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Aachen, July 18, 2020

Danksagung

Danke.

Contents

1	Introduction	11
1.1	Background	11
1.1.1	Railway Vehicle Operations	11
1.1.2	Automatic Train Protection and Cab Signaling	12
1.1.3	Braking Curves	13
1.2	Problem	13
1.3	Solution	14
2	Fundamentals of Railway Vehicle Engineering	15
2.1	The train brake	15
2.2	Influences on braking performance	16
2.2.1	Inherent factors, model variables	16
2.2.2	Relations	18
2.3	Constants	20
2.4	Time considerations	20
3	Modeling of Train Operations	23
3.1	Matlab Simulink	23
3.2	Initial Model	23
3.3	Model Expansion	26
3.4	Further Expansion	33
4	Data Generation	35
4.1	Matlab Code	36
4.2	Data Structure	40
4.3	Analysis of generated Data	42
5	Performance Analysis	43
6	Conclusion	45
	Abbildungsverzeichnis	46
	Tabellenverzeichnis	48

Anhang	49
A Quellcode	51
B Data visualization	53

Abstract Modern day railway system operations require automated train control mechanisms, e.g. European Train Control System ETCS, to maximize efficiency, which is often times limited by outdated infrastructure, as well as safety of operations. One way to achieve this is by lowering the required distance between two trains on the same track, which in turn demands a reliable method of predicting the braking distance at any given moment.

While determination of the necessary braking curves is feasible for a limited number of train formations, the large diversity of vehicles in freight operations poses an issue. One approach for a solution would be using Big Data, which would be able to process the required amounts of data to calculate reliable braking curves even for freight operations.

The problem here is that there is simply not enough data available since freight trains usually don't have the sensory equipment needed. To circumvent that obstacle, this work proposes generation of artificial data via white box modeling to be then used in further big data operations.

Chapter 1

Introduction

Introduction This section describes the background and motivation of the research (Sect. 1.1), the problem to be addressed (Sect. 1.2) and the proposed solution (Sect. 1.3)

1.1 Background

In recent years, data science has become more and more prominent. Since large quantities of data have become omnipresent, big data processing is applicable in various fields of research and operations. This work focuses on the application of big data processing to railway system operations, more specifically the preconditions. Mainly, two areas show promise to benefit from big data usage, which is predictive maintenance as well as optimization of railway operations. As the name suggests, lots of data is required, think hundreds of terabyte for freight operations in Germany alone. As it stands though, unfortunately, this data source remains largely untapped today, owing to freight wagons typically lacking necessary sensory equipment. This is where this work comes into play.

1.1.1 Railway Vehicle Operations

Road and rail traffic are fundamentally different, mainly in two regards. First, the physical properties, which will be discussed in chapter 2, second, the actual modalities of operations, which will be topic of this section.

In road traffic, there is many different vehicles, all operating independently from one another. Although there is ongoing experimentation to utilize autonomous vehicles to recreate train-like lorry configurations, this is not the norm. In contrast to that, the track guiding of wheels offered by rails enables the formation of trains possibly kilometers long, reducing labor cost, infrastructure usage and energy consumption. This, of course, calls for special safety measures to be taken, since higher speeds and payloads result in long braking distances.

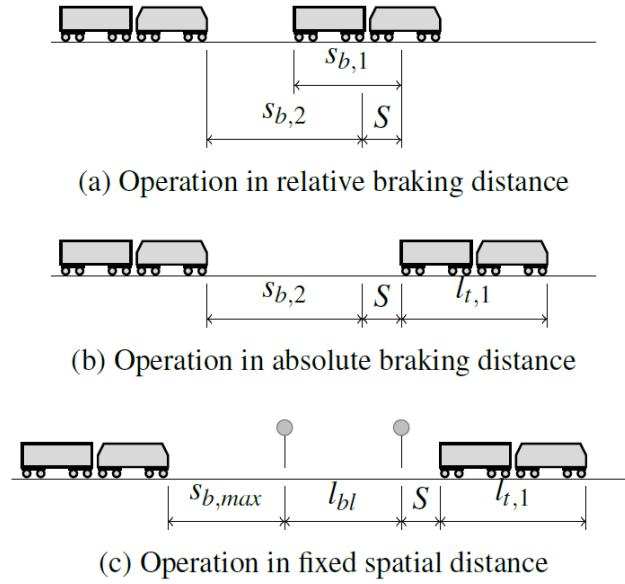


Figure 1.1: Spacing paradigms

The above figure illustrates the three main principles of spacing between two trains on the same track. $s_{b,i}$ denoted the braking distance of train i , $l_{t,i}$ the length of train i , l_{bl} the length of a track section, and S a safety margin. Fixed spatial distance, the most commonly used today, is very inefficient in terms of track utilization, but offers the most protection against accidents. In order to optimize efficiency, it is desirable to move towards relative braking distances, which requires the ability to very accurately predict braking capacity of trains.

1.1.2 Automatic Train Protection and Cab Signaling

Automatic train protection systems are designed to ensure safe operation in case of human or technical error or malpractice by the train operator. Generally, all trains operate on track sections which are free of other vehicles, reserved and locked. Think for example a section between two signals. These sections are also referred to as movement authority, and a train has to be capable of coming to a complete halt before the end of movement authority as to not violate a track section locked by another train. For this, the driver and or the onboard computer needs to be informed about the endpoint of the current movement authority as well as speed limits. The train protection system enforces application of brakes in case of violation of restrictions, for example if the train exceeds the speed limit or the train would otherwise be unable to stop in time before movement authority expires. Train protection systems may be categorized by means of information transfer. Spatially discrete acting systems use transmitters placed at strategic points along the track, for example signals, whereas continuous systems may transmit information at all times, either via track-sided wire loops or radio communication. These allow higher degrees of automation than discrete systems, as trains have access to the necessary real-time data.

Cab signaling relays all relevant information to the train operator so they may act in the most optimal way. The European train control system, short ETCS, encompasses both of these.

1.1.3 Braking Curves

For the ETCS to be able to supervise train velocity, it needs to determine the vehicle's braking capacity for any given moment in time, using a mathematical model of the braking dynamics and of the track characteristics. This prediction is called a braking curve, which describe the probable braking process for a set of input parameters. As a simple example, refer to figure 1.2. Since braking performance cannot be predicted with absolute certainty, an ϵ parameter needs to be factored in to account for random behavior. Therefore, there is a number of discrete braking curves for any set of parameters, forming a probability distribution. The parameters may be classified in four categories:

- Physical parameters, which is real time measurements from on-board equipment
- Fixed values, like driver reaction time
- Trackside data, like track gradient or signaling data
- Train data, mostly captured beforehand, relating to the rolling stock braking system itself

The fourth category, train data, is the key factor for this work, as will be explained below.

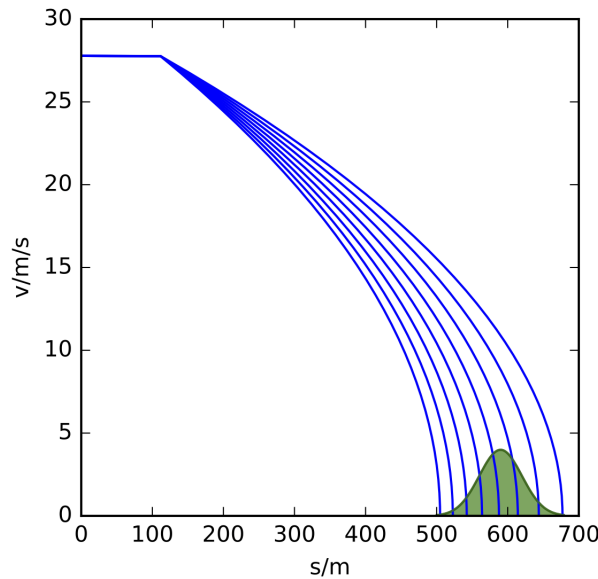


Figure 1.2: Braking curves

1.2 Problem

As mentioned, one category of input parameters for the calculation of braking curves is data directly associated with the rolling stock, and in particular to the braking system itself. While this does not necessarily present itself as an issue in passenger trains, freight wagons, in contrast, are usually not electrified and therefore do not currently possess the sensory equipment that would be necessary to obtain such data in an adequate quantity and quality, especially in regards

to *big data processing*. Although it has been proposed to equip freight wagons accordingly (Refer to the concept “freight wagon 4.0” by Dr. Manfred Enning and Dr. Raphael Pfaff), it will be years, possibly decades, before enough rolling stock has been retrofitted as to make it possible to obtain the desired data. Since braking curves vary according to the rolling stock, this lack of data makes calculation thereof impossible.

1.3 Solution

Since the problem is lack of data from real life operations, this work proposes to circumvent this by generation of artificial, simulated data instead. The data set should replicate the actual distribution of braking behavior as close as possible. It is therefore necessary to first create a model encompassing the braking process of a freight train. This model will be discussed in depth in chapter 3. By using that model to run a large number of simulated braking processes, one may obtain data about the behavior of the braking system, which, albeit being artificial, should at least satisfy requirements for the calculation of rudimentary braking curves. A freely configurable simulation environment further allows for great flexibility in terms of input parameters, therefore enabling for covering a very large range of data, where computing power and time are the only limiting factors. The process of data generation and simulation will be discussed further in chapter 4.

