

Exactly3Divisors

Time Complexity: $O(N^{1/2} * N^{1/4})$

Space complexity : $O(1)$

```
class Solution
{
    public boolean isPrime(int n)
    {
        if(n<=1)
            return false;

        for(int i=2;i<=Math.sqrt(n);i++)
            if(n%i==0)
                return false;

        return true ;
    }

    public int exactly3Divisors(int N)
    {

        int counter=0;
        N = (int)Math.sqrt(N);
        for(int i=1;i<=N;i++)
        {

            if(isPrime(i))
                counter++;
        }
        return counter;
    }
}
```

if number is perfect square or has sqrt as prime number then it has exactly 3 divisors

Factorial

Time Complexity : O(n)

Space Complexity : O(1)

```
int fact =1;
for (int i=2;i<=n;i++){
    fact = fact * i;
}
return fact;
```

Time Complexity : O(2^n)

Space Complexity : O(1)

```
if(n==0){
    return 1
}
return n * fact(n-1);
```

Gcd or Hcf

1st Approach

Time Complexity : $O(\log(\min(n1,n2)))$

Space Complexity : $O(1)$

```
while(n1>0 & n2>0){  
    if(n1>n2){  
        n1 =n1 % n2;  
    }  
    else{  
        n2 = n2 % n1;  
    }  
}  
if(n1==0) return n2;  
return n1;
```

2nd Approach

Time Complexity : $O(\min(N1,N2))$

Space Complexity : $O(1)$

```
for(int i=1 ; i< Math.min(n1,n2); i++){  
    if(n1%i==0 & n2%i==0){  
        gcd = i;  
    }  
}  
return gcd;
```

Prime Number

1st Approach

Time Complexity : $O(\sqrt{N})$

Space Complexity : $O(1)$

```
class Solution {

    public boolean isPrime(int n) {

        if(n < 2) return false;
        int count = 0;
        for(int i = 1; i <= Math.sqrt(n); ++i) {
            if(n % i == 0) {
                count = count + 1;
                if(n % i != i) {
                    count = count + 1;
                }
            }
        }
        if(count == 2) return true;
        return false;
    }
}
```

2nd Approach

Time Complexity : $O(N^{1/2} * N^{1/4}) = O(N^{3/4})$

Space Complexity : $O(1)$

```
public static boolean isPrime(int n) {
    // Handle small numbers
    if (n <= 1) return false;
    if (n <= 3) return true;
    if (n % 2 == 0 || n % 3 == 0) return false;
```

```
// Start checking from 5 using 6k ± 1 optimization
for (int i = 5; i * i <= Math.sqrt(n); i += 6) {
    if (n % i == 0 || n % (i + 2) == 0) return false;
}
return true;
}
```

Prime Till N

1st Approach

Time Complexity: $O(n^{3/2})$

Space Complexity : $O(1)$

```
class Solution
{
    public boolean isPrime(int n)
    {
        for(int i = 1; i <= Math.sqrt(n); ++i) {
            if(n % i == 0) {
                count = count + 1;
                if(n % i != i) {
                    count = count + 1;
                }
            }
        }
        return count==2
    }

    public int exactly3Divisors(int N)
    {

        int counter=0;
        for(int i=1;i<=N;i++)
        {

            if(isPrime(i))
                counter++;
        }
        return counter;
    }
}
```