

COMPUTER VISION AND
PHOTOGRAMMETRY

SELF-CALIBRATION

TODAY

- ▶ so far...
- ▶ Geometrical definitions
- ▶ Self-Calibration

SUMMARY

KEYPOINT DETECTORS

- ▶ Harris Corners
- ▶ DoG
- ▶ LoG
- ▶ Scale and orientation

FEATURE DESCRIPTOR

- ▶ Invariant to illumination
- ▶ Invariant to rotation
- ▶ Invariant (somehow) to viewing angle

MATCHING

- ▶ Nearest Neighbour Distance Ratio
- ▶ RANSAC
 - ▶ Evaluate a (random) hypothesis to reject outliers

RELATING IMAGES

- ▶ Fundamental Matrix (more views?)
- ▶ Projection Matrices
- ▶ Triangulation
 - ▶ PROJECTIVE RECONSTRUCTION
- ▶ if K (calibrated) Essential Matrix
 - ▶ METRIC RECONSTRUCTION
- ▶ IF NOT?? Self-calibration (TODAY)

DENSE MATCHING

- ▶ Stereo Matching
- ▶ Rectification
- ▶ SSD, NCC

3D MODELING

- ▶ From 3D points to triangles
- ▶ Texturing
- ▶ Other material properties??

PROJECTIVE GEOMETRY

HOMOGENEOUS COORDINATES

Homogeneous representation of lines

$$ax + by + c = 0 \quad (a, b, c)^T$$

$$(ka)x + (kb)y + kc = 0, \forall k \neq 0 \quad (a, b, c)^T \sim k(a, b, c)^T$$

equivalence class of vectors, any vector is representative

Set of all equivalence classes in $\mathbf{R}^3 - (0, 0, 0)^T$ forms \mathbf{P}^2

Homogeneous representation of points

$$x = (x, y)^T \text{ on } l = (a, b, c)^T \text{ if and only if } ax + by + c = 0$$

$$(x, y, 1)(a, b, c)^T = (x, y, 1)l = 0 \quad (x, y, 1)^T \sim k(x, y, 1)^T, \forall k \neq 0$$

The point x lies on the line l if and only if $x^T l = l^T x = 0$

Homogeneous coordinates $(x_1, x_2, x_3)^T$ but only 2DOF

Inhomogeneous coordinates $(x, y)^T$

POINTS FROM LINES AND VICE-VERSA

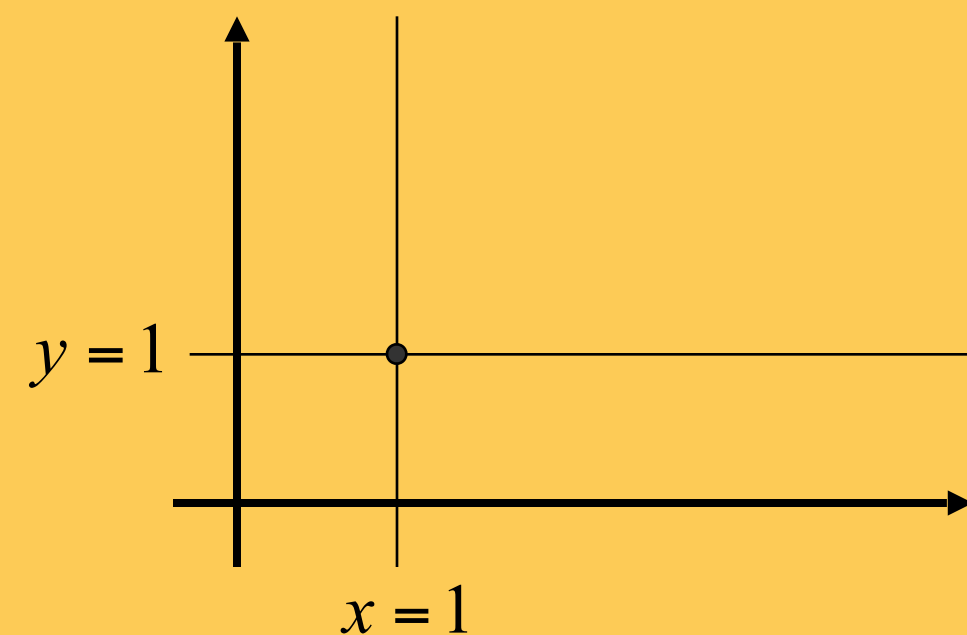
Intersections of lines

The intersection of two lines l and l' is $x = l \times l'$

Line joining two points

The line through two points x and x' is $l = x \times x'$

Example

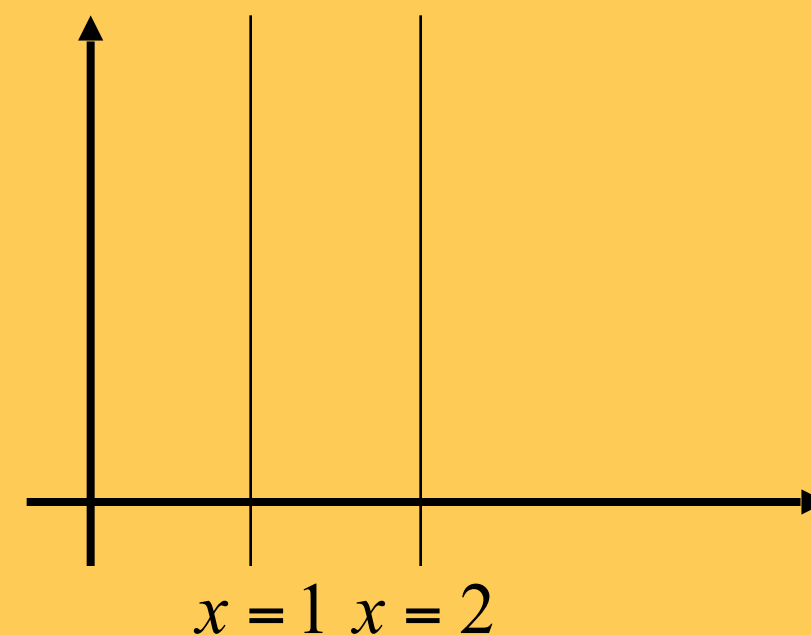


IDEAL POINTS AND THE LINE AT INFINITY

Intersections of parallel lines

$$l = (a, b, c)^T \text{ and } l' = (a, b, c')^T \quad l \times l' = (b, -a, 0)^T$$

Example



$(b, -a)$ tangent vector
 (a, b) normal direction

Ideal points $(x_1, x_2, 0)^T$

Line at infinity $l_\infty = (0, 0, 1)^T$

$$\mathbf{P}^2 = \mathbf{R}^2 \cup l_\infty$$

Note that in \mathbf{P}^2 there is no distinction between ideal points and others

DUALITY

x	\longleftrightarrow	l
$x^T l = 0$	\longleftrightarrow	$l^T x = 0$
$x = l \times l'$	\longleftrightarrow	$l = x \times x'$

Duality principle:

To any theorem of 2-dimensional projective geometry there corresponds a dual theorem, which may be derived by interchanging the role of points and lines in the original theorem