As real life operations would yield very high quantities of data, the simulation output must be stored in a data structure which is suitable for big data processing. This structure will also be discussed in chapter 4.

Chapter 2

Fundamentals of Railway Vehicle Engineering

Introduction This section deals with the engineering backgrounds of the work, especially in regards to railway vehicle engineering and railway physics. For the creation of a braking model, it is necessary to have at least a basic understanding of the engineering and physics behind rail traffic. The most fundamental component to understand is, of course, the actual braking process.

2.1 The train brake

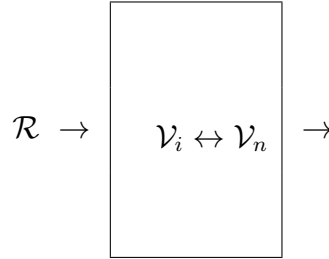
There is a number of different construction methods for brakes, but each must address two problems: The means of transmission of commands and the actual form of brake force generation. The focus here will lie on the pneumatic brake, since it is still the most prevalent in cargo vehicles. From a macro perspective, the pneumatic brake has three main components: The train driver's brake valve, the brake pipe and one or more brake cylinders for each wagon or locomotive. The driver's valve and the brake pipe are primarily the means of command transmission, while the brake cylinder's job is the generation of brake force.

The braking system is an indirect one, which means the brake pipe needs to be vented to apply the brakes. Therefore, the brake pipe is kept at a running pressure of 5 bar. One advantage of this approach is that brakes are automatically applied in case of train separation. The downside, however, is that command transmission is limited to the speed of sound. In order to generate that pressure, the locomotive contains a compressor and an air reservoir. Initially, the brake pipe as well as all auxiliary air reservoirs are brought to operating pressure. If the train operator wishes to brake, he has to actuate the driver's brake valve, which in turn vents the brake pipe, usually as far as 3.5 bar (full braking), sometimes even lower. As rule of thumb, the more pressure is vented, the more braking force is applied. Each wagon brake has, in essence, an auxiliary air reservoir, a distributor valve and a braking cylinder. When the brake pipe is vented, the air in the auxiliary reservoir has a higher pressure. This difference in pressure triggers a switch of the distributor valve, and the air from the reservoir may go into the brake cylinder. This increase in the cylinder generates the actual braking force. To summarize, the amount of generated braking pressure is directly proportional to the amount

of pressure vented.

2.2 Influences on braking performance

Since the aim of this work is to monitor braking performance, it becomes necessary to understand which factors influence the braking process, and how. The braking process is, in its core, a system. A system may be defined as a set of objects, which are interconnected by relations. It is enclosed by its environment, which may or may not affect the system itself. Below is an illustration, also called box model:



The box represents the actual system, \mathcal{V}_i are the system variables, or objects, their relations represented by the \leftrightarrow . The \mathcal{R} represents the system's environment and its influence on the system itself. Finally, the rightmost arrow \rightarrow is the influence the system might have on the environment, though this is often disregarded as the focus lies on what happens inside the system. Creating a box model for the braking process makes for an easier identification of the influencing factors, and allows for their categorization into inherent, i.e. system variables, and external, i.e. system environment.

From a modeling perspective, it is sensible to differentiate as follows: Everything related to the train itself is part of the system, and everything else is part of the system's environment. As per definition, it is compromised of a set of variables, a set of relations, and a set of constants. Let us make a formal definition of the model for the braking process system:

$$\mathcal{M} = \{\{\mathcal{V}\}, \{\mathcal{R}\}, \{c\}\}$$

where $\{\mathcal{V}\}$ is the set of system variables, $\{\mathcal{R}\}$ is the set of relations (a) between elements of $\{\mathcal{V}\}$ and (b) between system and environment, and $\{c\}$ is the set of system constants. The system variables may be subsystems themselves. We shall take a closer look at $\{\mathcal{V}\}$ first.

2.2.1 Inherent factors, model variables

Looking at \mathcal{M} , which is the system describing the braking process, $\{\mathcal{V}\}$ consists of all factors inherent to the train which have an impact on the braking, as well as the relevant quantifiers. The main ones are:

- The train brake
- The wagon mass, denoted as m

- The train velocity, denoted as v
- The train composition, i.e. in which order the wagons are, for example the heaviest wagons being in front and the lighter ones at the back, denoted as $comp$
- The generated braking force, denoted as F_b
- The train's deceleration, denoted as a
- The train's braking distance, denoted as d

It is noteworthy that the train brake is another system in itself, which is perfectly fine of course. Alas, it is therefore necessary to define another model.

$$\mathcal{M}_B = \{\{\mathcal{V}_B\}, \{\mathcal{R}_B\}, \{c_B\}\}$$

Let \mathcal{M}_B be the model describing the system train brake, with $\{\mathcal{V}_B\} = \{\mathcal{M}_{bv}, \mathcal{M}_{bp}, \mathcal{M}_{bc}\}$, where \mathcal{M}_{bv} is the model of the brake valve, \mathcal{M}_{bp} the model of the brake pipe and \mathcal{M}_{bc} the model of the brake cylinder, which in turn shall be defined as follows:

$$\mathcal{M}_{bv} = \{\{\mathcal{V}_{bv}\}, \{\mathcal{R}_{bv}\}, \{c_{bv}\}\}$$

Let \mathcal{M}_{bv} be the model describing the system brake valve, with $\mathcal{V}_{bv} = \{x\}$, $\mathcal{R}_{bv} = \emptyset$ and $c_{bv} = \emptyset$, where x is the state of the brake valve, i.e. its opening percentage, ranging from 0 (fully closed) to 1 (fully open, full braking).

$$\mathcal{M}_{bp} = \{\{\mathcal{V}_{bp}\}, \{\mathcal{R}_{bp}\}, \{c_{bp}\}\}$$

Let \mathcal{M}_{bp} be the model describing the system brake pipe, with $\mathcal{V}_{bp} = \{l_{bp}, p_{bp}\}$, $\mathcal{R}_{bp} = \emptyset$ and $c_{bp} = \{v_{bp}\}$, where l_{bp} is the physical length of the brake pipe, p_{bp} is the pressure on the brake pipe and v_{bp} is the propagation velocity of the pipe's medium.

$$\mathcal{M}_{bc} = \{\{\mathcal{V}_{bc}\}, \{\mathcal{R}_{bc}\}, \{c_{bc}\}\}$$

Let \mathcal{M}_{bc} be the model describing the system brake cylinder, with $\mathcal{V}_{bc} = \{p_{bc}\}$, $\mathcal{R}_{bc} = \emptyset$ and $c_{bc} = \{t_{bc}\}$, where p_{bc} is the cylinder's pressure and t_{bc} is the cylinder's fill time.

This wraps up the definition of \mathcal{V}_B . We may now get to the definition of \mathcal{R}_B , which is the relations (a) between the elements of \mathcal{V}_B and (b) between \mathcal{M}_B and its environment. Let us begin with (a):

Convention For readability purposes, \propto shall from here on denote direct proportionality, and \sim shall denote inverse proportionality.

\mathcal{M}_{bv} relates to \mathcal{M}_{bp} in the sense that the state of the brake valve has a direct influence on the pressure on the brake pipe. More specifically, $x \in \mathcal{V}_{bv}$ is inversely proportional to $p_{bp} \in \mathcal{V}_{bp}$. The higher the value of x , i.e. the opening percentage of the brake valve, the lower the value of p_{bp} , i.e. the pressure on the brake pipe. We can therefore denote $x \sim p_{bp}$, and subsequently define a relation $R_{bv,bp} : \mathcal{M}_{bv} \sim \mathcal{M}_{bp}$.

\mathcal{M}_{bp} relates to \mathcal{M}_{bc} in the sense that the pressure on the brake pipe has a direct influence on the brake cylinder's pressure. More specifically, $p_{bp} \in \mathcal{V}_{bp}$ is inversely proportional to $p_{bc} \in \mathcal{V}_{bc}$. The lower the value of p_{bp} , i.e. the pressure on the brake pipe, the higher the value p_{bc} , i.e. the pressure in the brake cylinder. We can therefore denote $p_{bp} \sim p_{bc}$, and subsequently define a relation $R_{bp,bc} : \mathcal{M}_{bp} \sim \mathcal{M}_{bc}$.

For simplicity, we can look at \mathcal{M}_B as being isolated from its environment, i.e. the environment does not impact \mathcal{M}_B , and vice versa. Therefore, (b) is void. Consequently, we can define \mathcal{R}_B as follows:

$$\mathcal{R}_B = \{R_{bv,bp}, R_{bp,bc}\}$$

This finally leaves us with c_B . Since call constants are specific to the respective sub-models $\in \mathcal{V}_B$, \mathcal{M}_B has no constants of its own, therefore $c_B = \emptyset$. This completes the definition of \mathcal{M}_B , and we can properly define the set of model variables of the model braking process:

$$\{\mathcal{V}\} = \{\mathcal{M}_B, m, v, comp, F_b, a, d\}$$

2.2.2 Relations

Looking at our model \mathcal{M} , we have now defined its set of variables, \mathcal{V} . Next, it is necessary to define its set of relations, \mathcal{R} , which may be distinguished into internal and external relations.

