DIAGNOSTICS & SUBSET SELECTION

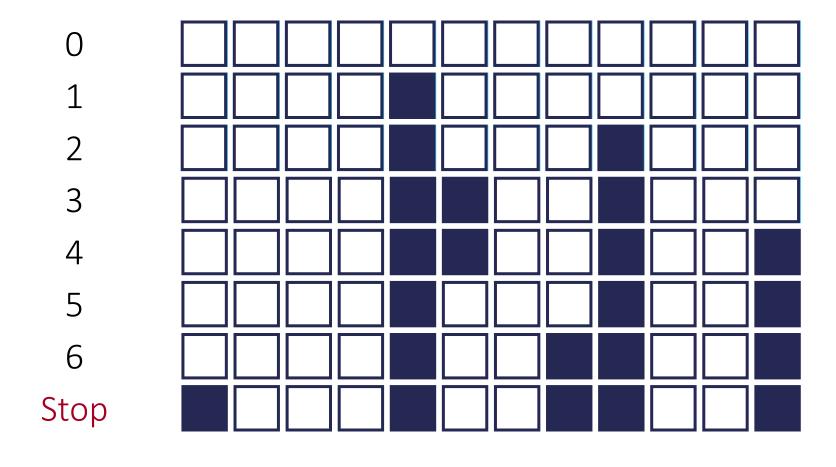
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Institute for Advanced Analytics

SUBSET SELECTION METHODS

Ames Real Estate Data

- 2930 homes in Ames, Iowa in the early 2000's.
- Physical attributes of homes along with sales price of home.





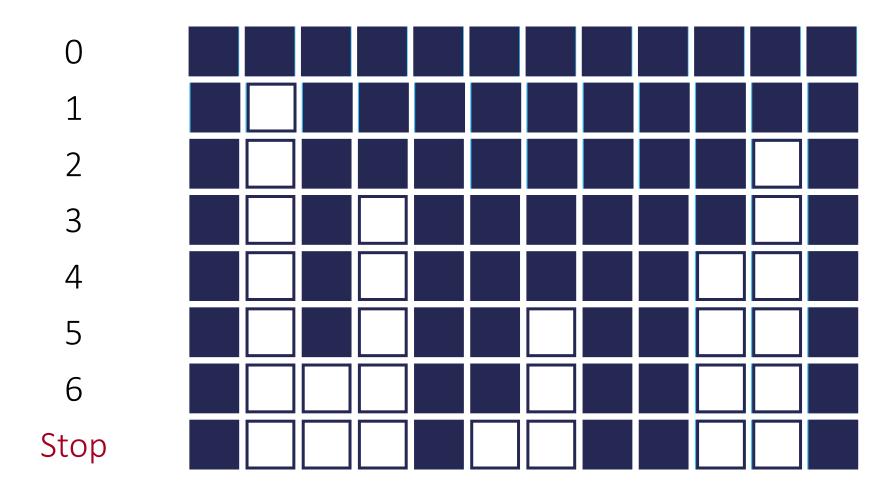
```
full.model <- glm (Bonus ~ Gr Liv Area + factor (House Style) + Garage Area +
                          Fireplaces + factor(Full Bath) + factor(Half Bath) +
                          Lot Area + factor(Central Air) + Second Flr SF +
                          TotRms AbvGrd + First Flr SF,
                  data = train, family = binomial(link = "logit"))
empty.model <- glm(Bonus ~ 1,
                   data = train, family = binomial(link = "logit"))
step.model <- step(empty.model,</pre>
                   scope = list(lower=formula(empty.model),
                                upper=formula(full.model)),
                   direction = "both")
```

```
Start: AIC=2777.81
Bonus ~ 1
```

Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept)
                                 -1.041e+01 1.537e+00 -6.775 1.24e-11 ***
                                 -6.860e-01 1.325e+00 -0.518 0.60469
factor(Full Bath)1
factor(Full Bath)2
                                 1.894e+00 1.341e+00 1.412 0.15785
                                 4.152e+00 1.610e+00 2.579 0.00991 **
factor(Full Bath)3
factor (Full Bath) 4
                                 -1.261e+00 2.493e+00 -0.506 0.61305
                                  3.583e-03 5.187e-04 6.907 4.96e-12 ***
Garage Area
                                 9.142e-01 1.272e-01 7.186 6.67e-13 ***
Fireplaces
                                  3.827e-03 4.033e-04 9.488 < 2e-16 ***
Gr Liv Area
factor (House Style) One and Half Unf -8.941e+00 3.682e+02 -0.024 0.98063
factor (House Style) One Story
                             2.396e+00 3.285e-01 7.295 2.99e-13 ***
factor (House Style) SFoyer
                        1.760e+00 6.382e-01 2.757 0.00583 **
                                  1.105e+00 4.530e-01 2.438 0.01476 *
factor(House Style)SLvl
factor (House Style) Two and Half Fin -4.855e-01 6.945e+00 -0.070 0.94427
factor (House Style) Two and Half Unf 8.329e-01 8.891e-01 0.937 0.34890
                             9.801e-01 3.380e-01 2.900 0.00373 **
factor (House Style) Two Story
                                 1.195e+00 2.153e-01 5.553 2.81e-08 ***
factor (Half Bath) 1
                                 -1.301e-01 8.053e-01 -0.162 0.87163
factor (Half Bath) 2
                                 -4.322e-01 8.128e-02 -5.317 1.05e-07 ***
TotRms AbvGrd
factor(Central Air)Y
                                 1.620e+00 5.866e-01 2.762 0.00575 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Backward Elimination



Backward Selection

Backward Selection

Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept)
                                  -1.028e+01 1.541e+00 -6.673 2.51e-11 ***
factor (House Style) One and Half Unf -9.208e+00 3.686e+02 -0.025 0.98007
factor (House Style) One Story
                             2.062e+00 4.945e-01 4.171 3.04e-05 ***
                               1.464e+00 7.213e-01 2.030 0.04234 *
factor (House Style) SFoyer
factor (House Style) SLvl
                        9.390e-01 4.891e-01
                                                        1.920 0.05489 .
factor (House Style) Two and Half Fin 1.085e+00 6.908e+00
                                                        0.157 0.87524
factor (House Style) Two and Half Unf 8.376e-01 8.904e-01 0.941 0.34687
factor(House Style) Two Story
                                 1.010e+00 3.498e-01 2.886 0.00390 **
                                  3.499e-03 5.210e-04 6.716 1.87e-11 ***
Garage Area
                                 8.965e-01 1.279e-01 7.010 2.39e-12 ***
Fireplaces
                                 -6.540e-01 1.330e+00 -0.492 0.62302
factor(Full Bath)1
                                 1.930e+00 1.347e+00 1.433 0.15196
factor(Full Bath) 2
                                 4.355e+00 1.618e+00 2.691 0.00712 **
factor(Full Bath) 3
factor (Full Bath) 4
                                 -1.073e+00 2.436e+00 -0.440 0.65971
factor(Half Bath)1
                               1.228e+00 2.215e-01 5.545 2.94e-08 ***
factor(Half Bath) 2
                                 -6.069e-02 8.103e-01 -0.075 0.94030
factor(Central Air)Y
                                 1.590e+00 5.909e-01 2.690 0.00715 **
                                 3.466e-03 6.632e-04 5.226 1.73e-07 ***
Second Flr SF
                                 -4.339e-01 8.142e-02 -5.329 9.86e-08 ***
TotRms AbvGrd
First Flr SF
                                  4.011e-03 4.351e-04 9.220 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Comparison of Backward with Stepwise

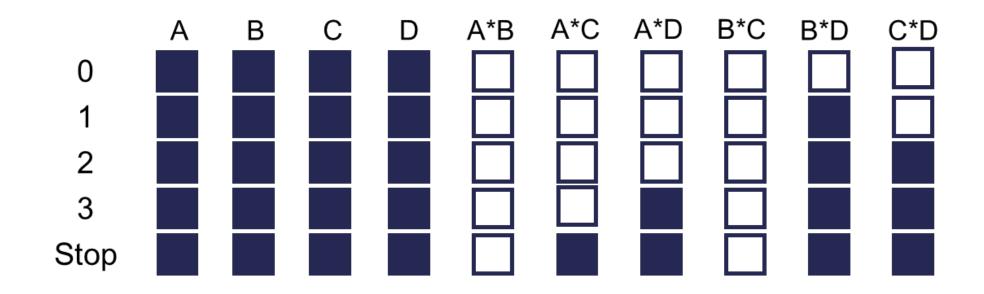
Stepwise Selection Variables

- Full Bath
- Garage Area
- Fireplaces
- Greater Living Area
- House Style
- Half Bath
- Total Rooms (Above Ground)
- Central Air

Backward Selection Variables

- Full Bath
- Garage Area
- Fireplaces
- House Style
- Half Bath
- Total Rooms (Above Ground)
- Central Air
- 1st Floor Sqft
- 2nd Floor Sqft

