

# 1. Matrix multiplication Good. (15/15)

**1.1 [5 points]** Write a program `Main.f90` to read `fortran_demo1/M.dat` as the matrix `M`, and `fortran_demo1/N.dat` as the matrix `N`.

```
Program Main

Implicit none

integer                :: u, i, j
real(4), dimension(5,3) :: M
real(4), dimension(3,5) :: N
real(4), dimension(5,5) :: MN

u = 50

open(unit=u, file='M.dat', status='old')
read(u,*) ((M(i,j),j=1,3),i=1,5)
close(u)

print *, 'M matrix'

do i = 1,5
    write(*,*) M(i,:)
enddo

open(unit=u, file='N.dat', status='old')
read(u,*) ((N(i,j),j=1,5),i=1,3)
close(u)
```

```

print *, 'M matrix'

do i = 1,5
    write(*,*) M(i,:)
enddo

open(unit=u, file='N.dat', status='old')
read(u,*) ((N(i,j),j=1,5),i=1,3)
close(u)

print *, 'N matrix'

do i = 1,3
    write(*,*) N(i,:)
enddo

call Matrix_multip(M,N,MN)

write(*,*) 'shape MN:', shape(MN)

open(unit=u, file='MN.dat', status='replace')
do i = 1,5
    write(u,'(f9.2)') MN(i,:)

```

Have you found your MN.dat is shown in one column? To get 5\*5 matrix, please use write(u, '(5f9.2)') MN(i,:)

```

do i = 1,3
    write(*,*) N(i,:)
enddo

call Matrix_multip(M,N,MN)

write(*,*) 'shape MN:', shape(MN)

open(unit=u, file='MN.dat', status='replace')
do i = 1,5
    write(u,'(f9.2)') MN(i,:)
enddo

close(u)

End Program Main

```

**1.2 [5 points]** Write a subroutine `Matrix_multip.f90` to do matrix multiplication.

```

subroutine Matrix_multip(a,b,c)

implicit none

real(4), dimension(5,3), intent(in)  :: a
real(4), dimension(3,5), intent(in)  :: b
real(4), dimension(5,5), intent(out) :: c

c = matmul(a, b)

end subroutine Matrix_multip