Relations between system variables

Obviously, the train brake \mathcal{M}_B relates to F_B as it is the actor responsible for generating the braking force. More specifically, $p_{bc} \in \mathcal{V}_{bc}$, which is the pressure in the brake cylinder, is directly proportionate to F_b , meaning the higher the pressure, the more force is applied. We can therefore denote $p_{bc} \propto F_b$, and subsequently define a relation $R_{\mathcal{M}_B, F_b} : \mathcal{M}_B \propto F_b$.

Furthermore, the wagon mass m relates to F_B as well. The vehicle mass is proportional to the kinetic energy to dissipate during braking actions. The larger m is, the more kinetic energy ($E = \frac{1}{2} \cdot m \cdot v^2$), and thus the higher the required braking force to slow the train down. As the vehicle mass varies, so must the applied braking force in order to avoid wheel slip and locking of the wheels which occurs if too much force is applied [train braking, 19]. We can therefore denote $m \propto F_b$, and subsequently define a relation $R_{m, F_b} : m \propto F_b$.

The braking deceleration a , neglecting other resistances, is influenced by two factors: The applied braking force F_b , and the vehicle's mass m . As per Newton's second law of motion, $F = m \cdot a$, so $a = \frac{F_b}{m}$ [train braking, 23]. In practice, this means the braking force is directly proportional to the braking deceleration, and the vehicle mass is inversely proportional to a ,

not taking into consideration wheel slip. We can therefore denote $F_b \propto a$, and $m \sim a$, and subsequently define two relations $R_{F_b,a} : F_b \propto a$, and $R_{m,a} : m \sim a$.

Finally, the braking distance d is also dependent on two factors: The running speed v , and the braking deceleration a . We have

$$\begin{aligned} d &= \frac{1}{2} \cdot a \cdot t^2 \\ v &= a \cdot t \quad \rightarrow \quad s = \frac{v^2}{2 \cdot a} \end{aligned} \tag{2.1}$$

where t is the stopping time [train braking, 23]. So in practice, the running speed v is directly proportional to the braking distance, and the braking deceleration is inversely proportional to d . We can therefore denote $v \propto d$, and $a \sim d$, and subsequently define two relations $R_{v,d} : v \propto d$, and $R_{a,d} : a \sim d$.

This completes the set of internal relations of \mathcal{R} .

Relations between environment and system

To recapitulate, \mathcal{M} is a model for the braking process. Having handled its internal relations, it is now time to focus on the relation between the system and its environment. As established in section 2.2, the environment consists of all factors which have an influence on the braking process, but are not inherent to the train itself. In practice, this is the track which the train operates on. More specifically, it is two main properties of the track:

- The track gradient, denoted as α
- The wheel/rail friction coefficient, denoted as μ

As shown earlier, the braking deceleration has a substantial influence on the braking process, namely on the braking distance and on the stopping time (see equation 2.1). So far, the deceleration was only related to vehicle mass m and applied braking force F_b , both being internal relations. However, the track gradient, also has an influence on a . As the train goes uphill, the deceleration increases; as it goes downhill, it decreases, due to gravity. A simple formula might look like this:

$$a = a_{brake} + a_{grad} \tag{2.2}$$

where a is the total braking deceleration, a_{brake} is the deceleration resulting from the application of the brakes, and a_{grad} is the acceleration/deceleration resulting from the track gradient. Let a_{grad} be positive for upward, negative for downward slopes. We can define a_{grad} as a step function

$$a_{grad}(\alpha) = \begin{cases} \geq 0 & \text{if } \alpha \geq 0 \\ < 0 & \text{if } \alpha < 0 \end{cases} \tag{2.3}$$

where α is the value of the gradient, e.g. a percentage or an angle. This shows the track gradient is directly proportional to the total braking deceleration. We can therefore denote $\alpha \propto a$, and subsequently define a relation $R_{\alpha,a} : \alpha \propto a$.

The second factor to look at is the wheel/rail adhesion. Environmental effects like rain, ice or contaminants such as leaves have a degrading effect on the wheel/rail friction. This is expressed by a friction coefficient μ , where a lower value, for example $\mu = 0.2$ for a wet rail surface, means worse braking performance compared to a higher value, e.g. $\mu = 0.4$ for normal conditions. The friction coefficient is a limiting factor for the applied braking force, in the sense that when too much force is applied, wheel slip occurs, and braking performance decreases [design and simulation, 12]. While μ does not have a direct influence on F_b , it is, in practice, still related to it in that it is a limiting factor; an indirect influence, so to speak. In that regard, we might say it is directly proportional to the braking force: The higher the friction coefficient, the higher the maximum braking force that may be applied. We can therefore denote $\mu \propto F_b$, and subsequently define a relation $R_{\mu, F_b} : \mu \propto F_b$.

We may now properly define the set of relations of the model braking process:

$$\{\mathcal{R}\} = \{R_{\mathcal{M}_B, F_b}, R_{m, F_b}, R_{F_b, a}, R_{m, a}, R_{v, d}, R_{a, d}, R_{\alpha, a}, R_{\mu, F_b}\}$$

2.3 Constants

The braking process, being a dynamic one, has no constants in itself. Some of its components do, in particular the models making up the train brake, like the brake pipe \mathcal{M}_{bp} 's propagation velocity v_{bp} . However, these have already been discussed; we can therefore conclude that $\{c\} = \emptyset$.

To summarize, we have now defined all necessary components of \mathcal{M} , namely its set of model variables $\{\mathcal{V}\}$, its set of relations $\{\mathcal{R}\}$, and its set of constants $\{c\}$. This model will be used in chapter 3 as a theoretical basis upon which to build a simulink model, simulating the braking process.

2.4 Time considerations

So far, we have looked at the braking process from a static point of view. However, in reality it is a dynamic process and thus, time has to be taken into consideration. More specifically, it is a continuous model: For \mathcal{M} , the state of its variables changes all the time for the whole duration of the process.

Remember how we have defined the model. It is a set comprising of a number of subsets; but it describes a system, in this case the braking process of a train. This means that the model variables, i.e. the elements of $\{\mathcal{V}\}$, are subject to change as the process progresses. This can be expressed by another equation, in form of a function f :

$$\begin{aligned} \{V\} &= f(\mathcal{M}) \\ &= f(\{\mathcal{V}\}, \{\mathcal{R}\}, \{c\}) \end{aligned}$$

This suffices to determine the system's state before and after a relation has changed. As an example, v might be $25 \frac{m}{s}$ when the train operator engages the brakes, and $10 \frac{m}{s}$ when the brakes have been released. However, since we wish to monitor the whole braking process, it is also interesting to see how the state changes over time. In this example, v would be $25 \frac{m}{s}$ for $t = 0$, $22.3 \frac{m}{s}$ for $t = 50$ etc. We therefore need a new equation where $\{\mathcal{V}\}$ is also dependent on t .

$$\mathcal{V}(t)' = f(\mathcal{M})$$

This allows for the calculation of the rate of change for any given point in time. By integrating the equation, one can also obtain the actual values of the elements of $\{\mathcal{V}\}$, e.g. the value of v for $t = 120$. The function f is one, or a set of, differential equations; how these look like goes beyond the scope of this work, however.

We have now laid all the necessary groundwork to build a functioning model of the braking process, which can then be used for simulation and data generation. The next chapter will deal with this.

Chapter 3

Modeling of Train Operations

Introduction Chapter 2 has established the theoretical model of the train braking process. It will serve as a foundation to build a practical model suitable for conducting actual simulations.

3.1 Matlab Simulink

The model has been built utilizing the software Matlab Simulink by Mathworks. It offers several distinct advantages: It uses a graphical block diagramming tool which makes it very intuitive to use. At the same time, various official and third-party add-on libraries make it very versatile. Most importantly, as it is tightly integrated with the Matlab environment, it can be used for both modeling and simulating dynamical systems, like the braking process of a train.

3.2 Initial Model

Looking back at chapter 2, the aim is to build a model for the braking process of a freight train. An initial model of a single braking procedure, kindly provided by Dr. Raphael Pfaff, will serve as a basis. Most of the components previously designed in chapter 2 can already be found therein.