Interactions with Forward Selection





P-VALUE VS. AIC/BIC METRICS

- Lot of attention being given to p-values and how other selection techniques are better.
- Some of these are the same as p-values...

$$AIC = -2\log(L) + 2p$$

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$$AIC = -2\log(L) + 2p$$

Model better with lower AIC...

$$AIC_{p+1} < AIC_p$$

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$$AIC = -2\log(L) + 2p$$
Model better with lower AIC...
$$AIC_{p+1} < AIC_p$$

$$-2\log(L_{p+1}) + 2(p+1) < -2\log(L_p) + 2(p)$$

$$2 < 2(\log(L_{p+1}) - \log(L_p))$$

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$$AIC_{p+1} < AIC_{p}$$

$$-2\log(L_{p+1}) + 2(p+1) < -2\log(L_{p}) + 2(p)$$

$$2 < 2(\log(L_{p+1}) - \log(L_{p})) \text{ LRT}$$

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$$AIC = -2\log(L) + 2p$$
 Model better with lower AIC...
$$AIC_{p+1} < AIC_{p}$$

$$-2\log(L_{p+1}) + 2(p+1) < -2\log(L_{p}) + 2(p)$$

$$2 < \chi_1^2$$

- Lot of attention being given to p-values and how other selection techniques are better.
- Some of these are **the same as** p-values...

$$AIC = -2\log(L) + 2p$$

Model better with lower AIC...

$$AIC_{p+1} < AIC_p$$

$$-2\log(L_{p+1}) + 2(p+1) < -2\log(L_p) + 2(p)$$

$$2 < \chi_1^2$$

Model better with variable p-value below sig. level...

variable p-value
$$1 - P(\chi_1^2 > 2) = 0.1573$$

- Lot of attention being given to p-values and how other selection techniques are better.
- Some of these are the same as p-values...

$$BIC = -2\log(L) + p \times \log(n)$$

Model better with lower BIC...

$$BIC_{p+1} < BIC_p$$

$$-2\log(L_{p+1}) + \log(n)(p+1) < -2\log(L_p) + \log(n)(p)$$

$$\log(n) < \chi_1^2$$

Model better with variable p-value below sig. level...

variable p-value
$$1 - P(\chi_1^2 > \log(n)) = \cdots$$

 For our Ames housing data set, BIC selection is the same as the p-value selection with the following alpha:

$$1 - P(\chi_1^2 > \log(n)) = 1 - P(\chi_1^2 > \log(2051)) = 0.0057$$

- Lot of attention being given to p-values and how other selection techniques are better.
- Attention **should** be on significance level (α) , **not** on p-value.
- DON'T ALWAYS USE 0.05!



GOODNESS-OF-FIT

OPTIONAL: SELF-PACED STUDY

Calibration

- Calibration measures how well predicted probabilities agree with actual frequency counts of outcomes.
- Helps detect bias!
 - Are predictions systematically too low or too high?

Calibration Curve

- Curve above 45° line indicates the model is predicting lower probabilities than actually observed.
- Curve below 45° line indicates the model is predicting higher probabilities than actually observed.

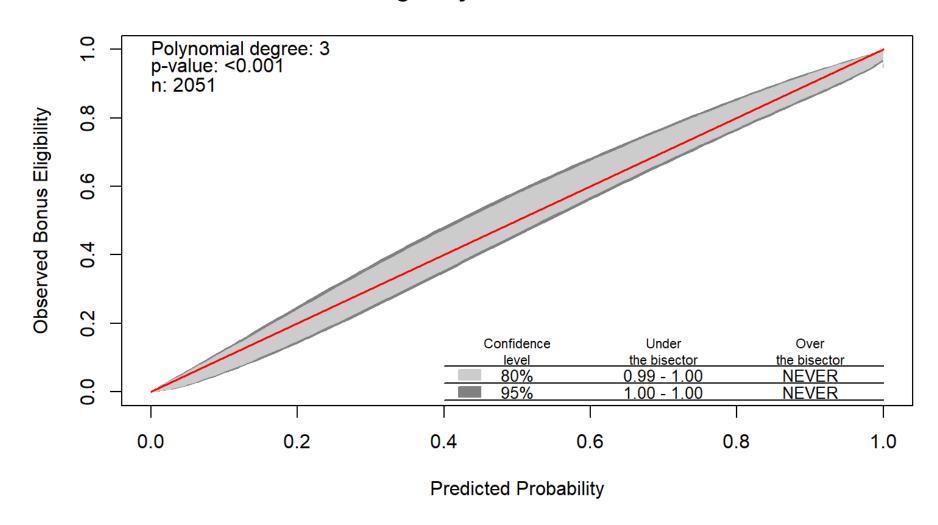
Caveat:

- Calibration depends on the observed proportion of events in the data, so models will likely have poor calibration on out-of-sample data.
- Best used for goodness-of-fit in training, not on validation.