CONICS

Curve described by 2nd-degree equation in the plane

$$ax^2 + bxy + cy^2 + dx + ey + f = 0$$

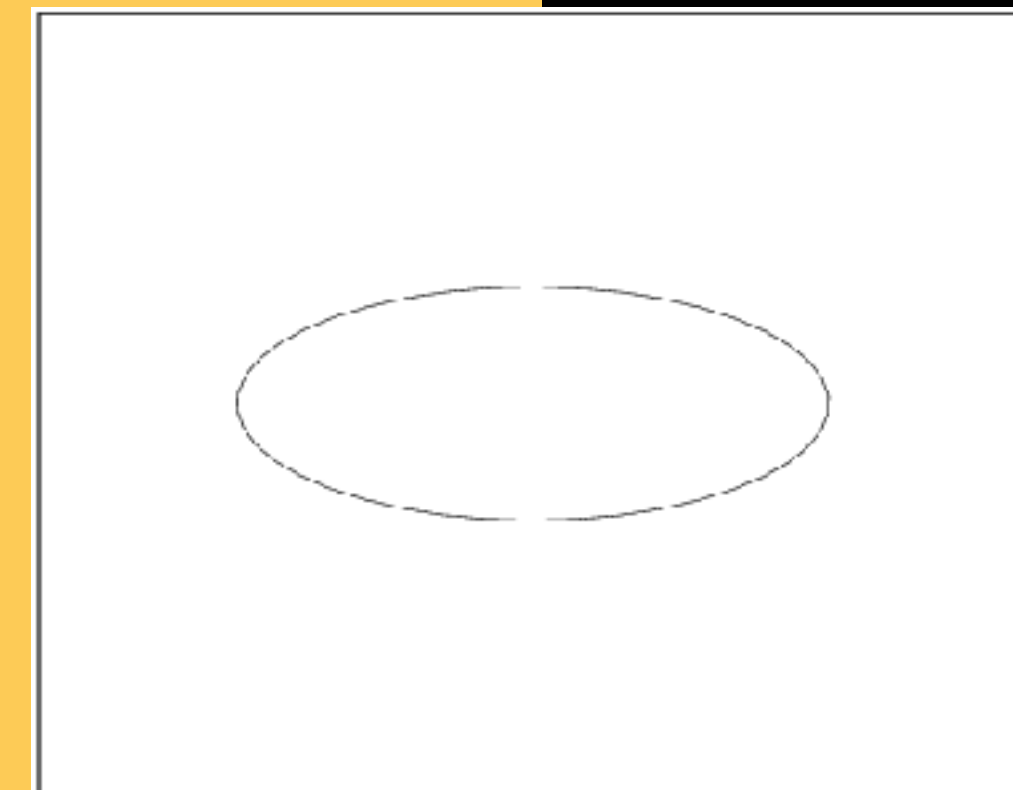
or *homogenized* $x = \frac{x_1}{x_3}, y = \frac{x_2}{x_3}$

$$ax_1^2 + bx_1x_2 + cx_2^2 + dx_1x_3 + ex_2x_3 + fx_3^2 = 0$$

or in matrix form

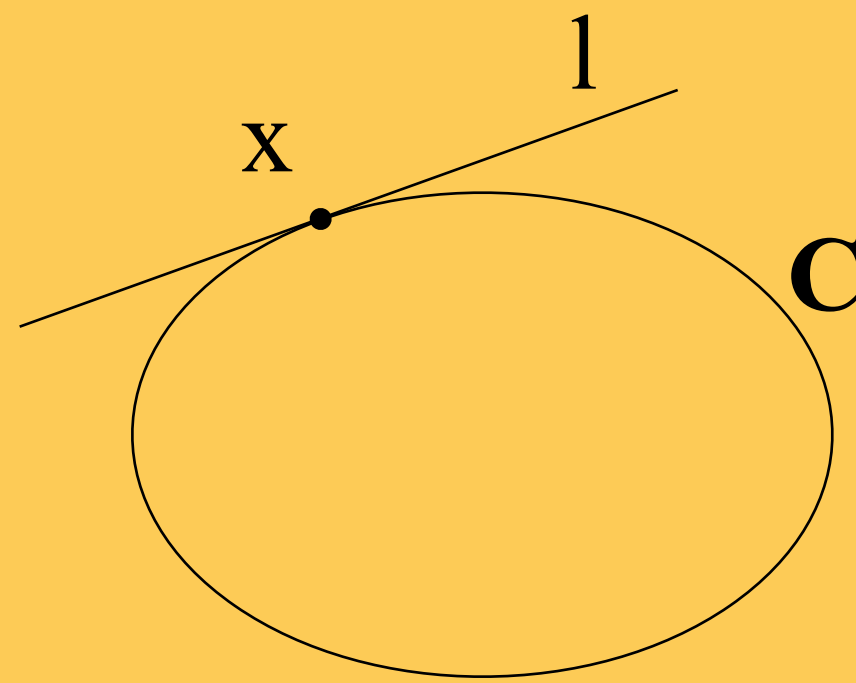
$$\mathbf{x}^T \mathbf{C} \mathbf{x} = 0 \quad \text{with} \quad \mathbf{C} = \begin{bmatrix} a & b/2 & d/2 \\ b/2 & c & e/2 \\ d/2 & e/2 & f \end{bmatrix}$$

5DOF: $\{a:b:c:d:e:f\}$



TANGENT LINES TO CONICS

The line l tangent to C at point x on C is given by $l=Cx$

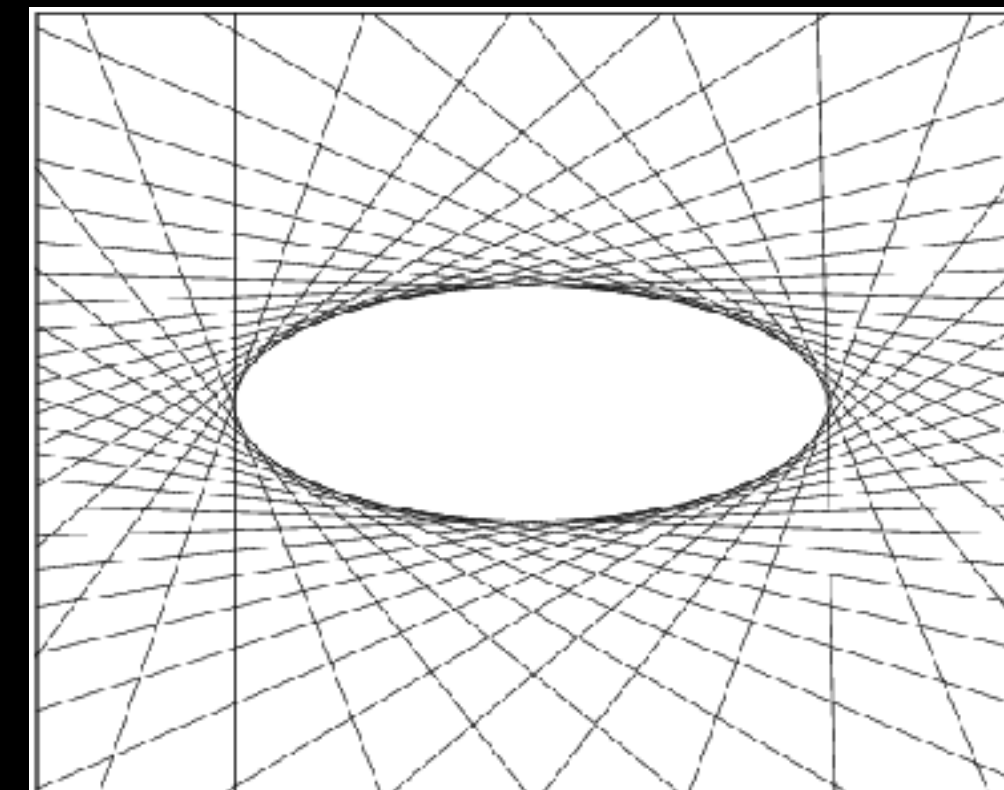
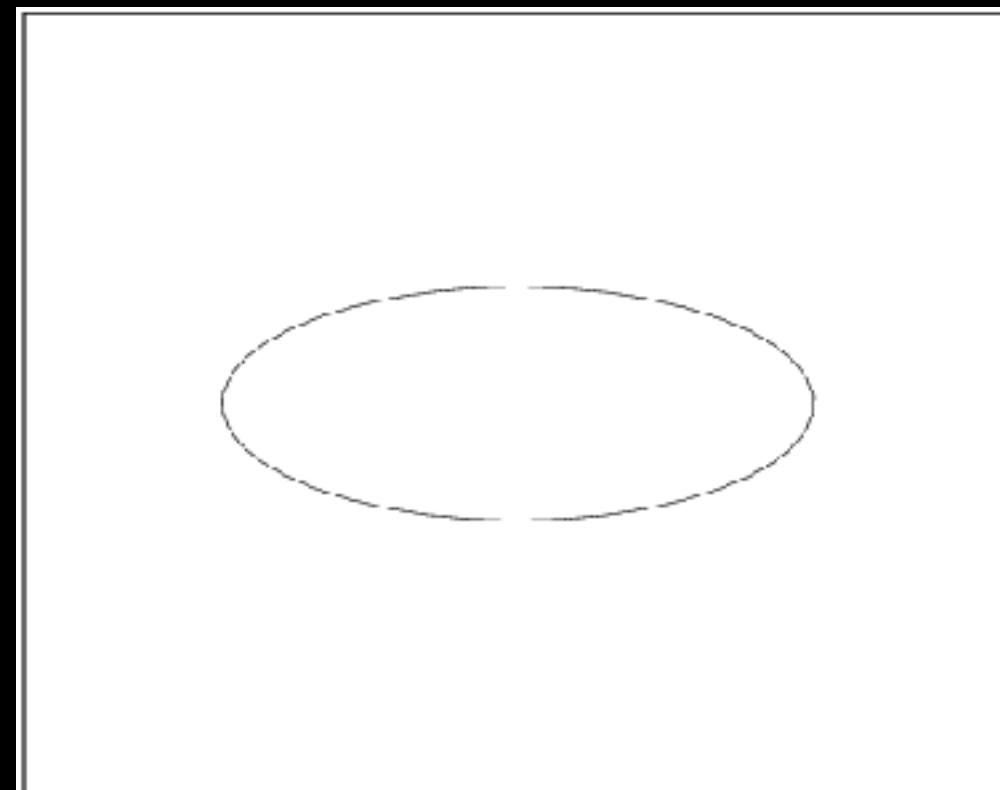


