tmvar, x, y, f, m, n variables

covar, c coercion variables

 $\begin{array}{c} datacon, \ K \\ const, \ T, \ F \end{array}$ 

index, i indices

```
relflag, \rho
                                                                                                                                                 relevance flag
                                                             ::=
                                                                       +
                                                                                                                         S
                                                                       app_rho \nu
                                                                                                                         S
                                                                       (\rho)
                                                                                                                                                 applicative flag
appflag, \ \nu
                                                             ::=
                                                                       R
                                                                       \rho
role, R
                                                                                                                                                 Role
                                                             ::=
                                                                       \mathbf{Nom}
                                                                       Rep
                                                                                                                         S
                                                                       R_1 \cap R_2
                                                                                                                         S
                                                                       \mathbf{param}\,R_1\,R_2
                                                                                                                         S
                                                                       \mathbf{app\_role}\,\nu
                                                                                                                         S
                                                                       (R)
constraint, \phi
                                                             ::=
                                                                                                                                                 props
                                                                       a \sim_{A/R} b
                                                                                                                         S
                                                                       (\phi)
                                                                                                                         S
                                                                       \phi\{b/x\}
                                                                                                                         S
                                                                       |\phi|
                                                                                                                         S
                                                                       a \sim_R b
                                                                                                                                                 types and kinds
tm, a, b, p, v, w, A, B, C
                                                                       \boldsymbol{x}
                                                                       \lambda^{\rho}x:A.b
                                                                                                                         \mathsf{bind}\ x\ \mathsf{in}\ b
                                                                       \lambda^{\rho}x.b
                                                                                                                         \mathsf{bind}\ x\ \mathsf{in}\ b
                                                                       a b^{\nu}
                                                                       \Pi^{\rho}x:A\to B
                                                                                                                         \mathsf{bind}\ x\ \mathsf{in}\ B
                                                                       \Lambda c : \phi . b
                                                                                                                         bind c in b
                                                                                                                         \mathsf{bind}\ c\ \mathsf{in}\ b
                                                                       \Lambda c.b
                                                                       a[\gamma]
                                                                                                                         \mathsf{bind}\ c\ \mathsf{in}\ B
                                                                       \forall c : \phi.B
                                                                       a \triangleright_R \gamma
                                                                       F
                                                                       \mathsf{case}_R \ a \ \mathsf{of} \ F 	o b_1 \|_{\scriptscriptstyle{-}} 	o b_2
                                                                       \mathbf{match}\ a\ \mathbf{with}\ brs
                                                                       \operatorname{\mathbf{sub}} R a
                                                                       a\{b/x\}
                                                                                                                         S
                                                                                                                         S
                                                                       a\{\gamma/c\}
                                                                                                                         S
                                                                       a\{b/x\}
                                                                                                                         S
                                                                       a\{\gamma/c\}
```

```
S
                           a
                                                            S
                           a
                                                            S
                           (a)
                                                             S
                                                                                         parsing precedence is hard
                                                             S
                           |a|_R
                                                             S
                           \mathbf{Int}
                                                            S
                           Bool
                                                            S
                           Nat
                                                            S
                           Vec
                                                             S
                           0
                                                             S
                           S
                           {\bf True}
                                                             S
                                                            S
                           Fix
                                                            S
                           Age
                                                             S
                           a \rightarrow b
                                                             S
                           \phi \Rightarrow A
                           a b
                                                             S
                                                            S
                           \lambda x.a
                                                             S
                           \lambda x : A.a
                           \forall\,x:A\to B
                                                             S
                           if \phi then a else b
                                                            S
                                                                                     case branches
brs
                  ::=
                           none
                           K \Rightarrow a; brs
                           brs\{a/x\}
                                                             S
                                                            S
                           brs\{\gamma/c\}
                                                             S
                           (brs)
co, \gamma
                                                                                    explicit coercions
                           \mathbf{red} \ a \ b
                           \mathbf{refl}\;a
                           (a \models \mid_{\gamma} b)
                           \mathbf{sym}\,\gamma
                           \gamma_1; \gamma_2
                           \mathbf{sub}\,\gamma
                           \Pi^{R,\rho}x\!:\!\gamma_1.\gamma_2
                                                             bind x in \gamma_2
                           \lambda^{R,\rho}x:\gamma_1.\gamma_2
                                                             bind x in \gamma_2
                           \gamma_1 \ \gamma_2^{R,\rho}
                           \mathbf{piFst}\,\gamma
                           \mathbf{cpiFst}\,\gamma
                           \mathbf{isoSnd}\,\gamma
                           \gamma_1@\gamma_2
                           \forall c: \gamma_1.\gamma_3
                                                            bind c in \gamma_3
```

```
\lambda c: \gamma_1.\gamma_3@\gamma_4
                                                                                  bind c in \gamma_3
                                              \gamma(\gamma_1,\gamma_2)
                                              \gamma@(\gamma_1 \sim \gamma_2)
                                              \gamma_1 \triangleright_R \gamma_2
                                              \gamma_1 \sim_A \gamma_2
                                              conv \phi_1 \sim_{\gamma} \phi_2
                                              \mathbf{eta}\,a
                                              left \gamma \gamma'
                                              right \gamma \gamma'
                                                                                  S
                                              (\gamma)
                                                                                  S
                                              \gamma
                                              \gamma\{a/x\}
                                                                                  S
role\_context, \ \Omega
                                                                                                           {\rm role}_contexts
                                               Ø
                                              x:R
                                              \Omega, x: R
                                              \Omega, \Omega'
                                                                                  Μ
                                              \mathbf{var}_{-}\mathbf{pat}\;p
                                                                                  Μ
                                              (\Omega)
                                                                                  Μ
                                              \Omega
                                                                                  Μ
roles,\ Rs
                                    ::=
                                              \mathbf{nil}\mathbf{R}
                                               R, Rs
                                                                                  S
                                              \mathbf{range}\,\Omega
                                                                                                           signature classifier
sig\_sort
                                    ::=
                                               A@Rs
                                               p \sim a : A/R@Rs
sort
                                    ::=
                                                                                                           binding classifier
                                              \operatorname{\mathbf{Tm}} A
                                               \mathbf{Co}\,\phi
context, \Gamma
                                    ::=
                                                                                                           contexts
                                              Ø
                                              \Gamma, x : A
                                              \Gamma, c: \phi
                                              \Gamma\{b/x\}
                                                                                  Μ
                                              \Gamma\{\gamma/c\}
                                                                                  Μ
                                              \Gamma, \Gamma'
                                                                                  Μ
                                              |\Gamma|
                                                                                  Μ
                                              (\Gamma)
                                                                                  Μ
                                              Γ
                                                                                  Μ
sig, \Sigma
                                                                                                           signatures
                                    ::=
```

```
\Sigma \cup \{F: sig\_sort\}
                                            \Sigma_0
                                                                            M
                                            \Sigma_1
                                                                            Μ
                                             |\Sigma|
                                                                            Μ
available\_props, \ \Delta
                                             Ø
                                            \Delta, x
                                            \Delta, c
                                            \mathsf{fv}\, a
                                                                            Μ
                                            \Delta, \Delta'
                                                                            Μ
                                                                            Μ
                                            \widetilde{\Omega}
                                                                            Μ
                                            (\Delta)
                                                                            Μ
Nat, \mathbb{N}
                                    ::=
                                            |a|
                                                                            S
pattern\_arg
                                    ::=
                                                                                   Pattern arguments
                                            \backslash RelaR
                                             \backslash Irra
                                             \Coe\gamma
pattern\_args,\ PA
                                            none
                                            PA, pattern\_arg
terminals
                                             \leftrightarrow
                                             \Leftrightarrow
                                            min
                                            \in
                                            \dashv
```

