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1  ll power_mod(ll a, ll b) {
2      ll ret = 1; a %= mod;
3      assert(b >= 0);
4      for(; b; b >>= 1, a = a * a % mod)
5          if(b & 1) ret = ret * a % mod;
6      return ret;
7  }
8  namespace linear_seq {
9      const int N=10010;
10     ll res[N],base[N],_c[N],_md[N];
11
12     vector<ll> Md;
13     void mul(ll *a,ll *b,ll k) {
14         rep(i,0,k+k) _c[i]=0;
15         rep(i,0,k) if (a[i]) rep(j,0,k) _c[i+j]=(_c[i+j]+a[i]*b[j])%mod;
16         for (ll i=k+k-1;i>=k;i--) if (_c[i])
17             rep(j,0,SZ(Md)) _c[i-k+Md[j]]=( _c[i-k+Md[j]]-
18 _c[i]*_md[Md[j]])%mod;
19         rep(i,0,k) a[i]=_c[i];
20     }
21     ll solve(ll n,VI a,VI b) {
22         ll ans=0,pnt=0;
23         ll k=SZ(a);
24         assert(SZ(a)==SZ(b));
25         rep(i,0,k) _md[k-1-i]=-a[i];_md[k]=1;
26         Md.clear();
27         rep(i,0,k) if (_md[i]!=0) Md.push_back(i);
28         rep(i,0,k) res[i]=base[i]=0;
29         res[0]=1;
30         while ((1ll<<pnt)<=n) pnt++;
31         for (ll p=pnt;p>=0;p--) {
32             mul(res,res,k);
33             if ((n>>p)&1) {
34                 for (ll i=k-1;i>=0;i--) res[i+1]=res[i];res[0]=0;
35                 rep(j,0,SZ(Md)) res[Md[j]]=(res[Md[j]]-res[k]*_md[Md[j]])%mod;
36             }
37         }
38         rep(i,0,k) ans=(ans+res[i]*b[i])%mod;
39         if (ans<0) ans+=mod;
40         return ans;
41     }
42     VI BM(VI s) {
43         VI C(1,1),B(1,1);
44         ll L=0,m=1,b=1;
45         rep(n,0,SZ(s)) {
46             ll d=0;
47             rep(i,0,L+1) d=(d+(ll)C[i]*s[n-i])%mod;
48             if (d==0) ++m;
49             else if (2*L<=n) {
50                 VI T=C;
51                 ll c=mod-d*power_mod(b,mod-2)%mod;
52                 while (SZ(C)<SZ(B)+m) C.pb(0);
53                 rep(i,0,SZ(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
54                 L=n+1-L; B=T; b=d; m=1;

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55         } else {
56             ll c=mod-d*power_mod(b,mod-2)%mod;
57             while (SZ(C)<SZ(B)+m) C.pb(0);
58             rep(i,0,SZ(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
59             ++m;
60         }
61     }
62     return C;
63 }
64 ll gao(VI a,ll n) {
65     VI c=BM(a);
66     c.erase(c.begin());
67     rep(i,0,SZ(c)) c[i]=(mod-c[i])%mod;
68     return solve(n,c,VI(a.begin(),a.begin()+SZ(c)));
69 }
70 };
71

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