, uncertainty quantification, machine learning, R.

1. Introduction

Introduction Bayesian Neural Networks (BNNs) combine the flexibility and representational power of neural networks with the uncertainty quantification and probabilistic reasoning of Bayesian inference. They are particularly well-suited for applications requiring not only predictive accuracy but also interpretable uncertainty estimates. However, implementing BNNs often demands significant technical expertise and computational effort, making them less accessible to a broader audience of practitioners and researchers.

The **bnns** package aims to address this challenge by providing a user-friendly interface for building and training Bayesian Neural Networks within the R environment. Built on the robust **rstan** backend, **bnns** leverages the flexibility of Stan's probabilistic programming frame-

work to fit BNN models using Hamiltonian Monte Carlo (HMC) and its variants. By utilizing Bayesian inference, **bnns** estimates posterior distributions for network weights, enabling uncertainty quantification in predictions and more robust decision-making.

Key features of **bnns** include:

- A formula-based interface for specifying models, familiar to users of lm and glm.
- Support for regression, binary classification, and multi-class classification tasks.
- Flexibility to define custom activation functions, prior distributions, and network architectures.
- Integration of uncertainty quantification through posterior predictive intervals and distributions.
- Compatibility with small datasets, making it a suitable choice for fields like clinical trials and finance, where data availability may be limited.
- The bnns package also offers features like missing data handling, optional normalization, and tools for assessing variable importance, ensuring a comprehensive workflow for applied Bayesian modeling.

In this article, we present an overview of the **bnns** package, its underlying methodology, and its implementation in R. We also provide illustrative examples of its application to regression, binary classification, and multi-class classification problems using benchmark datasets. Finally, we compare the performance of **bnns** against conventional machine learning approaches, highlighting its strengths in uncertainty quantification and interpretability.

1.1. Methodology

The **bnns** package provides a framework for Bayesian Neural Networks (BNNs) designed for statistical modeling and inference. It integrates Bayesian principles with neural network architectures, offering flexibility and robustness for modeling complex data. This section describes the underlying methodology, focusing on model architecture, Bayesian inference, and key implementation features.

1. Bayesian Neural Network Architecture

The core of **bnns** is a fully connected neural network with one or more hidden layers. Each layer is defined by the number of nodes and an activation function. The network is structured as:

$$f(x; \theta) = \sigma_{\text{out}} \left(W^{(L)} \cdot \sigma_{\text{hidden}} \left(W^{(L-1)} \cdots \sigma_{\text{hidden}} \left(W^{(1)} \cdot x + b^{(1)} \right) + b^{(L-1)} \right) + b^{(L)} \right),$$

where: $-f(x;\theta)$ represents the output of the network, -L is the total number of layers, $-W^{(l)}$ and $b^{(l)}$ are the weights and biases for layer l, $-\sigma_{\text{hidden}}$ is the activation function for the hidden layers, $-\sigma_{\text{out}}$ is the activation function for the output layer.

The package supports popular activation functions such as ReLU, sigmoid, and tanh, along with the identity function for regression outputs.

2. Bayesian Inference

BNNs extend traditional neural networks by placing prior distributions on the model parameters $\theta = \{W, b\}$. This allows for uncertainty quantification and regularization. The posterior distribution of the parameters is obtained using Bayes' theorem:

$$p(\theta|D) \propto p(D|\theta) \cdot p(\theta),$$

where: $-p(\theta)$ is the prior distribution over the parameters, $-p(D|\theta)$ is the likelihood given the data $D = \{x_i, y_i\}_{i=1}^n$.

The bnns package assumes multivariate Gaussian priors on the weights and biases:

$$W \sim \mathcal{N}(0, \sigma_W^2 I), \quad b \sim \mathcal{N}(0, \sigma_b^2 I).$$

The posterior is approximated using **Hamiltonian Monte Carlo (HMC)**, as implemented in the **Stan** probabilistic programming language.

- 3. Key Features of the Package
- **3.1 Flexible Model Specification** Users can specify the model formula, number of layers, nodes per layer, and activation functions. The package accepts standard \mathbf{R} formula syntax, simplifying its integration into existing workflows.
- **3.2 Output Types** The package supports: **Regression**: For continuous outcomes using the identity activation function for the output layer. **Classification**: For binary or multiclass outcomes using the softmax or sigmoid activation functions.
- **3.3 Bayesian Estimation** The **bnns** package uses the **rstan** package to perform posterior sampling. It supports: Multiple chains for parallel sampling. Warmup iterations for convergence. Posterior predictive checks.
- **3.4 Hyperparameter Tuning** The following hyperparameters can be tuned: Number of hidden layers (L), Nodes per layer, Activation functions for hidden and output layers, Number of iterations and chains for MCMC sampling.