 $\models$ 

```
\models
                                              \neq
                                               ok
                                              Ø
                                              fv
                                              dom
                                              \sim
                                              \simeq
                                              \mathbf{fst}
                                              \operatorname{snd}
                                              \mathbf{a}\mathbf{s}
                                              |\Rightarrow|
                                              \vdash_=
                                              \operatorname{refl}_2
                                              ++
                                               {
}
formula, \psi
                                              judgement
                                              x:A\in\Gamma
                                              x:R\,\in\,\Omega
                                              c:\phi\in\Gamma
                                              F: sig\_sort \, \in \, \Sigma
                                              x \in \Delta
                                              c\,\in\,\Delta
                                              c \, \mathbf{not} \, \mathbf{relevant} \, \in \, \gamma
                                              x \not\in \Delta
                                              \mathit{uniq}\;\Gamma
                                              uniq(\Omega)
                                              c \not\in \Delta
                                               T \not \in \operatorname{dom} \Sigma
                                              F \not\in \operatorname{dom} \Sigma
                                              \mathbb{N}_1 < \mathbb{N}_2
\mathbb{N}_1 \le \mathbb{N}_2
                                              \nu = \rho
                                              R_1 = R_2
                                              a = b
```

```
\phi_1 = \phi_2
                                     \Gamma_1 = \Gamma_2
                                     \psi_1 \wedge \psi_2
                                     \psi_1 \vee \psi_2
                                     \psi_1 \Rightarrow \psi_2
                                     (\psi)
                                     c:(a:A\sim b:B)\in\Gamma
                                                                                                   suppress lc hypothesis gen
JSubRole
                               ::=
                                     R_1 \leq R_2
                                                                                                   Subroling judgement
JPath
                                     Path a = F@Rs
                                                                                                   Type headed by constant
JPatCtx
                                     \Omega; \Gamma \vDash p :_F B \Rightarrow A
                                                                                                   Contexts generated by a p
JRename
                               ::=
                                     rename p \to a to p' \to a' excluding \Delta and \Delta'
                                                                                                   rename with fresh variable
JMatchSubst
                               ::=
                                     match a_1 with p \rightarrow b_1 = b_2
                                                                                                   match and substitute
JPatData
                               ::=
                                     uncurry p = F@PA
                                                                                                   Pattern data (head argun
JIsPattern
                               ::=
                                     pattern p
JSubPat
                                     subpattern p' p
                                                                                                   Subpattern
JTmPatternAgree
                                                                                                   term and pattern agree
                                     a \leftrightarrow p
JTmSubPatternAgree
                                     a \sqsubseteq p
                                                                                                   sub-pattern agrees with te
JSub\,TmPatternAgree
                                     a \sqsubseteq p
                                                                                                   sub-term agrees with patt
JValuePath
```

Type headed by constant

 $\mathsf{ValuePath}\ a = F$ 

JCasePath	$::= \\    CasePath_R \ a = F$	Type headed by constant (role-sensitive part
JApplyArgs	$ ::= \\    \text{apply args } a \text{ to } b \mapsto b' $	apply arguments of a (headed by a constant
JValue	$::=$ $ $ Value $_R$ $A$	values
JValueType	$::= \\    ValueType_R \ A$	Types with head forms (erased language)
J consistent	$::=$ $\mid$ consistent $_R \ a \ b$	(erased) types do not differ in their heads
Jroleing	$::= \\    \Omega \vDash a : R$	Roleing judgment
JChk	$::= \\   (\rho = +) \lor (x \not\in fv\ A)$	irrelevant argument check
Jpar	$ \Box = \\    \Omega \vDash a \Rightarrow_R b \\    \Omega \vDash a \Rightarrow_R^* b \\    \Omega \vDash a \Leftrightarrow_R b $	parallel reduction (implicit language) multistep parallel reduction parallel reduction to a common term
$\it Jbeta$	::=	primitive reductions on erased terms single-step head reduction for implicit langu multistep reduction
JB ranch Typing	$ ::= \\ \mid  \Gamma \vDash case_R \ a : A \ of \ b : B \Rightarrow C \mid C' $	Branch Typing (aligning the types of case)
Jett	$ \begin{aligned} & ::= \\ & \mid  \Gamma \vDash \phi \   \text{ok} \\ & \mid  \Gamma \vDash a : A \\ & \mid  \Gamma; \Delta \vDash \phi_1 \equiv \phi_2 \\ & \mid  \Gamma; \Delta \vDash a \equiv b : A/R \\ & \mid  \vDash \Gamma \end{aligned} $	Prop wellformedness typing prop equality definitional equality context wellformedness
Jsig	$::= \\ \mid  \models \Sigma$	signature wellformedness
Jann		prop wellformedness typing

