

# ACCELERATED FAILURE TIME MODEL

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# MODEL STRUCTURE

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# Parametric Models

- AFT models are **parametric** – we assume failure time (T) has a particular structure and distribution...we will be modeling time until failure (T)
- Kaplan-Meier estimation is **nonparametric** – makes no assumption on failure time.
- Parametric methods allow for more detailed/precise estimation than nonparametric methods **IF** the distribution is specified correctly.
  - Ex: Easier to estimate medians, survival & hazard functions.

# Accelerated Failure Time Model

- The accelerated failure time (AFT) model is a regression that relates covariates (independent variables) to the event time  $T$ .
- The AFT model is a parametric model – depends on knowledge of the underlying distribution of the data.

$$T_i = e^{\beta_0 + \beta_1 x_{i,1} + \dots + \beta_k x_{i,k} + \sigma e_i}$$

# Accelerated Failure Time Model

- We can transform this model into a linear regression model by taking the natural log of both sides of the equation:

$$T_i = e^{\beta_0 + \beta_1 x_{i,1} + \dots + \beta_k x_{i,k} + \sigma e_i}$$

- The equation now becomes:

$$\log T_i = \beta_0 + \beta_1 x_{i,1} + \dots + \beta_k x_{i,k} + \sigma e_i$$

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Variables used to predict  $T$



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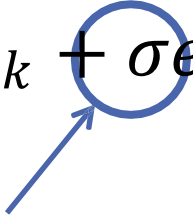
- The equation now becomes:

$$\log T_i = \beta_0 + \beta_1 x_{i,1} + \dots + \beta_k x_{i,k} + \sigma e_i$$

Scale parameter of the distribution



## Scale vs. Rate

$$\log T_i = \beta_0 + \beta_1 x_{i,1} + \cdots + \beta_k x_{i,k} + \sigma e_i$$


Scale parameter for distribution

- Another common form is the inverse of the scale, called the **rate**:  $(1/\sigma)$ .
- If  $\sigma$  is small, then events are not spread out  $\rightarrow$  events happening close to one another or rate is large
- If  $\sigma$  is large, then events are spread out  $\rightarrow$  smaller rate of events.



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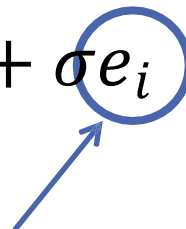
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Errors in the model



# Accelerated Failure Time Model

$$\log T_i = \beta_0 + \beta_1 x_{i,1} + \cdots + \beta_k x_{i,k} + \sigma e_i$$


Errors in the model

- The errors in the AFT model can follow many different distributions.
- Assumptions:
  - Specify correct distribution of errors
  - Constant Mean
  - Constant Variance
  - Independence across observations

# Common distributions for AFT model

Need a distribution that only takes on positive values and is right skewed:

- Weibull distribution

- Lognormal distribution

- Log-Logistic

- Exponential

More to come on distributions later....

# AFT Model – R with Lognormal

```
recid.aft.ln <- survreg(Surv(week, arrest) ~ fin + age + mar + prio, data = recid,  
dist = 'lognormal')  
summary(recid.aft.ln)
```

# AFT Model - R

Call:

```
survreg(formula = Surv(week, arrest) ~ fin + age + mar + prio,  
        data = recid, dist = "lognormal")
```

|             | Value   | Std. Error | z     | p       |
|-------------|---------|------------|-------|---------|
| (Intercept) | 4.0146  | 0.3897     | 10.30 | < 2e-16 |
| fin         | 0.3319  | 0.1657     | 2.00  | 0.04524 |
| age         | 0.0333  | 0.0153     | 2.18  | 0.02959 |
| mar         | 0.5609  | 0.2928     | 1.92  | 0.05541 |
| prio        | -0.0743 | 0.0264     | -2.82 | 0.00481 |
| Log(scale)  | 0.2723  | 0.0765     | 3.56  | 0.00037 |

Scale= 1.31

Log Normal distribution

Loglik(model)= -685.5      Loglik(intercept only)= -697.9

Chisq= 24.85 on 4 degrees of freedom, p= 5.4e-05

Number of Newton-Raphson Iterations: 4

n= 432

# AFT Model - R

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survreg(formula = Surv(week, arrest) ~ fin + age + mar + prio,  
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Parameter estimates

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P-values for estimates in the model



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Test to see if the “scale” (variance-like parameter) is equal to 1 (or  $\log(1)=0$ )

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Distribution assumed for the data



# AFT Model - R

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Log Normal distribution

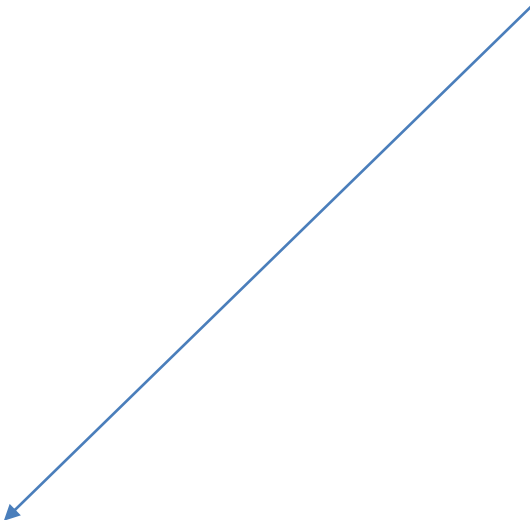
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Chisq= 24.85 on 4 degrees of freedom, p= 5.4e-05

Number of Newton-Raphson Iterations: 4

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Similar to an overall F test:  $H_0$ : Intercept model is appropriate (i.e. NO covariates are significant) versus  $H_A$ : At least one covariate is significant



# INTERPRETATION

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# AFT Model Parameter Interpretation

- If a parameter estimate is **positive**, increases in that variable **increase** the expected survival time.
- If a parameter estimate is **negative**, increases in that variable **decrease** expected survival times.
- If a parameter estimate is **zero**, increases in that variable have **no impact** on expected survival times.
- $100 \times (e^{\beta} - 1)$  is the % increase in the expected survival time for each one-unit increase in the variable.

# Recidivism Parameter Interpretation

| Variable          | $\beta$ Estimate | $100(e^{\beta} - 1)$ |
|-------------------|------------------|----------------------|
| Financial Aid     | 0.3319           | 39.36%               |
| Age at Release    | 0.0333           | 3.39%                |
| Marital Status    | 0.5609           | 75.22%               |
| Prior Convictions | -0.0743          | -7.16%               |

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For individuals who received financial aid, we expect their length of time until recidivism to be 39.4% longer than those who did not receive financial aid.


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For every increase in age by one year at time of release, we expect their length of time until recidivism to increase by 3.4%.

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For every increase in prior convictions, we expect their length of time until recidivism to decrease by 7.2%.