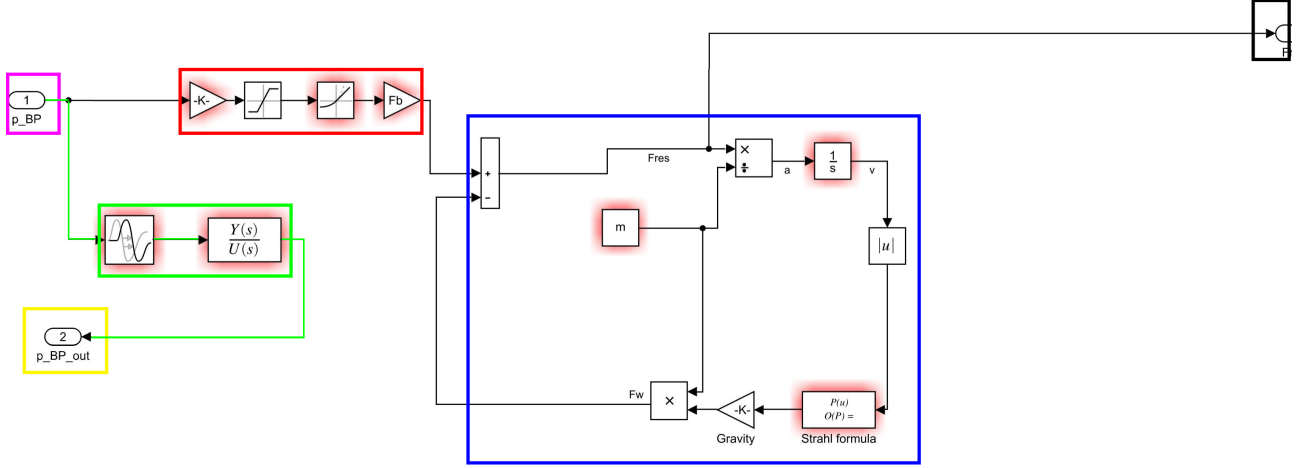


Figure 3.2: Initial Model - Wagon

Figure 3.6 shows a model of a freight wagon. It already encompasses several of the model variables defined in section 2.2.1. The brake pipe \mathcal{M}_{bp} is represented by the green arrows. It leads from input port (pink rectangle) to output port (yellow rectangle); the propagation delay is realized by a transport delay block (green rectangle), using propagation velocity v_{bp} and wagon length l_{bp} . The brake pressure p_{bp} is the value of the signal traveling through the connection. Note that in the simulation, the signal value for p_{bp} is the difference between regular operating pressure and actual pressure, e.g. if simulated pressure on the brake pipe is 3.5 bar, the signal value is $3.5 - 5 = -1.5$.

The brake cylinder \mathcal{M}_{bc} is represented by the red rectangle. The pressure on the brake pipe p_{bp} is converted into a coefficient between zero and one, where zero equals no brakes applied, or $p_{bp} = 5$, and one equals full braking pressure, or $p_{bp} = 3.5$. The exact formula is this:

$$p_{bc} = p_{bp} \cdot \frac{-1}{5 - 3.5}$$

So for a braking pressure of 4 bar, the coefficient would be $(4 - 5) \cdot \frac{-1}{5 - 3.5} = -1 \cdot \frac{-1}{1.5} = \frac{2}{3}$. A rate limiter block accounts for the brake cylinder's filling time t_{bc} . Finally, the braking force is calculated by multiplying the maximum braking force, which is mainly dependent on the wagon mass m [train braking, 22]. So for the braking pressure, we have:

$$F_b = F_{b,max} \cdot p_{bc}$$

The final component is the factoring in of the driving resistance of the train, utilizing Strahl's formula. This is represented by the blue rectangle. By continuous-time integration of the acceleration, which is calculated according to Newton's second law of motion ($a = \frac{F}{m}$), it is possible to determine the velocity, which in turn allows for the calculation of the force generated by the driving resistance. This force is then added to the braking force and fed into an output port, marked with the black rectangle.

Regarding simulation, this initial model is only fit for one single braking process, where a

train of fixed length and fixed composition, brakes from an initial velocity all the way to a halt; the only variation is the pressure on the brake pipe, which is also the sole input for the simulation. Appendix B.2 shows how that input might look like.

3.3 Model Expansion

This initial model is however not of sufficient detail. Where it merely simulates a single, rather undynamic braking process, the goal is the simulation of a train ride, with alternating phases of braking and accelerating. The model should furthermore factor in more components of the theoretical model \mathcal{M} discussed in chapter 2, as well as allow for the recording of more properties specific to the braking process. For that purpose, the model has to be expanded. The simulation input needs to be changed in order to allow for the simulation of a train ride. Previously, it being only one braking process, using braking pressure as input was the obvious choice. This will be replaced by a track profile, according to which the train either engages its brakes, or accelerates. This will be discussed in further detail in chapter 4.

In the initial model, the train is only able to decelerate by engaging its brakes. To allow for acceleration, it is necessary to expand the model accordingly. This may be realized by a rather simple two-point controller, which means the train is either accelerating or decelerating. The decision on whether to engage brakes or apply traction force at a particular point in time is made utilizing the track profile: If the current velocity of the train v_{real} is greater than the maximum allowed velocity v_{max} at that time, the train engages its brakes by lowering the pressure on the brake pipe p_{bp} . If v_{real} is less than v_{max} , the train applies a traction force F_t in order to increase speed. Both p_{bp} and F_t scale with the discrepancy between v_{real} and v_{max} . This means the higher the value of v_{dif} is, the more pressure is vented from the brake pipe (or the more traction force is applied). This prevents the train from overcompensating, for example applying full braking pressure to decrease velocity by $2 \frac{m}{s}$. Notice there is actually no case for when v_{real} equals v_{max} , i.e. $v_{dif} = 0$. One might expect that this would lead to the train constantly oscillating between accelerating and decelerating, but in practice this does not occur, and it is thus unnecessary to account for that case.

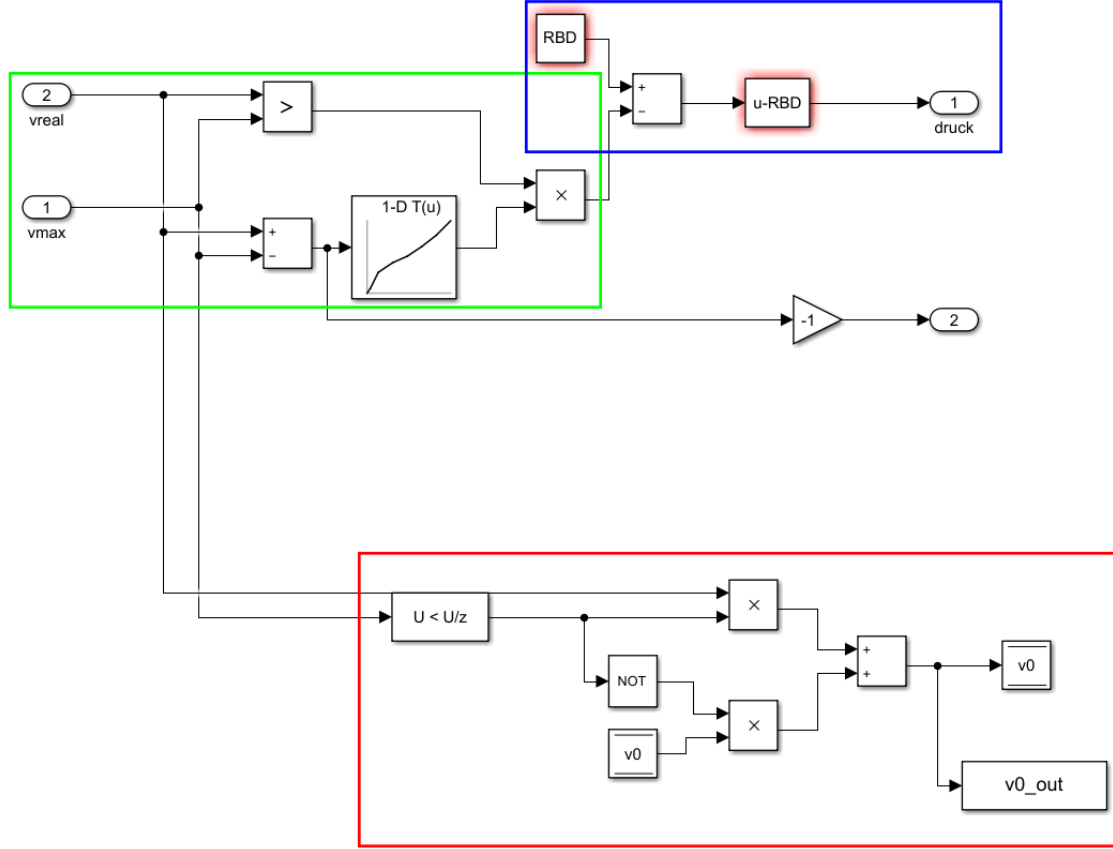


Figure 3.3: Expanded Model - Pressure Calculation

Figure 3.3 shows the subsystem responsible for the calculation of the braking pressure p_{bp} . The difference between v_{real} and v_{max} is used as input for a one-dimensional lookup table, which in essence is a step-function mapping different input values to discrete output values.

$$H(n) = \begin{cases} 0.1 & \text{if } n = 1 \\ 0.7 & \text{if } n = 15 \\ 0.8 & \text{if } n = 20 \\ \dots & \end{cases} \quad (3.1)$$

Equation 3.1 is an example for how this function might look like. The input parameter n stands for the discrepancy between actual and maximum velocity v_{dif} , and the output of the $H(n)$ represents the amount of pressure to vent from the brake pipe. This allows for adjusted braking, where p_{bp} is directly proportional to v_{dif} .

