Teamnote of 2mic1cup

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1 Helpers

1.1 Stress Tester

Overview

Simple .bat file for stress testing.

Implementation

```
@echo off
   g++ -std=c++20 -o solution test.cpp
   g++ -std=c++20 -o brute brute.cpp
   g++ -std=c++20 -o gen gen.cpp
   for /1 %%x in (1, 1, 1000) do (
       gen > input.in
       solution < input.in > output.out
9
       brute < input.in > output2.out
       fc output.out output2.out > nul
10
11
       if ERRORLEVEL 1 (
12
13
            echo INPUT
            type input.in
14
15
            echo.
            echo SOLUTION OUTOUT
16
            type output.out
            echo.
18
            echo CORRECT OUTPUT
19
20
            type output2.out
21
            echo.
22
23 )
   echo all tests passed
```

1.2 Random

■ Overview

Self explanatory.

Implementation

1 Usage

• uid(a,b) returns random integer between [a,b]

2 Data Structure

2.1 Iterative Segment Tree

Overview

For-loop implementation of segment tree, faster than recursive. Note: Operation that depends on ordering is not supported (For example: Minimum prefix sum)

§ Time complexity: $\mathcal{O}(n)$ for constructor, $\mathcal{O}(\log n)$ for query

Implementation

```
template<typename T>
    struct SegmentTreeFast{
        vector<T> a;
3
        T defv:
        int n;
6
        SegmentTreeFast(int n, T defv) : n(n), defv(defv){
            a = vector < T > (2 * n, defv);
9
10
        T \ cmb(T \ a, \ T \ b){\it (//change if needed)}
11
12
            return a + b;
13
14
        void build(){ //array is at i + n index
15
            for (int i = n - 1; i > 0; --i)
16
                a[i] = cmb(a[i << 1], a[i << 1 | 1]);
17
18
19
        void update(int i, T v){
20
            for (a[i += n] = v; i > 1; i >>= 1)
21
22
                a[i >> 1] = cmb(a[i], a[i ^ 1]);
23
24
        T get(int 1, int r){
25
26
            T res = defv;
27
            for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1){
28
29
                if (1&1) res = cmb(res, a[1++]);
                if (r&1) res = cmb(res, a[--r]);
30
31
32
            return res;
34
   }:
35
```

2.2 Lazy Segment Tree

■ Overview

Segment tree that supports ranged update.

• Time complexity: $\mathcal{O}(n)$ for constructor, $\mathcal{O}(\log n)$ for query

⟨/> Implementation

```
template<typename T>
   class SegmentTreeLazy{
       vector<T> st, lazy;
       T defv;
       SegmentTreeLazy( \verb"int" n, T defv") : n(n), defv(defv) \{
            st = vectorT>(n * 4, defv);
            lazy = vector<T>(n * 4, defv);
10
11
12
        void update(int 1, int r, T v){
13
            _update(0, n - 1, 0, 1, r, v);
14
15
16
       T get(int 1, int r){
17
            return _get(0, n - 1, 1, r, 0);
18
```

```
}
19
20
   private:
21
        T cmb(T 1, T r){
22
23
            return 1 + r;
24
25
        void push(int i, int 1, int r){
   int mid = (1 + r) / 2;
26
27
             lazy[i * 2 + 1] += lazy[i];
28
            lazy[i * 2 + 2] += lazy[i];
29
30
             st[i * 2 + 1] += (mid - 1 + 1) * lazy[i];
             st[i * 2 + 2] += (r - mid) * lazy[i];
32
33
            lazy[i] = 0;
34
35
36
        void _update(int 1, int r, int crr, int q1, int qr,
37
            if (qr < 1 || ql > r)
38
39
                 return:
             if (1 >= q1 && r <= qr){</pre>
41
                 st[crr] += (r - 1 + 1) * v;
42
                 lazy[crr] += v;
43
44
45
46
            push(crr, 1, r);
             int mid = (1 + r) / 2;
48
             _update(1, mid, crr * 2 + 1, ql, qr, v);
49
             _{update(mid + 1, r, crr * 2 + 2, ql, qr, v);}
50
51
             st[crr] = cmb(st[crr * 2 + 1], st[crr * 2 + 2]);
52
53
        }
55
        T _get(int 1, int r, int q1, int qr, int crr){
            if (qr < 1 || ql > r)
56
57
                 return defv;
             if (1 >= q1 && r <= qr)</pre>
58
                 return st[crr];
59
60
             push(crr, 1, r);
             int mid = (1 + r) / 2;
62
            return cmb(_get(1, mid, q1, qr, crr * 2 + 1),
63
             \rightarrow _get(mid + 1, r, ql, qr, crr * 2 + 2));
64
   };
65
```

2.3 Sparse Table

Overview

Uses binary lifting for efficient queries, offline only.

§ Time complexity: $\mathcal{O}(n \log n)$ for constructor, $\mathcal{O}(1)$ for query

\'\> Implementation

```
lg = vector < int > (n + 1, 0);
9
10
               for (int i = 2; i <= n; i++)</pre>
              lg[i] = lg[i / 2] + 1;
for (int i = 0; i < n; i++){</pre>
11
12
                    f.push_back(vector<int>(lg[n] + 1, -1));
13
                    f[i][0] = init[i];
14
15
              for (int j = 1; (1 << j) <= n; j++){
   for (int i = 0; (i + (1 << j) - 1) < n; i++)</pre>
16
17
                         f[i][j] = cmb(f[i][j-1], f[i+(1 <<
18
                         \hookrightarrow (j - 1))][j - 1]);
19
              }
         }
20
21
         T get(int 1, int r){
22
               int k = lg[r - l + 1];
23
               return cmb(f[1][k], f[r - (1 << k) + 1][k]);</pre>
24
25
26 };
```

9 Usage

• Init minimum range query and uses integer type

```
SparseTable<int> rmq(a, [](int a, int b){
return min(a, b);
});
```

2.4 Implicit Treap

Overview

Implicit treap implementation with range add update and range sum query. push() and upd() functions should be changed accordingly like lazy segment tree.

§ Time complexity: $O(\log n)$ on average for all operations, large constant!!

⟨♦⟩ Implementation

```
typedef node* pnode;
   struct ImplicitTreap{
   public:
3
        pnode root;
        ImplicitTreap(){
            root = new node(-1, 0);
        void insert(int i, ll val){
            pnode t1, t2;
            split(root, i + 1, 0, t1, t2);
10
            merge(t1, t1, new node(val));
11
12
            merge(root, t1, t2);
13
        void erase(int i){
14
            _erase(root, i + 1, 0);
15
16
        }
        11 query(int 1, int r){
17
            pnode t1, t2, t3;
18
            split(root, r + 2, 0, t2, t3);
19
            split(t2, 1 + 1, 0, t1, t2);
20
21
            11 \text{ res} = t2 -> sum;
22
23
            merge(root, t1, t2);
            merge(root, root, t3);
24
25
```

```
26
            return res;
27
        void update(int 1, int r, 11 val){
28
            pnode t1, t2, t3;
29
            split(root, r + 2, 0, t2, t3);
30
            split(t2, 1 + 1, 0, t1, t2);
32
            t2->add += val;
33
            merge(root, t1, t2);
34
            merge(root, root, t3);
35
36
37
        void split(pnode t, int key, int add, pnode &1,
        → pnode &r){
            if (!t){
38
                1 = r = nullptr;
39
                return:
            }
41
            push(t);
42
            int impl_key = add + _cnt(t->1);
            if (key <= impl_key)</pre>
44
                split(t->1, key, add, l, t->l), r = t;
45
            else
46
47
                split(t->r, key, add + \_cnt(t->l) + 1, t->r,
                 \hookrightarrow r), 1 = t;
            upd(t);
48
        }
49
50
        void merge(pnode &t, pnode 1, pnode r){
51
52
            push(1); push(r);
            if (!1 || !r)
                t = 1? 1 : r;
54
            else if (l->prior > r->prior)
55
                merge(r->1, 1, r->1), t = r;
57
                merge(1->r, 1->r, r), t = 1;
58
59
            upd(t);
        }
60
61
   private:
        void _erase(pnode &t, int key, int add){
62
63
            push(t);
            int impl_key = add + _cnt(t->1);
64
            if (impl_key == key){
65
                pnode it = t;
66
                merge(t, t->1, t->r);
                delete it;
68
69
            else if (key < impl_key)</pre>
70
                _erase(t->1, key, add);
72
                 _erase(t->r, key, add + _cnt(t->l) + 1);
73
            upd(t);
75
        void push(pnode t){
76
            if (!t) return;
77
            t->sum += t->add * (11)_cnt(t);
            t->val += t->add;
79
            if (t->1) t->1->add += t->add;
80
            if (t->r) t->r->add += t->add;
82
            t->add = 0:
83
        }
        int _cnt(pnode t){
85
            if (!t) return 0;
86
87
            return t->cnt;
        11 _sum(pnode t){
89
            if (!t) return 0;
90
91
            push(t);
92
            return t->sum;
93
        void upd(pnode t){
94
            if (!t) return;
            t -> sum = t -> val + _sum(t -> 1) + _sum(t -> r);
96
            t \rightarrow cnt = _cnt(t \rightarrow 1) + _cnt(t \rightarrow r) + 1;
97
98
        }
99 };
```