# DISTRIBUTIONS

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## Common Distributions

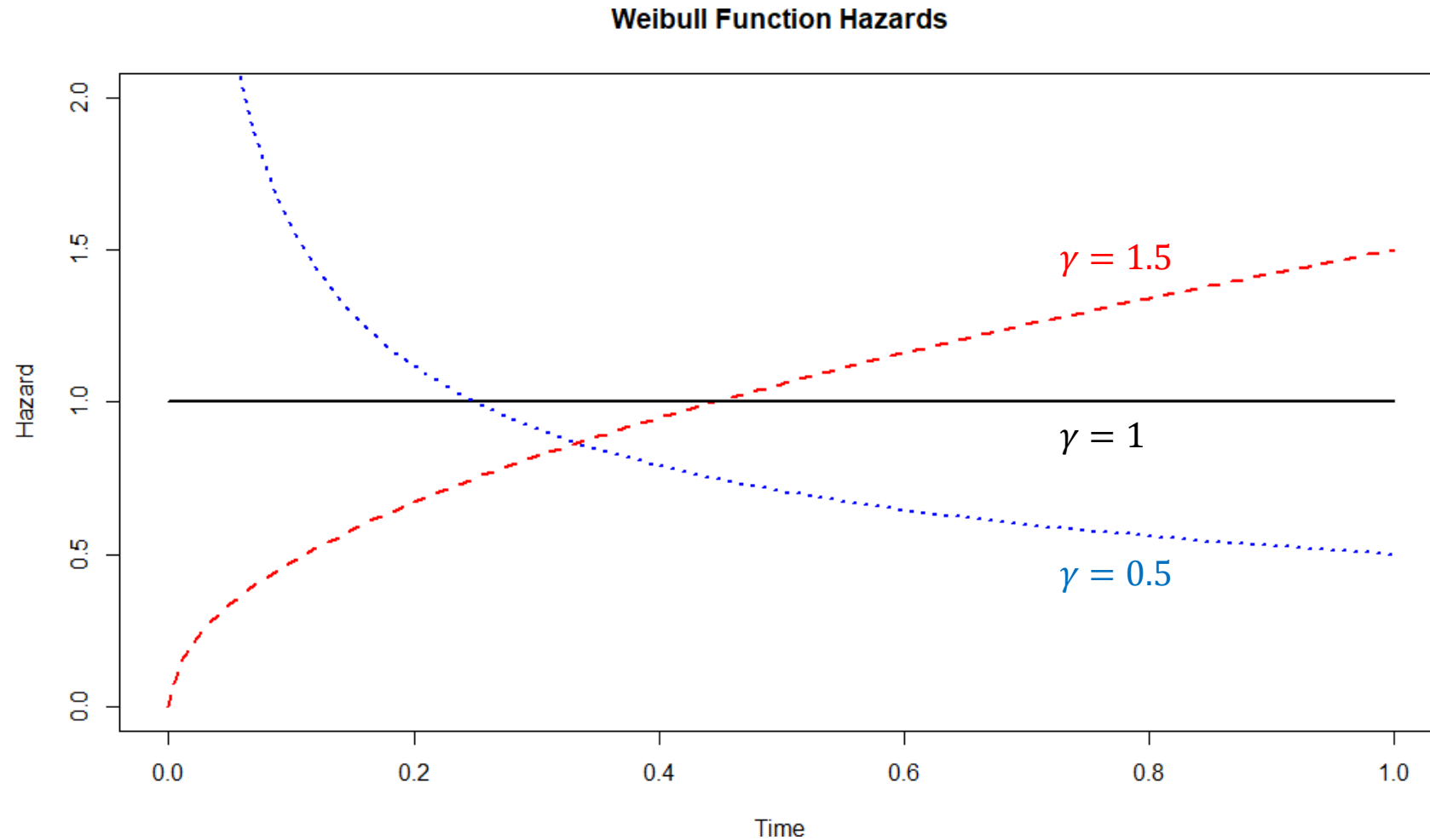
# Exponential Distribution

- Simplest distribution is the **exponential distribution** – constant hazard that doesn't depend on time.
- Survival function:  $S(t) = e^{-\lambda t}$
- Hazard function:  $h(t) = \lambda$
- Constant hazard commonly used when failures are completely random:
  - Light bulbs
  - Electronics
  - Etc.

# Weibull Distribution

- Most commonly used distribution is the **Weibull** distribution, which has an additional parameter  $\gamma$ .
- Survival function:  $\mathcal{S}(t) = e^{-(\lambda t)^\gamma}$
- Hazard function:  $h(t) = \lambda \gamma (\lambda t)^{\gamma-1}$
- The parameter  $\gamma$  is a rate parameter  $(1/\sigma) > 0$  and determines whether the hazard increases or decreases with time:
  - $\gamma > 1$ : hazard **increasing** with time (Ex: aging parts “wear out”)
  - $\gamma < 1$ : hazard **decreasing** with time (Ex: post-surgery complications)

# Weibull Distribution Hazards



# Exponential vs. Weibull

- Hazard for Weibull is constant when  $\gamma = 1$ .
- Weibull distribution **IS** the exponential distribution when  $\gamma = 1$ !
- R: Log(scale) p-value  $\rightarrow$  testing if  $H_0 : \log(\gamma) = 0$

# Weibull Distribution - R

```
recid.aft.w <- survreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio,  
data = recid, dist = 'weibull')  
summary(recid.aft.w)
```

# R output

$H_0: \gamma = 1$  (or  $\text{Log}(\gamma) = 0$ )

$H_A: \gamma \neq 1$  (or  $\text{Log}(\gamma) \neq 0$ )

|             | Value   | Std. Error | z     | p       |
|-------------|---------|------------|-------|---------|
| (Intercept) | 3.8086  | 0.3762     | 10.12 | < 2e-16 |
| fin         | 0.2625  | 0.1376     | 1.91  | 0.05650 |
| age         | 0.0400  | 0.0159     | 2.51  | 0.01210 |
| wexp        | 0.1115  | 0.1516     | 0.74  | 0.46196 |
| mar         | 0.3389  | 0.2725     | 1.24  | 0.21366 |
| paro        | 0.0538  | 0.1394     | 0.39  | 0.69956 |
| prio        | -0.0646 | 0.0210     | -3.08 | 0.00208 |
| Log(scale)  | -0.3383 | 0.0891     | -3.80 | 0.00015 |