To account for the train only engaging its brakes in case its current velocity is higher than the maximum allowed velocity, a relational operator $>$ is used to compare v_{real} to v_{max} .

$$P(n, t) = H(n) \cdot (v_{real}(t) > v_{max}(t)) \quad (3.2)$$

Equation 3.2 describes the logic. The braking pressure for a velocity discrepancy n at a point in time t equals the result of $H(n)$ (equation 3.1) multiplied with the result of the relational operation comparing $v_{real}(t)$ to $v_{max}(t)$, which is 1 if $v_{real}(t)$ is greater than $v_{max}(t)$, and otherwise 0.

This ensures that $P(n, t)$ is zero when the train's velocity is lower than the maximum allowed velocity, and thus no pressure is vented from the brake pipe, and no brakes are engaged. This part of the system is marked by the green rectangle in figure 3.3. The blue rectangle marks the conversion of the braking pressure into a signal fit for further calculations, analogous to the initial model, discussed previously. Finally, the red rectangle marks the component for storing the initial velocity of a braking process, which is needed to calculate the braking distance further down the line. This is achieved by using a block to detect a decrease of v_{max} , i.e. the block outputs a signal of 1 or 0, accordingly.

$$v_0 = v_{real} \cdot b + v_{0,old} \cdot \bar{b} \quad (3.3)$$

Equation 3.3 describes the logic. The initial velocity of a braking process v_0 equals the train's velocity multiplied with the result of the decrease detection block, denoted as b , added with the previously stored initial velocity $v_{0,old}$ multiplied with the inverse of b , denoted as \bar{b} . If there is a decrease of v_{max} , i.e. the train starts braking, we get $v_0 = v_{real} \cdot 1 + v_{0,old} \cdot 0 = v_{real}$. In any other case, we get $v_0 = v_{real} \cdot 0 + v_{0,old} \cdot 1 = v_{0,old}$, i.e. the value of v_0 does not change as no new braking process has begun.

This completes the description of this subsystem. It is worthy to note that, reaching back to chapter 2, this is the practical implementation of the brake valve \mathcal{M}_{bv} .

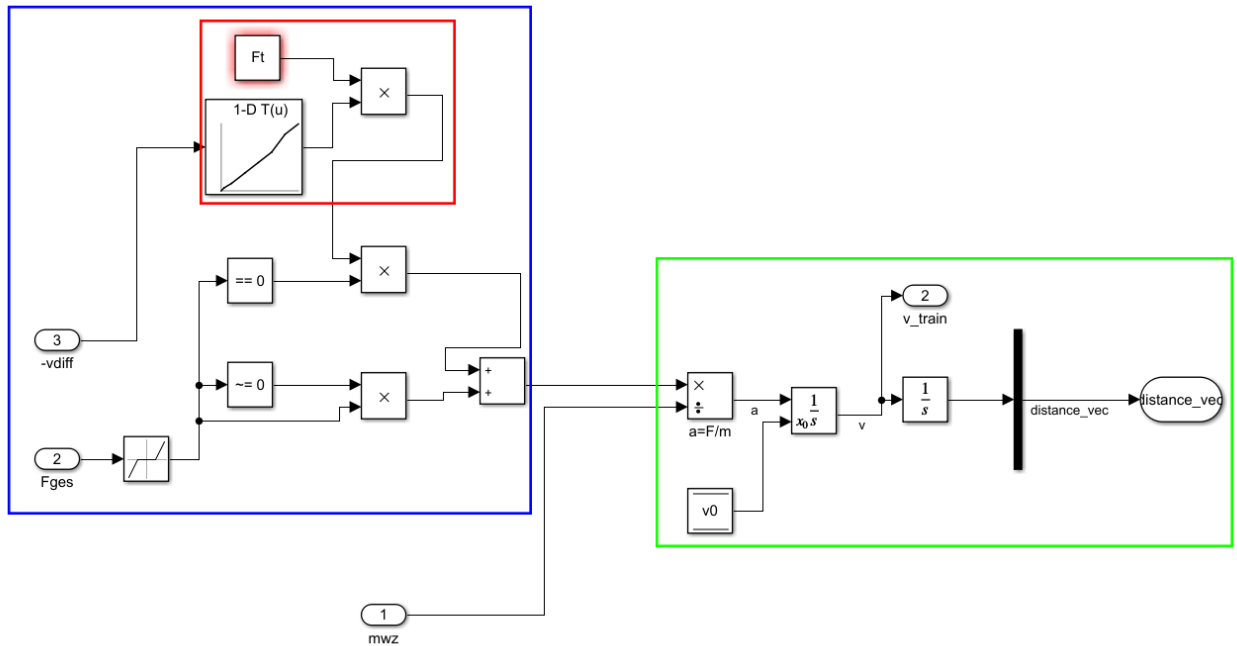


Figure 3.4: Expanded Model - Traction Force Calculation

Figure 3.4 shows the subsystem responsible for the calculation of the traction force, the train's acceleration, the train's velocity and the train's traveled distance. The applied traction force

scales with v_{dif} in a similar fashion to how p_{bp} does. Again, a one-dimensional lookup table is used to calculate the appropriate value for F_t .

$$H(n) = \begin{cases} 0.05 & \text{if } n = 1 \\ 0.45 & \text{if } n = 15 \\ 0.6 & \text{if } n = 20 \\ .. & \end{cases} \quad (3.4)$$

Equation 3.4 shows an example for how the function for the table might look like. The key difference to the calculation of the braking pressure is that the output values of the function are coefficients which are then multiplied with the maximum possible traction force, rather than raw values like in equation 3.1. This part of the system is marked by the red rectangle.

Remember that we have established the train is at any given time either accelerating or decelerating. Since there is, as previously discussed, already a system in place to determine whether the train should engage its brakes, it now suffices to make the following examination: If the train is generating a braking force, i.e. F_b is greater than zero, it will apply no traction force, and vice versa.

$$F_t(n, t) = (H(n) \cdot F_{t,max}) \cdot (F_b(n, t) == 0) \quad (3.5)$$

Equation 3.5 describes the logic. $F_b(t) == 0$ is a relational operation, the result being either 1 if there is a braking force at a particular point in time t , otherwise 0. We can apply the same logic to the braking force F_b :

$$F_b(n, t) = F_B(n, t) \cdot (F_b(n, t) \neq 0) \quad (3.6)$$

With equations 3.5 and 3.6 we can now determine the actual force applied at any given point in time t :

$$F(n, t) = F_t(n, t) + F_b(n, t) \quad (3.7)$$

Since either of the summands is always zero, equation 3.7 outputs either the traction force or the braking force being applied at a point in time t , for a value of v_{dif} n . This part of the system is marked by the blue rectangle, and together with the brake valve completes the system responsible for controlling the train.

Let's reach back to our model \mathcal{M} from chapter 2, in particular to three elements of its set of model variables $\{\mathcal{V}\}$: The train's acceleration a , its velocity v , and its braking distance d . Since we can now determine the applied force $F(n, t)$, it is now also possible to calculate the values of these three variables.

$$F = m \cdot a \quad (3.8)$$

Once again making use of Newton's second law of motion, we may calculate the value of a by substituting $F(n, t)$ for F , and the combined mass of all wagons m_{total} for m :

$$a = \frac{F(n, t)}{m_{total}} \quad (3.9)$$

The train's velocity may now be calculated by integration of its acceleration a . In simulink, this is achieved by feeding the signal value of a into a continuous-time integration block:

$$v = \int a \, da \quad (3.10)$$

Finally, the train's braking distance can be calculated by integration of its velocity v . This is once again achieved by usage of a continuous-time integration block:

$$d = \int v \, dv \quad (3.11)$$

This part of the system is marked by the green rectangle. This also completes the description of this subsystem. Looking back at our model \mathcal{M} , the last elements of $\{\mathcal{V}\}$ left to deal with are the brake pipe \mathcal{M}_{bp} , the brake cylinder \mathcal{M}_{bc} , the wagon mass m , the train composition $comp$, and finally the braking force F_b .

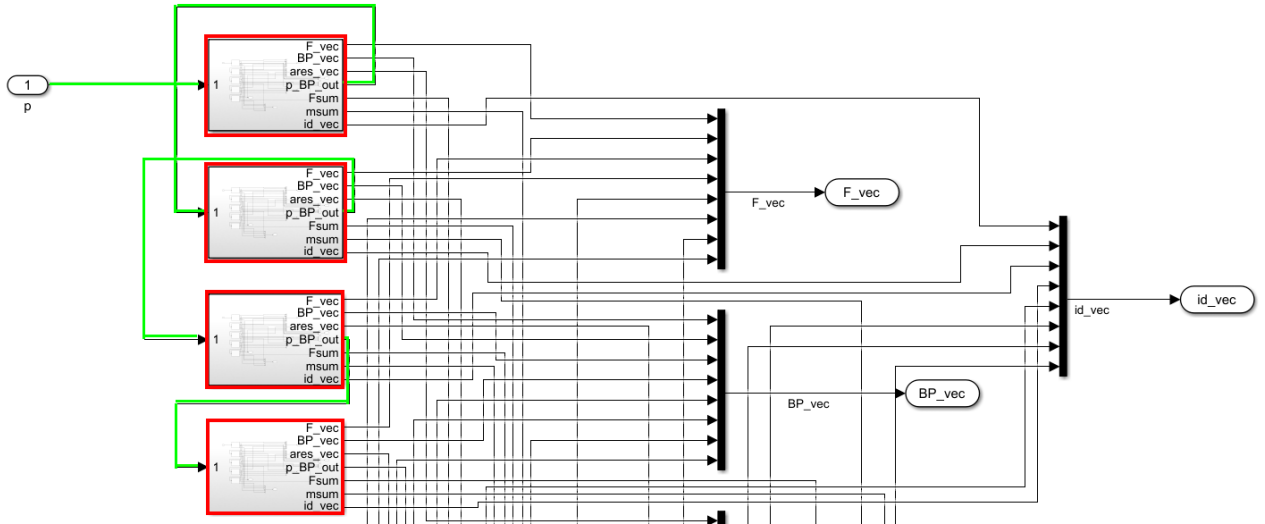


Figure 3.5: Expanded Model - Brake Pipe

Figure 3.5 shows how the wagons (marked by red rectangles) are interconnected by the brake pipe (marked by green arrows). This is analogous to how the wagons were connected in the initial model from section 3.2.