DUAL CONICS

A line tangent to the conic \mathbf{C} satisfies $\mathbf{l}^\top \mathbf{C}^* \mathbf{l} = 0$

In general (\mathbf{C} full rank): $\mathbf{C}^* = \mathbf{C}^{-1}$

Dual conics = line conics = conic envelopes



PROJECTIVE TRANSFORMATIONS

Definition:

A *projectivity* is an invertible mapping h from P^2 to itself such that three points x_1, x_2, x_3 lie on the same line if and only if $h(x_1), h(x_2), h(x_3)$ do.

Theorem:

A mapping $h: P^2 \rightarrow P^2$ is a projectivity if and only if there exist a non-singular 3×3 matrix \mathbf{H} such that for any point in P^2 represented by a vector x it is true that $h(x) = \mathbf{H}x$

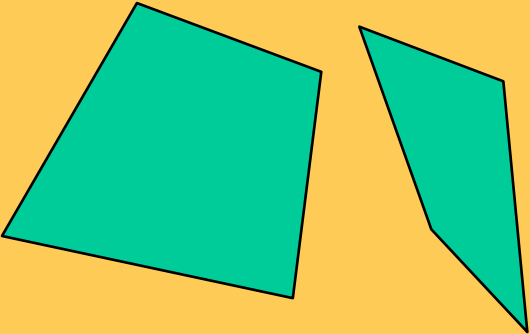
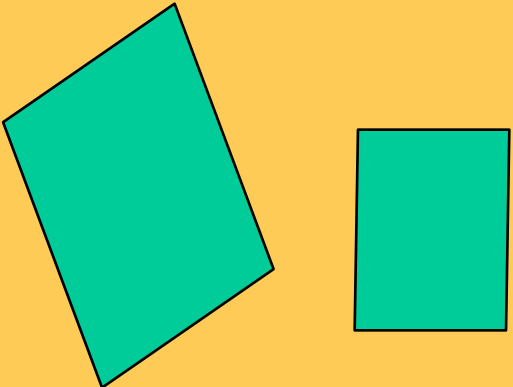
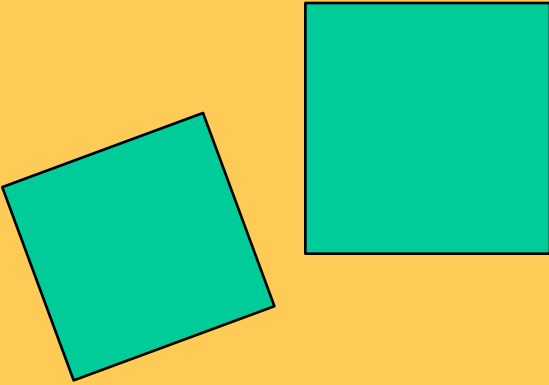
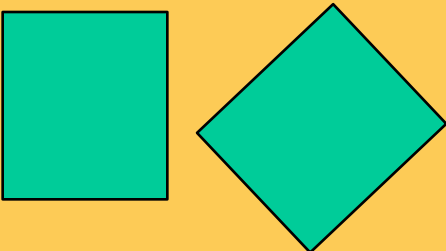
Definition: Projective transformation

$$\begin{pmatrix} x'_1 \\ x'_2 \\ x'_3 \end{pmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \quad \text{or} \quad x' = \mathbf{H}x$$

8DOF

projectivity=collineation=projective transformation=homography

OVERVIEW TRANSFORMATIONS

Projective 8dof	$\begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix}$		Concurrency, collinearity, order of contact (intersection, tangency, inflection, etc.), cross ratio
Affine 6dof	$\begin{bmatrix} a_{11} & a_{12} & t_x \\ a_{21} & a_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}$		Parallellism, ratio of areas, ratio of lengths on parallel lines (e.g midpoints), linear combinations of vectors (centroids). The line at infinity l_∞
Similarity 4dof	$\begin{bmatrix} sr_{11} & sr_{12} & t_x \\ sr_{21} & sr_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}$		Ratios of lengths, angles. The circular points I,J
Euclidean 3dof	$\begin{bmatrix} r_{11} & r_{12} & t_x \\ r_{21} & r_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}$		lengths, areas.

3D POINTS

3D point

$$(X, Y, Z)^T \text{ in } \mathbf{R}^3$$

$$X = (X_1, X_2, X_3, X_4)^T \text{ in } \mathbf{P}^3$$

$$X = \left(\frac{X_1}{X_4}, \frac{X_2}{X_4}, \frac{X_3}{X_4}, 1 \right)^T = (X, Y, Z, 1)^T \quad (X_4 \neq 0)$$

projective transformation

$$X' = \mathbf{H} X \quad (4 \times 4 - 1 = 15 \text{ dof})$$

PLANES

3D plane

$$\pi_1 X + \pi_2 Y + \pi_3 Z + \pi_4 = 0$$

$$\pi_1 X_1 + \pi_2 X_2 + \pi_3 X_3 + \pi_4 X_4 = 0$$

$$\pi^\top X = 0$$

Transformation

$$X' = \mathbf{H} X$$

$$\pi' = \mathbf{H}^{-\top} \pi$$

Dual: points \leftrightarrow planes

QUADRICS AND DUAL QUADRICS

► Quadric

$$X^T Q X = 0 \quad (Q : 4 \times 4 \text{ symmetric matrix})$$

$$Q = \begin{bmatrix} \cdot & \cdot & \cdot & \cdot \\ \boxed{?} & \cdot & \cdot & \cdot \\ \boxed{?} & \boxed{?} & \cdot & \cdot \\ \boxed{?} & \boxed{?} & \boxed{?} & \cdot \end{bmatrix}$$

1. 9 d.o.f.
2. (plane \cap quadric)=conic $C = M^T Q M$
3. transformation $Q' = H^{-T} Q H^{-1}$

► Dual Quadric

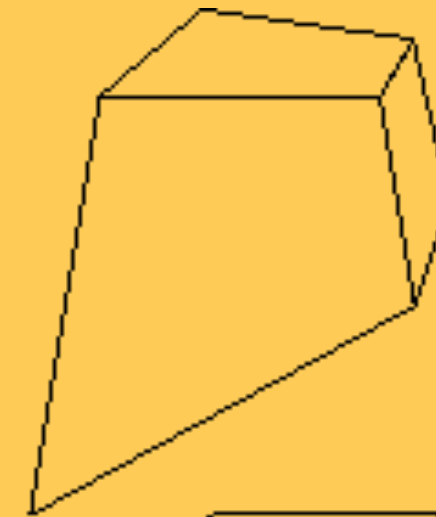
$$\pi^T Q^* \pi = 0$$

1. relation to quadric $Q^* = Q^{-1}$ (non-degenerate)
2. transformation $Q'^* = H Q^* H^T$