2.5 Dynamic Segment Tree

Overview

Range queries and updates on larger range $(1 \le l \le r \le 10^9)$

Q Time complexity: $\mathcal{O}(\log M)$ for every operations, where M is max range

\'> Implementation

```
ll sum, tl, tr;
        Node *1 = nullptr, *r = nullptr;
3
        Node (ll _tl, ll _tr){
            tl = _tl;
tr = _tr;
6
            sum = 0;
9
10
11
        void extend(){
            if (tl == tr) return;
12
            11 \text{ mid} = (t1 + tr) / 2;
13
14
15
            if (!1)
                1 = new Node(t1, mid);
16
            if (!r)
17
18
                r = new Node(mid + 1, tr);
        }
19
20 };
21
22 class funkysegtree{
        void _upd(Node *node, 11 x, 11 val){
23
            node->sum += val;
24
            if (node->tl > x || node->tr < x)</pre>
25
26
                return;
            if (node->tl == node->tr)
27
28
                return:
29
            11 mid = (node->tl + node->tr) / 2;
30
            node->extend():
31
32
            if (x <= mid)
33
                _upd(node->1, x, val);
34
35
36
                _upd(node->r, x, val);
37
38
        11 _get(Node *node, 11 q1, 11 qr){
39
            if (qr < node->tl || ql > node->tr)
40
                return 0;
41
42
            else if (ql <= node->tl && qr >= node->tr)
43
44
                return node->sum;
45
            11 mid = (node->t1 + node->tr) / 2;
46
            node->extend();
47
48
            if (ql > mid)
49
50
                return _get(node->r, ql, qr);
51
            else if (qr <= mid)</pre>
               return _get(node->1, q1, qr);
52
            else
53
                return _get(node->1, ql, mid) +
54

    _get(node->r, mid + 1, qr);

        }
55
56
57
        Node *root = nullptr;
```

```
59
        ll _size;
60
        funkysegtree(ll __size){
61
            root = new Node(0, __size);
62
            _size = __size;
63
64
65
        void upd(ll x, ll val){
66
            _upd(root, x, val);
67
68
69
        ll get(ll l, ll r){
70
           return _get(root, 1, r);
72
73 };
```

2.6 Persistent Segment Tree

■ Overview

Preserving history for every segment tree updates.

1 Time complexity: $\mathcal{O}(\log N)$ for every operations

⟨/> Implementation

```
struct Vertex {
       Vertex *1, *r;
        int sum;
       Vertex(int val) : l(nullptr), r(nullptr), sum(val) {}
        \label{eq:Vertex} \mbox{Vertex *1, Vertex *r) : 1(1), r(r), sum(0) { } \\
            if (1) sum += 1->sum;
            if (r) sum += r->sum;
8
9
   };
10
11
   Vertex* build(ll a[], int tl, int tr) {
12
       if (tl == tr)
13
            return new Vertex(a[t1]);
14
        int tm = (tl + tr) / 2;
15
       return new Vertex(build(a, tl, tm), build(a, tm+1,
16

    tr));
  }
17
18
19
   int get_sum(Vertex* v, int tl, int tr, int l, int r) {
       if (1 > r)
20
21
            return 0;
        if (1 == tl && tr == r)
22
           return v->sum;
       int tm = (t1 + tr) / 2;
24
       return get_sum(v->1, t1, tm, 1, min(r, tm))
25
             + get_sum(v->r, tm+1, tr, max(l, tm+1), r);
  }
27
28
   Vertex* update(Vertex* v, int tl, int tr, int pos, int
29
    → new_val) {
       if (tl == tr)
30
31
            return new Vertex(new_val);
        int tm = (tl + tr) / 2;
32
        if (pos <= tm)</pre>
33
            return new Vertex(update(v->1, tl, tm, pos,
34

    new_val), v->r);
35
            return new Vertex(v->1, update(v->r, tm+1, tr,
36

→ pos, new_val));
37 }
```

0 Usage

• Init and update segment tree with n nodes, each function returns a pointer, save if needed for later.

• Query the segment tree at a specific moment.

```
1 ll res = get_sum(roots[x], 0, n - 1, 1, r);
```

2.7 2D Fenwick Tree

■ Overview

Query and update on a 2D array.

• Time complexity: $\mathcal{O}(\log^2 n)$ for every operations

⟨▶ Implementation

```
1 ll bit[1001][1001];
2
   ll n, m;
   void update(ll x, ll y, ll val){
            for (; y <= n; y += (y & (-y))){</pre>
5
                     for (11 i = x; i <= m; i += (i & (-i)))</pre>
6
                             bit[y][i] += val;
            }
8
   }
9
10
   11 query(11 x, 11 y){
11
            11 \text{ res} = 0;
12
            for (ll i = y; i; i -= (i & (-i)))
13
                     for (11 j = x; j; j -= (j & (-j)))
14
                             res += bit[i][j];
15
16
            return res;
   }
17
18
   ll query(ll x1, ll y1, ll x2, ll y2){
19
            11 res = query(x2, y2) - query(x1 - 1, y2) -
20
            \rightarrow query(x2, y1 - 1) + query(x1 - 1, y1 - 1);
            return res;
21
22
   }
```

8 Usage

- query(x, y) returns sum of value from (1,1) to (x,y).
- query(x1, y1, x2, y2) returns sum of value from (x1, y1) to (x2, y2).

2.8 Disjoint Set Union

Overview

Union disjoint set lol.

• Time complexity: $\mathcal{O}(\alpha(\mathbf{n}))$

⟨⟩ Implementation

```
struct DissjointSet{
        vector<int> p;
        int cnt = 0;
3
        DissjointSet(){}
6
        DissjointSet(int n){
            cnt = n;
            p = vector < int > (n, -1);
        }
10
        int find(int n){
11
            return p[n] < 0 ? n : p[n] = find(p[n]);</pre>
12
13
14
        void merge(int u, int v){
15
            if ((u = find(u)) == (v = find(v)))
                 return;
17
18
            cnt--
19
20
            if (p[v] < p[u])</pre>
                 swap(u, v);
21
22
            p[u] += p[v];
23
            p[v] = u;
24
        }
25
26 };
```

2.9 Line Container

Overview

Add lines of the form y = kx + m, and query maximum value at point x.