Scale= 0.713

Weibull distribution

Loglik(model)= -680.5   Loglik(intercept only)= -696.6

Chisq= 32.28 on 6 degrees of freedom, p= 1.4e-05

Number of Newton-Raphson Iterations: 6

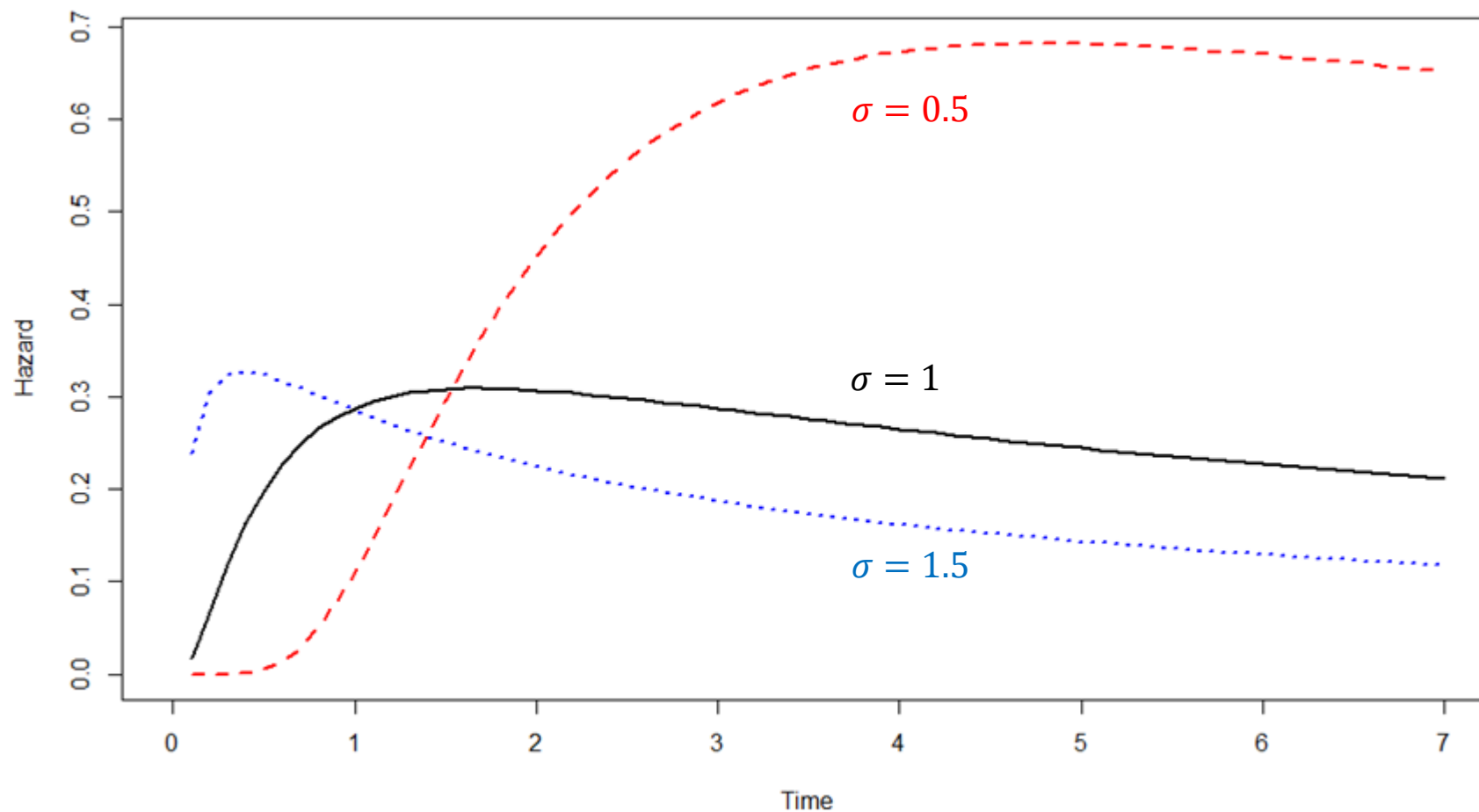
n= 432

# Other Distributions

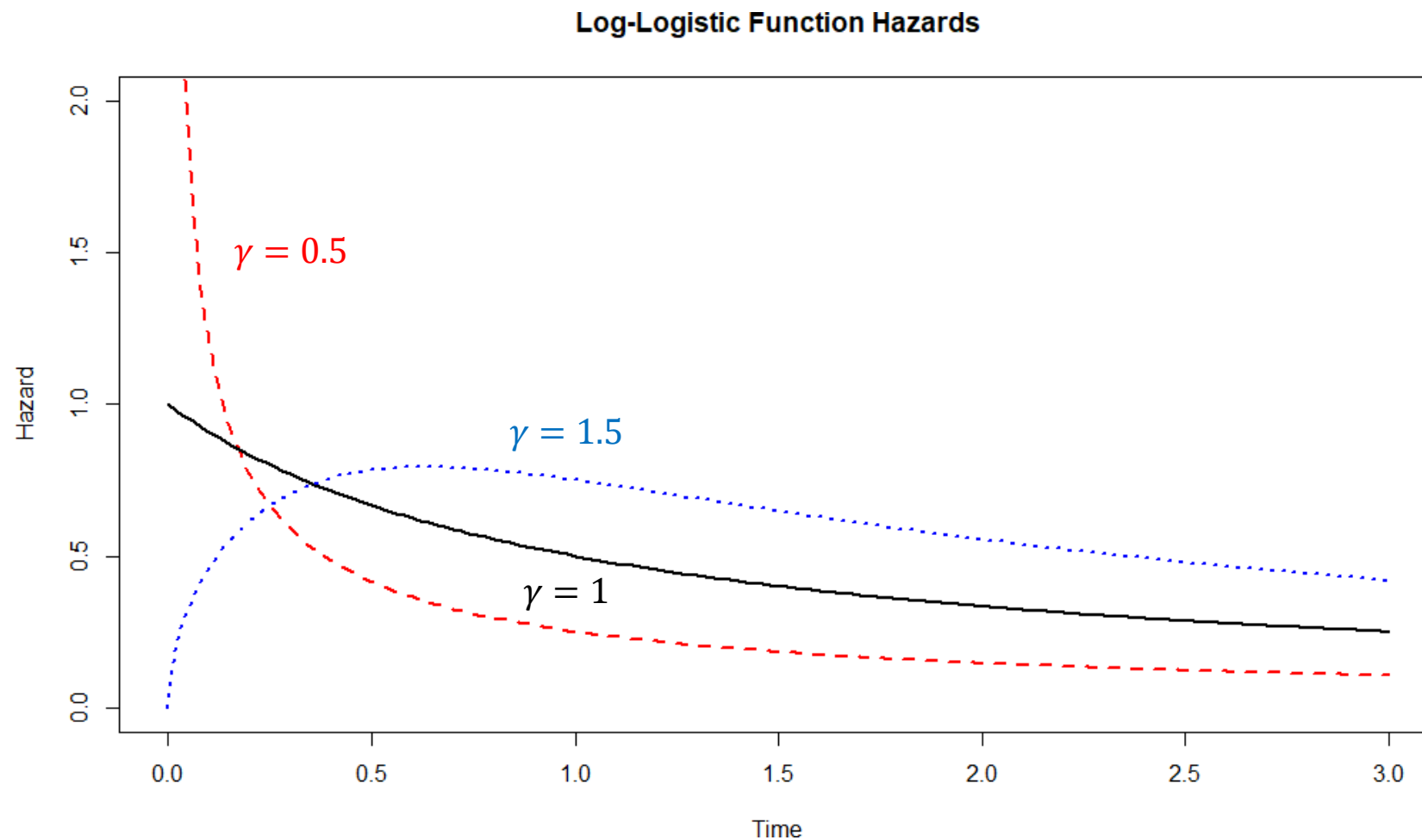
- **Log-Normal Distribution:** If  $T$  has a log-normal distribution, then  $\varepsilon$  follows a normal distribution.
  - IF NO CENSORING, log-normal AFT = linear regression with  $y = \log T$  are equivalent.
  - Hazard has different forms depending on the scale parameter
- **Log-Logistic Distribution:**
  - Hazard takes on different forms depending on the scale parameter
- **Generalized Gamma Distribution:**
  - Hazard takes on different forms depending on the scale parameter