HIERARCHY OF TRANSFORMATIONS

Projective
15dof

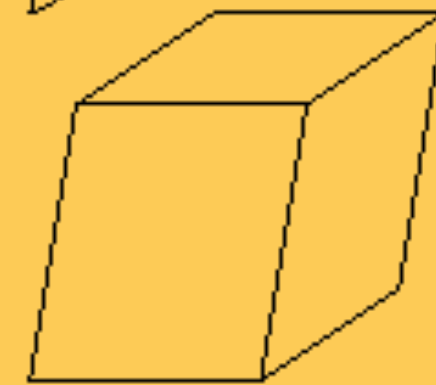
$$\begin{bmatrix} A & t \\ v^T & v \end{bmatrix}$$



Intersection and tangency

Affine
12dof

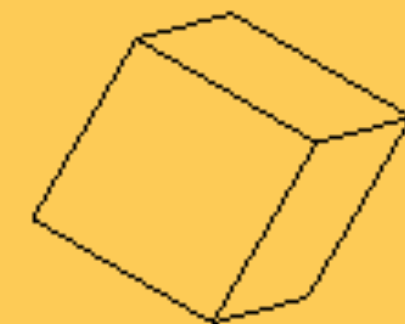
$$\begin{bmatrix} A & t \\ 0^T & 1 \end{bmatrix}$$



Parallellism of planes,
Volume ratios, centroids,
The plane at infinity π_∞

Similarity
7dof

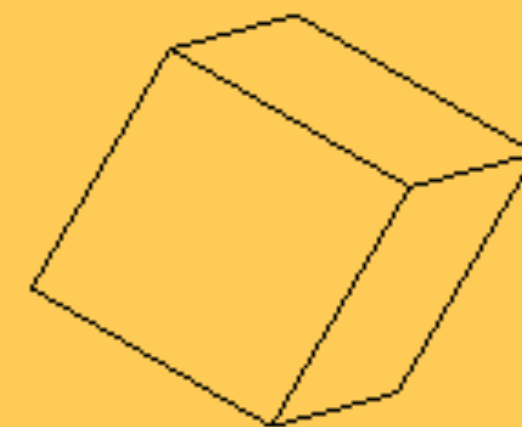
$$\begin{bmatrix} sR & t \\ 0^T & 1 \end{bmatrix}$$



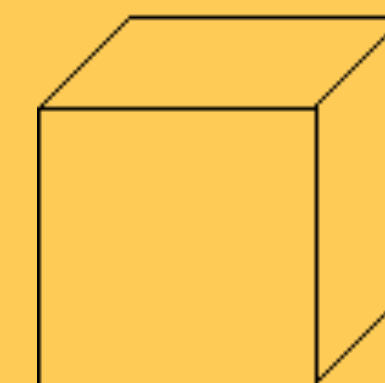
The absolute conic Ω_∞

Euclidean
6dof

$$\begin{bmatrix} R & t \\ 0^T & 1 \end{bmatrix}$$



Volume



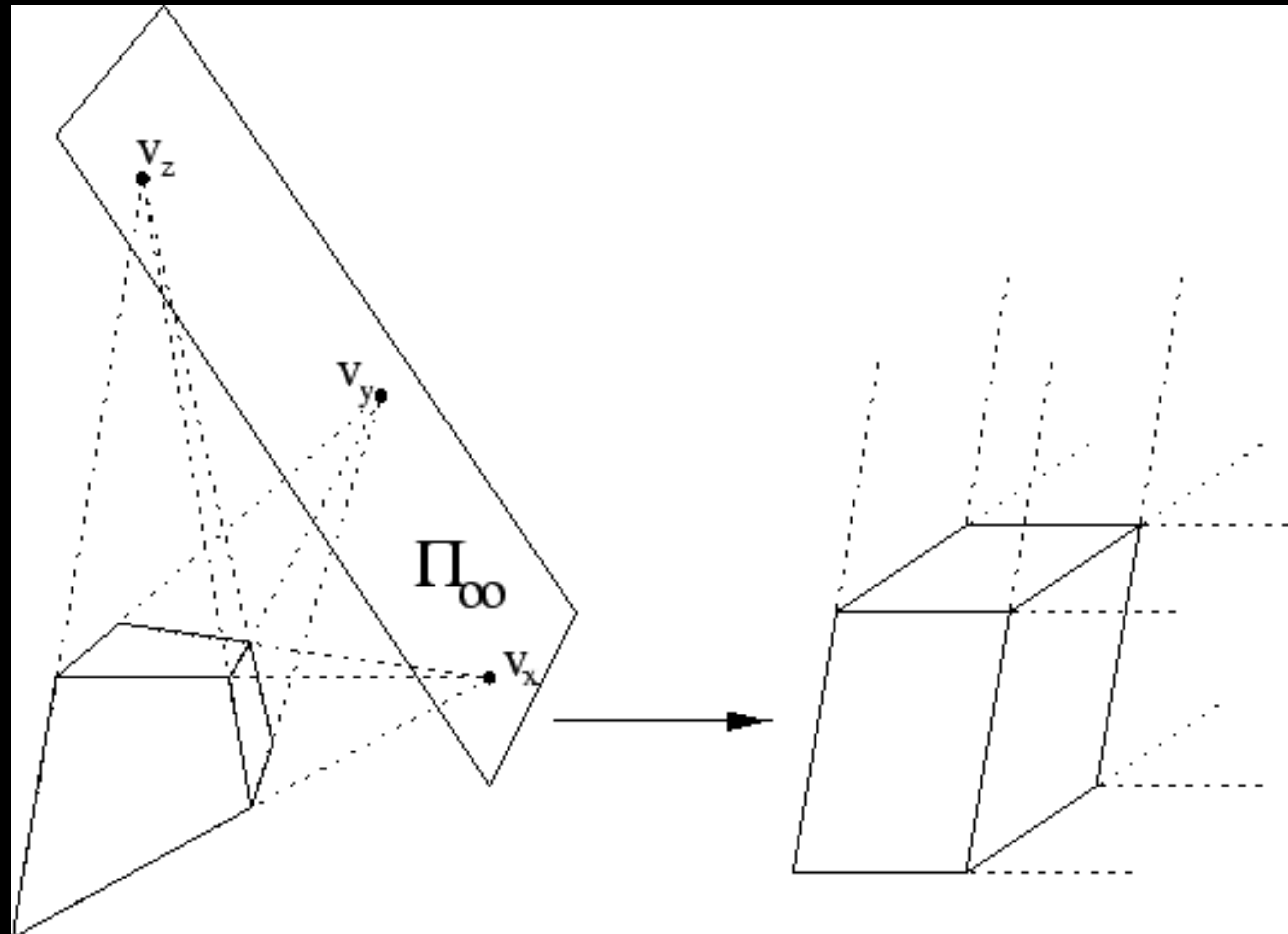
THE PLANE AT INFINITY

$$\pi'_\infty = \mathbf{H}_A^{-\top} \pi_\infty = \begin{bmatrix} \mathbf{A}^{-\top} & 0 \\ -\mathbf{A} \mathbf{t} & 1 \end{bmatrix} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \pi_\infty$$

The plane at infinity π_∞ is a fixed plane under a projective transformation \mathbf{H} if \mathbf{H} is an affinity

1. canonical position $\pi_\infty = (0,0,0,1)^\top$
2. contains directions $\mathbf{D} = (X_1, X_2, X_3, 0)^\top$

THE PLANE AT INFINITY



THE ABSOLUTE CONIC

The absolute conic Ω_∞ is a (point) conic on π_∞ .

