

SUMMER WORKSHOP IN MATHEMATICS

(SWIM@KSOM - 2025)

Algebra

(Problem Sheet 1)

1. Define subgroup generated by a set S . What is the subgroup generated by $[0, 1]$ in \mathbb{R} with respect to addition?
2. Prove any finitely generated subgroup of \mathbb{Q} is cyclic.
3. Identify the group $9\mathbb{Z} + 12\mathbb{Z}$.
4. Prove that intersection of subgroups is a subgroup. What about union?
5. What is the subgroup formed by intersection of $n\mathbb{Z} \cap m\mathbb{Z}$.
6. Find a finite subgroup of non-zero reals with multiplication as the group operation.
7. Find a group of order 3 of non-zero complex numbers with multiplication as the group operation.
8. Find a group of order n of non-zero complex numbers with multiplication as the group operation.