• Time complexity: $\mathcal{O}(\log n)$

Implementation

```
struct Line {
            mutable ll k, m, p;
2
             bool operator<(const Line& o) const { return k <</pre>
3
            bool operator<(ll x) const { return p < x; }</pre>
   };
   struct LineContainer : multiset<Line, less<>>> {
             // (for doubles, use inf = 1/.0, div(a,b) = a/b)
8
            11 div(11 a, 11 b) { // floored division
            return a / b - ((a ^ b) < 0 && a % b); }
bool isect(iterator x, iterator y) {
10
11
                     if (y == end()) return x->p = inf, 0;
12
                      if (x->k == y->k) x->p = x->m > y->m ?
13

    inf : -inf;

                      else x->p = div(y->m - x->m, x->k -
14
                      \hookrightarrow y->k);
                     return x->p >= y->p;
15
16
        //add line y = kx + m
17
             void add(ll k, ll m) {
18
                     auto z = insert({k, m, 0}), y = z++, x =
19
                      while (isect(y, z)) z = erase(z);
20
                      if (x != begin() && isect(--x, y))
21
                      \rightarrow isect(x, y = erase(y));
                      while ((y = x) != begin() \&\& (--x)->p >=
                      → y->p)
```

2.10 Lichao Tree

Overview

Add lines of the form y = ax + b, and query maximum value at point x, segment tree implementation.

• Time complexity: $\mathcal{O}(\log n)$

⟨⟩ Implementation

```
struct LichaoTree{
2
        struct Line{
            ll a, b;
            Line() : a(0), b(-inf) {}
4
            Line(ll a, ll b): a(a), b(b) {}
            11 get(11 x){
6
                return a * x + b;
       };
   public:
10
        vector<Line> st;
11
        LichaoTree(int n) : n(n){
13
            st.resize(4 * n):
14
16
        void add_line(Line line, int indx = 1, int l = 0,
        \hookrightarrow int r = -1){
            if (r == -1) r = n;
17
            int m = (1 + r) / 2;
18
            bool left = line.get(1) > st[indx].get(1);
19
20
            bool mid = line.get(m) > st[indx].get(m);
^{21}
            if (mid)
22
23
                swap(line, st[indx]);
            if (r - 1 == 1) return;
24
            else if (left != mid)
                add_line(line, 2 * indx, 1, m);
26
27
                add_line(line, 2 * indx + 1, m, r);
29
        ll query(ll x, int indx = 1, int l = 0, int r = -1){
30
31
            if (r == -1) r = n;
            if (r - l == 1) return st[indx].get(x);
32
            int mid = (1 + r) / 2;
33
            if (x < mid)
34
                return max(st[indx].get(x), query(x, 2 *
35

    indx, 1, mid));
            else
36
37
                return max(st[indx].get(x), query(x, 2 *
                 \hookrightarrow indx + 1, mid, r));
38
        }
   };
39
```

2.11 Ordered Set

■ Overview

A set that supports finding k-th maximum value, or getting the order of an element.

• Time complexity: $O(\log n)$, large constant

Implementation

1 Usage

 Uses just like a normal set, but with some added functions.

```
ordset<int> s;
s.insert(1);
s.insert(2);
s.insert(4);
s.find_by_order(0) //Returns 1
s.order_of_key(4) //Returns 2
```

2.12 Minimum Stack/Deque

Overview

Maintains minimum value in a stack/deque.

• Time complexity: $\mathcal{O}(\alpha(\mathbf{n}))$, large constant

⟨⟩ Implementation

```
struct minstack {
1
            stack<pair<int, int>> st;
2
            int getmin() {return st.top().second;}
            bool empty() {return st.empty();}
            int size() {return st.size();}
            void push(int x) {
                     int mn = x;
                     if (!empty()) mn = min(mn, getmin());
9
                     st.push({x, mn});
10
            void pop() {st.pop();}
            int top() {return st.top().first;}
12
13
            void swap(minstack &x) {st.swap(x.st);}
   };
15
   struct mindeque {
16
            minstack 1, r, t;
17
            void rebalance() {
18
                    bool f = false;
19
20
                     if (r.empty()) {f = true; l.swap(r);}
                     int sz = r.size() / 2;
21
                     while (sz--) {t.push(r.top()); r.pop();}
22
                     while (!r.empty()) {l.push(r.top());
23
                     \hookrightarrow r.pop();}
                     while (!t.empty()) {r.push(t.top());
24
                     \hookrightarrow t.pop();}
                     if (f) 1.swap(r);
            int getmin() {
27
```

```
if (1.empty()) return r.getmin();
28
29
                    if (r.empty()) return l.getmin();
                    return min(l.getmin(), r.getmin());
30
31
32
            bool empty() {return l.empty() && r.empty();}
            int size() {return l.size() + r.size();}
33
            void push_front(int x) {1.push(x);}
34
            void push_back(int x) {r.push(x);}
35
            void pop_front() {if (l.empty()) rebalance();
36
            → 1.pop();}
            void pop_back() {if (r.empty()) rebalance();
37
               r.pop();}
            int front() {if (l.empty()) rebalance(); return
38
            \hookrightarrow 1.top();}
            int back() {if (r.empty()) rebalance(); return
39
            → r.top();}
            void swap(mindeque &x) {1.swap(x.1);
40

    r.swap(x.r);}

41 };
```

2.13 Dynamic Bitset

Overview

Bitset with varied length support. NOTE: This requires relatively new version of GCC, and it might be BUGGED using the shift operator.

• Time complexity: O(n / 32)

⟨►⟩ Implementation

```
#include <tr2/dynamic_bitset>
using namespace tr2;
```

② Usage

• Init a dynamic bitset with length n.

```
dynamic_bitset<> bs;
bs.resize(n);
```

3 Graph

3.1 Graph

Overview

Helper class, some implementations below will use this.

⟨**/>>** Implementation

```
struct Graph{
vector<vector<int>> edg;
int n;

Graph(int n) : n(n){
    edg = vector<vector<int>>(n, vector<int>());
}

void add(int u, int v){
```

```
9
            edg[u].push_back(v);
10
        }
        void bi_add(int u, int v){
11
            edg[u].push_back(v);
12
13
            edg[v].push_back(u);
        void clear(){
15
            for (int u = 0; u < n; u++)</pre>
16
17
                edg[u].clear();
18
        void remove_dup(){
19
20
            for (int u = 0; u < n; u++){
                sort(edg[u].begin(), edg[u].end());
                edg[u].erase(unique(edg[u].begin(),
22
                    edg[u].end()), edg[u].end());
            }
24
   };
25
```

3.2 Tree

■ Overview

Helper class, some implementations below will use this.

⋄ Implementation

```
struct Tree{
       vector<vector<int>> edg;
2
        vector<int> par, depth;
       int n, root;
       Tree(int n, int root) : n(n), root(root){
            edg = vector<vector<int>>(n, vector<int>());
9
        void add(int u, int v){
            edg[u].push_back(v);
            edg[v].push_back(u);
11
12
        void clear(){
13
            for (int u = 0; u < n; u++)</pre>
                edg[u].clear();
15
16
        void remove_dup(){
            for (int u = 0; u < n; u++){
18
                sort(edg[u].begin(), edg[u].end());
19
                edg[u].erase(unique(edg[u].begin(),
20

    edg[u].end()), edg[u].end());

            }
21
22
       }
        void get_info(){
23
            par = depth = vector<int>(n, 0);
24
            par[root] = -1;
25
            dfs(root, -1);
27
        void dfs(int u, int pre){
28
29
            for (int v : edg[u]){
30
                if (v == pre) continue;
                par[v] = u; depth[v] = depth[u] + 1;
31
                dfs(v, u);
32
            }
33
34
35
  };
```