		$\Gamma; \Delta \vdash \gamma : \phi_1 \sim \phi_2$ $\Gamma; \Delta \vdash \gamma : A \sim_R B$ $\vdash \Gamma$
Jred	::=	$\Gamma \vdash a \leadsto b/R$
judgement		JSubRole JPath JPatCtx JRename JMatchSubst JPatData JIsPattern JSubPat JTmPatternAgree JTmSubPatternAgree JSubTmPatternAgree JValuePath JCasePath JApplyArgs JValue JValueType Jconsistent Jroleing JChk Jpar Jbeta JBranchTyping Jett Jsig Jann Jred
$user\_syntax$	::=	tmvar covar datacon const index
		relflag $appflag$ $role$ $constraint$ $tm$

brs

9

coercion between props coercion between types context wellformedness

single-step, weak head reduction to values for annotated la

| co | role\_context | roles | sig\_sort | sort | context | sig | available\_props | Nat | pattern\_arg | pattern\_args | terminals | formula

## $R_1 \leq R_2$ Subroling judgement

$$\overline{\text{Nom} \leq R}$$
 NomBot
 $\overline{R \leq \text{Rep}}$  Reptop
 $\overline{R \leq R}$  Refl
 $R_1 \leq R_2$ 
 $\overline{R_2 \leq R_3}$ 
 $\overline{R_1 \leq R_3}$  Trans

Path a = F@Rs Type headed by constant (partial function)

$$F:A@Rs \in \Sigma_0 \\ \hline Path \ F = F@Rs \\ \hline Path \ a = F@R_1, Rs \\ \hline Path \ (a \ b'^{R_1}) = F@Rs \\ \hline \hline Path \ a = F@Rs \\ \hline Path \ (a \ \Box^-) = F@Rs \\ \hline \hline Path \ a = F@Rs \\ \hline Path \ (a \ \Box^-) = F@Rs \\ \hline \hline Path \ (a \ \Box^-) = F@Rs \\ \hline \hline Path \ (a \ \Box^-) = F@Rs \\ \hline Path \ (a \ \Box^-) = F@Rs \\ \hline \hline \ Path \ (a \ \Box^-) = F@Rs \\ \hline \ Path \ (a \ \Box^-)$$

 $\Omega; \Gamma \vDash p :_F B \Rightarrow A$  Contexts generated by a pattern (variables bound by the pattern)

```
rename p \to a to p' \to a' excluding \Delta and \Delta'
                                                                                     rename with fresh variables
                                                                                                                 RENAME_BASE
                             rename F \to a to F \to a excluding \Delta and \varnothing
                        rename p_1 
ightarrow a_1 to p_2 
ightarrow a_2 excluding \Delta and \Delta'
   \frac{y \not\in (\Delta,\Delta')}{\mathsf{rename}\ (p_1\ x^R) \to a_1\ \mathsf{to}\ (p_2\ y^R) \to (a_2\{y/x\})\ \mathsf{excluding}\ \Delta\ \mathsf{and}\ (\Delta',y)}
                                                                                                                                     RENAME_APPREL
           rename p_1 \to a_1 to p_2 \to a_2 excluding \Delta and \Delta' rename (p_1 \square^-) \to a_1 to (p_2 \square^-) \to a_2 excluding \Delta and \Delta'
                                                                                                                          Rename_AppIrrel
                  \frac{\text{rename }p_1\to a_1\text{ to }p_2\to a_2\text{ excluding }\Delta\text{ and }\Delta'}{\text{rename }(p_1[\bullet])\to a_1\text{ to }(p_2[\bullet])\to a_2\text{ excluding }\Delta\text{ and }\Delta'}
                                                                                                                           RENAME_CAPP
match a_1 with p \to b_1 = b_2 match and substitute
                                                                                       MatchSubst_Const
                                        \overline{\mathsf{match}\ F\ \mathsf{with}\ F\to b=b}
                  \frac{\text{match }a_1 \text{ with }p_1 \to b_1 = b_2}{\text{match }(a_1 \ a^R) \text{ with }(p_1 \ x^R) \to b_1 = (b_2 \{a/x\})} \quad \text{MATCHSUBST\_APPRELR}
                         \frac{\text{match }a_1 \text{ with }p_1 \to b_1 = b_2}{\text{match }(a_1 \ a^-) \text{ with }(p_1 \ \Box^-) \to b_1 = b_2} \quad \text{MATCHSubst\_AppIrrel}
                               \frac{\text{match } a_1 \text{ with } a_2 \to b_1 = b_2}{\text{match } (a_1[\bullet]) \text{ with } (a_2[\bullet]) \to b_1 = b_2} \quad \text{MATCHSUBST\_CAPP}
uncurry p = F@PA Pattern data (head arguments)
                                                                                            PatData_Head
                                              \overline{\mathbf{uncurry}\,F = F@\mathbf{none}}
                                                  uncurry p = F@PA
                                                                                                         PATDATA_REL
                                     \overline{\mathbf{uncurry}\,(p\ a^R) = F@PA, \backslash Rel\,a\,R}
pattern p
                                                                                 PATTERN_HEAD
                                                          \overline{\operatorname{pattern} F}
                                                            \mathbf{pattern}\ p
                                                                                     Pattern_Rel
                                                       \overline{\mathbf{pattern}\left(p\ a^R\right)}
                                                            \mathbf{pattern}\ p
                                                                                      Pattern_Irr
                                                       \overline{\mathbf{pattern}(p \ a^{-})}
                                                        \frac{\mathbf{pattern}\:p}{\mathbf{pattern}\:(p[\gamma])}
                                                                                      Pattern_Coe
subpattern p'p
                                    Subpattern
                                                       \frac{\mathbf{pattern}\,p}{\mathbf{subpattern}\,p\,p}\quad \mathsf{SubPat\_RefL}
                                                   \frac{\mathbf{subpattern} \ p' \ p}{\mathbf{subpattern} \ p' \ (p \ x^R)}
                                                                                              SubPat_Rel
                                                   \frac{\mathbf{subpattern}\,p'\,p}{\mathbf{subpattern}\,p'\,(p\ \Box^-)}
                                                                                             SubPat_Irr
```

