



Mo Tu We Th Fr Sa Su

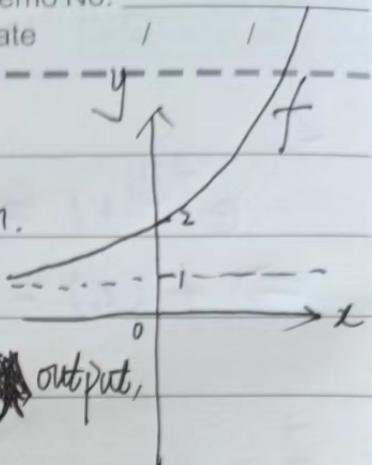
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Q2

1. ①  $f(x)$  is an injective function.~~PROVE (EXPLANATION):~~

given a  $x$ , it map to the unique ~~out~~ output,  
which is  $e^x + 1$ .



PROVE:

for all  $a, b \in \mathbb{R}$ , if  $f(a) = f(b)$ ,

then  $e^a + 1 = e^b + 1$

$$\Rightarrow e^a = e^b$$

$$\Rightarrow a = b.$$

②  $f(x)$  is a surjective function.~~PROVE:~~for all  $y \in [1, +\infty)$ , there exist ~~x~~  $\exists$ 

$$y = f(x) = e^x + 1 \quad \text{or}$$

$$\Rightarrow x = \ln(y-1) \in \mathbb{R}$$



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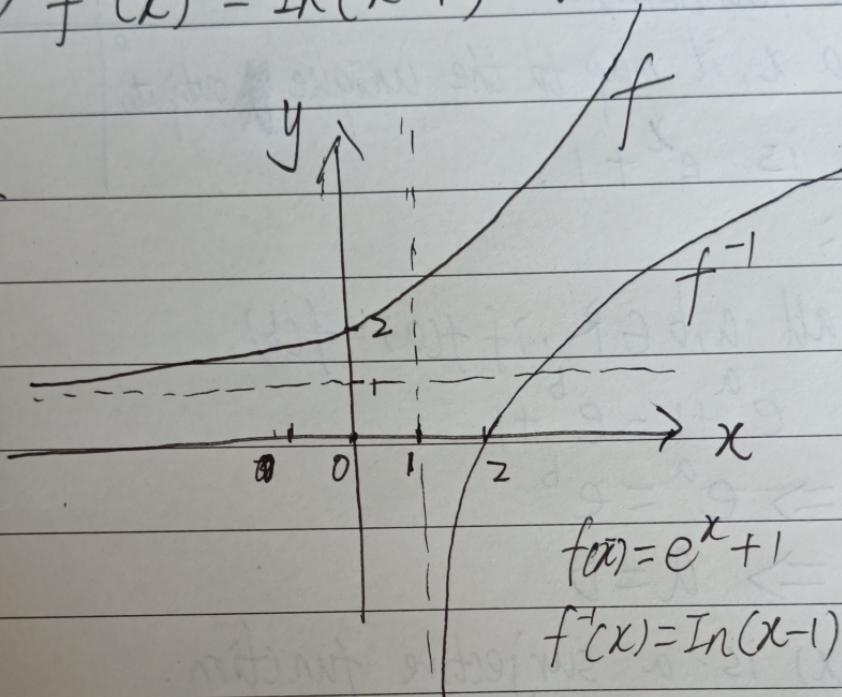
2.

$$e^{f^{-1}(x)} + 1 = x$$

So the inverse function

$$\Rightarrow f^{-1}(x) = \ln(x-1) \quad f(x) = \ln(x-1).$$

3.



4. These two curves are symmetric with the line ~~y=x~~.

It's like  $x$  and  $y$  change their stand in these two curves, so it makes sense.