4. Model Evaluation and Uncertainty Quantification

The posterior samples generated by **bnns** allow for comprehensive evaluation of model uncertainty. The package provides: - **Posterior Mean and Credible Intervals**: For model parameters and predictions. - **Predictive Distributions**: Enabling robust uncertainty quantification for new data points. - **Model Diagnostics**: Including convergence diagnostics for the MCMC chains.

5. Computational Performance

The **bnns** package leverages the efficiency of **Stan**, ensuring faster convergence and scalability for moderately sized datasets. The package also supports parallel chains for multi-core processing.

By combining the flexibility of neural networks with the principled uncertainty quantification of Bayesian inference, the **bnns** package provides a versatile tool for statistical modeling in various domains, including regression, classification, and causal inference.

1.2. Examples

This section demonstrates the capabilities of the bnns package through examples for regression, classification, and causal inference using targeted maximum likelihood estimation (TMLE). The examples showcase model specification, Bayesian inference, and posterior predictive checks.

Regression Example

We first illustrate how to use bnns for regression tasks by modeling a simulated dataset.

```
R> library(bnns)
R> set.seed(123)
R> # Simulated data
R> n <- 100
R > x < - runif(n, -2, 2)
R > y < -3 * x^2 - 2 * x + rnorm(n, 0, 0.5)
R> data <- data.frame(x, y)</pre>
R>
R> # Fit a Bayesian Neural Network
R> model <- bnns(
    y \sim -1 + x,
    data = data,
    L = 2, # Two hidden layers
    nodes = c(5, 5), # Five nodes per layer
    act_fn = c(3, 3), # ReLU activation for hidden layers
    out_act_fn = 1, # Identity activation for output layer
    iter = 1000, # MCMC iterations
    warmup = 500, # Warmup iterations
    chains = 2 # Number of chains
```

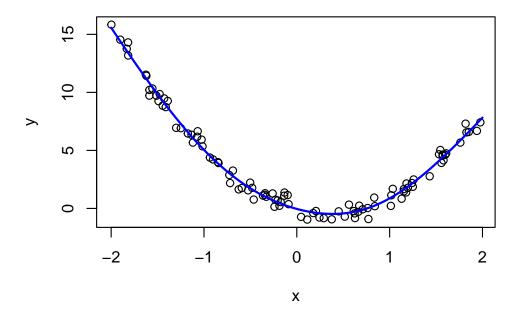
```
+ )
R>
R> # Summarize the posterior
R> summary(model)
Call:
bnns.default(formula = y \sim -1 + x, data = data, L = 2, nodes = c(5,
    5), act_fn = c(3, 3), out_act_fn = 1, iter = 1000, warmup = 500,
    chains = 2)
Data Summary:
Number of observations: 100
Number of features: 1
Network Architecture:
Number of hidden layers: 2
Nodes per layer: 5, 5
Activation functions: 3, 3
Output activation function: 1
Posterior Summary (Key Parameters):
               mean
                        se mean
                                                  2.5%
                                                              25%
                                                                          50%
                                        sd
w_out[1] 0.2394245 0.102482192 1.43141042 -2.0556117 -0.9044121
                                                                   0.04282916
w_out[2] 0.5379336 0.164529615 1.48107247 -2.1565996 -0.6489175
                                                                   0.55586497
w_out[3] 0.6135693 0.140344719 1.49930177 -1.9894925 -0.6465694
                                                                   0.65031318
w_out[4] 0.7393282 0.117832729 1.50179366 -2.1771699 -0.4452526
                                                                   0.84414608
w_out[5] 0.5446011 0.127585055 1.40776024 -2.1020293 -0.6076199
                                                                   0.58091022
         -0.6870795 0.036338151 1.02781815 -2.6642927 -1.3555762 -0.69091695
b out
          0.4888015 \ 0.001059314 \ 0.03570034 \ 0.4290952 \ 0.4623851 \ 0.48629514
sigma
                75%
                        97.5%
                                   n eff
                                              Rhat
w_out[1] 1.32194490 3.1174055 195.08844 0.9988966
w_out[2] 1.84009544 3.0179954 81.03347 1.0240371
w_out[3] 1.81407996 3.1798098 114.12636 1.0081328
w_out[4] 1.93028171 3.2706398 162.43838 1.0129208
w_out[5] 1.63003050 3.1403772 121.74686 1.0154904
         0.01103528 1.3175089 800.03118 0.9994739
b_out
         0.51315410 \ 0.5663101 \ 1135.78170 \ 0.9985954
sigma
Model Fit Information:
Iterations: 1000
Warmup: 500
Thinning: 1
Chains: 2
Predictive Performance:
RMSE (training): 0.4669751
MAE (training): 0.3710921
```