# $\frac{\mathbf{subpattern}\,p'\,p}{\mathbf{subpattern}\,p'\left(p[\bullet]\right)}\quad \mathsf{SUBPAT\_COE}$

 $a \leftrightarrow p$  term and pattern agree

 $a \sqsubseteq p$  sub-pattern agrees with term

$$\frac{a \leftrightarrow p}{a \sqsubseteq p} \qquad \text{TM\_SUBPATTERN\_AGREE\_BASE}$$
 
$$\frac{a \sqsubseteq p}{a \sqsubseteq (p \ x^R)} \qquad \text{TM\_SUBPATTERN\_AGREE\_APPRELR}$$
 
$$\frac{a \sqsubseteq p}{a \sqsubseteq (p \ \Box^-)} \qquad \text{TM\_SUBPATTERN\_AGREE\_APPIRREL}$$
 
$$\frac{a \sqsubseteq p}{a \sqsubseteq (p [\bullet])} \qquad \text{TM\_SUBPATTERN\_AGREE\_CAPPP}$$

 $a \supseteq p$  sub-term agrees with pattern

$$\frac{a \leftrightarrow p}{a \sqsupseteq p} \quad \text{SUBTM\_PATTERN\_AGREE\_BASE}$$
 
$$\frac{a \sqsupseteq p}{a \ a_2^{\nu} \sqsupseteq p} \quad \text{SUBTM\_PATTERN\_AGREE\_APP}$$
 
$$\frac{a \sqsupseteq p}{a[\bullet] \sqsupseteq p} \quad \text{SUBTM\_PATTERN\_AGREE\_CAPPP}$$

ValuePath a = F Type headed by constant (role-sensitive partial function used in value)

$$\frac{F:A@Rs \in \Sigma_0}{\text{ValuePath } F = F} \qquad \text{ValuePath\_AbsConst}$$
 
$$F:p \sim a:A/R_1@Rs \in \Sigma_0 \\ \text{ValuePath } F = F \\ \text{ValuePath } a = F \\ \text{ValuePath } (a\ b'^{\nu}) = F \\ \text{ValuePath } a = F \\ \text{ValuePath } (a\ b^{\prime \nu}) = F \\ \text{ValuePath} (a\ b^{\prime \nu}) =$$

CasePath<sub>R</sub> a = F Type headed by constant (role-sensitive partial function used in case)

$$\begin{tabular}{lll} \mbox{ValuePath } a = F \\ \hline F: A@Rs \in \Sigma_0 \\ \hline \mbox{CasePath}_R \ a = F \end{tabular} \begin{tabular}{l} \mbox{CASEPATH\_ABSCONST} \\ \hline \end{tabular}$$

$$\begin{array}{c} \mathsf{ValuePath} \ a = F \\ F: p \sim b: A/R_1@Rs \in \Sigma_0 \\ \neg (R_1 \leq R) \end{array} \qquad \mathsf{CASEPATH\_CONST} \\ \hline \mathbf{CasePath}_R \ a = F \\ F: p \sim b: A/R_1@Rs \in \Sigma_0 \\ \neg (a \sqsupset p) \\ \hline \mathbf{CasePath}_R \ a = F \\ \hline \text{CasePath\_UNMATCH} \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \\ \hline \text{apply args } a \text{ to } b \mapsto b' \text{ operators} \\ \hline \text{Value}_R \ A^p \text{ Value\_STAR} \\ \hline \hline \text{Value}_R \ A^p \text{ Value\_PI} \\ \hline \hline \text{Value}_R \ \lambda^+ x : A . a \\ \hline \text{Value}_R \ \lambda^+ x : A . a \\ \hline \text{Value}_R \ \lambda^+ x : A . a \\ \hline \text{Value}_R \ \lambda^+ x : A . a \\ \hline \text{Value}_R \ \lambda^- x . a \\ \hline \text{Value}_R \ \lambda^- x . a \\ \hline \text{Value}_R \ \lambda^- x . a \\ \hline \text{Value}_R \ A c : \phi . a \\ \hline \text{Value}_R \ A c : \phi . a \\ \hline \text{Value\_CABS} \\ \hline \text{Value}_R \ a = F \\ \hline \text{Value}_R \ a = F \\ \hline \text{Value}_R \ b \Rightarrow F \\ \hline \text{Value}_R \ b \Rightarrow F \\ \hline \text{Value}_R \ a \Rightarrow F \\ \hline \text{Value}_R \$$