# Log-Normal Hazard

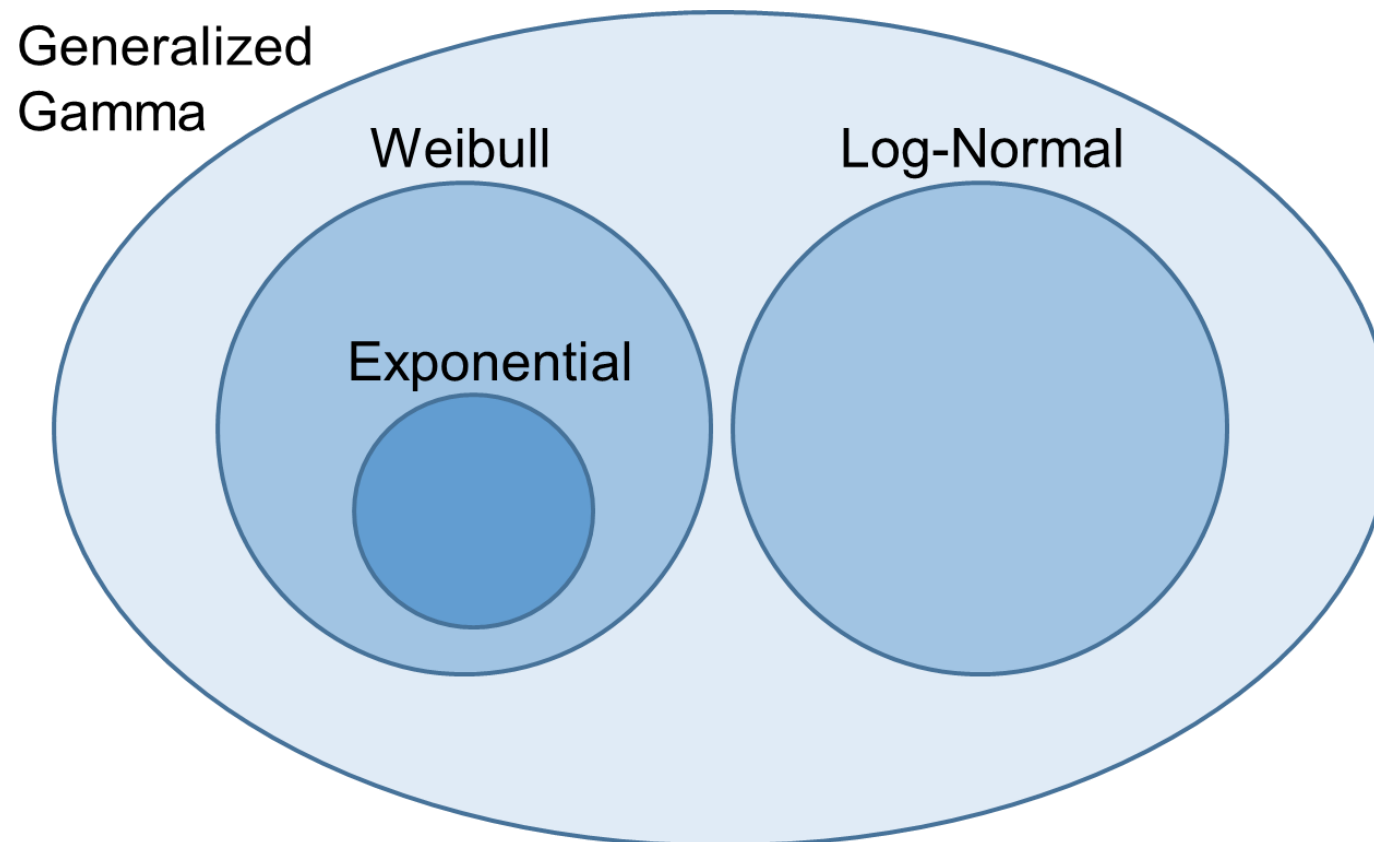


# Log-Logistic Hazard



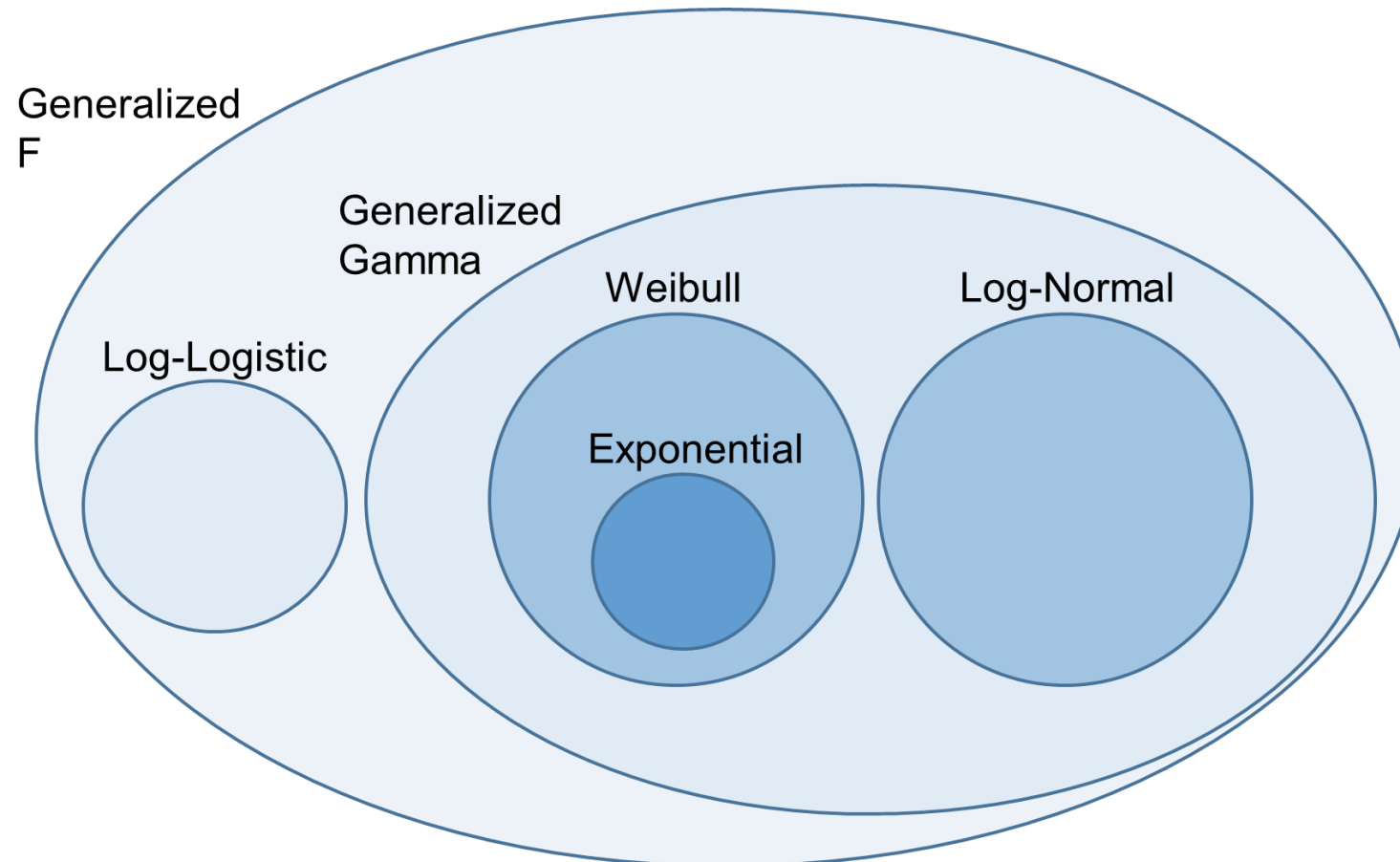
# Other Distributions

- **Generalized Gamma Distribution:** Includes log-normal and Weibull as special cases.



# Other Distributions

- **Generalized F Distribution:** Includes log-logistic and generalized gamma as special cases.