3.3 Strongly Connected Components

Overview

Find strongly connected components, compress the graph if needed

• Time complexity: $\mathcal{O}(N)$

⟨▶ Implementation

```
struct StronglyConnected{
        Graph &G;
        vector<vector<int>> components;
3
        vector<int> low, num, new_num;
4
        vector<bool> deleted;
        stack<int> st;
6
        int indx, scc, n;
        StronglyConnected(Graph &G) : G(G), n(G.n){
            low = num = new_num = vector<int>(n, 0);
10
            indx = scc = 0:
11
12
            deleted = vector<bool>(n, 0);
13
            for (int i = 0; i < n; i++){</pre>
14
                 if (!num[i])
15
                     dfs(i);
16
17
        }
18
        void dfs(int u){
20
            low[u] = num[u] = ++indx;
21
22
            st.push(u);
23
            for (int v : G.edg[u]){
24
                if (deleted[v]) continue;
25
                 if (!num[v]){
26
                     dfs(v);
27
                     low[u] = min(low[u], low[v]);
28
                }
29
                     low[u] = min(low[u], num[v]);
31
32
33
34
            if (low[u] == num[u]){
                int crr = -1;
35
36
                vector<int> cmp;
37
                 while (crr != u){
38
                     crr = st.top();
39
40
                     cmp.push_back(crr);
41
                     st.pop();
42
43
                     new_num[crr] = scc;
                     deleted[crr] = 1;
44
45
46
47
                 components.push_back(cmp);
48
                 scc++;
            }
49
        }
50
51
        void compress(){
52
            Graph _G(scc);
53
54
            for (int u = 0; u < n; u++){
                for (int v : G.edg[u]){
55
                     int _u = new_num[u], _v = new_num[v];
56
                     if (_u != _v)
57
                         _G.add(_u, _v);
                }
59
60
            G = _G;
61
        }
62
63 };
```

3.4 Bridges and Articulations

■ Overview

Find bridges and articulations!!

• Time complexity: O(N)

⟨⟩ Implementation

```
struct BridgeArt{
        Graph &G;
        vector<int> low, num, arts;
3
        vector<bool> isart;
        vector<pair<int, int>> bridges;
        int indx, n;
        {\tt BridgeArt(Graph \&G) : G(G), n(G.n)\{}
            indx = 0;
            low = num = vector<int>(n, 0);
10
            isart = vector<bool>(n, 0);
11
            for (int i = 0; i < n; i++){</pre>
13
                 if (!num[i])
14
15
                     dfs(i, i);
16
            for (int i = 0; i < n; i++){</pre>
17
                 if (isart[i])
18
19
                     arts.push_back(i);
            }
20
        }
21
22
        void dfs(int u, int pre){
            low[u] = num[u] = ++indx;
24
            int cnt = 0;
25
26
            for (int v : G.edg[u]){
                 if (v == pre) continue;
28
29
                 if (!num[v]){
                     dfs(v, u);
                     low[u] = min(low[u], low[v]);
31
                     cnt++;
32
                     if (u == pre){
33
                         if (cnt > 1)
34
                              isart[u] = 1;
35
                     }
36
                     else{
                          if (num[u] <= low[v])</pre>
38
                              isart[u] = 1;
39
40
                     }
41
                     if (num[v] == low[v])
                         bridges.push_back({u, v});
42
43
                 }
44
                 else
                     low[u] = min(low[u], num[v]);
45
            }
46
47
        }
48 };
```

3.5 Two SAT

■ Overview

Solve a system of boolean formula, where every clause has exactly two literals.

• Time complexity: $\mathcal{O}(N+M)$, M can be a slowing factor

Implementation

```
struct TwoSAT{
1
        vector<vector<int>> edg1, edg2;
2
        vector<int> scc, res;
        vector<bool> b;
        stack<int> topo;
5
        int n;
        TwoSAT(int n) : n(n){
 8
             edg1 = edg2 = vector<vector<int>>(2 * n);
9
             scc = res = vector < int > (2 * n, 0);
10
             b = vector < bool > (2 * n, 0);
11
12
13
        void dfs1(ll u){
14
             b[u] = 1;
15
             for (ll v : edg1[u]){
16
17
                 if (!b[v])
                      dfs1(v);
18
19
20
21
             topo.push(u);
^{22}
23
24
        void dfs2(ll u, ll root){
25
             scc[u] = root;
             for (11 v : edg2[u]){
26
                 if (scc[v] == -1)
27
                      dfs2(v, root);
29
        }
30
31
32
        bool solve(){
            for (int i = 0; i < 2 * n; i++){
33
                 scc[i] = -1;
34
35
                 if (!b[i])
                      dfs1(i);
36
             }
37
38
             int j = 0;
             while (siz(topo)){
40
                 11 u = topo.top();
41
                 topo.pop();
42
43
                 if (scc[u] == -1)
44
45
                      dfs2(u, j++);
46
47
             for (int i = 0; i < n; i++){</pre>
48
49
                 if (scc[i * 2] == scc[i * 2 + 1])
                      return 0;
50
                 res[i] = scc[i * 2] > scc[i * 2 + 1];
51
             }
52
53
             return 1;
54
        }
55
        void add(int x, bool a, int y, bool b){
  int X = x * 2 + (a & 1), Y = y * 2 + (b & 1);
57
58
             int _X = x * 2 + 1 - (a & 1), _Y = y * 2 + 1 -
59
             \hookrightarrow (b & 1);
60
61
             edg1[_X].push_back(Y);
             edg1[_Y].push_back(X);
62
             edg2[Y].push_back(_X);
63
             edg2[X].push_back(_Y);
64
        }
65
66 };
```

8 Usage

- The add(x, a, y, b) function add the clause (x OR y), where a, b signify whether x or y is negated or not.
- The solve() function returns 1 if there exist a valid assignment, and 0 otherwise. The valid assignment will then be stored in res.

3.6 MCMF

Overview

Find a maximum flow with minimum cost, SPFA implementation.

• Time complexity: $\mathcal{O}(N^3)$ with a bullshit factor

⟨⟩ Implementation

```
struct edge{
       int v;
       ll cost, capacity;
3
       edge* rv;
       edge(int v, ll cost, ll capacity) : v(v),
        };
6
   struct MCMF{
       vector<vector<edge*>> edg;
9
10
       vector<pair<int, edge*>> par;
       vector<ll> dis;
12
       MCMF(int n){
13
           edg = vector<vector<edge*>>(n);
15
       void add_edge(int u, int v, ll capacity, ll cost){
16
17
           edge* e = new edge(v, cost, capacity);
           edge* re = new edge(u, -cost, 0);
19
20
           e->rv = re;
           re->rv = e;
21
           edg[u].push_back(e);
23
24
           edg[v].push_back(re);
25
       void spfa(int start){
26
           int n = edg.size();
27
           auto inq = vec(n, 0);
           dis = vec(n, inf);
           par = vector<pair<int, edge*>>(n, {-1, nullptr});
30
31
           queue<int> q;
32
           q.push(start);
33
           dis[start] = 0;
34
35
           while (q.size()){
               int u = q.front(); q.pop();
37
               inq[u] = 0;
38
39
               for (auto e : edg[u]){
40
                   if (e->capacity > 0 && dis[e->v] >
41
                       dis[u] + e->cost){
                        dis[e->v] = dis[u] + e->cost;
42
                       par[e->v] = {u, e};
43
44
                        if (!inq[e->v]){
                            inq[e->v] = 1;
46
                            q.push(e->v);
47
                       }
                   }
49
50
```

```
51
        }
52
       pl get(int start, int end, ll max_flow = inf){
53
            11 flow = 0, cost = 0;
54
            while (flow < max_flow){</pre>
55
                spfa(start);
                if (dis[end] == inf) break;
57
58
                11 f = max_flow - flow;
59
                int u = end;
60
61
62
                while (u != start){
                     f = min(f, par[u].y->capacity);
                     u = par[u].x;
64
65
67
                flow += f;
                cost += f * dis[end];
68
69
70
                u = end;
                while (u != start){
71
                     par[u].y->capacity -= f;
72
73
                     par[u].y->rv->capacity += f;
                     u = par[u].x;
74
75
76
            if (flow == max_flow || max_flow == inf)
77
                return {flow, cost};
78
            else
79
80
                return {-1, -1};
81
   }:
82
```

3.7 Maximum Flow (Dinic)

■ Overview

Maximum flow using Dinic's algorithm.