 $\underline{\text{consistent}_R \ a \ b}$  (erased) types do not differ in their heads

```
CONSISTENT_A_PI
                         \overline{\mathsf{consistent}_{R'} \; (\Pi^{\rho} x_1 \colon A_1 \to B_1) \; (\Pi^{\rho} x_2 \colon A_2 \to B_2)}
                                                                                                        CONSISTENT_A_CPI
                                 \overline{\mathsf{consistent}_R \; (\forall c_1 : \phi_1.A_1) \; (\forall c_2 : \phi_2.A_2)}
                                           \mathsf{CasePath}_R\ a_1 = F
                                           \mathsf{CasePath}_R\ a_2 = F
                                                                                 CONSISTENT_A_CASEPATH
                                             consistent_R a_1 a_2
                                                \neg ValueType_R b CONSISTENT_A_STEP_R
                                                \mathsf{consistent}_R \ a \ b
                                                \neg ValueType_R \ a consistent_A b CONSISTENT_A_STEP_L
|\Omega \vDash a : R|
                        Roleing judgment
                                                            \frac{uniq(\Omega)}{\Omega \vDash \square : R} \quad \text{ROLE\_A\_BULLET}
                                                               \frac{uniq(\Omega)}{\Omega \vDash \star : R} \quad \text{ROLE\_A\_STAR}
                                                               uniq(\Omega)
                                                               x:R\in\Omega
                                                              \frac{R \le R_1}{\Omega \vDash x : R_1} \quad \text{ROLE\_A\_VAR}
                                                      \frac{\Omega, x : \mathbf{Nom} \vDash a : R}{\Omega \vDash (\lambda^{\rho} x.a) : R} \quad \text{ROLE\_A\_ABS}
                                                            \Omega \vDash a : R
                                                           \frac{1}{\Omega \vDash (a \ b^{\rho}) : R} \quad \text{ROLE\_A\_APP}
                                                     \Omega \vDash a : R
                                                     Path a = F@R_1, Rs
                                                          \frac{\models b : R_1}{\Omega \models a \ b^{R_1} : R} ROLE_A_TAPP
                                                     \Omega \vDash b : R_1
                                                        \Omega \vDash A : R
                                                      \frac{\Omega, x: \mathbf{Nom} \vDash B: R}{\Omega \vDash (\Pi^{\rho}x: A \to B): R} \quad \text{ROLE\_A\_PI}
                                                               \Omega \vDash a : R_1
                                                               \Omega \vDash b : R_1
                                                               \Omega \vDash A : R_0
                                                               \Omega \vDash B:R
                                                                                                    role_a_CPi
                                                 \overline{\Omega \vDash (\forall c : a \sim_{A/R_1} b.B) : R}
                                                          \frac{\Omega \vDash b : R}{\Omega \vDash (\Lambda c.b) : R} \quad \text{ROLE\_A\_CABS}
                                                          \frac{\Omega \vDash a : R}{\Omega \vDash (a[\bullet]) : R} \quad \text{ROLE\_A\_CAPP}
```

$$\frac{uniq(\Omega)}{\Omega \vDash F: A@Rs \in \Sigma_0} \qquad \text{ROLE.A.CONST}$$

$$\frac{uniq(\Omega)}{P: P: R} \qquad \text{ROLE.A.CONST}$$

$$\frac{uniq(\Omega)}{P: P: R} \qquad \text{ROLE.A.FAM}$$

$$\frac{F: p \sim a: A/R@Rs \in \Sigma_0}{\Omega \vDash F: R_1} \qquad \text{ROLE.A.FAM}$$

$$\frac{\square \vDash a: R}{\square \vDash b: R_1} \qquad \text{ROLE.A.PATTERN}$$

$$\frac{\square \vDash a: R}{\square \vDash case_R \ a \ of \ F \rightarrow b_1 \parallel_- \rightarrow b_2 : R_1} \qquad \text{ROLE.A.PATTERN}$$

$$\frac{(\rho = +) \lor (x \not \in \text{fv} \ A)}{(- = +) \lor (x \not \in \text{fv} \ A)} \qquad \text{RHO.REL}$$

$$\frac{x \not \in \text{fv} \ A}{(- = +) \lor (x \not \in \text{fv} \ A)} \qquad \text{RHO.IRRREL}$$

$$\frac{\square \vDash a: R}{\square \vDash a \Rightarrow_R \ a} \qquad \text{PAR.REFL}$$

$$\frac{\square \vDash a: R}{\square \vDash a \Rightarrow_R \ a} \qquad \text{PAR.BETA}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash a \Rightarrow_R \ a' + b' \Rightarrow_R \ a' + b''} \qquad \text{PAR.APP}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash a \Rightarrow_R \ a' + b' \Rightarrow_R \ a' + b''} \qquad \text{PAR.CAPP}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash a \Rightarrow_R \ a'} \qquad \text{PAR.CAPP}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash A \Rightarrow_R \ a'} \qquad \text{PAR.ABS}$$

$$\frac{\square \vDash A \Rightarrow_R \ a'}{\square \vDash \Pi^p x: A \rightarrow B \Rightarrow_R \ \Pi^p x: A' \rightarrow B'} \qquad \text{PAR.PI}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Pi^p x: A \rightarrow B \Rightarrow_R \ \Pi^p x: A' \rightarrow B'} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Pi^p x: A \rightarrow B \Rightarrow_R \ \Pi^p x: A' \rightarrow B'} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

$$\frac{\square \vDash a \Rightarrow_R \ a'}{\square \vDash \Lambda^p \land A \Rightarrow_R \ A \land A} \qquad \text{PAR.CABS}$$

 $\frac{- \cdot A \mathcal{E}}{\Omega \vDash \forall c : a \sim_{A/R_1} b.B \Rightarrow_R \forall c : a' \sim_{A'/R_1} b'.B'} \quad \text{PAR\_CPI}$ 

 $\Omega \vDash B \Rightarrow_R B'$ 

$$F: F \sim b: A/R_1@Rs \in \Sigma_0$$

$$R_1 \leq R$$

$$umiq(\Omega)$$

$$Q \models F \Rightarrow_R b$$

$$F: p \sim b: A/R_1@Rs \in \Sigma_0$$

$$a \sqsubseteq p \land \neg (a \leftrightarrow p)$$

$$\Omega \models a \Rightarrow_R a'$$

$$\Omega \models a_1 \Rightarrow_{\text{capp role} \nu} a'_1$$
rename  $p \rightarrow b \text{ to } p' \rightarrow b' \text{ excluding } (\widetilde{\Omega}, \widehat{\text{fvp}}) \text{ and } \Delta'$ 

$$\text{match } (a' a'_1^{\nu}) \text{ with } p' \rightarrow b' = a_2$$

$$R_1 \leq R$$

$$\Omega \models a \Rightarrow_R a'$$

$$\Omega \models b_1 \Rightarrow_R b'$$

$$\Omega \models b_2 \Rightarrow_R b'$$

$$\Omega \models b_1 \Rightarrow_R$$

```
\models a > b/R
```

primitive reductions on erased terms

$$\frac{\mathsf{Value}_{R_1} \; (\lambda^{\rho} x. v)}{\vDash (\lambda^{\rho} x. v) \; b^{\rho} > v \{b/x\}/R_1} \quad \mathsf{Beta\_AppAbs}$$

$$= (\Lambda c.a')[\bullet] > a'\{\bullet/c\}/R$$
 BETA\_CAPPCABS

 $F: p \sim b: A/R_1@Rs \in \Sigma_0$ 

rename  $p \to b$  to  $p_1 \to b_1$  excluding (fva, fvp) and  $\Delta'$ 

match a with  $p_1 \rightarrow b_1 = b'$ 

$$\frac{R_1 \le R}{\models a > b'/R}$$

Beta\_Axiom

 $CasePath_R \ a = F$ 

 $\frac{\text{apply args } a \text{ to } b_1 \mapsto b_1'}{\models \mathsf{case}_R \ a \text{ of } F \to b_1 \parallel_{\text{-}} \to b_2 > b_1'[\bullet]/R_0} \quad \text{Beta\_PatternTrue}$ 