Calibration Curve

Calibration Curve

Bonus Eligibility Model Calibration Curve



DIAGNOSTICS

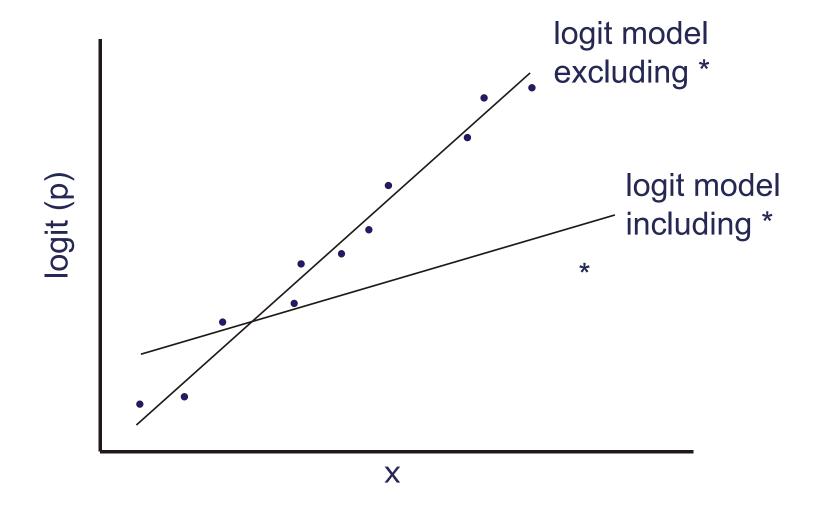
Residuals?

- Linear regression residuals have properties useful for model diagnostics.
- What is a residual in a binary response model?
- Many types of "residuals" in binary response model setting, just not as intuitive.
 - Deviance residuals
 - Partial residuals
 - Pearson residuals
 - Etc.

Deviance

- Model is a summary of a data set.
- The saturated model fits the data perfectly, but isn't really a useful summary.
- Deviance is a measure of how far a fitted model is from the saturated model essentially our "error."
- Logistic regression minimizes the sum of squared deviances!
- Deviance residuals tell us how much each observation reduces the deviance.

Influence Statistics



Influence Statistics

- DIFDEV
 - Measures change in deviance with deletion of the observation.
- DIFCHISQ
 - Measures change in Pearson Chi-square with deletion of observation.
- DFBETAS
 - Measure standardized change in each parameter estimate with deletion of observation.
- Cook's D
 - Measures the overall impact to the coefficients in the model.

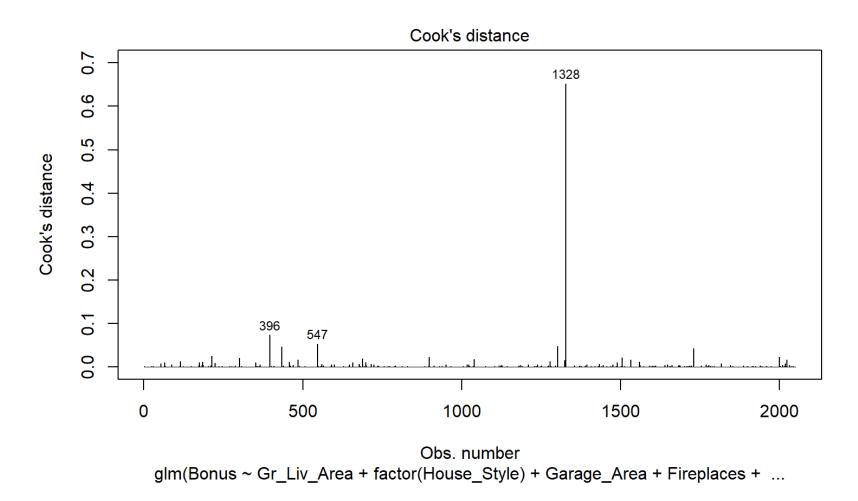
Diagnostics

Prints out metrics previously listed for every observation!

Output not shown here.

Diagnostics

plot(logit.model, 4)



Diagnostics