 $\mbox{\bf 0}$ Time complexity: $\mathcal{O}(V^2E)$ for general graphs, but in practice $\approx \mathcal{O}(E^{1.5})$

⟨/> Implementation

```
template<int V, class T=long long>
   class max_flow {
            static const T INF = numeric_limits<T>::max();
            struct edge {
                    int t, rev;
                    T cap, f;
            };
   public:
10
            vector<edge> adj[V];
11
            11 dist[V];
13
            int ptr[V];
14
            bool bfs(int s, int t) {
15
                    memset(dist, -1, sizeof dist);
16
                    dist[s] = 0;
17
                     queue<int> q({ s });
18
19
                     while (!q.empty() && dist[t] == -1) {
                             int n = q.front();
20
                             q.pop();
21
22
                             for (auto& e : adj[n]) {
                                      if (dist[e.t] == -1 &&
                                      \hookrightarrow e.cap != e.f) {
24
                                              dist[e.t] =

→ dist[n] + 1;

                                              q.push(e.t);
25
```

```
26
27
28
                      return dist[t] != -1;
29
             }
30
             T augment(int n, T amt, int t) {
32
                      if (n == t) return amt;
33
                      for (; ptr[n] < adj[n].size(); ptr[n]++)</pre>
                               edge& e = adj[n][ptr[n]];
35
                               if (dist[e.t] == dist[n] + 1 &&
                               \hookrightarrow e.cap != e.f) {
                                        T flow = augment(e.t,
37
                                         \hookrightarrow min(amt, e.cap -
                                           e.f), t);
                                        if (flow != 0) {
38
                                                 e.f += flow;
39
                                                  adj[e.t][e.rev].
40
                                                  \hookrightarrow f -= flow;
                                                  return flow;
41
                                        }
42
                               }
43
                      return 0;
45
46
             }
47
             void add(int u, int v, T cap=1, T rcap=0) {
48
                      adj[u].push_back({ v, (int)
49
                      \rightarrow adj[v].size(), cap, 0 });
                      adj[v].push_back({ u, (int)
50
                      \rightarrow adj[u].size() - 1, rcap, 0 });
52
             T calc(int s, int t) {
53
                      T flow = 0:
54
                      while (bfs(s, t)) {
                               memset(ptr, 0, sizeof ptr);
56
                               while (T df = augment(s, INF, t))
57
                                        flow += df;
59
                      return flow;
60
             }
61
             void clear() {
63
                      for (int n = 0; n < V; n++)</pre>
64
65
                               adj[n].clear();
66
   };
67
```

3.8 Maximum Matching (Hopcroft Karp)

Overview

Find maximum matching on bipartite graph.

• Time complexity: $\mathcal{O}(m\sqrt{n})$ worst case

⋄ Implementation

```
struct HopcroftKarp{
    vector<vector<int>> edg;
    vector<int> U, V;

    vector<int> pu, pv;
    vector<int> dist;

//NOTE: This graph is 1-indexed!!!

HopcroftKarp(int n, int m){
    edg = vector<vector<int>>(n + 1);
    for (int i = 0; i < n; i++)
    U.push_back(i + 1);</pre>
```

```
for (int i = 0; i < m; i++)</pre>
12
13
                 V.push_back(i + 1);
14
            pu = vector < int > (n + 1, 0);
15
16
            pv = vector < int > (m + 1, 0);
17
             dist = vector<int>(n + 1, inf);
18
19
20
        void add_edge(int u, int v){
21
             edg[u].push_back(v);
22
23
        bool bfs(){
24
            queue<int> q;
25
            for (int u : U){
26
27
                 if (!pu[u]){
28
                     q.push(u);
                     dist[u] = 0;
29
                 }
30
31
32
                     dist[u] = inf;
33
            }
34
35
            dist[0] = inf;
36
             while (q.size() > 0){
37
                 int u = q.front();
38
                 q.pop();
39
40
41
                 if (dist[u] < dist[0]){</pre>
42
                      for (int v : edg[u]){
                          if (dist[pv[v]] == inf){
43
44
                              q.push(pv[v]);
45
                              dist[pv[v]] = dist[u] + 1;
46
                     }
47
48
                 }
            }
49
50
             if (dist[0] == inf)
51
                 return 0;
             return 1;
53
54
56
        bool dfs(ll u){
            if (u == 0) return 1;
57
            for (int v : edg[u]){
58
59
                 if (dist[pv[v]] == (dist[u] + 1)){
                      if (dfs(pv[v])){
60
                          pu[u] = v;
61
62
                          pv[v] = u;
                          return 1;
63
64
                 }
65
            }
67
            dist[u] = 0;
68
69
             return 0;
70
71
        int solve(){
72
             int res = 0;
73
             while (bfs()){
74
                 for (int u : U){
75
76
                      if (!pu[u])
                          if (dfs(u))
77
                              res++;
78
79
80
            }
81
            return res:
82
        }
83
   };
84
```

3.9 General Matching (Blossom)

Overview

Find maximum matching on general graph.

• Time complexity: $\mathcal{O}(n^3)$ worst case

⟨/> Implementation

```
struct Matching {
1
       int n:
       vector<vector<int>> g;
        vector<int> mt;
       vector<int> is_ev, gr_buf;
       vector<pi> nx;
        int st;
        int group(int x) {
            if(gr_buf[x] == -1 || is_ev[gr_buf[x]] != st)
9

→ return gr_buf[x];

            return gr_buf[x] = group(gr_buf[x]);
10
11
        void match(int p, int b) {
12
            int d = mt[p];
13
            mt[p] = b;
14
            if(d == -1 || mt[d] != p) return;
15
            if(nx[p].second == -1) {
16
                mt[d] = nx[p].first;
17
                match(nx[p].first, d);
18
            } else {
19
                match(nx[p].first, nx[p].second);
                match(nx[p].second, nx[p].first);
21
            }
22
23
        bool arg() {
24
            is_ev[st] = st;
25
            gr_buf[st] = -1;
26
            nx[st] = pi(-1, -1);
            queue<int> q;
28
            q.push(st);
29
30
            while(q.size()) {
                int a = q.front();
31
                q.pop();
32
33
                for(auto b : g[a]) {
                     if(b == st) continue;
                     if(mt[b] == -1) {
35
                         mt[b] = a:
36
                         match(a, b);
                         return true;
                     }
39
                     if(is_ev[b] == st) {
40
                         int x = group(a), y = group(b);
                         if(x == y) continue;
int z = -1;
42
43
                         while(x != -1 | | y != -1) {
44
                             if(y != -1) swap(x, y);
                             if(nx[x] == pi(a, b)) {
46
47
                                 z = x;
                                 break;
49
                             nx[x] = pi(a, b);
50
                             x = group(nx[mt[x]].first);
51
                         for(int v : {group(a), group(b)}) {
53
                             while(v != z) {
54
                                 q.push(v);
                                 is_ev[v] = st;
56
                                 gr_buf[v] = z;
57
                                 v = group(nx[mt[v]].first);
60
                     } else if(is_ev[mt[b]] != st) {
61
                         is_ev[mt[b]] = st;
62
                         nx[b] = pi(-1, -1);
63
                         nx[mt[b]] = pi(a, -1);
64
```

```
gr_buf[mt[b]] = b;
65
                          q.push(mt[b]);
66
67
                }
68
            }
69
            return false;
70
71
        Matching(const vector<vector<int>> &_g) :
72
        \rightarrow n(int(_g.size())), g(_g), mt(n, -1), is_ev(n,
            -1), gr_buf(n), nx(n) {
            for(st = 0; st < n; st++)</pre>
73
74
                 if(mt[st] == -1) arg();
75
        vector<pi> max match() {
76
77
            vector<pi> res;
            for (int i = 0; i < n; i++){
78
                 if(i < mt[i])
79
                     res.push_back({i, mt[i]});
80
81
            }
            return res;
82
        }
83
84
  };
```

4 Math

4.1 Modular Int

Overview

Helper class, some implementations below will use this.