 $\frac{\neg(\mathsf{CasePath}_R\ a = F)}{\models \mathsf{case}_R\ a \text{ of } F \to b_1 \|_- \to b_2 > b_2/R_0} \quad \text{Beta\_PatternFalse}$ 

single-step head reduction for implicit language

$$\frac{\models a \leadsto a'/R_1}{\models \lambda^- x.a \leadsto \lambda^- x.a'/R_1} \quad \text{E\_ABSTERM}$$

$$\frac{\vDash a \leadsto a'/R_1}{\vDash a \ b^{\nu} \leadsto a' \ b^{\nu}/R_1} \quad \text{E\_Appleft}$$

$$\frac{\vDash a \leadsto a'/R}{\vDash a[\bullet] \leadsto a'[\bullet]/R} \quad \text{E\_CAPPLEFT}$$

$$\frac{\models a \leadsto a'/R}{\models \mathsf{case}_R \ a \ \mathsf{of} \ F \to b_1 \parallel_{-} \to b_2 \leadsto \mathsf{case}_R \ a' \ \mathsf{of} \ F \to b_1 \parallel_{-} \to b_2/R_0} \quad \text{E.1}$$

$$\frac{\models a > b/R}{\models a \leadsto b/R} \quad \text{E\_PRIM}$$

 $\vDash a \leadsto^* b/R$ multistep reduction

 $= a \leadsto^* a/R$  Equal

 $\Gamma \vDash \mathsf{case}_R \ a : A \ \mathsf{of} \ b : B \Rightarrow C \mid C'$ Branch Typing (aligning the types of case)

 $\frac{\texttt{lc\_tm}\ C}{\Gamma \vDash \mathsf{case}_R\ a : A \ \mathsf{of}\ b : A \Rightarrow \forall c \colon\! (a \sim_{A/R} b) . C \mid C}$ 

BranchTyping\_Base

 $\Gamma, x : A \vDash \mathsf{case}_R \ a : A_1 \ \mathsf{of} \ b \ x^+ : B \Rightarrow C \mid C'$ 

 $\Gamma \vDash \mathsf{case}_R \ a : A_1 \text{ of } b : \Pi^+ x : A \to B \Rightarrow \Pi^+ x : A \to C \mid C'$ 

 $BRANCHTYPING\_PIREL$ 

 $\frac{\Gamma, x: A \vDash \mathsf{case}_R \ a: A_1 \ \mathsf{of} \ b \ \Box^-: B \Rightarrow C \mid C'}{\Gamma \vDash \mathsf{case}_R \ a: A_1 \ \mathsf{of} \ b: \Pi^- x: A \to B \Rightarrow \Pi^- x: A \to C \mid C'}$ 

BranchTyping\_PiIrrel

$$\frac{\Gamma,\,c:\phi\vDash\mathsf{case}_R\;a:A\;\mathsf{of}\;b[\bullet]:B\Rightarrow C\;|\;C'}{\Gamma\vDash\mathsf{case}_R\;a:A\;\mathsf{of}\;b:\forall c\!:\!\phi.B\Rightarrow\forall c\!:\!\phi.C\;|\;C'}\quad\mathsf{BranchTyping\_CPi}$$

### $\Gamma \vDash \phi$ ok Prop wellformedness

$$\begin{split} & \Gamma \vDash a : A \\ & \Gamma \vDash b : A \\ & \frac{\Gamma \vDash A : \star}{\Gamma \vDash a \sim_{A/R} b \text{ ok}} \quad \text{E-Wff} \end{split}$$

#### $\Gamma \vDash a : A$ typing

$$\begin{array}{c} \models \Gamma \\ F:A@Rs \in \Sigma_0 \\ & \varnothing \vDash A:\star \\ \hline \Gamma \vDash F:A \end{array} \quad \text{E\_CONST} \\ \\ \stackrel{\models \Gamma}{F:p} \sim a:A/R_1@Rs \in \Sigma_0 \\ & \varnothing \vDash A:\star \\ \hline \Gamma \vDash F:A \end{array} \quad \text{E\_FAM} \\ \\ \Gamma \vDash A:\star \\ \hline \Gamma \vDash F:A \end{array} \quad \text{E\_FAM} \\ \\ \Gamma \vDash a:A \\ \Gamma \vDash F:A_1 \\ \Gamma \vDash b_1:B \\ \Gamma \vDash b_2:C \\ \hline \Gamma \vDash \mathsf{case}_R \ a:A \ \mathsf{of} \ F:A_1 \Rightarrow B \mid C \\ \hline \Gamma \vDash \mathsf{case}_R \ a \ \mathsf{of} \ F \to b_1 \|_{-} \to b_2:C \end{array} \quad \text{E\_CASE}$$