```

**1.3 [5 points]** Call the subroutine `Matrix_multip()` from `Main.f90` to compute  $M \times N$ ; write the output to a new file `MN.dat`, values are in formats of `f9.2`.

```

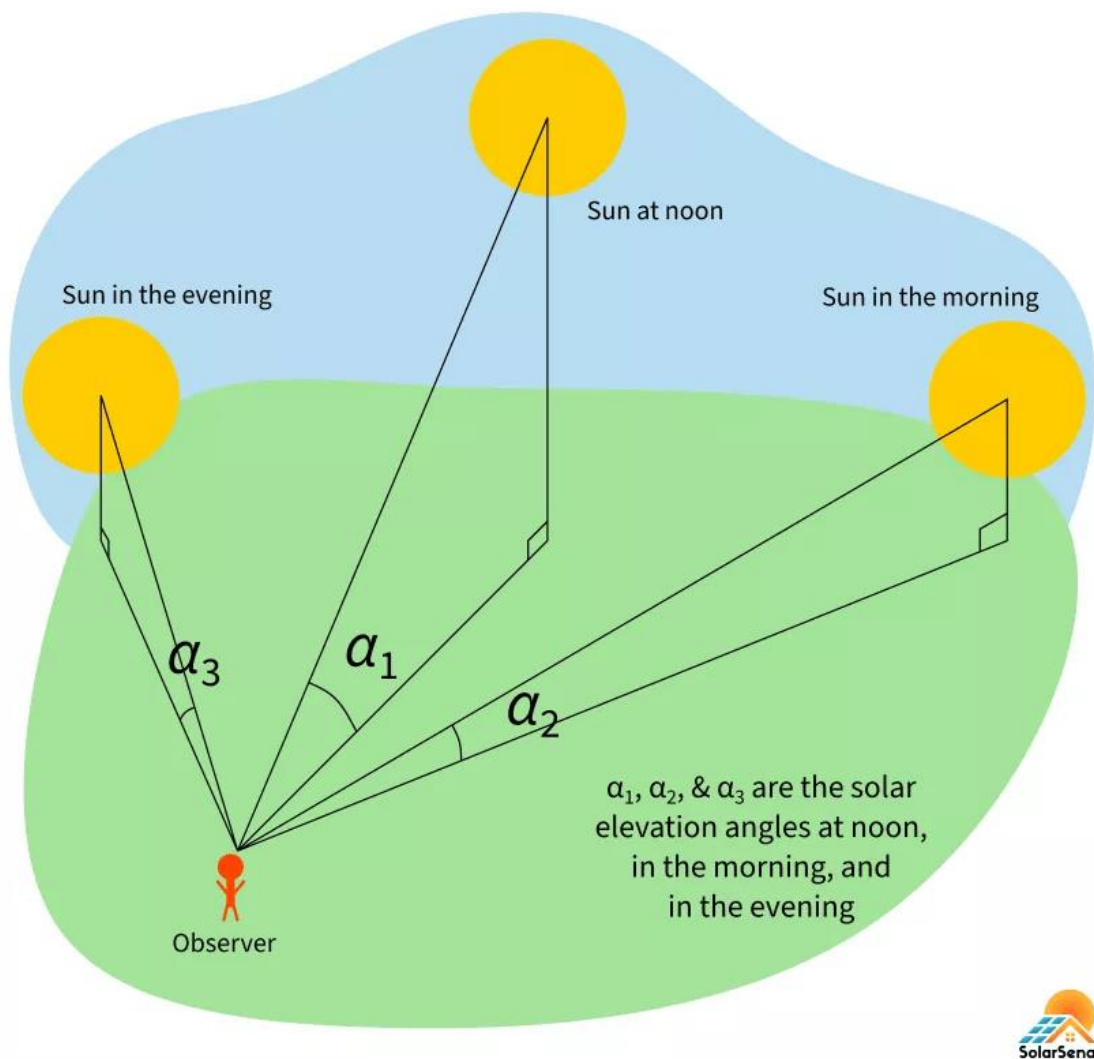
M matrix
19.4799995      15.7900000      19.2800007
19.2800007      12.9200001      15.8599997
15.8599997      11.2900000      14.0400000
11.9300003      18.6000004      18.2299995
19.2800007      12.9200001      15.8599997
N matrix
7.71999979      4.11000013      1.44000006      4.80000019      5.55000019
5.55000019      4.80000019      4.03999996      0.589999974      8.57999992
0.589999974      8.57999992      2.25999999      7.71999979      4.11000013
shape MN:      5      5

```

## 2. Calculate the Solar Elevation Angle

The solar elevation angle (SEA) is the angle between the imaginary horizontal plane on which you are standing and the sun in the sky. SEA is very important in deciding the inclination of solar panels, in both photovoltaics (PV) and thermal. The value of the SEA depends on the location on the Earth and the local date and time.

Please read this [Solar Elevation Angle – Calculating Altitude of Sun](#) and links therein for how to calculate SEA.



[Figure source](#)

**2.1 [5 points]** Write a module `Declination_angle` that calculates the *declination angle* on a given date.

[**Hint:** using the “Better formula” from [Solar Declination Angle & How to Calculate it](#)]

I suggest you to use `asind` and `sin`, instead of using `toarc`.

```
MODULE Declination_angle_module
CONTAINS

subroutine Declination_angle(days,angle)
  implicit none
  integer, intent(in) :: days
  real(8), intent(out) :: angle
  real(8) :: pi,toarc,delta

  pi = 3.1415926
  toarc = pi / 180.0

  delta = asin(sin(-23.44*toarc)*cos(toarc*(360.0/365.24*(days+10)+(360.0/pi)*0.0167*sin(3$
  angle = delta

end subroutine Declination_angle
end MODULE Declination_angle_module
```

**2.2 [10 points]** Write a module `Solar_hour_angle` that calculates the *solar hour angle* in a given location for a given date and time.