⟨⟩ Implementation

```
template<11 mod = 1000000007>
1
2
   struct modu{
       ll val;
       modu(ll x){
4
           val = x;
5
            val %= mod;
            if (val < 0) val += mod;</pre>
7
8
       modu(){ val = 0; }
9
10
        operator 11() const { return val; }
11
       modu operator+(modu const& other){ return val +
12
        modu operator-(modu const& other){ return val -
13
        → other.val; }
       modu operator*(modu const& other){ return val *
14

    other.val; }

       modu operator/(modu const& other){ return *this *
15

    other.inv(); }

       modu operator+=(modu const& other) { *this = *this +
16
        → other; return *this; }
       modu operator-=(modu const& other) { *this = *this -

    other; return *this; }

       modu operator*=(modu const& other) { *this = *this *
18

    other; return *this; }

       modu operator/=(modu const& other) { *this = *this /
19
        → other; return *this; }
       modu operator++(int) {modu tmp = *this; *this += 1;

    return tmp;
}
       modu operator++() {*this += 1; return *this;}
21
       modu operator--(int) {modu tmp = *this; *this -= 1;
22
        \hookrightarrow return tmp;}
       modu operator--() {*this -= 1; return *this;}
23
24
       modu operator-() {return modu(-val);}
        friend ostream& operator<<(ostream& os, modu const&</pre>
        \hookrightarrow m) { return os << m.val; }
```

```
friend istream& operator>>(istream& is, modu & m) {
26

    return is >> m.val; }

27
       modu pow(11 x) const{
28
29
            if (x == 0)
30
                return 1;
            if (x \% 2 == 0){
31
                modu tmp = pow(x / 2);
32
                return tmp * tmp;
34
            else
35
36
                return pow(x - 1) * *this;
38
       modu inv() const{ return pow(mod - 2); }
39
```

4.2 Modular Square Root

Overview

Operations on field

$$\langle u, v \rangle = u + v\sqrt{k} \mod p$$

⟨▶ Implementation

```
11 MOD = 999999893;
2 11 sq = 2;
   class EX {
4
     int re, im;
     static int trim(int a) {
       if (a >= MOD) a -= MOD;
       if (a < 0) a += MOD;</pre>
9
       return a;
10
     static int inv(const int a) {
11
12
       int ans = 1;
       for (int cur = a, p = MOD - 2; p; p >>= 1, cur = 111
       if (p&1) ans = 111 * ans * cur % MOD;
14
15
16
       return ans;
     };
17
   public:
18
     EX(int re = 0, int im = 0) : re(re), im(im) {}
     EX& operator=(EX oth) { return re = oth.re, im =
20

    oth.im, *this; }

     int norm() const {
21
       return trim((111 * re * re - 111 * sq * im % MOD *
22
       \hookrightarrow im) % MOD);
23
     EX conj() const {
24
       return EX(re, trim(MOD - im));
25
26
     EX operator*(EX oth) const {
27
       return EX((111 * re * oth.re + 111 * sq * im % MOD *
28

→ oth.im) % MOD,

                  (111 * re * oth.im + 111 * im * oth.re) %

→ MOD);
30
     EX operator/(int n) const {
31
       return EX(111 * re * inv(n) % MOD, 111 * im * inv(n)
32
       \hookrightarrow % MOD);
33
     EX operator/(EX oth) const { return *this * oth.conj()
```

```
EX operator+(EX oth) const { return EX(trim(re +
35
      → oth.re), trim(im + oth.im)); }
     EX operator-(EX oth) const {
36
       return EX(trim(re - oth.re), trim(im - oth.im));
37
38
39
     EX pow(long long n) const {
       EX ans(1);
40
        for (EX a = *this; n; n >>= 1, a = a * a) {
41
         if (n&1) ans = a * ans;
42
43
       return ans:
44
45
     bool operator==(EX oth) const { return re == oth.re
46

    and im == oth.im; }

     bool operator!=(EX oth) const { return not (*this ==
47
      \hookrightarrow oth): }
     int real() const& { return re; }
48
     int imag() const& { return im; }
49
```

4.3 Discrete Log

Overview

Given a, b, m, find any x that satisfy

```
a^x = b \mod m
```

• Time complexity: $\mathcal{O}(N \log \log N)$

⟨**/>>** Implementation

```
// Returns minimum x for which a \hat{x} \% m = b \% m.
   int solve(int a, int b, int m) {
2
        a \%= m, b \%= m;
3
        int k = 1, add = 0, g;
        while ((g = gcd(a, m)) > 1) {
            if (b == k)
                 return add;
            if (b % g)
9
                 return -1;
            b /= g, m /= g, ++add;
k = (k * 111 * a / g) % m;
10
11
12
        int n = sqrt(m) + 1;
14
        int an = 1;
15
        for (int i = 0; i < n; ++i)</pre>
16
             an = (an * 111 * a) % m;
17
18
19
        unordered_map<int, int> vals;
        for (int q = 0, cur = b; q <= n; ++q) {</pre>
20
            vals[cur] = q;
21
             cur = (cur * 111 * a) % m;
22
23
24
        for (int p = 1, cur = k; p <= n; ++p) {</pre>
25
             cur = (cur * 111 * an) % m;
26
             if (vals.count(cur)) {
                 int ans = n * p - vals[cur] + add;
28
                 return ans;
29
30
            }
31
        return -1:
32
33 }
```

4.4 Primite Root

■ Overview

Given a, n, find g so that for any a such that gcd(a, n) = 1, there exists k such that

$$g^k = a \mod n$$

• Time complexity: $\mathcal{O}(Ans \cdot \log \phi(n) \cdot \log n)$)

⟨**/>>** Implementation

```
int powmod (int a, int b, int p) {
1
        int res = 1;
2
        while (b)
            if (b & 1)
                res = int (res * 111 * a % p), --b;
            else
                a = int (a * 111 * a % p), b >>= 1;
        return res;
9
   }
10
   int generator (int p) {
11
        vector<int> fact;
12
        int phi = p-1, n = phi;
13
        for (int i=2; i*i<=n; ++i)</pre>
14
            if (n % i == 0) {
15
                fact.push_back (i);
16
                while (n \% i == 0)
                    n /= i;
18
            }
19
        if (n > 1)
20
            fact.push_back (n);
22
        for (int res=2; res<=p; ++res) {</pre>
23
24
            bool ok = true;
            for (size_t i=0; i<fact.size() && ok; ++i)</pre>
                ok &= powmod (res, phi / fact[i], p) != 1;
26
27
            if (ok) return res;
        }
        return -1;
29
  }
30
```

4.5 Euler's Totient Funnction

■ Overview

Find $\phi(i)$ for i from 1 to N.

• Time complexity: $\mathcal{O}(N \log \log N)$

⟨**/>>** Implementation

```
int phi[def];
void phi(int n) {
    phi[0] = 0;
    phi[1] = 1;
    for (int i = 2; i <= n; i++)
        phi[i] = i - 1;

for (int i = 2; i <= n; i++)
    for (int j = 2 * i; j <= n; j += i)
        phi[j] -= phi[i];
}</pre>
```

4.6 Chinese Remainder Theorem

Overview

Given a system of congruences

```
a = a_1 \mod M_1, a = a_2 \mod M_2, \dots
```

where M_i might not be pairwise coprime, find any a that satisfy it.