In a metric frame:

$$\left. \begin{array}{c} X_1^2 + X_2^2 + X_3^2 \\ X_4 \end{array} \right\} = 0$$

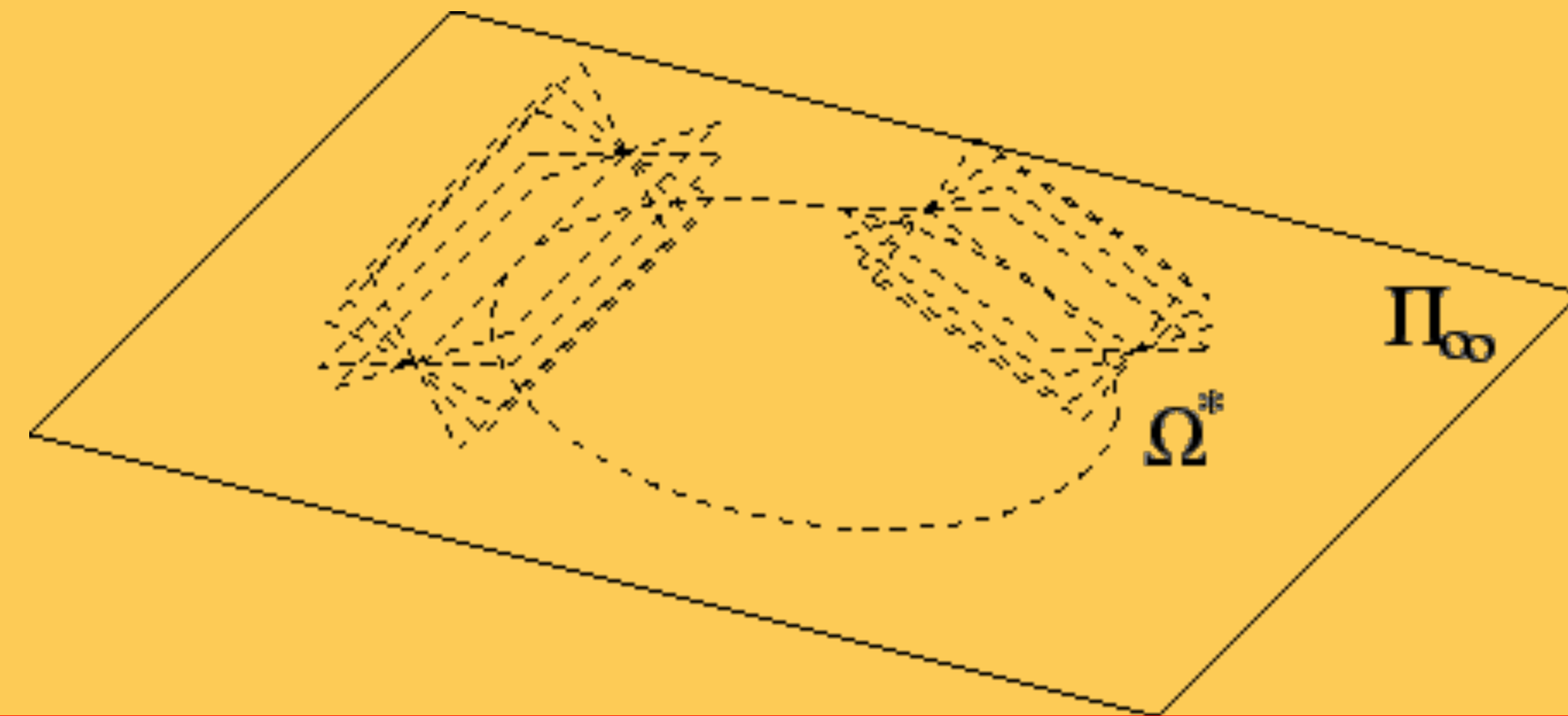
or conic for directions: $(X_1, X_2, X_3) \mathbb{I} (X_1, X_2, X_3)^\top$
(with no real points)

The absolute conic Ω_∞ is a fixed conic under the projective transformation \mathbf{H} if \mathbf{H} is a similarity

1. Ω_∞ is only fixed as a set
2. Circle intersect Ω_∞ in two points
3. Spheres intersect π_∞ in Ω_∞

THE DUAL ABSOLUTE QUADRIC

$$\Omega_{\infty}^* = \begin{bmatrix} \mathbf{I} & 0 \\ 0^T & 0 \end{bmatrix}$$



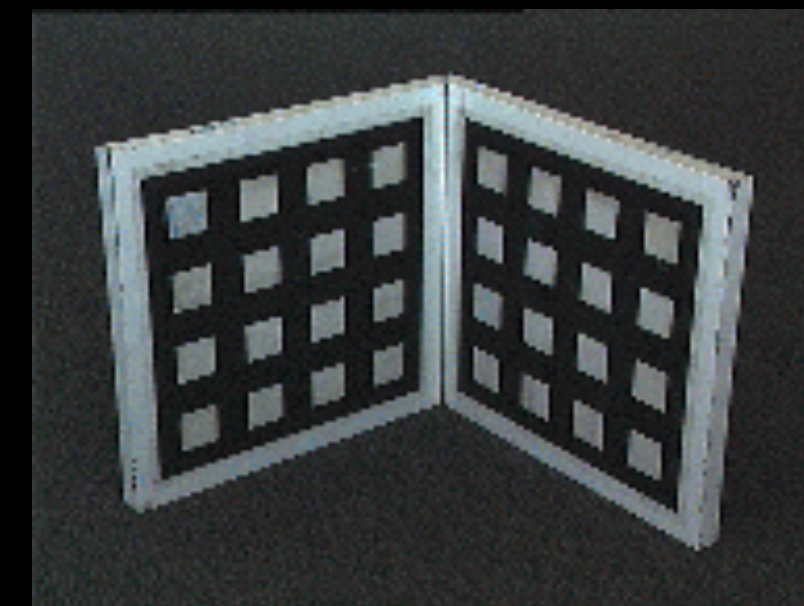
The absolute conic Ω_{∞}^* is a fixed conic under the projective transformation \mathbf{H} if \mathbf{H} is a similarity

1. 8 dof
2. plane at infinity π_{∞} is the nullvector of Ω_{∞}

SELF-CALIBRATION

MOTIVATION

- Avoid explicit calibration procedure
 - Complex procedure
 - Need for calibration object
 - Need to maintain calibration



MOTIVATION

- Allow flexible acquisition
 - No prior calibration necessary
 - Possibility to vary intrinsics
 - Use archive footage