# Distributions

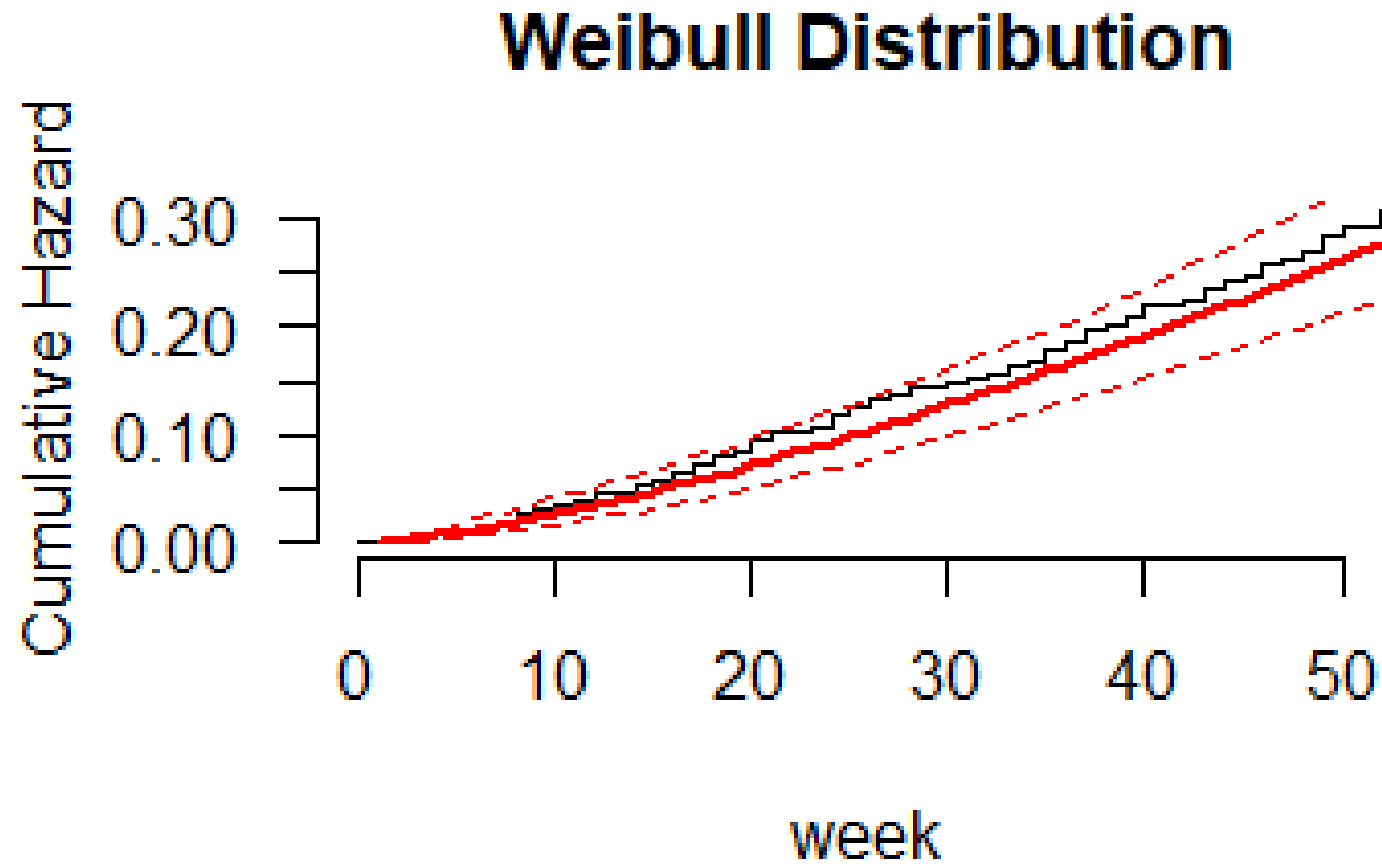
- Distributions are commonly checked two ways:
  1. Graphically (need to use the flexsurvreg and will compare cumulative hazard functions to actual data)
  2. Statistical Tests (if distributions are nested)
- There is **no guarantee** that your data will adequately match just one of the distributions here, or even any of them at all.
- Typically, use **full model** (all variables) since we don't know which p-values are correct

# Checking distributions - R

```
recid.aft.w <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro +  
prio, data = recid, dist = "weibull")
```

```
plot(recid.aft.w, type = "cumhaz", ci = TRUE, conf.int = FALSE, las = 1, bty = "n",  
      xlab = "week", ylab = "Cumulative Hazard", main = "Weibull Distribution")
```

# Cumulative Hazard - Weibull



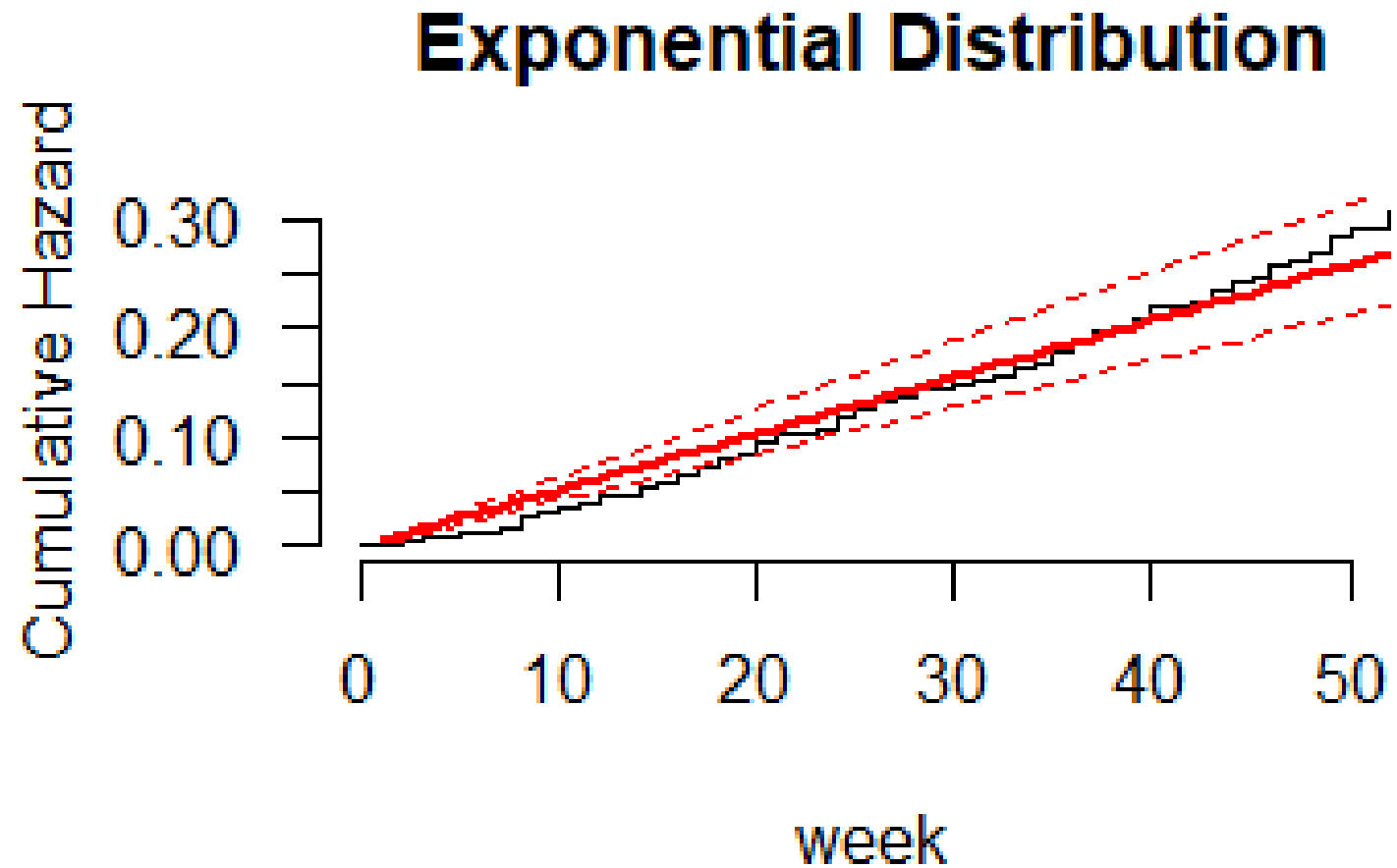
# Exponential

```
recid.aft.e <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio,  
data = recid, dist = "exp")
```

```
plot(recid.aft.e, type = "cumhaz", ci = TRUE, conf.int = FALSE, las = 1, bty = "n",  
xlab = "week", ylab = "Cumulative Hazard", main = "Exponential Distribution")
```



