

Chem132A Discussion 3 Homework

Moises Romero (moiseser@uci.edu), Shane Flynn (swflynn@uci.edu)

10/15/17

1 Entropy

1.1 Entropy is a State Function

Entropy can be used to describe the disorder in a system. In class we defined the entropy to be:

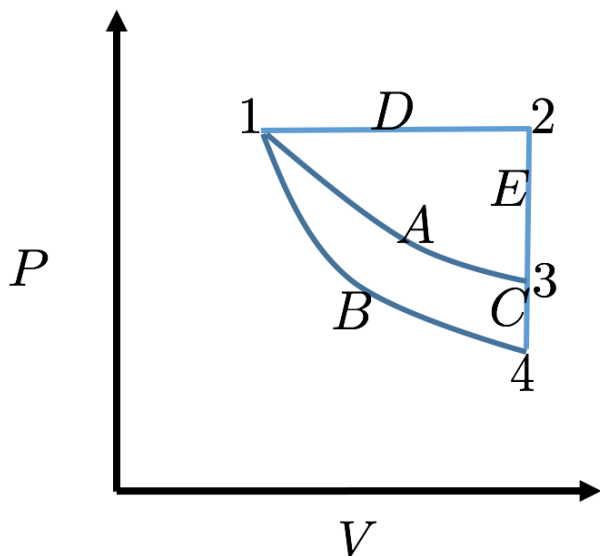
$$\Delta S \equiv \int \frac{\delta q_r}{T} \quad (1)$$

If we wish to consider irreversible processes, a more general description of the Entropy would be the inequality:

$$\Delta S \geq \int \frac{\delta q_r}{T} \quad (2)$$

Consider the following figure (it should look familiar from Discussion Problem Set 2).

Figure 1: Point 1: (P_1, V_1, T_1) , Point 2: (P_1, V_2, T_3) , Point 3: (P_2, V_2, T_1) , Point 4: (P_3, V_2, T_2)



This week we will explore the Second Law, again through the various pathways as defined in the diagram.

Consider a closed system containing 1 mole of gas. We will assume that the gas obeys the following Equation of State (x and y are constants).

$$\frac{P}{V} = \frac{RTx}{V} + \frac{RTy}{V} \quad (3)$$

For this question please compute the Entropy for 1 mole of gas traversing pathway A; take path A to be an isothermal expansion.

Next compute the Entropy for 1 mole of gas traversing pathways B and then C. Take path B to be a reversible adiabatic expansion and path C a reversible isochoric process.

Comment: We will assume that any gas obeying our equation of state has an internal energy that is only a function of Temperature; $U(T)$.

Finally: without doing any calculations associated with pathways D and E what can we say about the change in Entropy associated with traversing these pathways?

1.2 Entropy of a Free Expansion

A **Free Expansion** is an irreversible process which occurs when a gas expands into a vacuum. Because the gas expands into vacuum, there is no work done on/by the gas.

A gas at T is allowed to expand from V_1 to an end volume of V_2 . This is an irreversible process, and there is no heat transfer that occurs during the process: $q_{irr} = 0$.

Calculate the change in Entropy associated with one mole of gas undergoing this Free Expansion. Again we will assume the gas follows this Equation of State:

$$\frac{P}{V} = \frac{RTx}{V} + \frac{RTy}{V} \quad (4)$$

And that the gas has an Internal Energy that is only a function of T: $U(T)$.

2 Fundamental Equations

2.1 Internal Energy and Entropy

Consider a closed system, reversible expansion of an ideal gas assuming only PV work. Re-write the differential form of the First Law of Thermodynamics, by explicitly substituting in an expression for heat (in terms of Entropy). What variables do you find that Internal Energy naturally depends on from only the Two Laws of Thermodynamics: $U(?,?)$.

The work-flow for the question should look something like

$$\begin{aligned} dU &= \delta q + \delta w \\ dU &= \delta q + -PdV \\ &\dots \\ dU &=?d? + -PdV \end{aligned} \quad (5)$$

Write a total differential associated with each of these variables. Can you relate the partial derivatives of your total differential to the differential equation?

One of the partial derivatives you can write will be $U(?,V)$

$$\begin{aligned} dU &=?d? + \left(\frac{\partial U}{\partial V}\right)_? dV \\ &\Rightarrow \left(\frac{\partial U}{\partial V}\right)_? = -P \end{aligned} \quad (6)$$

2.2 Enthalpy and The First 2 Laws

Using your result from the previous problem, please determine the two natural variables associated with the Enthalpy, when considering the First and Second Law: $H(?,?)$.

Comment: Start with your definition of Enthalpy, and substitute the equation you find for dU from above.

Write a total differential associated with each of these variables. Can you relate the partial derivatives of your total differential to the differential equation?

2.3 Helmholtz and The First 2 Laws

Using the definition of the Helmholtz Free Energy determine the two natural variables associated with the Helmholtz, using the same process: $A(?,?)$

Write a total differential associated with each of these variables. Can you relate the partial derivatives of your total differential to the differential equation?

2.4 Gibbs as a Double Transformation

Using the definition of the Gibbs Free Energy determine the two natural variables associated with the Gibbs Free Energy: $G(?,?)$

Write a total differential associated with each of these variables. Can you relate the partial derivatives of your total differential to the differential equation?

3 Time to Type

The exam is just around the corner. Spend this week to start studying for the exam. Try working through your notes and the textbook to type up a formal study guide for the course. Think about including key definitions and their meaning, key equations and their conditions for being true, and highlight any sections of the course that you did not understand the first time around.

Any conceptual topics (and associated problems) that were particularly difficult should be revisited before the exam!