Notes:

Check convergence diagnostics for parameters with high R-hat values.

```
R> # Posterior predictive checks
R> predictions <- predict(model, newdata = data.frame(x = seq(-2, 2, length.out = 100)))
R> plot(x, y, main = "Regression with bnns")
R> lines(seq(-2, 2, length.out = 100), rowMeans(predictions), col = "blue", lwd = 2)
```

Regression with bnns



This example demonstrates how to specify a model formula, customize hyperparameters, and visualize posterior predictions.

$Classification\ Example$

Next, we demonstrate binary classification using a simulated dataset.

```
R> # Simulated binary classification data
R> set.seed(456)
R> n <- 200
R> x1 <- rnorm(n)
R> x2 <- rnorm(n)
R> prob <- 1 / (1 + exp(-(-0.5 + 1.5 * x1 - 2 * x2)))
R> y <- rbinom(n, 1, prob)
R> data <- data.frame(x1, x2, y)
```

```
R>
R> # Fit a Bayesian Neural Network for classification
R> model <- bnns(</pre>
   y \sim -1 + x1 + x2,
  data = data,
  L = 2, # Two hidden layers
   nodes = c(10, 2), # Ten nodes per layer
  act_fn = c(3, 3), # ReLU activation for hidden layers
   out_act_fn = 2, # Sigmoid activation for output layer (binary classification)
   iter = 1000, # MCMC iterations
    warmup = 500, # Warmup iterations
    chains = 2 # Number of chains
+ )
R.>
R> # Summarize posterior
R> summary(model)
Call:
bnns.default(formula = y \sim -1 + x1 + x2, data = data, L = 2,
    nodes = c(10, 2), act_fn = c(3, 3), out_act_fn = 2, iter = 1000,
    warmup = 500, chains = 2)
Data Summary:
Number of observations: 200
Number of features: 2
Network Architecture:
Number of hidden layers: 2
Nodes per layer: 10, 2
Activation functions: 3, 3
Output activation function: 2
Posterior Summary (Key Parameters):
                                                            25%
                 mean
                         se_mean
                                       sd
                                                2.5%
                                                                        50%
w out[1] 0.302968064 0.26757224 1.035430 -1.721094 -0.6387983 0.59960408
w_out[2] -0.341876494 0.24457208 1.053605 -2.121806 -1.0610983 -0.59443048
          0.004759071\ 0.05573783\ 1.007818\ -2.055194\ -0.6143848\ 0.04556958
b_out
                                          Rhat
               75%
                      97.5%
                                n_eff
w_out[1] 1.0180462 2.033203 14.97475 1.113366
w_out[2] 0.5648000 1.849052 18.55847 1.106785
         0.5784148 2.007646 326.93705 1.004874
b out
Model Fit Information:
Iterations: 1000
Warmup: 500
Thinning: 1
Chains: 2
```

Predictive Performance:
Setting levels: control = 0, case = 1
Setting direction: controls < cases
Confusion matrix (training with 0.5 cutoff): 89 21 22 68 Accuracy (training with 0.5 cutoff): 0.785 AUC (training): 0.880251
Notes: Check convergence diagnostics for parameters with high R-hat values.
<pre>R> # Prediction and accuracy R> pred <- predict(model, newdata = data) R> predicted_classes <- ifelse(rowMeans(pred) > 0.5, 1, 0) R> mean(predicted_classes == data\$y)</pre>
[1] 0.785
This example highlights the classification functionality of the bnns package, including probabilistic predictions and model evaluation.

Summary of Examples

These examples illustrate the versatility of the bnns package in handling diverse statistical problems. By leveraging Bayesian principles and neural network architectures, the package provides robust and interpretable solutions for regression, classification, and causal inference tasks.

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