# Cumulative Hazard - Exponential



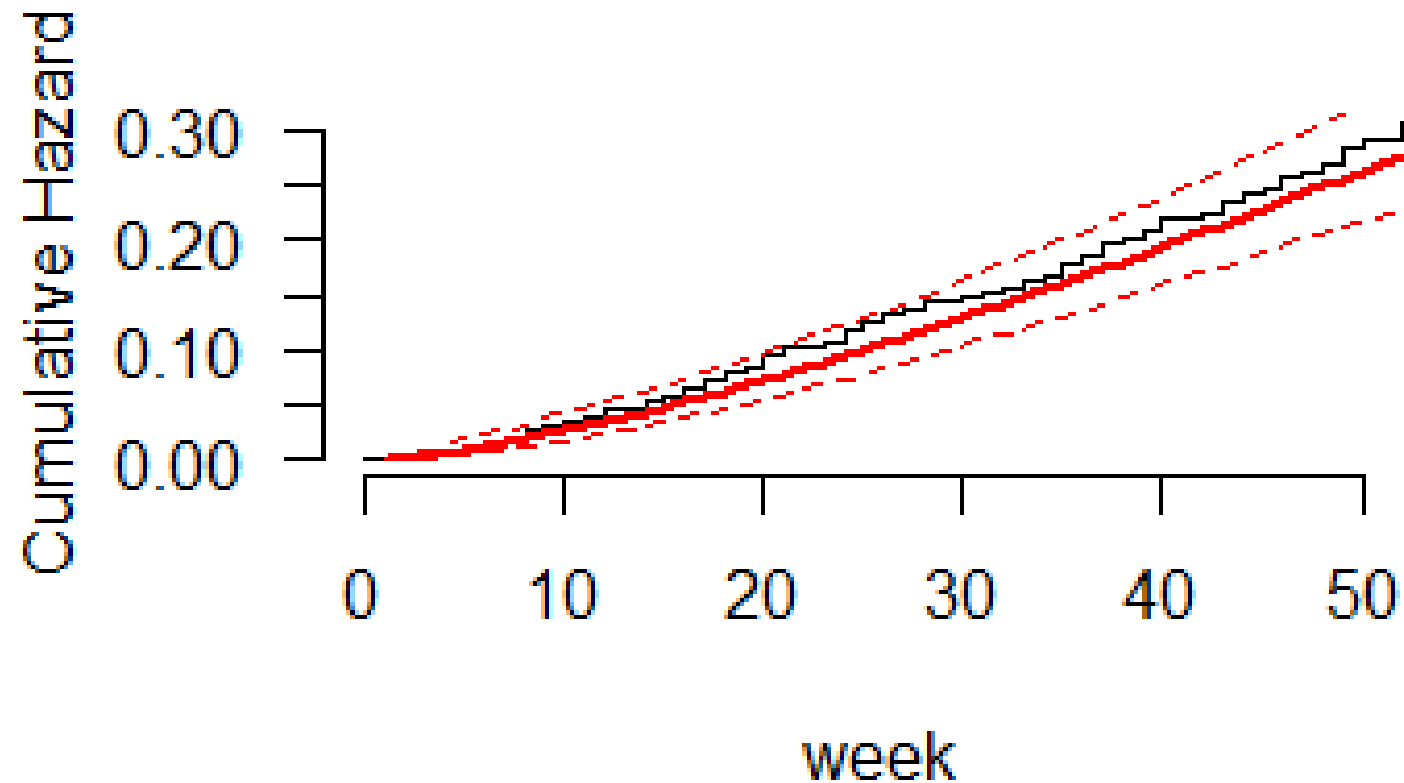
# Gamma

```
recid.aft.g <- flexsurvreg(Surv(week, arrest) ~ fin + age + race + wexp + mar + paro  
+ prio, data = recid, dist = "gamma")
```

```
plot(recid.aft.g, type = "cumhaz", ci = TRUE, conf.int = FALSE, las = 1, bty = "n",  
      xlab = "week", ylab = "Cumulative Hazard", main = "Gamma Distribution")
```

# Cumulative Hazard - Gamma

## Gamma Distribution

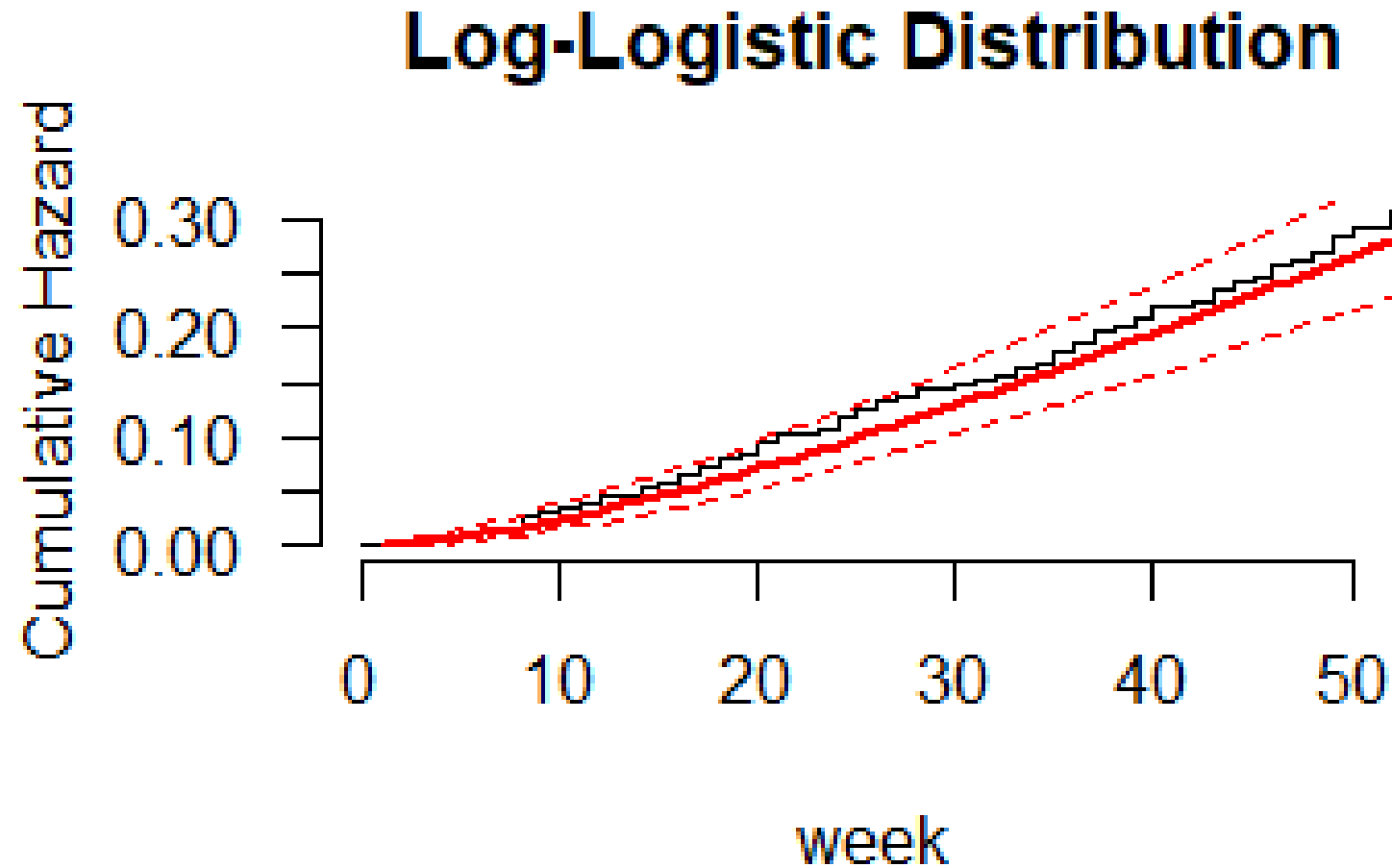


# Log-Logistic

```
recid.aft.ll <- flexsurvreg(Surv(week, arrest) ~ fin + age + race + wexp + mar + paro +  
prio, data = recid, dist = "llogis")
```

```
plot(recid.aft.ll, type = "cumhaz", ci = TRUE, conf.int = FALSE, las = 1, bty = "n",  
      xlab = "week", ylab = "Cumulative Hazard", main = "Log-Logistic Distribution")
```