 $\Gamma; \Delta \vDash \phi_1 \equiv \phi_2$  pr

prop equality

$$\begin{split} &\Gamma; \Delta \vDash A_1 \equiv A_2 : A/R \\ &\Gamma; \Delta \vDash B_1 \equiv B_2 : A/R \\ \hline &\Gamma; \Delta \vDash A_1 \sim_{A/R} B_1 \equiv A_2 \sim_{A/R} B_2 \end{split} \quad \text{E-PropCong} \\ &\Gamma; \Delta \vDash A_1 \sim_{A/R} B_1 \equiv A_2 \sim_{A/R} B_2 \\ &\Gamma; \Delta \vDash A \equiv B : \star/R_0 \\ &\Gamma \vDash A_1 \sim_{A/R} A_2 \text{ ok} \\ &\Gamma \vDash A_1 \sim_{B/R} A_2 \text{ ok} \\ \hline &\Gamma; \Delta \vDash A_1 \sim_{A/R} A_2 \equiv A_1 \sim_{B/R} A_2 \end{split} \quad \text{E-IsoConv}$$

$$\frac{\Gamma; \Delta \vDash \forall c : (a_1 \sim_{A/R_1} a_2) . B_1 \equiv \forall c : (b_1 \sim_{B/R_2} b_2) . B_2 : \star / R'}{\Gamma; \Delta \vDash a_1 \sim_{A/R_1} a_2 \equiv b_1 \sim_{B/R_2} b_2} \quad \text{E_CPIFST}$$