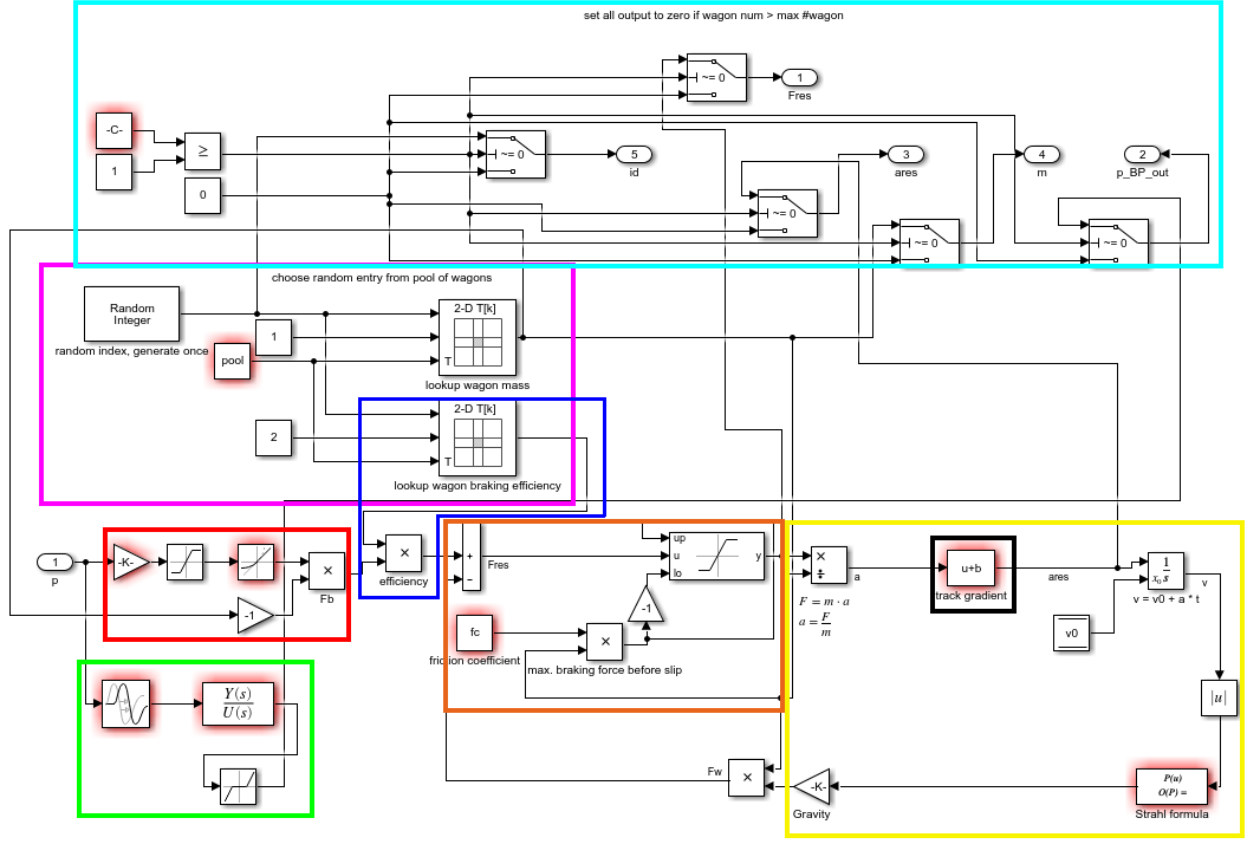


Figure 3.6: Expanded Model - Wagon

Figure 3.6 shows the expanded model of the freight wagon. There are components which have remained largely unchanged, while others have been added or altered to account for the changes required to implement \mathcal{M} . To recapitulate, the initial model's freight wagon comprised of three components: The brake cylinder \mathcal{M}_{bc} , the brake pipe \mathcal{M}_{bp} , and the driving resistance. The implementation of the brake pipe has remained largely unchanged, the only exception being the addition of a dead zone to filter out very small values of p_{bp} , ranging from -0.005 to 0.005 . This was necessary as these small values interfered with the simulation result in a negative way. The implementation of the brake pipe \mathcal{M}_{bp} is marked by the green rectangle.

The implementation of the brake cylinder \mathcal{M}_{bc} has also remained largely unchanged from the initial model, though the wagon's mass used to calculate $F_{b,max}$ is now read dynamically rather than being a static value (More on this later). The brake cylinder is marked by the red rectangle. The implementation of the calculation of the train's driving resistance has too remained unchanged except for the wagon's mass, used to determine the acceleration, being read dynamically, analogous to the brake cylinder. This component is marked by the yellow rectangle.

According to the definition of \mathcal{M} , the following factors still need to be accounted for: The wagon mass m , the train composition $comp$, the track gradient α , and the wheel/rail friction coefficient μ . It is therefore necessary to add new components implementing these to the wagon

model.

While the initial model's wagons did indeed have a mass, it had a static value, and it was the same for all 40 wagons, making them identical and indistinguishable from one another. This is of course undesirable as it poorly reflects reality. To make up for this flaw, a pool of 500 wagons has been randomly generated via python script:

```
import csv
import random

with open('pool.csv', 'w', newline='') as pool:
    fieldnames = ['Wagon_ID', 'Mass', 'Braking_eff']
    writer = csv.DictWriter(pool, fieldnames=fieldnames)

    writer.writeheader()
    for i in range(0,500):
        mass = random.randrange(12000, 90000, 100)
        braking_eff = round(random.uniform(0.75, 0.95),2)
        writer.writerow({'Wagon_ID': i, 'Mass': mass, 'Braking_eff': braking_eff
                          })
```

This creates a table with 500 entries of the following structure:

Wagon_ID	Wagon Mass	Braking Efficiency
0	53800	0.83
1	60800	0.77
...
499	66600	0.81

Each wagon contained in the pool is identifiable by its ID and has the properties wagon mass and braking efficiency, i.e. a characteristic for the integrity of its brakes. Both properties are randomly generated for each wagon, the mass being assigned a value between 12000 and 90000 kilograms (with a step size of 100 kilograms), and the braking efficiency following a uniform distribution between 75 and 95 percent integrity. In order to read the values from the table, during simulation, each of the 40 wagon subsystems generates a random index between 0 and 499, i.e. each wagon is assigned an ID. By utilizing two direct lookup table blocks, the row with the assigned ID is selected, and the corresponding values for mass and braking efficiency are read from the table. The implementation of this component is marked by the pink rectangle. The value of m is then used to calculate F_b , a , the driving resistance, the maximum braking force before slip, and the overall mass of the train m_{total} . The value of the braking efficiency is multiplied with F_b , meaning a lower integrity will result in a lower effective braking force.

Another requirement was to make the number of wagons variable. In the initial model, the modeled train had a fixed number of 40 wagons, therefore also 40 wagon subsystems.

Unfortunately, simulink offers no way to disable certain subsystems dynamically, but only by manually turning them off via model explorer, which would be unfeasible for such a large number of simulations. To circumvent this issue, output gets disabled for all unwanted wagons. For a simulation of a train of 20 wagons, the first 20 remain untouched, while the latter 20 produce no output and therefore also have no impact on the overall simulation. The turning off is achieved by simple switches; each wagon subsystem has a unique index from one to forty. If the index is greater than the specified number of wagons, all switches are turned to output zero.

3.4 Further Expansion

<TODO>

- more complex calculation of braking pressure, factoring in things like pad/block friction coefficient, brake radius etc
- curve resistance
- different braking systems

< / >

Chapter 4

Data Generation

Introduction With the finished model, it is now possible to generate the actual data, via simulation. For this purpose, a matlab script initializes all relevant model parameters and feeds the simulation input, in this case the previously discussed track profile, into the model.