# Cumulative Hazard – Log Logistic

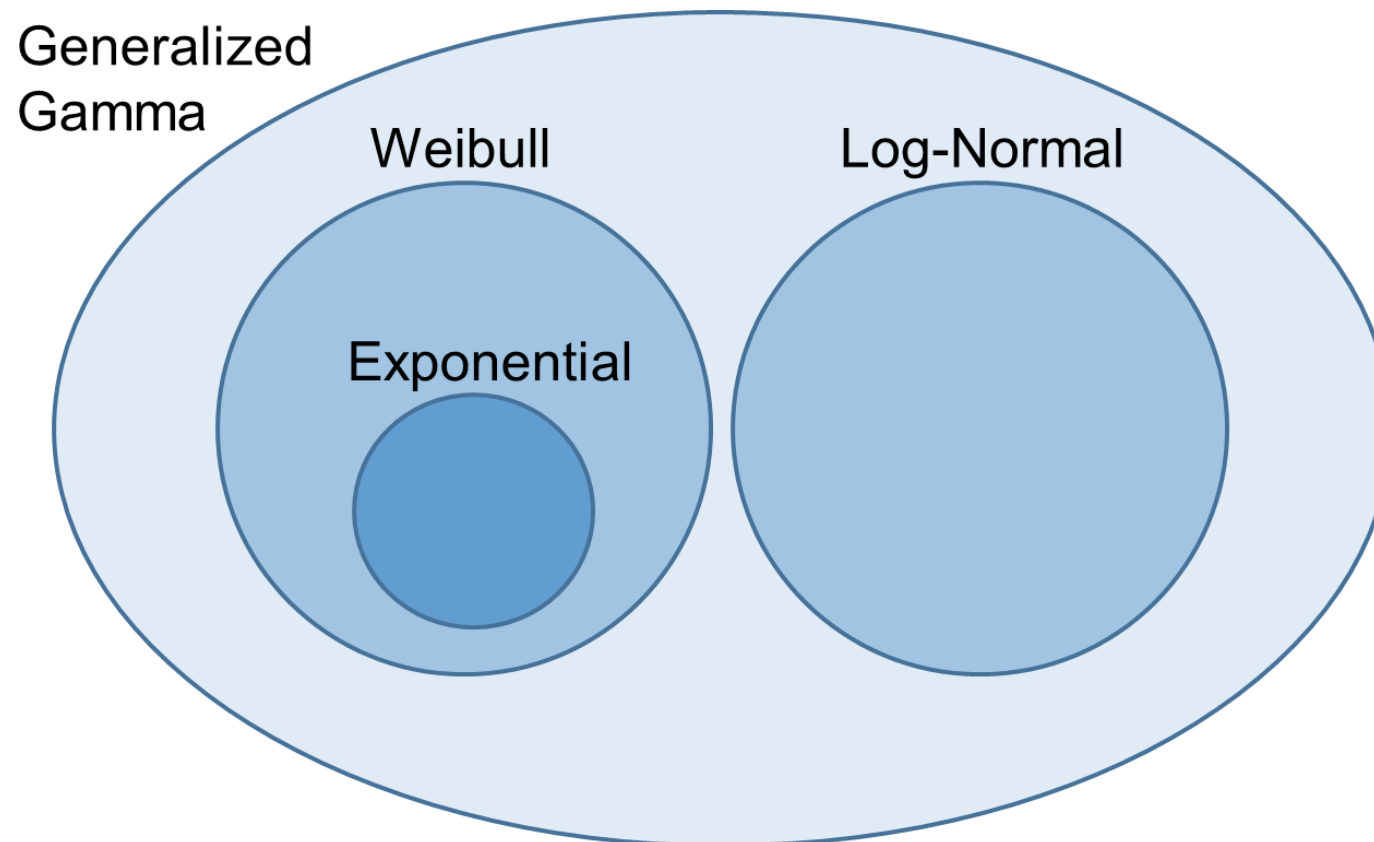


# Distributions

- Distributions are commonly checked two ways:
  1. Graphically
  2. Statistical Tests.... For nested distributions
- There is **no guarantee** that your data will adequately match just one of the distributions here, or even any of them at all.

# Nested Distributions!

- **Generalized Gamma Distribution:** Includes log-normal and Weibull as special cases.



# Goodness-of-Fit Tests

- Since these models are nested within the generalized gamma, we can use the **likelihood ratio test**.
- Likelihood Ratio Test:

$$\text{LRT} = -2(\log L_{\text{Nested}} - \log L_{\text{Full}})$$

- Typically, use **full model** (all variables) since we don't know which p-values are correct.



# Code to get likelihoods...

```
like.e <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist =  
"exp")$loglik
```

```
like.w <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist =  
"weibull")$loglik
```

```
like.ln <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist =  
"lnorm")$loglik
```

```
like.g <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist =  
"gamma")$loglik
```

```
like.ll <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist =  
"llogis")$loglik
```

#####DO NOT RUN the F –distribution....does NOT converge!!

```
like.f <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist =  
"genf")$loglik
```

# Code to get likelihoods...

```
like.e <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist = "exp")$loglik
```

```
like.w <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist = "weibull")$loglik
```

```
like.ln <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist = "lnorm")$loglik
```

```
like.g <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist = "gamma")$loglik
```

```
like.ll <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist = "llogis")$loglik
```

#####DO NOT RUN the F –distribution....does NOT converge!!

```
like.f <- flexsurvreg(Surv(week, arrest) ~ fin + age + wexp + mar + paro + prio, data = recid, dist = "genf")$loglik
```

# Calculate p-values

```
Tests = c('Exp vs. Gam', 'Wei vs. Gam', 'LogN vs. Gam')  
P_values = c(pval.e.g, pval.w.g, pval.ln.g)  
cbind(Tests, P_values)
```

$H_0$ : No “significant difference” in fit between the two distributions (Simpler distribution is fine)

$H_A$ : Significant difference in fit between the two distributions (More complex distribution is needed)

| Tests          | P_values |
|----------------|----------|
| "Exp vs. Gam"  | 0.0019   |
| "Wei vs. Gam"  | 1        |
| "LogN vs. Gam" | 0.0077   |

# After finding best distribution

After finding best distribution, we can select the best model (by hand...forward selection or backward elimination)

Using the Weibull distribution, we will use the following model moving forward:

|             | Value          | Std. Error    | z            | p              |
|-------------|----------------|---------------|--------------|----------------|
| (Intercept) | 3.7738         | 0.3581        | 10.54        | < 2e-16        |
| <b>fin</b>  | <b>0.2495</b>  | <b>0.1372</b> | <b>1.82</b>  | <b>0.06901</b> |
| <b>age</b>  | <b>0.0478</b>  | <b>0.0154</b> | <b>3.11</b>  | <b>0.00189</b> |
| <b>prio</b> | <b>-0.0698</b> | <b>0.0201</b> | <b>-3.47</b> | <b>0.00051</b> |
| Log(scale)  | -0.3367        | 0.0892        | -3.77        | 0.00016        |

Scale= 0.714

# PREDICTING SURVIVAL & EVENT TIMES

---

# Making Predictions

- AFT models assume a distribution for  $T$ , meaning that we expect event times to behave in a certain way.
- **IF WE ASSUME CORRECT DISTRIBUTION** we can predict quantiles, survival probabilities, event times, survival curves, and changes in expected values as predictor variable values change.

# Example Predictions

- Median survival time:
  - Find  $t$  such that  $\hat{S}_i(t) = 0.5$
- The time by which  $q\%$  of people with the same values for predictor variables have the event:
  - Find  $t$  such that  $\hat{S}_i(t) = 1 - q$
- 20 week predicted survival probability:
  - $\hat{S}_i(20)$
- **CAREFUL:**  $\hat{S}_i(t)$  is entirely determined by the distribution used so estimates WON'T be the same across different distributions.

