

"Success is not final; failure is not fatal: It is the courage to continue that counts." — Winston S. Churchill

ARMA

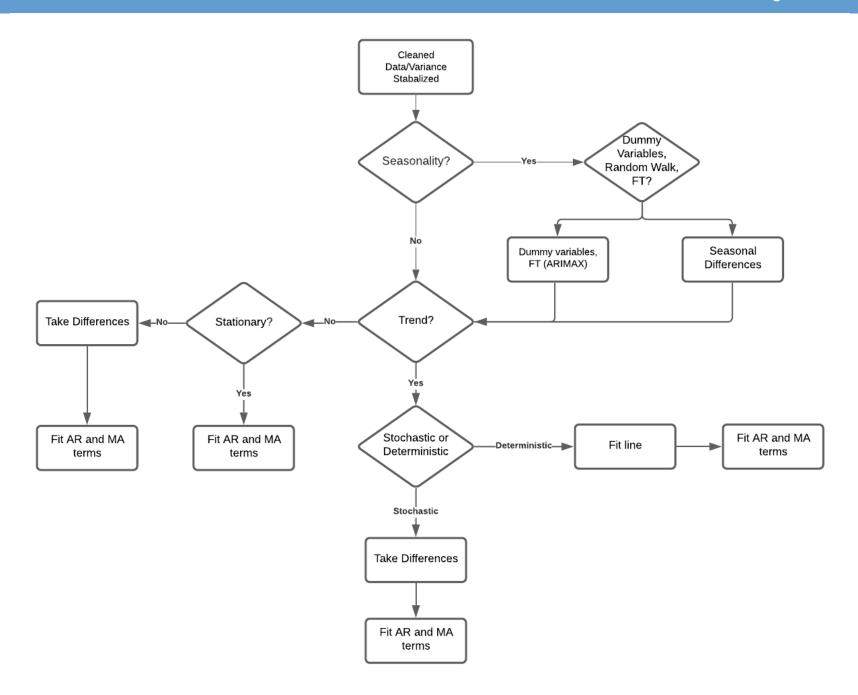
ARMA

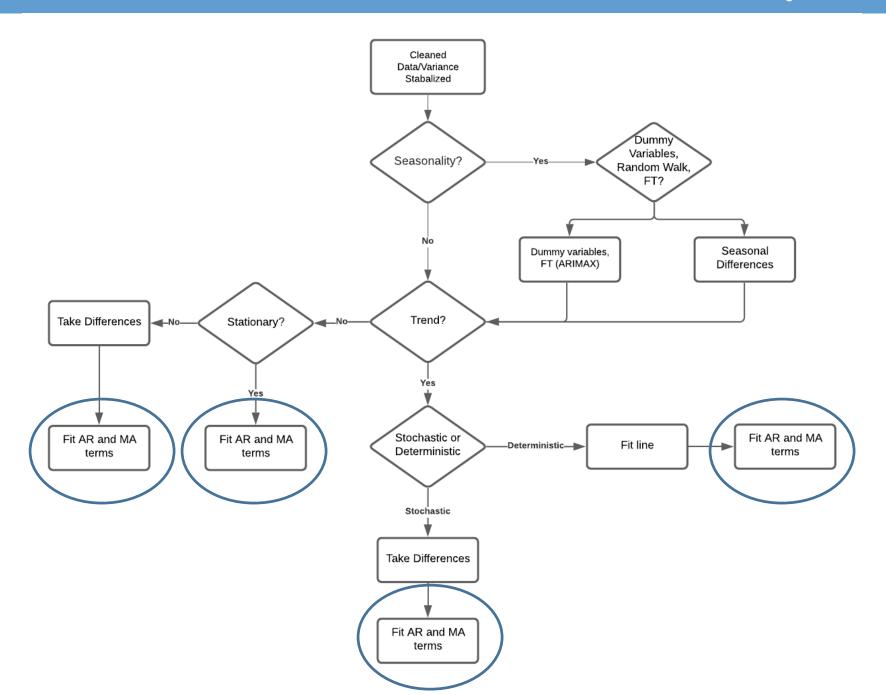
- ARMA stands for AutoRegressive Moving Averages (AR and MA terms are used to model the dependency structure in the data!)
- ARMA models are based upon statistical methods (will assume a distribution!!)
- When creating ARMA models, it can be a circular process (when changing something later in a model might make you reevaluate what you did earlier)
- Best model will be found by an iterative process!!