 $\Gamma; \Delta \vDash a \equiv b : A/R$ 

definitional equality

$$c: (a \sim_{A/R} b) \in \Gamma$$

$$c \in \Delta$$

$$\Gamma; \Delta \vDash a \equiv b : A/R$$

$$\Gamma; \Delta \vDash a \equiv a : A/R$$

$$\Gamma; \Delta \vDash a \equiv a : A/R$$

$$\Gamma; \Delta \vDash b \equiv a : A/R$$

$$\Gamma; \Delta \vDash a \equiv b : A/R_1$$

$$R_1 \leq R_2$$

$$\Gamma; \Delta \vDash a \equiv b : A/R_2$$

$$\Gamma; \Delta$$

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\Gamma; \Delta \vDash A_1 \equiv A_2 : \star / R'
                            \Gamma, x: A_1; \Delta \vDash B_1 \equiv B_2: \star/R'
                            \Gamma \vDash A_1 : \star
                            \Gamma \vDash \Pi^{\rho} x : A_1 \to B_1 : \star
                            \Gamma \vDash \Pi^{\rho} x : A_2 \to B_2 : \star
                                                                                                              E_PICONG
         \Gamma; \Delta \models (\Pi^{\rho}x : A_1 \to B_1) \equiv (\Pi^{\rho}x : A_2 \to B_2) : \star /R'
                           \Gamma, x: A_1; \Delta \vDash b_1 \equiv b_2: B/R'
                           \Gamma \vDash A_1 : \star
                           (\rho = +) \lor (x \not\in \mathsf{fv}\ b_1)
                           (\rho = +) \lor (x \not\in \mathsf{fv}\ b_2)
                                                                                                         E_AbsCong
        \overline{\Gamma; \Delta \vDash (\lambda^{\rho} x. b_1) \equiv (\lambda^{\rho} x. b_2) : (\Pi^{\rho} x: A_1 \to B) / R'}
                     \Gamma; \Delta \vDash a_1 \equiv b_1 : (\Pi^+ x : A \to B)/R'
                     \Gamma; \Delta \vDash a_2 \equiv b_2 : A/\mathbf{Nom}
                                                                                                   E_AppCong
                \overline{\Gamma; \Delta} \models a_1 \ a_2^+ \equiv b_1 \ b_2^+ : (B\{a_2/x\})/R'
                   \Gamma; \Delta \vDash a_1 \equiv b_1 : (\Pi^+ x : A \to B)/R'
                   \Gamma; \Delta \vDash a_2 \equiv b_2 : A/R
                   Path a_1 = F@R, Rs
                   Path b_1 = F'@R, Rs'
              \overline{\Gamma; \Delta \vDash a_1 \ a_2{}^R \equiv b_1 \ b_2{}^R : (B\{a_2/x\})/R'}
                                                                                                E_TAPPCONG
                    \Gamma; \Delta \vDash a_1 \equiv b_1 : (\Pi^- x : A \rightarrow B)/R'
                    \Gamma \vDash a : A
                                                                                              E_IAppCong
                \overline{\Gamma; \Delta \vDash a_1 \square^- \equiv b_1 \square^- : (B\{a/x\})/R'}
              \frac{\Gamma; \Delta \vDash \Pi^{\rho} x : A_1 \to B_1 \equiv \Pi^{\rho} x : A_2 \to B_2 : \star / R'}{\Gamma; \Delta \vDash A_1 \equiv A_2 : \star / R'}
              \Gamma; \Delta \vDash \Pi^{\rho} x : A_1 \to B_1 \equiv \Pi^{\rho} x : A_2 \to B_2 : \star / R'
              \Gamma; \Delta \vDash a_1 \equiv a_2 : A_1/\mathbf{Nom}
                                                                                                              E_PiSnd
                       \Gamma; \Delta \vDash B_1\{a_1/x\} \equiv B_2\{a_2/x\} : \star/R'
                   \Gamma; \Delta \vDash a_1 \sim_{A_1/R} b_1 \equiv a_2 \sim_{A_2/R} b_2
                   \Gamma, c: a_1 \sim_{A_1/R} b_1; \Delta \vDash A \equiv B: \star/R'
                   \Gamma \vDash a_1 \sim_{A_1/R} b_1 ok
                   \Gamma \vDash \forall c : a_1 \sim_{A_1/R} b_1.A : \star
                   \Gamma \vDash \forall c : a_2 \sim_{A_2/R} b_2.B : \star
                                                                                                                E_CPICONG
   \overline{\Gamma; \Delta \vDash \forall c : a_1 \sim_{A_1/R} b_1.A \equiv \forall c : a_2 \sim_{A_2/R} b_2.B : \star/R'}
                           \Gamma, c: \phi_1; \Delta \vDash a \equiv b: B/R
                           \Gamma \vDash \phi_1 ok
                                                                                            E_CABSCONG
                 \overline{\Gamma; \Delta \vDash (\Lambda c.a) \equiv (\Lambda c.b) : \forall c : \phi_1.B/R}
               \Gamma; \Delta \vDash a_1 \equiv b_1 : (\forall c : (a \sim_{A/R} b).B)/R'
               \Gamma; \widetilde{\Gamma} \vDash a \equiv b : A/\mathbf{param} R R'
                   \Gamma; \Delta \vDash a_1[\bullet] \equiv b_1[\bullet] : (B\{\bullet/c\})/R' E_CAPPCONG
\Gamma; \Delta \vDash \forall c : (a_1 \sim_{A/R} a_2).B_1 \equiv \forall c : (a'_1 \sim_{A'/R'} a'_2).B_2 : \star/R_0
\Gamma; \widetilde{\Gamma} \vDash a_1 \equiv a_2 : A/\mathbf{param} \, R \, R_0
\Gamma; \widetilde{\Gamma} \vDash a_1' \equiv a_2' : A'/\mathbf{param} R' R_0
                                                                                                                         E_CPiSnd
                       \Gamma; \Delta \vDash B_1\{\bullet/c\} \equiv B_2\{\bullet/c\} : \star/R_0
```

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\Gamma; \Delta \vDash a \equiv b : A/R
                                               \frac{\Gamma; \Delta \vDash a \sim_{A/R} b \equiv a' \sim_{A'/R'} b'}{\Gamma; \Delta \vDash a' \equiv b' : A'/R'} \quad \text{E-CAST}
                                                      \Gamma; \Delta \vDash a \equiv b : A/R
                                                      \Gamma; \widetilde{\Gamma} \vDash A \equiv B : \star / \mathbf{Rep}
                                                      \Gamma \vDash B : \star
                                                      \frac{\Gamma \vDash B : \star}{\Gamma; \Delta \vDash a \equiv b : B/R} \quad \text{E\_EQCONV}
                                          \frac{\Gamma; \Delta \vDash a \sim_{A/R_1} b \equiv a' \sim_{A'/R_1} b'}{\Gamma; \Delta \vDash A \equiv A' : \star/\mathbf{Rep}} \quad \text{E\_ISOSND}
                                                     \Gamma; \Delta \vDash a \equiv a' : A/R
                                                     \Gamma; \Delta \vDash b_1 \equiv b'_1 : B/R_0
                                                    \Gamma; \Delta \vDash b_2 \equiv b_2' : B/R_0
\frac{1}{\Gamma; \Delta \vDash \mathsf{case}_R \ a \ \mathsf{of} \ F \to b_1 \parallel_{-} \to b_2 \equiv \mathsf{case}_R \ a' \ \mathsf{of} \ F \to b_1' \parallel_{-} \to b_2' : B/R_0} \quad \text{E\_PATCONG}
                                      ValuePath a = F
                                      ValuePath a' = F
                                      \Gamma \vDash a : \Pi^+ x : A \to B
                                      \Gamma \vDash b : A
                                      \Gamma \vDash a' : \Pi^+ x : A \to B
                                      \Gamma \vDash b' : A
                                      \Gamma; \Delta \vDash a \ b^{R_1} \equiv a' \ b'^{R_1} : B\{b/x\}/R'
                                          \frac{\mathcal{L}_{\{0\}} x_{f} = \mathcal{B}\{0'/x\} : \star/R'}{\Gamma; \Delta \vDash a \equiv a' : \Pi^{+}x : A \to B/R'} \quad \text{E-LeftRel}
                                      \Gamma; \widetilde{\Gamma} \vDash B\{b/x\} \equiv B\{b'/x\} : \star/R'
                                     ValuePath a = F
                                     ValuePath a' = F
                                     \Gamma \vDash a : \Pi^- x : A \to B
                                     \Gamma \vDash b : A
                                     \Gamma \vDash a' : \Pi^- x : A \to B
                                     \Gamma \vDash b' : A
                                     \Gamma; \Delta \vDash a \square^- \equiv a' \square^- : B\{b/x\}/R'
                                     \frac{\Gamma; \widetilde{\Gamma} \vDash B\{b/x\} \equiv B\{b'/x\} : \star/R_0}{\Gamma; \Delta \vDash a \equiv a' : \Pi^- x : A \to B/R'} \quad \text{E_LEFTIRREL}
                                           ValuePath a = F
                                           ValuePath a' = F
                                           \Gamma \vDash a : \Pi^+ x : A \to B
                                            \Gamma \vDash b : A
                                            \Gamma \vDash a' : \Pi^+ x \colon\! A \to B
                                            \Gamma \vDash b' : A
                                            \Gamma; \Delta \vDash a \ b^+ \equiv a' \ b'^+ : B\{b/x\}/R'
                                           \frac{\Gamma; \widetilde{\Gamma} \vDash B\{b/x\} \equiv B\{b'/x\} : \star/R_0}{\Gamma; \Delta \vDash b \equiv b' : A/\mathbf{param} R_1 R'}
                                                                                                                            E_Right
                                              ValuePath a = F
                                              ValuePath a' = F
                                              \Gamma \vDash a : \forall c : (a_1 \sim_{A/R_1} a_2).B
                                              \Gamma \vDash a' : \forall c : (a_1 \sim_{A/R_1} a_2).B
                                              \Gamma; \widetilde{\Gamma} \vDash a_1 \equiv a_2 : A/R'
                                      \frac{\Gamma;\Delta \vDash a[\bullet] \equiv a'[\bullet]: B\{\bullet/c\}/R'}{\Gamma;\Delta \vDash a \equiv a': \forall c \colon\! (a_1 \sim_{A/R_1} a_2).B/R'}
                                                                                                                               E_{-}CLeft
```

#### $\models \Gamma$ context wellformedness

### $\models \Sigma$ signature wellformedness

 $\Gamma \vdash \phi$  ok prop wellformedness

 $\Gamma \vdash a : A/R$  typing

 $\Gamma; \Delta \vdash \gamma : \phi_1 \sim \phi_2$  coercion between props

 $\Gamma; \Delta \vdash \gamma : A \sim_R B$  coercion between types

 $\vdash \Gamma$  context wellformedness

 $\Gamma \vdash a \leadsto b/R$  single-step, weak head reduction to values for annotated language

Definition rules: 169 good 0 bad Definition rule clauses: 464 good 0 bad