• Time complexity: $\mathcal{O}(N \log \max(M_i))$

⟨♦⟩ Implementation

```
typedef __int128_t i128;
    i128 exeuclid(i128 a, i128 b, i128& x, i128& y){
        if (b == 0) {
            x = 1;
            y = 0;
            return a;
        }
        i128 x1, y1;
        i128 d = exeuclid(b, a % b, x1, y1);
10
        x = y1;
        y = x1 - y1 * (a / b);
11
        return d;
^{12}
13
14
15
   struct CBT{
        i128 A = 0, M = 0;
16
        void add(i128 a, i128 m){
17
            a = ((a \% m) + m) \% m;
18
            i128 _M = M;
19
            if (M == 0){
20
                A = a, M = m;
21
22
                return;
            if (A == -1) return;
24
            i128 p, q;
25
26
            i128 g = exeuclid(M, m, p, q);
            if ((a - A) % g != 0){
27
                A = -1, M = -1;
28
29
                return;
30
            i128 \text{ mul} = (a - A) / g;
31
            M = m * M / g;
32
            A = (((_M * p * mul + A) % M) + M) % M;
33
        }
34
35 };
```

8 Usage

- The add(x,y) function add the condition $a = x \mod y$.
- If $a \neq -1$, the solution a will satisfy $a = A \mod M$.

4.7 Extended Euclidean

■ Overview

Given a, b, find any x, y that satisfy

$$ax + by = gcd(a, b)$$

Note that the function pass x, y by reference and returns $\gcd(a, b)$.

• Time complexity: $\mathcal{O}(\log n)$

⟨⟩ Implementation

```
int extended_euclid(int a, int b, int& x, int& y) {
    if (b == 0) {
        x = 1;
        y = 0;
        return a;
    }
    int x1, y1;
    int d = extended_euclid(b, a % b, x1, y1);
    x = y1;
    y = x1 - y1 * (a / b);
    return d;
}
```

4.8 Linear Diophantine

■ Overview

Given a, b, c, find any x, y that satisfy

$$ax + by = c$$

• Time complexity: $\mathcal{O}(\log n)$

Implementation

4.9 Matrix

Overview

Matrix helper class.

⟨→ Implementation

```
template <typename T>
   struct Matrix{
       vector<vector<T>> m;
       Matrix (vector<vector<T>> &m) : T(m){}
       Matrix (int r, int c) {
           m = vector<vector<T>>(r, vector<T>(c));
        int row() const {return m.size();}
       int col() const {return m[0].size();}
10
11
        static Matrix identity(int n){
^{12}
            Matrix res = Matrix(n, n);
13
            for (int i = 0; i < n; i++)</pre>
14
```

```
res[i][i] = 1;
15
16
             return res;
17
18
        auto & operator [] (int i) { return m[i]; }
19
        const auto & operator[] (int i) const { return m[i];
20
21
        Matrix operator * (const Matrix &b){
22
             Matrix a = *this;
23
             assert(a.col() == b.row());
24
25
             Matrix c(a.row(), b.col());
26
             for (int i = 0; i < a.row(); i++)
    for (int j = 0; j < b.col(); j++)</pre>
27
28
                     for (int k = 0; k < a.col(); k++)</pre>
                          c[i][j] += a[i][k] * b[k][j];
30
             return c:
31
        }
32
33
        Matrix pow(ll x){
34
             assert(row() == col());
35
36
             Matrix crr = *this, res = identity(row());
             while (x > 0){
37
38
                 if (x % 2 == 1)
39
                      res = res * crr;
                 crr = crr * crr;
                 x /= 2;
41
             }
42
43
             return res;
        }
44
45 };
```

4.10 Miller Rabin Primality Test

Overview

Deterministic implementation of Miller Rabin.

• Time complexity: Should be fast

⟨/> Implementation

```
ll binpower(ll base, ll e, ll mod) {
       11 result = 1;
        base %= mod;
3
        while (e) {
            if (e & 1)
               result = (__int128_t)result * base % mod;
            base = (__int128_t)base * base % mod;
            e >>= 1:
10
        return result;
11 }
12
   bool check_composite(ll n, ll a, ll d, int s) {
13
        11 x = binpower(a, d, n);
14
        if (x == 1 | | x == n - 1)
15
           return false;
17
        for (int r = 1; r < s; r++) {</pre>
            x = (_int128_t)x * x % n;
18
19
            if (x == n - 1)
20
                return false;
21
22
        return true:
   };
23
24
   bool MillerRabin(ll n) { // returns true if n is prime,
25

→ else returns false.

        if (n < 2)
26
27
            return false;
```

```
28
       int r = 0;
29
       11 d = n - 1;
30
       while ((d & 1) == 0) {
31
           d >>= 1;
32
           r++;
34
35
       for (int a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29,
36
        if (n == a)
37
38
               return true;
            if (check_composite(n, a, d, r))
39
               return false:
40
       }
41
       return true;
43
```

4.11 Fast Fourier Transform

Overview

multiplymod(A, B, M) returns C where

$$C[u] = \sum_{i=1}^{|A|} \sum_{j=1}^{|B|} A_i \cdot B_j \mod M \ (i+j=u)$$

• Time complexity: $\mathcal{O}(n \log n)$

⟨⟩ Implementation

```
using cpx = complex<double>;
    const double PI = acos(-1);
    vector<cpx> roots = {{0, 0}, {1, 0}};
    void ensure_capacity(int min_capacity) {
        for (int len = roots.size(); len < min_capacity; len</pre>
           *= 2) {
             for (int i = len >> 1; i < len; i++) {</pre>
                 roots.emplace_back(roots[i]);
                 double angle = 2 * PI * (2 * i + 1 - len) /
 9
                  \hookrightarrow (len * 2):
                 roots.emplace_back(cos(angle), sin(angle));
10
             }
11
        }
12
   }
13
14
    void fft(vector<cpx> &z, bool inverse) {
15
16
        int n = z.size();
        assert((n & (n - 1)) == 0);
17
        ensure_capacity(n);
18
        for (unsigned i = 1, j = 0; i < n; i++) {</pre>
19
             int bit = n >> 1;
20
             for (; j >= bit; bit >>= 1)
21
             j -= bit;
j += bit;
22
23
             if (i < j)
                 swap(z[i], z[j]);
25
26
        for (int len = 1; len < n; len <<= 1) {</pre>
             for (int i = 0; i < n; i += len * 2) {</pre>
28
                 for (int j = 0; j < len; j++) {
    cpx root = inverse ? conj(roots[j +</pre>
29
30

    len]) : roots[j + len];

                      cpx u = z[i + j];
31
                      cpx v = z[i + j + len] * root;
32
                      z[i + j] = u + v;
33
                      z[i + j + len] = u - v;
34
35
```

```
36
       }
37
        if (inverse)
38
            for (int i = 0; i < n; i++)</pre>
39
40
                z[i] /= n;
   }
41
   vector<int> multiply_mod(const vector<int> &a, const
42
       vector<int> &b, int m) {
        int need = a.size() + b.size() - 1;
43
44
        int n = 1;
        while (n < need)
45
46
           n <<= 1;
        vector<cpx> A(n);
47
        for (size_t i = 0; i < a.size(); i++) {</pre>
48
            int x = (a[i] % m + m) % m;
49
            A[i] = cpx(x & ((1 << 15) - 1), x >> 15);
51
       fft(A, false):
52
53
54
        vector<cpx> B(n);
        for (size_t i = 0; i < b.size(); i++) {</pre>
55
            int x = (b[i] % m + m) % m;
56
57
            B[i] = cpx(x & ((1 << 15) - 1), x >> 15);
58
59
        fft(B. false):
60
        vector<cpx> fa(n);
61
        vector<cpx> fb(n);
62
        for (int i = 0, j = 0; i < n; i++, j = n - i) {
63
            cpx a1 = (A[i] + conj(A[j])) * cpx(0.5, 0);
            cpx a2 = (A[i] - conj(A[j])) * cpx(0, -0.5);
65
            cpx b1 = (B[i] + conj(B[j])) * cpx(0.5, 0);
66
            cpx b2 = (B[i] - conj(B[j])) * cpx(0, -0.5);
67
            fa[i] = a1 * b1 + a2 * b2 * cpx(0, 1);
68
            fb[i] = a1 * b2 + a2 * b1;
69
       }
70
71
72
       fft(fa, true);
       fft(fb, true);
73
74
        vector<int> res(need);
        for (int i = 0; i < need; i++) {</pre>
75
            long long aa = (long long)(fa[i].real() + 0.5);
76
            long long bb = (long long)(fb[i].real() + 0.5);
77
            long long cc = (long long)(fa[i].imag() + 0.5);
79
            res[i] = (aa % m + (bb % m << 15) + (cc % m <<

→ 30)) % m;

80
       }
81
        return res;
82 }
```