# Predicting Survival Quantiles

```
# Predicted Survival Quantiles
```

```
recid.aft.w = survreg(Surv(week, arrest) ~ fin + age +prio, data = recid, dist = 'weibull')  
summary(recid.aft.w)
```

```
#####Find the 25th, 50th and 75th percentile of survival  
curve for each individual
```

```
survprob.75.50.25 = predict(recid.aft.w, type = "quantile", se.fit = TRUE,p = c(0.25, 0.5,  
0.75))  
head(survprob.75.50.25$fit)
```

|      | [,1]     | [,2]      | [,3]      |
|------|----------|-----------|-----------|
| [1,] | 52.68849 | 98.72758  | 161.95827 |
| [2,] | 24.17956 | 45.30760  | 74.32514  |
| [3,] | 17.89085 | 33.52383  | 54.99438  |
| [4,] | 64.22717 | 120.34873 | 197.42682 |
| [5,] | 35.95471 | 67.37185  | 110.52057 |
| [6,] | 48.95457 | 91.73097  | 150.48064 |

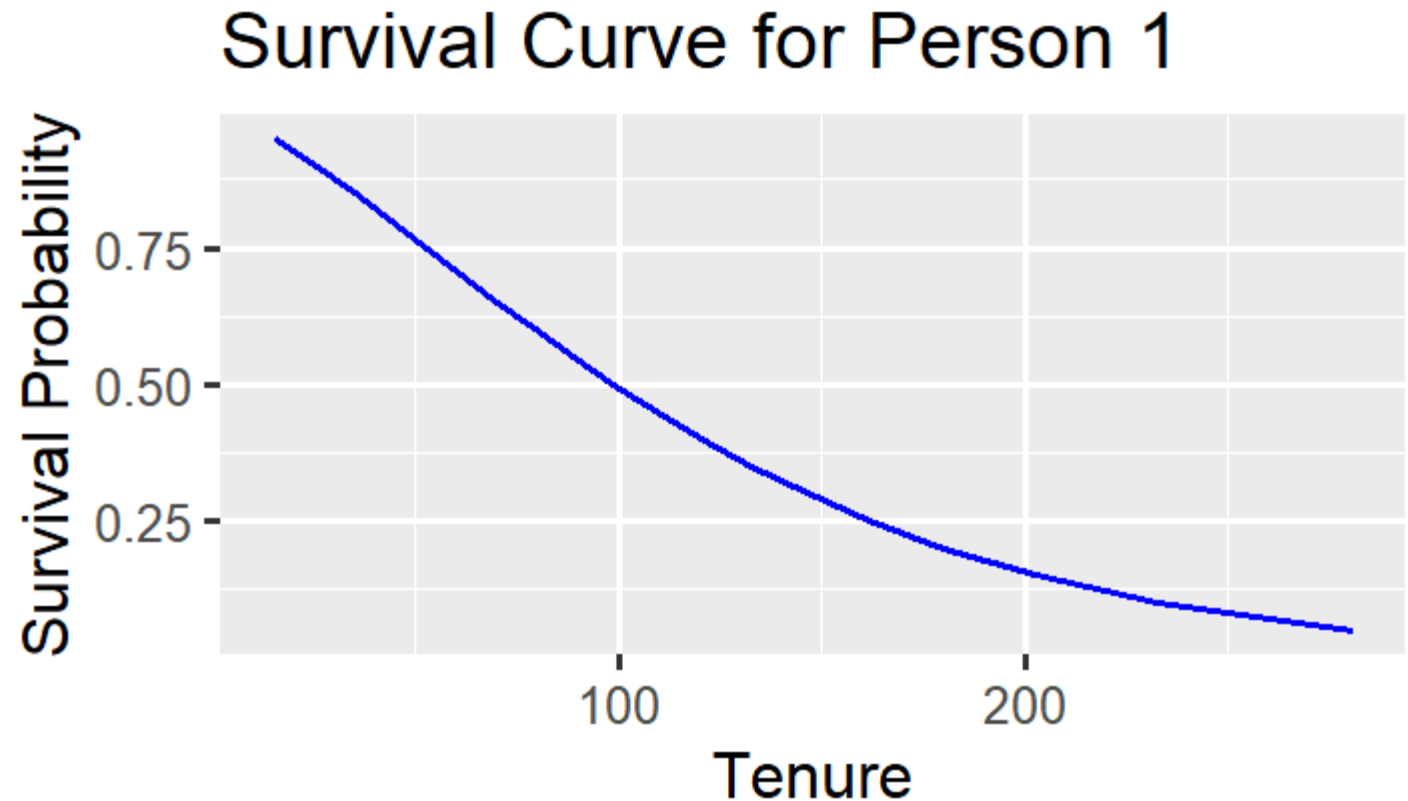


# Survival Curve for First Individual

```
quant.prob=seq(0.05,0.95,by=0.05)
survprob = predict(recid.aft.w, type = "quantile",
se.fit = TRUE,p = quant.prob)
surv.prob=rev(quant.prob)
```

```
graph.dat=data.frame(cbind(survprob$fit[1,],surv.
prob))
colnames(graph.dat)=c("Tenure","SurvivalProb")
```

```
ggplot(graph.dat,aes(x=Tenure,y=SurvivalProb))+g
eom_line(color="blue")+labs(title="Survival Curve
for Person 1",x="Tenure",y="Survival Probability")
```



# Predict mean survival time

```
p.time.mean <- predict(recid.aft.w, type = "response", se.fit = TRUE)  
head(p.time.mean$fit, n = 10)
```

```
[1] 128.26394  58.86229  43.55317 156.35349  87.52751  
[6] 119.17415 143.73152 115.26040  81.92984 113.19494
```

# Predict survival probabilities

```
survprob.actual = 1 - psurvreg(recid$week,  
  mean = predict(recid.aft.w, type = "lp"),  
  scale = recid.aft.w$scale, distribution = recid.aft.w$dist)  
head(survprob.actual, n = 10)
```

```
[1] 0.9285822 0.8389085 0.6315234 0.8073231 0.6173609  
[6] 0.7312118 0.9260438 0.7203354 0.5891529 0.7143008
```

# Predict survival probability at 10 weeks:

```
survprob.10wk = 1 - psurvreg(10,  
  mean = predict(recid.aft.w, type = "lp"),  
  scale = recid.aft.w$scale,  
  distribution = recid.aft.w$dist)  
head(survprob.10wk)
```

```
[1] 0.9723202 0.9198457 0.8803901 0.9789527 0.9531961  
[6] 0.9693657
```

# Predict Change in Event time

How much of an impact do we think there would be if we gave those individuals who did NOT have financial aid financial aid? We can use the tools that we just learned to explore this idea...

We will assume the “quantile” they fell on is still the same quantile, but we will use a new “linear predictor” (with financial aid =1)

```
new_time = qsurvreg(1 - survprob.actual,  
  mean = predict(recid.aft.w, type = "lp") +  
  coef(recid.aft.w)['fin'],  
  scale = recid.aft.w$scale,  
  distribution = recid.aft.w$dist)
```

# Predict Change in Event time

Now save new predict time to data set and find difference

Subset to only look at those that did NOT have financial to start!

```
recid$new_time = new_time  
recid$diff = recid$new_time - recid$week  
  
impact.fin=data.frame(recid$week, recid$new_time,  
recid$diff,recid$arrest,recid$fin)  
colnames(impact.fin)=c("O.Week","N.Week","Diff","Arrest","F  
in")  
impact.fin2=subset(impact.fin,Arrest==1 & Fin==0)  
head(impact.fin2)
```

# Output

|    | O.Week | N.Week   | Diff      | Arrest | Fin |
|----|--------|----------|-----------|--------|-----|
| 1  | 20     | 25.66776 | 5.667764  | 1      | 0   |
| 2  | 17     | 21.81760 | 4.817600  | 1      | 0   |
| 3  | 25     | 32.08471 | 7.084706  | 1      | 0   |
| 7  | 23     | 29.51793 | 6.517929  | 1      | 0   |
| 13 | 37     | 47.48536 | 10.485364 | 1      | 0   |
| 15 | 25     | 32.08471 | 7.084706  | 1      | 0   |