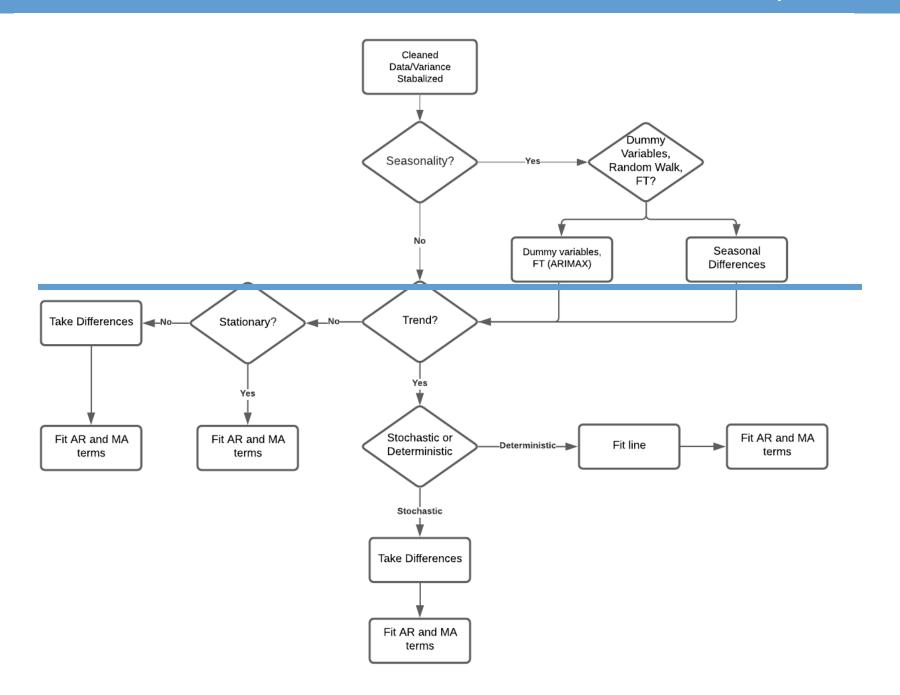
ARMA

SIGNAL:

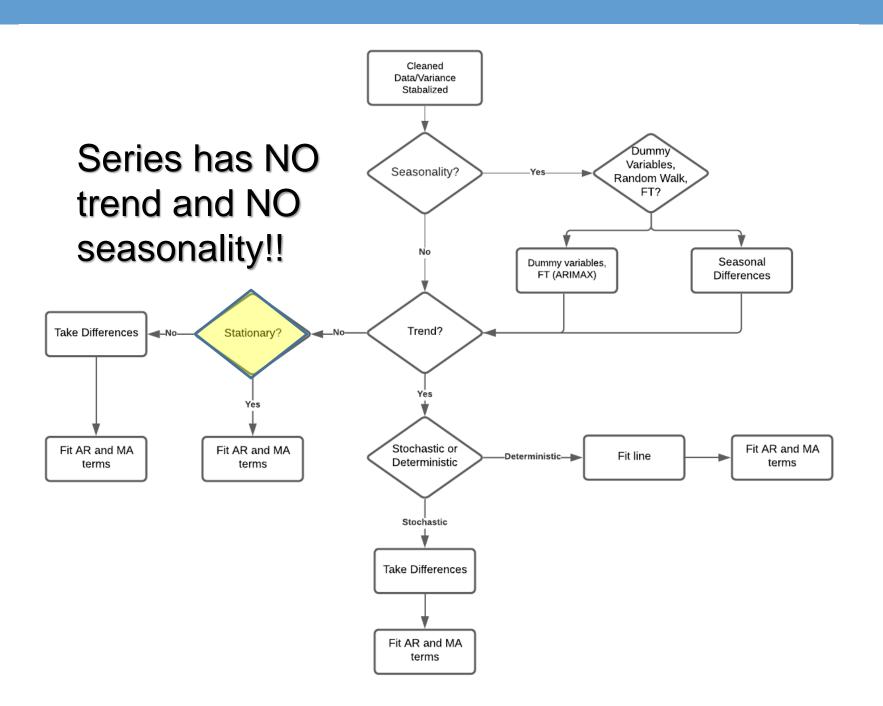
- Can have signal due to a seasonal pattern (will be discussed in Fall 2)
- Can have signal due to trend (we will discuss later in this class)
- Can have signal due to "correlation structure" which can be in the form of Autoregressive (AR) and moving averages (MA)
 - However, in order to model the dependency in the data appropriately, we will need to take care of the *functional form* (for example trend and/or seasonality) and any random walks first
 - After accounting for the above information, we can then begin modeling the dependency structure in the data