4.12 OR Convolution

■ Overview

convolute or(A, B) returns C where

$$C[u] = \sum_{i=1}^{|A|} \sum_{j=1}^{|B|} A_i \cdot B_j \mod M \ (i|j=u)$$

• Time complexity: $\mathcal{O}(2^N \cdot N)$

\'\> Implementation

```
b[j] += b[j - (1 << i)];
            }
8
        for (int i = n - 1; i >= 0; i--){
9
            for (int j = (1 << n) - 1; j >= 0; j--){
10
                if ((j >> i) & 1)
11
                     a[j] -= a[j - (1 << i)];
12
            }
13
        }
14
        auto c = vector<int>(n, 0);
15
        for (int i = n - 1; i < (1 << n); i++)
c[i] = a[i] * b[i];
16
17
        for (int i = n - 1; i >= 0; i--){
18
            for (int j = (1 << n) - 1; j >= 0; j--){
19
                if ((j >> i) & 1)
20
                     c[j] = c[j - (1 << i)];
21
22
        }
23
  }
24
```

4.13 XOR Convolution

■ Overview

idk lol.

⟨**/>>** Implementation

```
void xorconv(vector<int> &a,int modul){ // chuyen tu dang
    \leftrightarrow binh thuong sang dang dac biet, xong cu lay a[i] =
        b[i] * c[i]
        int n = a.size();
 2
        for(int m = n/2; m; m/=2){
 3
             for(int i = 0; i < n; i+= 2 * m){
                 for(int j = 0; j < m; ++ j){
                      int x = a[i + j];
                      int y = a[i + j + m];
                      a[i + j] = (x + y) \text{modul};
                      a[i + j + m] = (x-y+modul) \% modul;
 9
                 }
10
            }
11
        }
12
13 }
    void xorconv2(vector<int> &a,int modul){ // chuyen tu
14

→ dang dac biet ve dang binh thuong ⇒ dap an sau khi

15
        int n = a.size();
        for(int m = 1; m<n; m*=2){</pre>
16
            for(int i = 0; i < n; i+= 2 * m){
    for(int j = 0; j < m; ++ j){
17
18
                      int x = a[i + j];
19
                      int y = a[i + j + m];
20
                      a[i + j] = (x + y) \text{modul};
21
                      a[i + j + m] = (x-y+modul) \% modul;
22
                 }
            }
24
        }
25
26
        for(int i = 0;i<n;++i){</pre>
             a[i] = 1LL * (ll)a[i] * binpow(n,modul - 2,
27

    modul) %modul;

28
29 }
```

5 String

5.1 Rolling Hash

Overview

Rolling hash implementation, use multiple mod if necessary.

• Time complexity: $\mathcal{O}(N)$

⟨→ Implementation

```
struct hashu{
1
           11 n;
2
3
           vector<dd> p, h;
           hashu(string s){
5
                    n = s.size();
6
                    p = vector < dd > (n + 1);
                    h = vector < dd > (n + 1);
8
9
10
                    p[0] = \{1, 1\};
                    for (int i = 1; i <= n; i++)
11
                            p[i] = p[i - 1] * base;
12
                    for (int i = 1; i <= n; i++)</pre>
13
                            h[i] = (h[i - 1] * base) + (s[i
14
                             }
15
16
            dd get(11 1, 11 r){
17
                   return h[r + 1] - (h[l] * p[r - l + 1]);
18
19
20 };
```

5.2 Z-Function

■ Overview

Return an array where the i-th element corresponds to the longest sub-string starting from i that matches the prefix of s.

• Time complexity: $\mathcal{O}(N)$

⟨**/>>** Implementation

```
vector<int> z_func(string s){
             int n = s.size();
2
            vector<int> v(n);
3
             int 1 = 0, r = 0;
5
            for (int i = 1; i < n; i++){</pre>
6
                     if (i < r)
7
                              v[i] = min(r - i, v[i - 1]);
9
                      while ((v[i] + i) < n && s[v[i]] ==</pre>
                      \hookrightarrow s[v[i] + i])
                              v[i]++;
10
                      if ((v[i] + i) > r)
11
                               l = i, r = v[i] + i;
12
            }
13
14
15
            return v;
16
```

5.3 Prefix Function

Overview

Return an array where the i-th element corresponds to the longest sub-string ending at i that matches the prefix of s.

• Time complexity: $\mathcal{O}(N)$

Implementation

```
vector<int> pref_func(string s){
       int n = siz(s);
2
       vector<int> v(n);
       for (int i = 1; i < n; i++){</pre>
            11 j = v[i - 1];
            while (j > 0 \&\& s[j] != s[i])
                j = v[j - 1];
            if (s[j] == s[i])
9
                j++;
10
            v[i] = j;
11
12
13
       return v;
15
```

5.4 Manacher's Algorithm

■ Overview

Return an array where the i-th element corresponds to the longest palindrome that has i as the center, note that the algorithm only works for odd length palindrome, even can also be easily handled by inserting a dummy character in every even indicies.

• Time complexity: $\mathcal{O}(N)$

Implementation

```
vector<int> manacher(string s) {
       int n = s.size();
2
       s = "$" + s + '
       vector < int > p(n + 2);
       int 1 = 1, r = 1;
       for(int i = 1; i <= n; i++) {</pre>
            p[i] = max(0, min(r - i, p[1 + (r - i)]));
            while(s[i - p[i]] == s[i + p[i]]) {
                p[i]++;
9
10
            if(i + p[i] > r) {
11
12
                l = i - p[i], r = i + p[i];
13
14
       }
       return vector<int>(begin(p) + 1, end(p) - 1);
15
  }
16
```

5.5 Aho-Corasick

Overview

Construct an automaton of Trie nodes, where dp[i][c] is the next state of i when adding character c. If no state exists, we repeatedly go through the next longest available suffix j of i, and try to get dp[j][c].

• Time complexity: $\mathcal{O}(M*K)$, where M is the number of nodes in the Trie, and K is the alphabet size

Implementation

```
struct node{
2
        int p[26];
        int link;
3
4
        node(){
5
            for (int i = 0; i < 26; i++)
                p[i] = -1;
7
8
9
   };
10
   struct Trie{
11
        int indx = 1:
12
13
        int dp[def][26];
        vector<node> p;
14
15
        Trie(){
16
            p.push_back(node());
17
18
19
        int add(string s){
             11 crr = 0;
21
             for (int i = 0; i < s.size(); i++){</pre>
22
                 int c = s[i] - 'a';
23
24
                 if (p[crr].p[c] == -1){
                     p[crr].p[c] = indx++;
25
26
                     p.push_back(node());
27
28
29
                 crr = p[crr].p[c];
            }
30
31
             return crr;
32
        }
33
        void buildsuffix(){
35
             int n = p.size();
36
37
38
             queue<int> q;
            q.push(0);
39
40
41
             p[0].link = 0;
             for (int i = 0; i < n; i++) for (int j = 0; j <
42

→ 26; j++)

                      dp[i][j] = 0;
43
44
             while (q.size()){
45
46
                 int u = q.front();
                 q.pop();
47
48
                 for (int i = 0; i < 26; i++){
49
                     int v = p[u].p[i];
50
                      if (v != -1){
51
                          dp[u][i] = v;
52
                          p[v].link = (u == 0)? 0 :
53
                          \hookrightarrow dp[p[u].link][i];
                          q.push(v);
54
                     }
55
56
57
                          dp[u][i] = dp[p[u].link][i];
58
59
                 }
            }
60
61
```

62 };