[**Hint:** using the formulas from [Solar Hour Angle & How to Calculate it](#)]

```
MODULE Solar_hour_angle_module
CONTAINS

subroutine Solar_hour_angle(days,LST,lon,TZ,h)

  implicit none

  real(8), intent(in) :: lon, TZ, LST
  integer, intent(in) :: days
  real(8), intent(out) :: h
  real(8) :: pi,gamma, EoT, Offset, LST_corrected

  pi = 3.1415926

  gamma = 2*pi/365*(days-1+(LST-12)/24)

  EoT = 229.18*(0.000075+0.001868*cos(gamma)-0.032077*sin(gamma)-0.014615*cos(2*gamma)-0.04084$
  Offset = EoT + 4*(lon - 15*TZ)

  LST_corrected = LST + Offset/60

  h = 15*(LST_corrected - 12)

end subroutine Solar_hour_angle
```

```
end MODULE Solar_hour_angle_module
```

**2.3 [5 points]** Write a main program (`Solar_elevation_angle.f90`) that uses module `Declination_angle` and `Solar_hour_angle` to calculate and print the SEA in a given location for a given date and time.

#### Program Solar\_elevation\_angle

```
USE Declination_angle_module
USE Solar_hour_angle_module

implicit none

real(8), parameter :: pi = 3.1415926536
real(8) :: lat, lon, TZ, LST, h, angle, SEA, toarc
integer :: days, year, month, day
integer, dimension(12) :: month_array, month_leap_array

month_array=(/31,28,31,30,31,30,31,31,30,31,30,31/)
month_leap_array=(/31,29,31,30,31,30,31,31,30,31,30,31/)

toarc = pi / 180

lat = 22.542883
lon = 114.062996
TZ = 8.0
LST = 10.53333
year = 2021
month = 12
day = 31
```

```
if ((mod(year,400)==0) .or. (mod(year,4)==0 .and. mod(year,100)/=0)) then
    days = sum(month_leap_array(:month-1)) + day
else
    days = sum(month_array(:month-1)) + day
end if

call Declination_angle(days, angle)

call Solar_hour_angle(days,LST, lon, TZ, h)

SEA = asin(sin(lat*toarc)*sin(angle*toarc)+cos(lat*toarc)*cos(angle*toarc)*cos(h*toarc))*1/t$
write(*,'(a6,f7.3)') 'SEA = ', SEA

End Program Solar_elevation_angle
```

**2.4 [5 points]** Create a library (libsea.a) that contains Declination\_angle.o and Solar\_hour\_angle.o. Compile Solar\_elevation\_angle.f90 using libsea.a. Print the SEA for Shenzhen (22.542883N, 114.062996E) at 10:32 (Beijing time; UTC+8) on 2021-12-31.

```

[ese-tianxj@login02 ~]$ nano Declination_angle.f90
[ese-tianxj@login02 ~]$ nano Solar_hour_angle.f90
[ese-tianxj@login02 ~]$ nano Solar_elevation_angle.f90
[ese-tianxj@login02 ~]$ gfortran -c Declination_angle.f90
[ese-tianxj@login02 ~]$ gfortran -c Solar_hour_angle.f90
[ese-tianxj@login02 ~]$ gfortran Solar_elevation_angle.f90 Declination_angle.o Solar_hour_angle.o
-o Solar_elevation_angle.f90
gfortran: error: Declination_angle.o: No such file or directory
[ese-tianxj@login02 ~]$ gfortran -c Solar_elevation_angle.f90
[ese-tianxj@login02 ~]$ gfortran Solar_elevation_angle.f90 Declination_angle.o Solar_hour_angle.o
-o Solar_elevation_angle.x
gfortran: error: Declination_angle.o: No such file or directory
[ese-tianxj@login02 ~]$ gfortran Solar_elevation_angle.f90 Declination_angle.o Solar_hour_angle.o
-o Solar_elevation_angle.x
[ese-tianxj@login02 ~]$ ar rcvf libsea.a Declination_angle.o Solar_hour_angle.o
a - Declination_angle.o
a - Solar_hour_angle.o
[ese-tianxj@login02 ~]$ gfortran Solar_elevation_angle.f90 -o Solar_elevation_angle.x -L. -lsea
[ese-tianxj@login02 ~]$ ./Solar_elevation_angle.x
SEA = 36.544

```

Good, you have known how to create library and compile by using library