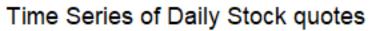


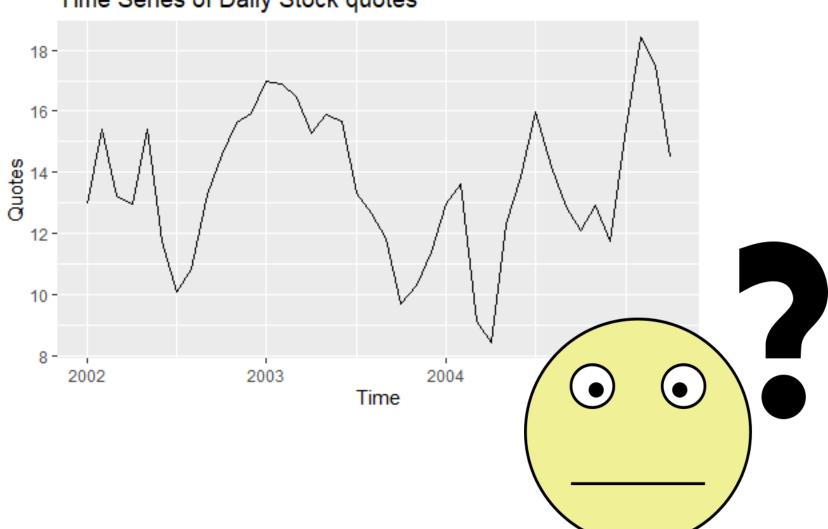
NO SEASON AND NO TREND (START SIMPLE....)



Stationarity

- To model the AR and MA terms, we must have stationarity first
- We will be using the idea of "weak stationarity" for modeling
 - No predictable pattern, constant variance and converges to a constant mean in the "long run"





What is a 'Random Walk'?

Random Walk Model

Random Walk Model:

$$Y_t = Y_{t-1} + e_t$$

Random Walk Model

 There are two types of random walk models (random walk with drift and random walk without drift):



Best guess for Y_t is Y_{t-1} . Best guess for Y_{t-1} is Y_{t-2} ...etc

Stochastic Trend: Differencing

General Model with Stochastic Trend:

$$Y_t - Y_{t-1} = \varepsilon_t$$

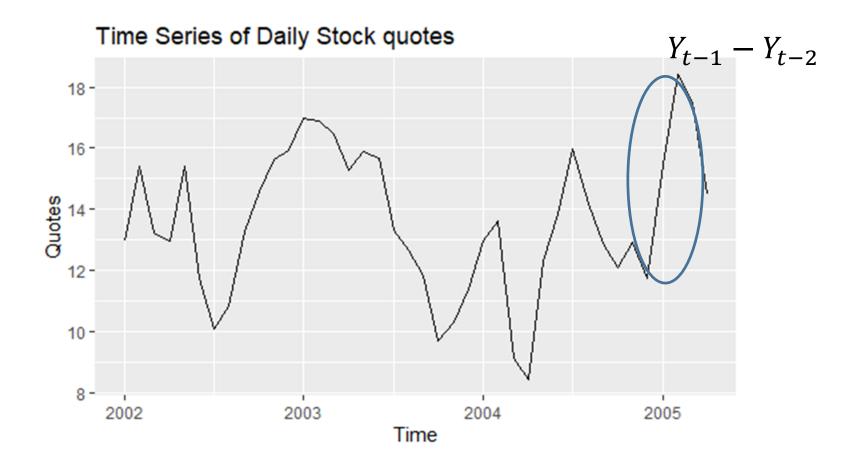
Patterns may exist in the differences!