TEXT

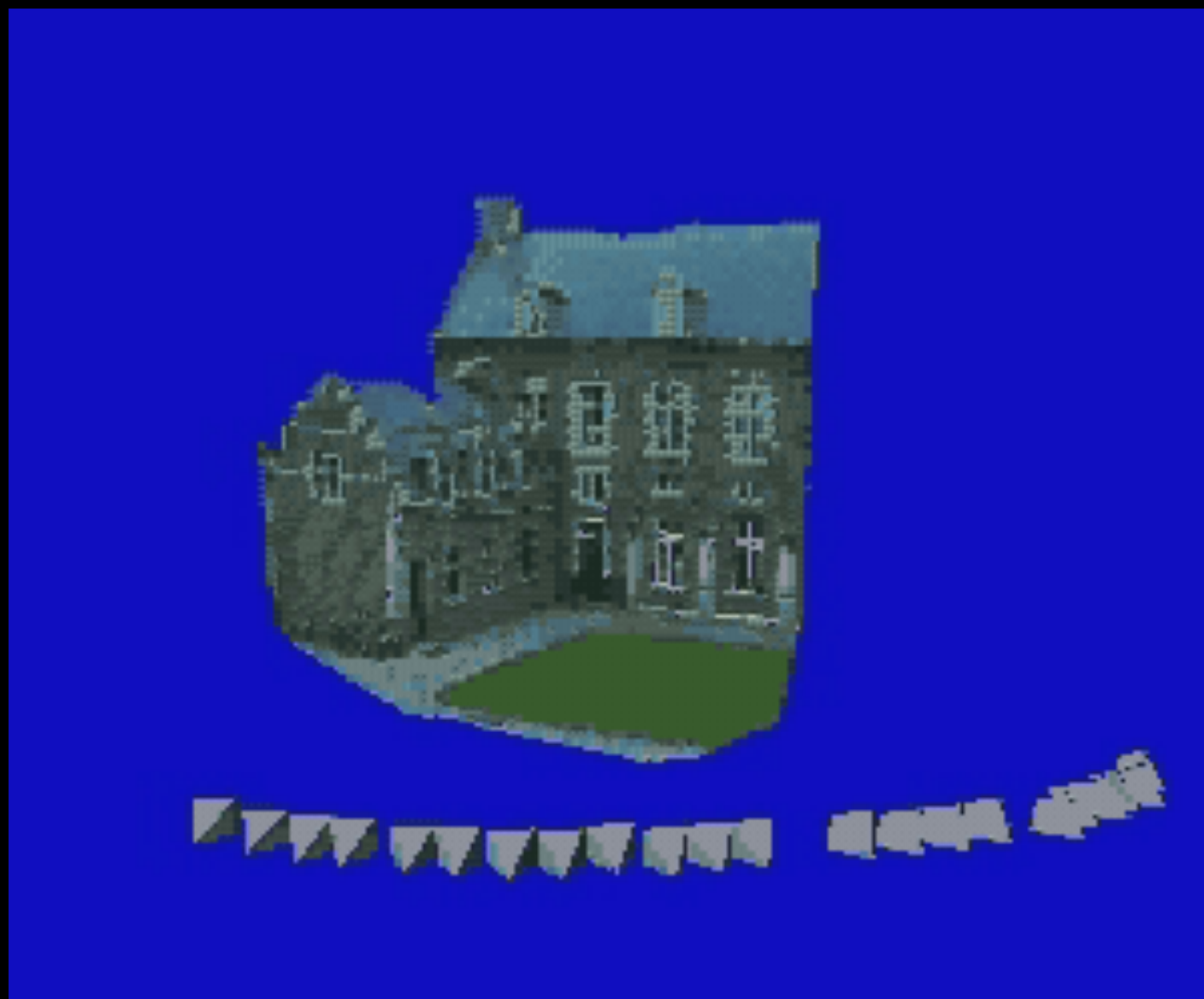
EXAMPLE



PROJECTIVE AMBIGUITY

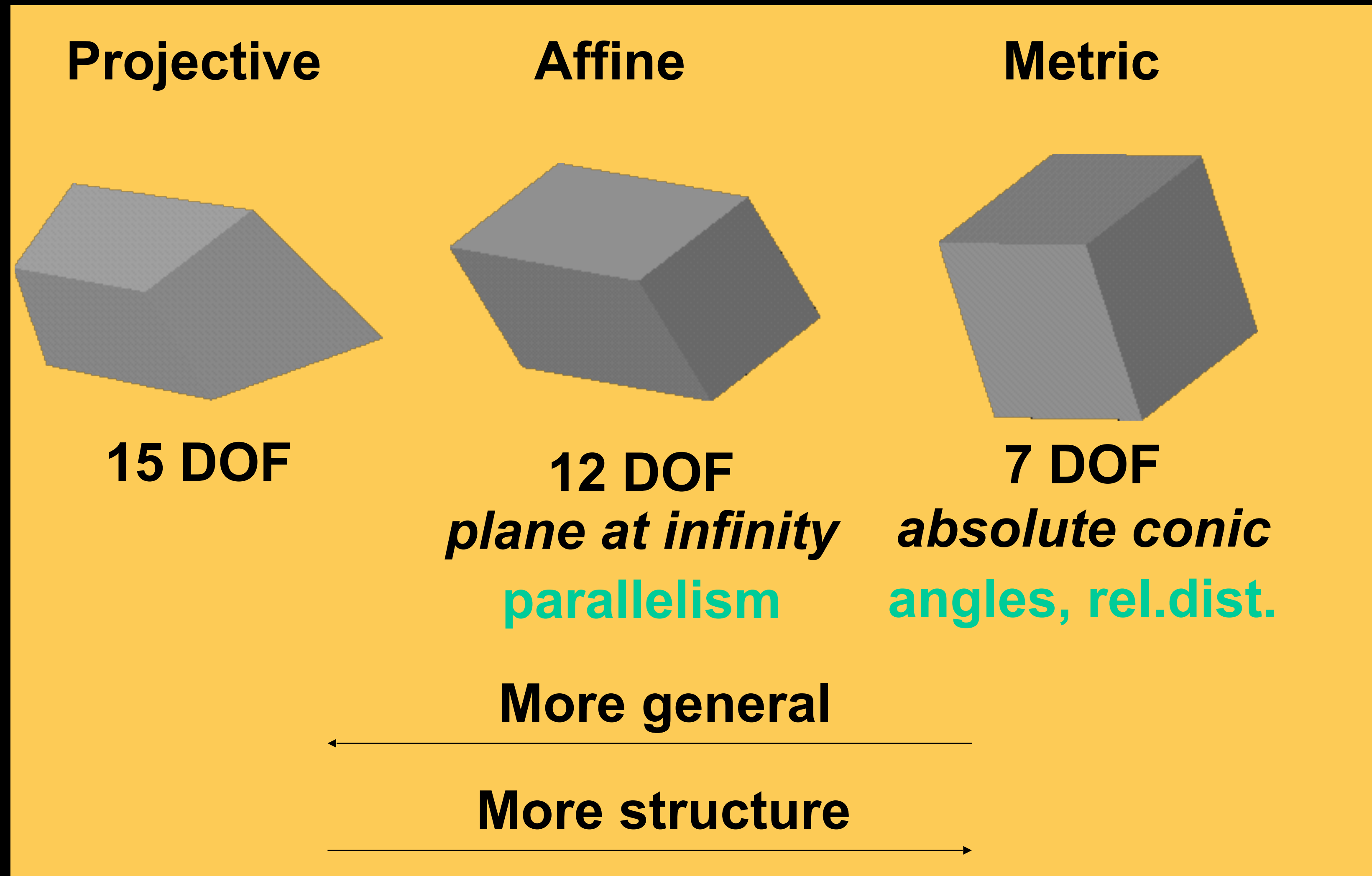
Reconstruction from uncalibrated images

⇒ projective ambiguity on reconstruction



$$\mathbf{m} = \mathbf{P} \mathbf{M} = (\mathbf{P} \mathbf{T}^{-1})(\mathbf{T} \mathbf{M}) = \mathbf{P}' \mathbf{M}'$$

STRATIFICATION OF GEOMETRY



CONSTRAINTS ?

- Scene constraints
 - Parallelism, vanishing points, horizon, ...
 - Distances, positions, angles, ...

Unknown scene → no constraints

- Camera extrinsics constraints
 - Pose, orientation, ...

Unknown camera motion → no constraints

- Camera intrinsics constraints
 - Focal length, principal point, aspect ratio & skew

Perspective camera model too general
→ some constraints

EUCLIDEAN PROJECTION MATRIX

Factorization of Euclidean projection matrix

$$\mathbf{P} = \mathbf{K} \left[\mathbf{R}^\top \mid -\mathbf{R}^\top \mathbf{t} \right]$$

$$\text{Intrinsics: } \mathbf{K} = \begin{bmatrix} f_x & s & u_x \\ & f_y & u_y \\ & & 1 \end{bmatrix} \quad (\text{camera geometry})$$

$$\text{Extrinsics: } (\mathbf{R}, \mathbf{t}) \quad (\text{camera motion})$$

Note: every projection matrix can be factorized,
but only meaningful for euclidean projection matrices

CONSTRAINTS ON INTRINSIC PARAMETERS

$$\mathbf{K} = \begin{bmatrix} f_x & s & u_x \\ & f_y & u_y \\ & & 1 \end{bmatrix}$$

Constant
e.g. fixed camera:

$$\mathbf{K}_1 = \mathbf{K}_2 = \boxed{?}$$

Known
e.g. rectangular pixels:

$$s = 0$$

$$\text{square pixels: } f_x = f_y, s = 0$$

principal point known:

$$(u_x, u_y) = \left(\frac{w}{2}, \frac{h}{2} \right)$$

SELF-CALIBRATION

Upgrade from projective structure to metric structure using constraints on intrinsic camera parameters

- ▶ Constant intrinsics

(Faugeras et al. ECCV'92, Hartley'93, Triggs'97, Pollefeys et al. PAMI'98, ...)

