

Exactly3Divisors

Time Complexity: $O(N^{1/2} * N^{1/4})$

Space complexity : $O(1)$

```
class Solution
{
    public boolean isPrime(int n)
    {
        if(n<=1)
            return false;

        for(int i=2;i<=Math.sqrt(n);i++)
            if(n%i==0)
                return false;

        return true ;
    }
    public int exactly3Divisors(int N)
    {
        int counter=0;
        N = (int)Math.sqrt(N);
        for(int i=1;i<=N;i++)
        {
            if(isPrime(i))
                counter++;
        }
        return counter;
    }
}
```

if number is perfect square or has sqrt as prime number then it has exactly 3 divisors

Factorial

Time Complexity : $O(n)$

Space Complexity : $O(1)$

```
int fact =1;
for (int i=2;i<=n;i++){
    fact = fact * i;
}
return fact;
```

Time Complexity : $O(2^n)$

Space Complexity : $O(1)$

```
if(n==0){
    return 1
}
return n * fact(n-1);
```

Gcd or Hcf

1st Approach

Time Complexity : $O(\log(\min(n1, n2)))$

Space Complexity : $O(1)$

```
while(n1>0 & n2>0){
    if(n1>n2){
        n1 =n1 % n2;
    }
    else{
        n2 = n2 % n1;
    }
}
if(n1==0) return n2;
return n1;
```

2nd Approach

Time Complexity : $O(\min(N1, N2))$

Space Complexity : $O(1)$

```
for(int i=1 ; i< Math.min(n1,n2); i++){
    if(n1%i==0 & n2%i==0){
        gcd = i;
    }
}
return gcd;
```

Prime Number

1st Approach

Time Complexity : $O(\sqrt{N})$

Space Complexity : $O(1)$

```
class Solution {  
  
    public boolean isPrime(int n) {  
  
        if(n < 2) return false;  
        int count = 0;  
        for(int i = 1; i <= Math.sqrt(n); ++i) {  
            if(n % i == 0) {  
                count = count + 1;  
                if(n % i != i) {  
                    count = count + 1;  
                }  
            }  
        }  
        if(count == 2) return true;  
        return false;  
    }  
}
```

2nd Approach

Time Complexity : $O(N^{1/2} * N^{1/4}) = O(N^{3/4})$

Space Complexity : $O(1)$

```
public static boolean isPrime(int n) {  
    // Handle small numbers  
    if (n <= 1) return false;  
    if (n <= 3) return true;  
    if (n % 2 == 0 || n % 3 == 0) return false;
```

```
// Start checking from 5 using 6k ± 1 optimization
for (int i = 5; i * i <= Math.sqrt(n); i += 6) {
    if (n % i == 0 || n % (i + 2) == 0) return false;
}
return true;
}
```

Prime Till N

1st Approach

Time Complexity: $O(n^{3/2})$

Space Complexity : $O(1)$

```
class Solution
{
    public boolean isPrime(int n)
    {
        for(int i = 1; i <= Math.sqrt(n); ++i) {
            if(n % i == 0) {
                count = count + 1;
                if(n % i != i) {
                    count = count + 1;
                }
            }
        }
        return count==2
    }
    public int exactly3Divisors(int N)
    {
        int counter=0;
        for(int i=1;i<=N;i++)
        {
            if(isPrime(i))
                counter++;
        }
        return counter;
    }
}
```