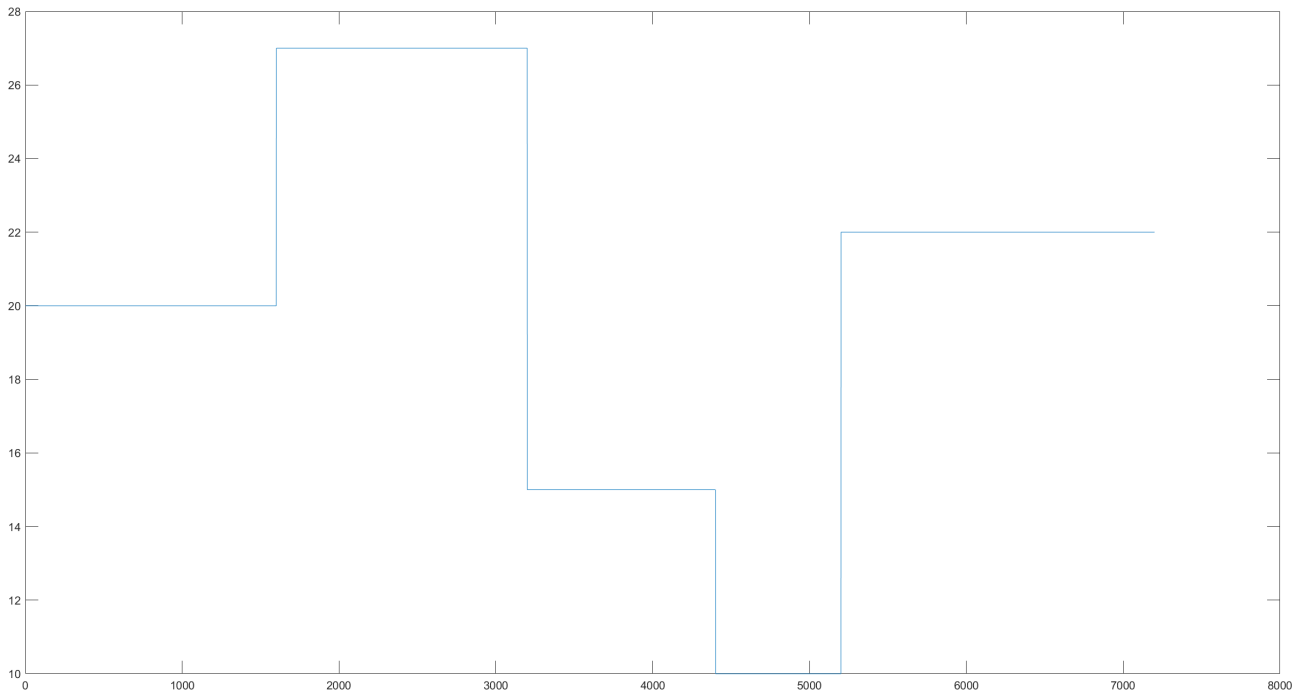


Figure 4.1: Simulation Input

Figure 4.1 visualizes how a track profile might look like. It stipulates the maximum allowed velocity for discrete points in time; the train either brakes or accelerates accordingly in order to match the corresponding value. An example: Let the simulation time be 1200 seconds, and $v_{max}(1200) = 20 \frac{m}{s}$. Let the train's velocity v be $25 \frac{m}{s}$. The train will engage its brakes (or continue braking, if they have already been engaged) in order to bring v down to $20 \frac{m}{s}$. If v were $15 \frac{m}{s}$, the train would accelerate instead.

4.1 Matlab Code

We need to do some general configuration first, like clearing the workspace off all output which might still be present from previous simulations.

```
clear all
clc
warning ('off','all');
numcores = 10;
```

We then need to initialise all constants which values remain the same for all simulations. Please refer to the code snippet below for descriptions:

<TODO> change all code environments to python, remove comments or make modification of package pythonhighlight for matlab </>

```
%% Constants

RBD = 5; % regular operations pressure (bar)
VBD = 3.5; % full breaking pressure (bar)

l = 18; % wagon length (meters)
c = 250; % propagation velocity (km/h)

tf = 4; % brake cylinder filling time
tl = .1;

p0 = 0; % initial pressure
Pres = 0/1000*[5.7/771 0 1.6]; % strahl formula for m/s velocity

alpha = 0.9;

BPnum = [0.3 alpha];
BPden = [1 alpha];

%% Simulation input
tmax = 3600; % simulation time (seconds)
nmax = tmax * 2; % number of data points
t = linspace(0, tmax, nmax); % simulation time input
u = [20*ones(800*2,1); 27*ones(800*2,1); 15*ones(600*2,1); 10*ones(400*2,1);
     22*ones(900*2,1); 0*ones(100*2,1)]; % track profile
simin.time = t; % set simulation time input
simin.signals.values = u; % set simulation signal input

trackgradient = 0; % pitch angle
```

After having initialised all necessary constants, we now get to configuring variable simulation input.

```

pool = readmatrix('pool.csv'); % read wagon pool
mkdir output; % make output directory

wagons = 1:1:40; % create array for number of wagons to loop over
friction = 0.05:0.01:0.78; % create array for friction coefficient to loop over
tracforce = 200000:1000:400000; % create array for traction force to loop over

track = 1; % counter to index input array for one batch of simulations
allruns = 1; % counter to keep track of total number of simulations completed

for i = length(tracforce):-1:1 % all possible combinations of traction force,
    for j = length(friction):-1:1 % friction coefficient and
        for k = length(wagons):-1:1 % number of wagons
            % save all previously initialised constans and sim input into
            % one array in
            in(track) = Simulink.SimulationInput('Simulation_v2');
            in(track) = in(track).setVariable('num_wagons',wagons(k));
            in(track) = in(track).setVariable('fc',friction(j));
            in(track) = in(track).setVariable('Ft',tracforce(i));

            in(track) = in(track).setVariable('alpha',alpha);
            in(track) = in(track).setVariable('BPden',BPden);
            in(track) = in(track).setVariable('BPnum',BPnum);
            in(track) = in(track).setVariable('c',c);
            in(track) = in(track).setVariable('l',l);
            in(track) = in(track).setVariable('nmax',nmax);
            in(track) = in(track).setVariable('p0',p0);
            in(track) = in(track).setVariable('pool',pool);
            in(track) = in(track).setVariable('Pres',Pres);
            in(track) = in(track).setVariable('RBD',RBD);
            in(track) = in(track).setVariable('simin',simin);
            in(track) = in(track).setVariable('t',t);
            in(track) = in(track).setVariable('tf',tf);
            in(track) = in(track).setVariable('tl',tl);
            in(track) = in(track).setVariable('tmax',tmax);
            in(track) = in(track).setVariable('trackgradient',trackgradient);
            in(track) = in(track).setVariable('u',u);
            in(track) = in(track).setVariable('VBD',VBD);

            % also save the respective values for traction force and
            % friction coefficient into arrays
            Ft(track) = tracforce(i);
            fc(track) = friction(j);
        end
    end
end

```

```

        track = track + 1;
    end
end

fprintf('Starting pool for %d simulation runs.\n',length(in));
parpool(numcores); % create a pool of #numcores workers for parallel processing
out = parsim(in,'ShowProgress','on');
% start parallel simulations for all
% entries of in, save output to out

matrix = []; % create an empty matrix

parfor l = 1:length(out)
    % parallel loop over out, which is an array that
    % holds all simulation outputs

    tmp = Write(l + allruns,out(l).get('velocity'),out(l).get('force'))
        ,out(l).get('pressure'),out(l).get('distance'),
        out(l).get('acceleration_neg'),out(l).get('ids'),t,u,
        trackgradient,Ft(l),fc(l)); % for each entry, pack all output into one
        single matrix
    matrix = [matrix;tmp]; % append to matrix
end

allruns = allruns + length(out); % update total number of simulations

writematrix(matrix,'output/output.tsv','FileType','text','WriteMode','append',
    'Delimiter','tab');
% write matrix, which holds all output matrices of the
% current batch, to a tsv file

track = 1; % reset batch index
delete(gcp('nocreate')); % delete parallel pool
fprintf('Run %d (of %d total) complete.\n',length(tracforce)-i,length(tracforce))
;
end

```

As our aim is to generate large quantities of data, it becomes feasible to use parallel processing for our simulations. For this purpose, we need to create an array to hold input for all simulation runs. There are three variables which change for each run, they are traction force of the locomotive, wheel/rail friction coefficient and number of wagons, respectively. A nested loop is used to create all possible combinations of these variables, and each single combination gets stored, as a new entry, in the array which holds all input.

Variable ranges are from one to 40 for number of wagons, .05 to .78 for friction coefficient

and 200000 to 400000 for traction force, with step sizes one, .01 and 1000 respectively. We therefore have a total number of $40 * 74 * 200 = 592000$ combinations. The obvious approach here would be to generate the full batch of 592000 input configurations, but performance and hardware limitations proved this to be unfeasible. Instead, we use rather small batch sizes of 2960 for parallel simulation.

Writing of the output is also done in smaller batches. The best approach to minimize the number of file accessions is of course writing everything into one big matrix, thus storing in RAM, and then writing the matrix in one go. Unfortunately, growing an array by assignment or concatenation can be expensive. For large arrays, MATLAB must allocate a new block of memory and copy the older array contents to the new array as it makes each assignment. The other extreme would of course be to write every single output line directly, but the large number of file accessions required makes this even more unfeasible, so a middle ground is needed, and a batch size of 3000 works relatively well, although this could surely be optimized with a bit of runtime analysis.