- ▶ Some known intrinsics, others varying

(Heyden&Astrom CVPR'97, Pollefeys et al. ICCV'98,...)

- ▶ Constraints on intrinsics and restricted motion

(Moons et al.'94, Hartley '94, Armstrong ECCV'96, ...)

(e.g. pure translation, pure rotation, planar motion)

A COUNTING ARGUMENT

- To go from projective (15DOF) to metric (7DOF) at least 8 constraints are needed
- Minimal sequence length should satisfy

$$n \times (\# \text{ known}) + (n - 1) \times (\# \text{ fixed}) \geq 8$$

- Independent of algorithm
- Assumes general motion (i.e. not critical)

SELF-CALIBRATION: CONCEPTUAL ALGORITHM

Given projective structure and motion $\{\mathbf{P}_j, \mathbf{M}_i\}$, then the metric structure and motion can be obtained as $\{\mathbf{P}_j \mathbf{T}^{-1}, \mathbf{T} \mathbf{M}_i\}$, with

$$\mathbf{T} = \arg \min_{\mathbf{T}} C\left(K\left(\mathbf{P}_1 \mathbf{T}^{-1}\right) K\left(\mathbf{P}_2 \mathbf{T}^{-1}\right) \boxed{?}, K\left(\mathbf{P}_n \mathbf{T}^{-1}\right)\right)$$

$C(\mathbf{K}_1, \mathbf{K}_2, \boxed{?}, \mathbf{K}_n)$ criterium expressing constraints

$K(\mathbf{P})$ function extracting intrinsics
from projection matrix

CONICS & QUADRICS

CONICS

$$\mathbf{m}^T \mathbf{C} \mathbf{m} = 0 \quad \mathbf{l}^T \mathbf{C}^* \mathbf{l} = 0$$

$$\mathbf{C}^* = \mathbf{C}^{-1}$$

QUADRICS

$$\mathbf{M}^T \mathbf{Q} \mathbf{M} = 0 \quad \mathbf{\Pi}^T \mathbf{Q}^* \mathbf{\Pi} = 0$$

$$\mathbf{Q}^* = \mathbf{Q}^{-1}$$

TRANSFORMATIONS

$$\mathbf{C} \stackrel{?}{\sim} \mathbf{C}' \sim \mathbf{H}^{-T} \mathbf{C} \mathbf{H}^{-1}$$

$$\mathbf{C}^* \stackrel{?}{\sim} \mathbf{C}^{*'} \sim \mathbf{H} \mathbf{C}^* \mathbf{H}^T$$

$$\mathbf{Q} \stackrel{?}{\sim} \mathbf{Q}' \sim \mathbf{T}^{-T} \mathbf{Q} \mathbf{T}^{-1}$$

$$\mathbf{Q}^* \stackrel{?}{\sim} \mathbf{Q}^{*'} \sim \mathbf{T} \mathbf{Q}^* \mathbf{T}^T$$

PROJECTION

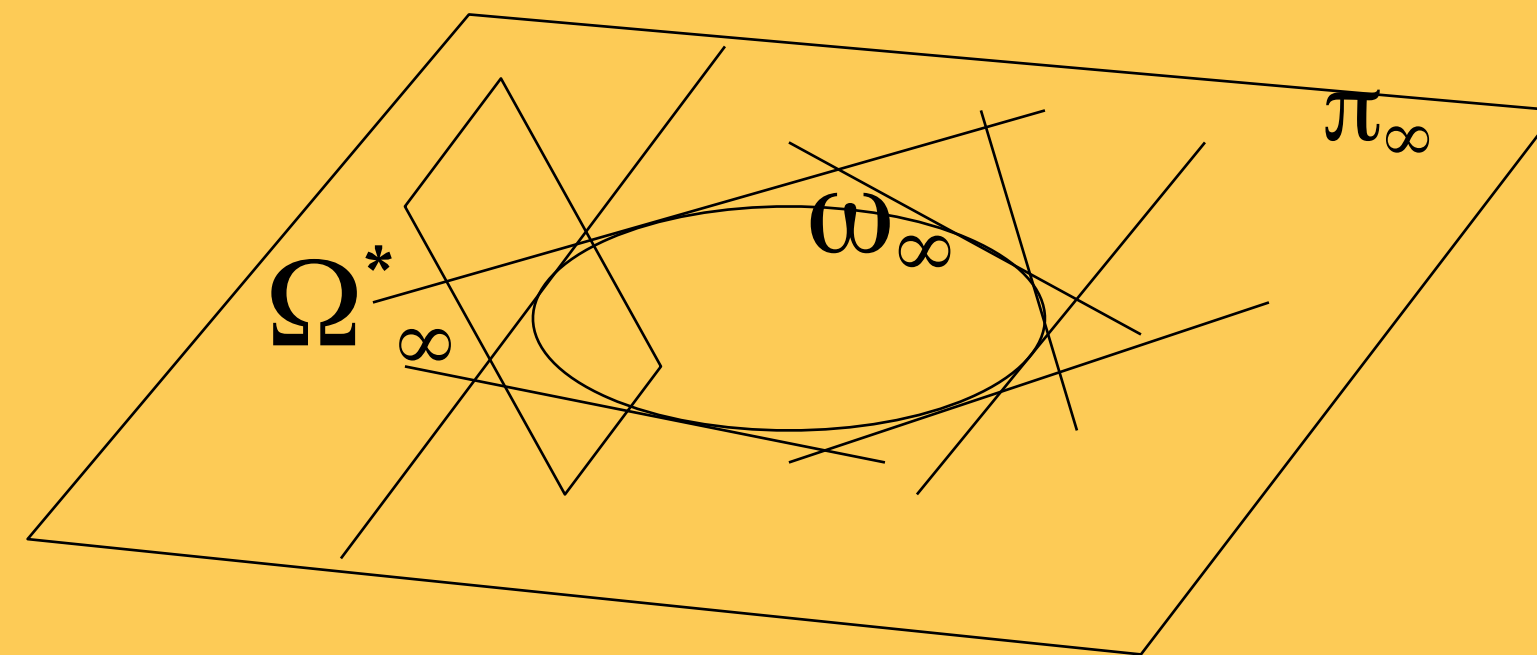
$$\mathbf{C}^* \sim \mathbf{P} \mathbf{Q}^* \mathbf{P}^T$$

THE ABSOLUTE DUAL QUADRIC

(Triggs CVPR '97)

Degenerate dual quadric Ω_{∞}^*

Encodes both absolute conic ω_{∞} and π_{∞}



for metric frame:

$$\pi^{\top} \begin{bmatrix} \mathbf{I} & \mathbf{0} \\ \mathbf{0}^{\top} & 0 \end{bmatrix} \pi = 0$$

ABSOLUTE DUAL QUADRIC AND SELF-CALIBRATION

Eliminate extrinsics from equation

$$\mathbf{K} \begin{bmatrix} \mathbf{R}^T & -\mathbf{R}^T \mathbf{t} \end{bmatrix} \longrightarrow \cancel{\mathbf{K} \mathbf{R}^T \mathbf{R} \mathbf{K}^T} \longrightarrow \mathbf{K} \mathbf{K}^T$$

Equivalent to projection of dual quadric

$$\mathbf{P} \Omega_{\infty}^* \mathbf{P}^T \propto \mathbf{K} \mathbf{K}^T \quad \Omega_{\infty}^* = \text{diag}(1 \ 1 \ 1 \ 0)$$

Abs. Dual Quadric also exists in projective world

$$\begin{aligned} \mathbf{K} \mathbf{K}^T &\propto \mathbf{P} \Omega_{\infty}^* \mathbf{P}^T \propto (\mathbf{P} \mathbf{T}^{-1}) (\mathbf{T} \Omega_{\infty}^* \mathbf{T}^T) (\mathbf{T}^{-T} \mathbf{P}^T) \\ &\propto \mathbf{P}' \Omega_{\infty}'^* \mathbf{P}'^T \end{aligned}$$