 Therefore, if a random walk exists, need to take difference of series

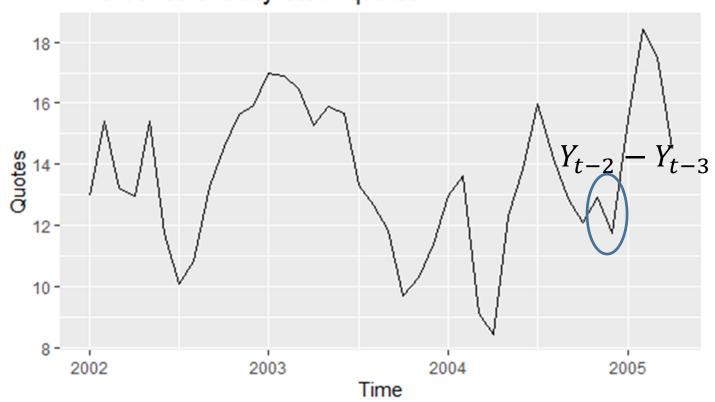


Time

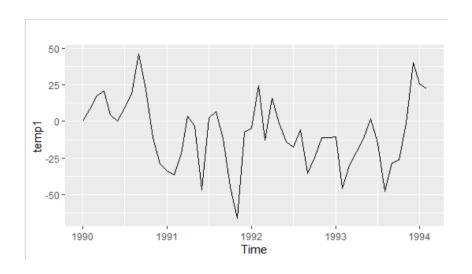
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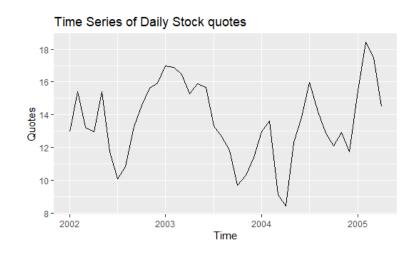


Time Series of Daily Stock quotes



Example of two series (one with Random walk)





How do we know if we have a Random Walk or not?

UNIT ROOT TESTING

The Augmented Dickey-Fuller Unit Root Test

- This test provides a statistical test for detecting a random walk.
- The null hypothesis is that differencing is required (nonstationary data).
- The alternative hypothesis:
 - Stationary mean about Zero (this is the test you will use if the series is centered about 0)
 - 2. Stationary Mean

The Dickey-Fuller Test

Null Hypothesis:

Non-stationary! i.e.....Random Walk

Alternative Hypothesis:

Stationary around 0 or mean (need to decide which test you are using based on the series)

Augmented Dickey-Fuller (ADF) Test

• It is called a "Unit Root Test" because it looks to see if the equation with the differenced series has a unit root ($\phi = 1....$ null hypothesis)

$$Y_t = \phi Y_{t-1} + e_t$$

- Unit roots can exist models with more than one lag of Y.
- Lag 0 tests are equivalent to what we have previously seen.
- Lag 1 tests consider models with differenced series of Y and first lag of differenced series.
- Lag 2 tests consider models with differenced series of Y and first and second lag of differenced series.

Augmented Dickey-Fuller Testing – R

```
# Augmented Dickey-Fuller Testing # aTSA::adf.test(Quotes.ts)
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can also use ndiffs(Quotes.ts)...but be careful with this!!

Augmented Dickey-Fuller Test alternative: stationary

ZERO MEAN

Type 1: no drift no trend lag ADF p.value

[1,] 0 -0.3061 0.550

[2,] 1-0.5980 0.458

[3,] 2-0.0632 0.620

[4,] 3-0.0950 0.611

SINGLE MEAN

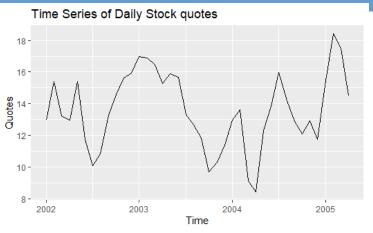
Type 2: with drift no trend lag ADF p.value

[1,] 0 -2.66 0.0939

[2,] 1-3.42 0.0192

[3,] 2 -2.45 0.1608

[4,] 3-2.36 0.1943



Type 3: with drift and trend lag ADF p.value

[1,] 0 -2.62 0.3212

[2,] 1 -3.36 0.0772

[3,] 2-2.41 0.4012

[4,] 3 -2.29 0.4463

Note: in fact, p.value = 0.01 means p.value <= 0.01

ADF test:

- First decide if you are doing the Zero Mean or Single Mean test (will talk about drift with trend in a few classes)
- Decide how many lags you would like to look at (commonly done in industry is between 3-5 lags)
- See if you reject ANY of these hypotheses!!
- If you reject all hypotheses (i.e. feel confident that this is a stationary time series), then you are ready to start modeling AR and MA terms.
- If you reject at least one, you have a random walk and will take differences and start modeling AR and MA terms on the differences.

Over-differencing

- When you difference and you don't need to difference, or you take too many differences, you will create the problem of over-differencing.
- This introduces more dependence on error terms in your model (creation of moving average terms that don't really exist).