The function below compresses all output of one single simulation into one matrix. Raw simulation output consists of a few time-series objects, like braking force and braking pressure, as well as some metadata. These objects are fed into the write function, which does as many loops as there are rows in the time-series objects. It then packs all rows from each time-series into one big row, adds the meta-data and appends the large row to the matrix, which gets returned at the end. Refer to section 4.2 for a more detailed look at the structure of the output matrix.

```
function ret = Write(id,velocity,force,pressure,distance,acceleration,wagon_ids,t,u,
    grad,ft,fc)
    numrows = get(force,'Length');
    wagon_ids = double(wagon_ids);
    time = force.Time;
    matrix = [];

    for i = 1:1:numrows
        f = getdatasamples(force,i);
        p = getdatasamples(pressure,i);
        v = getdatasamples(velocity,i);
        a = getdatasamples(acceleration,i);
        d = getdatasamples(distance,i);

        row = [id,time(i),f,p,v,a,d,wagon_ids,grad,ft,fc]; % TODO: add simulation
            input aka track profile to matrix
        % print wagon ids as list delimited by colon (,)
        % performance?
        matrix = [matrix;row];
    end
    fprintf('Created output matrix for simid_%d\n',id);
    % writematrix(matrix,'output/output.tsv','FileType','text','WriteMode','append','
```

```

        Delimiter','tab');
% ret = 1;
% fprintf('Create output matrix for Simulation ID %d\n', id);
ret = matrix;
end

```

```

import csv
import random

with open('pool.csv', 'w', newline='') as pool:
    fieldnames = ['Wagon_ID', 'Mass', 'Braking_eff']
    writer = csv.DictWriter(pool, fieldnames=fieldnames)

    writer.writeheader()
    for i in range(0,500): # create 500 randomized wagons
        mass = random.randrange(12000, 90000, 100) # create random wagon mass
                                                    between 12 t and 90 t with step size
                                                    100
        braking_eff = round(random.uniform(0.75, 0.95),2) # create random
                                                            braking efficiency as uniform
                                                            distribution between 75 % and 95 %
        writer.writerow({'Wagon_ID': i, 'Mass': mass, 'Braking_eff': braking_eff
                        })

```

The above python script is used to create a randomized pool of 500 wagons to be used in simulation. Each wagon has a unique id, a randomized mass, ranging between 12000 and 90000 kilograms, and a braking efficiency, which is a uniform distribution between .75 and .95.

4.2 Data Structure

As has been denoted previously, generated data should be suitable for big data processing. The first approach was to create a new directory for each iteration, and also save the different parameters to different files. Since this is very inefficient in terms of number of file accessions and therefore negatively impacts performance, as well as being unsuitable for transformations to big data file systems like Apache Hadoop or Apache Hive, it has been proposed to write all output into one single file. Let's take a look at the structure first.

simID	Timestamp	F_{wagon0}	...	P_{wagon0}	...	v_{wagon0}	...	a_{wagon0}	...	Distance	Wagons	Tr

Some output objects are time-series, namely braking force, braking pressure, acceleration, distance and velocity. Force, pressure and acceleration, which get measured for every wagon, look like this

Timestamp	$Wagon_1$	$Wagon_2$...	$Wagon_{40}$
0	0	0	0	0
10	x_1	x_2	...	x_{40}
...
3600	y_1	y_2	...	y_{40}

whereas distance and velocity only have two columns and thus look like this

Timestamp	Value
0	0
..	..
3600	x

Since they all possess the same number of lines, which is the number of timestamps at which measurements were taken, all columns from all these objects may be compressed into a single table. All columns containing meta-information, for example simulation id, which theoretically only needs to be printed once, get filled with the same value for all lines, and since the number of wagons may vary from one to 40, all possibly empty columns get filled with zeros, so that we do not get any columns containing no value.

4.3 Analysis of generated Data

Chapter 5

Performance Analysis

Chapter 6

Conclusion

List of Figures

1.1	Spacing paradigms	12
1.2	Braking curves	13
3.1	Initial Model	24
3.2	Initial Model - Wagon	25
3.3	Expanded Model - Pressure Calculation	27
3.4	Expanded Model - Traction Force Calculation	28
3.5	Expanded Model - Brake Pipe	30
3.6	Expanded Model - Wagon.....	31
4.1	Simulation Input	35
B.1	Initial Model	53
B.2	Initial Model	54

List of Tables

Appendix A

Quellcode

1. Source 1
2. Source 2

Appendix B

Data visualization

<TODO> Visualisierungen einfügen </>

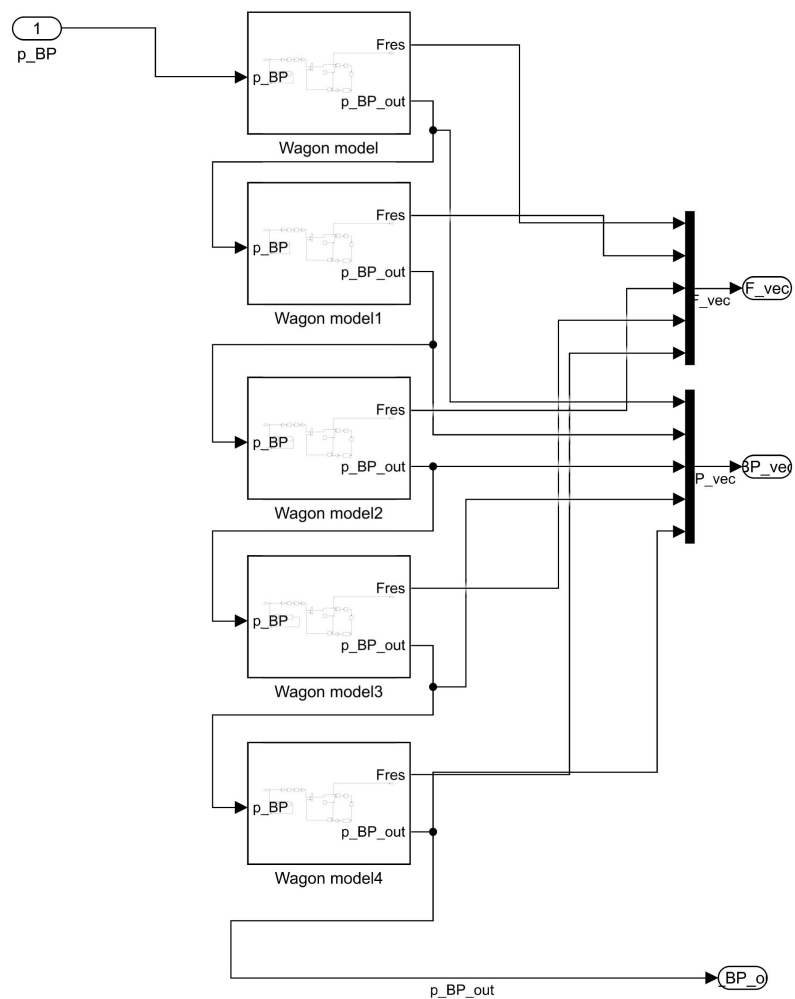


Figure B.1: Initial Model

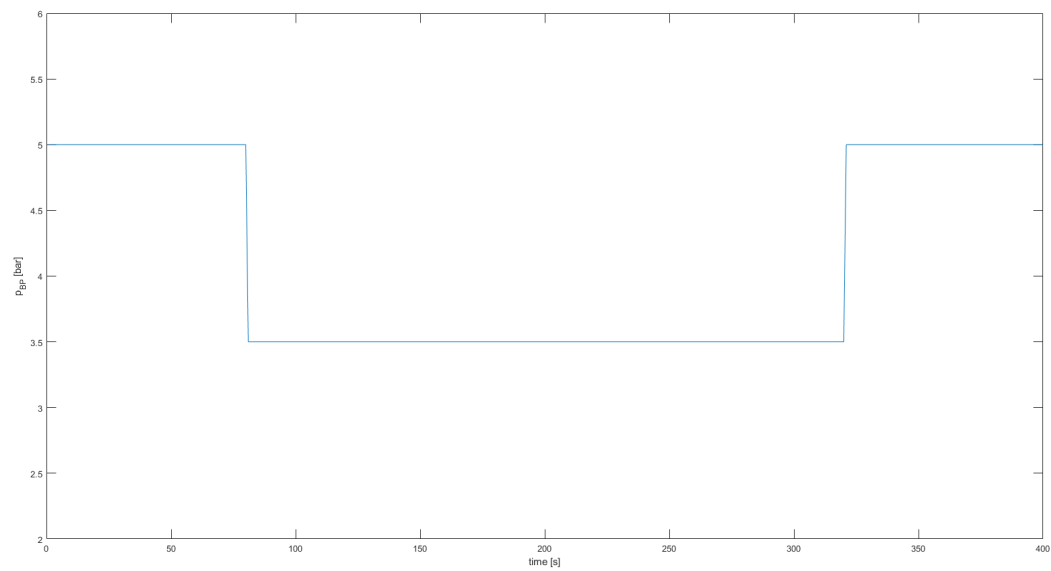


Figure B.2: Initial Model