

Practice Midterm

Practice conditions: You can use a double-sided cheat sheet and a digital calculator. You have 50 minutes.

Problem 1: (10 points) An urn contains 10 balls: 7 red and 3 yellow. Pick 4 balls, without replacement. What is the probability to have picked exactly 3 yellow?

Problem 2: (20 points) Roll 5 fair dice. What is the probability to get a square (4 identical digit, 5th one different)?

Problem 3: (20 points) Pick k numbers among $\{1, \dots, n\}$ with replacement. What is the probability that they two of them are the same?

This is the birthday problem: what is the probability that 2 students among the 120 enrolled in Math 394 have the same birthday? It corresponds to the probability of picking 120 numbers among $\{1, \dots, 365\}$ (with replacement) with two of them equal.

Problem 4: (20 points) Assume given two dice. One of them is fair. The other is biased: each odd digit arises with probability $1/4$ and each even digit arises with probability $1/12$.

Pick one of the two dice, roll it 3 times. Let X be the product of the three results. Knowing that X is odd, what is the probability that you picked the biased die?

Problem 5: Suppose that 1% of employees at a company use illegal drugs. The company performs drugs tests. If the tested person is a drug user, the test return POSITIVE 99% of the time. However, if the person is not a drug user, then the returns POSITIVE (this is called a false positive) 2% of the time.

(a) (5 points) What is the probability that Jordan tests POSITIVE?

(b) (5 points) Jordan tests POSITIVE. What is the probability that Jordan is a drug user?

(c) (10 points) Jordan plans to test again. What is the probability that Jordan tests POSITIVE again?

(d) (10 points) Jordan tests again, and is POSITIVE again. What is the probability that Jordan is a drug user?