

DAY – 3 : CRYPTOGRAPHY AND NETWORK SECURITY

12) Write a high level code for RSA system, the public key of a given user is $e = 31$, $n = 3599$. What is the private key of this user?

```
# define public key
```

```
e = 31
```

```
n=3599
```

```
# find p and q using factoring function
```

```
def factorize(n):
```

```
    for i in range(2, n):
```

```
        if n % i == 0:
```

```
            return i, n//i
```

```
p, q = factorize(n)
```

```
# calculate phi
```

```
phi = (p - 1) * (q - 1)
```

```
# find d such that  $e*d \equiv 1 \pmod{\phi}$ 
```

```
def extended_gcd(a, b):
```

```
    if b == 0:
```

```
        return a, 1, 0
```

```

else:
    d, x, y = extended_gcd(b, a % b)
    return d, y, x - (a // b) * y

d = extended_gcd(e, phi)[1]

# make sure d is positive
if d < 0:
    d += phi

# print private key
print("The private key is:", d)

```

RESULT :

The private key is: 3031

13) Write a high level code for set of blocks encoded with the RSA algorithm and we don't have the private key. Assume $n = pq$, e is the public key. Suppose also someone tells us they know one of the plaintext blocks has a common factor with n . Does this help us in any way?

```
import math
```

```
# Function to find the greatest common divisor (GCD) of two numbers
```

```
def gcd(a, b):
```

```
    if b == 0:
```

```
        return a
```

```
    else:
```

```
        return gcd(b, a % b)
```

```
# RSA public key
```

```
n = 13437231
```

```
e = 37
```

```
# Set of RSA-encoded blocks
```

```
ciphertext = [2314317, 3553782, 2855405, 5279019, 8534406,  
11797456, 4142155]
```

```
# Find p and q (the prime factors of n)
```

```
for i in range(2, int(math.sqrt(n))+1):
```

```
    if n % i == 0:
```

```
        p = i
```

```
        q = n // i
```

```
        break
```

```
# Find the ciphertext block with a common factor with n
```

```
for c in ciphertext:
```

```
    if gcd(c, n) != 1:
```

```
        common_factor = gcd(c, n)
```

```
        break
```

```
# Find the corresponding plaintext block
```

```
for c in ciphertext:
```

```
    if gcd(c, n) == common_factor:
```

```
        common_plaintext = pow(c, e, n) % common_factor
```

```
        break
```

```
# Find the factorization of the remaining part of n
```

```
if common_factor == p:
```

```
    remaining_factor = q
```

```
else:
```

```
    remaining_factor = p
```

```
# Decode the remaining ciphertext blocks
```

```
plaintext = []
```

```
for c in ciphertext:
```

```
    if gcd(c, n) == 1:
```

```
        plaintext.append(pow(c, e, n) // remaining_factor)
```

```
# Print the plaintext blocks
```

```
print("Decoded plaintext blocks:")  
for p in plaintext:  
    print(p)
```

RESULT :

Decoded plaintext blocks:

0

0

2