

This lecture's notes illustrate some uses of various L<sup>A</sup>T<sub>E</sub>X macros. Take a look at this and imitate.

## 0.1 Some theorems and stuff

We now delve right into the proof.

**Lemma 0.1** *This is the first lemma of the lecture.*

**Proof:** The proof is by induction on .... For fun, we throw in a figure.

Figure 0.1: A Fun Figure

This is the end of the proof, which is marked with a little box. ■

### 0.1.1 A few items of note

Here is an itemized list:

- this is the first item;
- this is the second item.

Here is an enumerated list:

1. this is the first item;
2. this is the second item.

Here is an exercise:

**Exercise:** Show that  $P \neq NP$ .

Here is how to define things in the proper mathematical style. Let  $f_k$  be the *AND – OR* function, defined by

$$f_k(x_1, x_2, \dots, x_{2^k}) = \begin{cases} x_1 & \text{if } k = 0; \\ AND(f_{k-1}(x_1, \dots, x_{2^{k-1}}), f_{k-1}(x_{2^{k-1}+1}, \dots, x_{2^k})) & \text{if } k \text{ is even;} \\ OR(f_{k-1}(x_1, \dots, x_{2^{k-1}}), f_{k-1}(x_{2^{k-1}+1}, \dots, x_{2^k})) & \text{otherwise.} \end{cases}$$

**Theorem 0.2** *This is the first theorem.*

**Proof:** This is the proof of the first theorem. We show how to write pseudo-code now.

Consider a comparison between  $x$  and  $y$ :

```
if  $x$  or  $y$  or both are in  $S$  then
    answer accordingly
else
    Make the element with the larger score (say  $x$ ) win the comparison
    if  $F(x) + F(y) < \frac{n}{t-1}$  then
         $F(x) \leftarrow F(x) + F(y)$ 
         $F(y) \leftarrow 0$ 
    else
         $S \leftarrow S \cup \{x\}$ 
         $r \leftarrow r + 1$ 
    endif
endif
```

This concludes the proof. ■