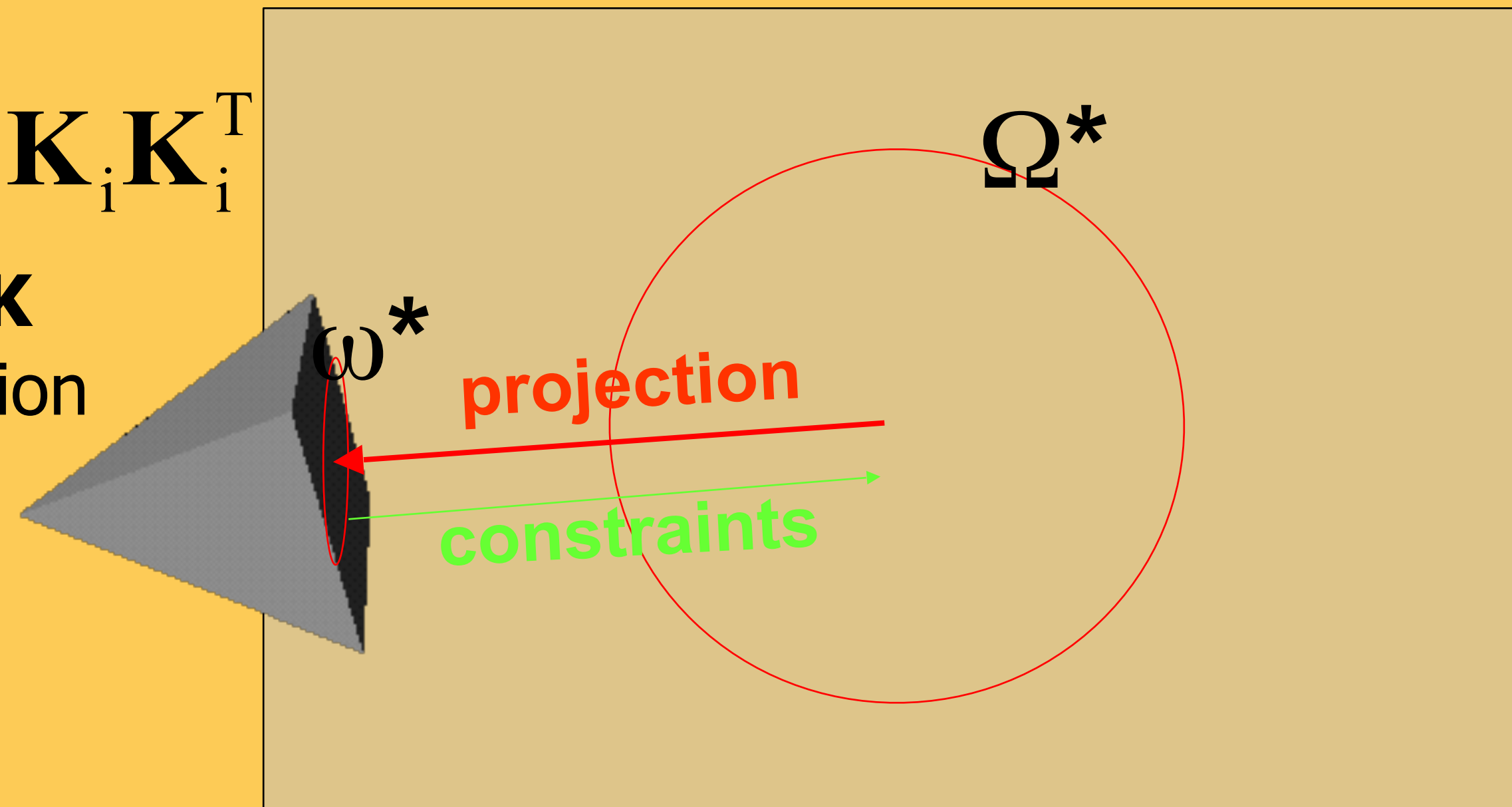
Transforming world so that $\Omega_{\infty}'^* \rightarrow \Omega_{\infty}^*$
reduces ambiguity to metric

IMAGE OF THE ABSOLUTE CONIC

Projection equation:

$$\omega_i^* \propto \mathbf{P}_i \Omega^* \mathbf{P}_i^T \propto \mathbf{K}_i \mathbf{K}_i^T$$

Translate constraints on \mathbf{K}
through projection equation
to constraints on Ω^*



Absolute conic = calibration object which is always present but can only be observed through constraints on the intrinsics

CONSTRAINTS ON Ω^*_∞

$$\omega^*_\infty = \begin{bmatrix} f_x^2 + s^2 + c_x^2 & sf_y + c_x c_y & c_x \\ sf_y + c_x c_y & f_y^2 + c_y^2 & c_y \\ c_x & c_y & 1 \end{bmatrix}$$

condition	constraint	type	#constraints
Zero skew	$\omega^*_{12}\omega^*_{33} = \omega^*_{13}\omega^*_{23}$	quadratic	m
Principal point	$\omega^*_{13} = \omega^*_{23} = 0$	linear	$2m$
Zero skew (& p.p.)	$\omega^*_{12} = 0$	linear	m
Fixed aspect ratio (& p.p.& Skew)	$\omega^*_{11}\omega'^*_{22} = \omega^*_{22}\omega'^*_{11}$	quadratic	$m-1$
Known aspect ratio (& p.p.& Skew)	$\omega^*_{11} = \omega^*_{22}$	linear	m
Focal length (& p.p. & Skew)	$\omega^*_{33} = \omega^*_{11}$	linear	m

LINEAR ALGORITHM

(Pollefeys et al., ICCV '98/IJCV '99)

Assume everything known, except focal length

$$\omega^* \approx \begin{bmatrix} \hat{f}^2 & 0 & 0 \\ 0 & \hat{f}^2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \propto \mathbf{P}\mathbf{\Omega}^*\mathbf{P}^T$$

$$\begin{aligned} (\mathbf{P}\mathbf{\Omega}^*\mathbf{P}^T)_{11} - (\mathbf{P}\mathbf{\Omega}^*\mathbf{P}^T)_{22} &= 0 \\ (\mathbf{P}\mathbf{\Omega}^*\mathbf{P}^T)_{12} &= 0 \\ (\mathbf{P}\mathbf{\Omega}^*\mathbf{P}^T)_{13} &= 0 \\ (\mathbf{P}\mathbf{\Omega}^*\mathbf{P}^T)_{23} &= 0 \end{aligned}$$

Yields 4 constraint per image

Note that rank-3 constraint is not enforced

FIRST NORMALISE P BY KN

$$\mathbf{P}_N = \mathbf{K}_N^{-1} \mathbf{P} \text{ with } \mathbf{K}_N = \begin{bmatrix} w+h & 0 & \frac{w}{2} \\ 0 & w+h & \frac{h}{2} \\ 0 & 0 & 1 \end{bmatrix}$$

$$\omega^* \sim \mathbf{K}\mathbf{K}^\top = \begin{bmatrix} f^2 + s^2 + u^2 & srf + uv & u \\ srf + uv & r^2 f^2 + v^2 & v \\ u & v & 1 \end{bmatrix} \approx \begin{bmatrix} 1 \pm 9 & \pm 0.01 & \pm 0.1 \\ \pm 0.01 & 1 \pm 9 & \pm 0.1 \\ \pm 0.1 & \pm 0.1 & 1 \end{bmatrix}$$

LINEAR ALGORITHM REVISITED

(Pollefeys et al., ECCV'02)

Weighted linear equations

$$\mathbf{K}\mathbf{K}^T \approx \begin{bmatrix} \hat{f}^2 & 0 & 0 \\ 0 & \hat{f}^2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\hat{f} \approx 1$$

$$\frac{1}{0.2} (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{11} - (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{22} = 0$$

$$\frac{1}{0.01} (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{12} = 0$$

$$\frac{1}{0.1} (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{13} = 0$$

$$\frac{1}{0.1} (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{23} = 0$$

$$\frac{1}{9} (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{11} - (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{33} = 0$$

$$\frac{1}{9} (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{22} - (\mathbf{P}\mathbf{\Omega}^* \mathbf{P}^T)_{33} = 0$$

PROJECTIVE TO METRIC

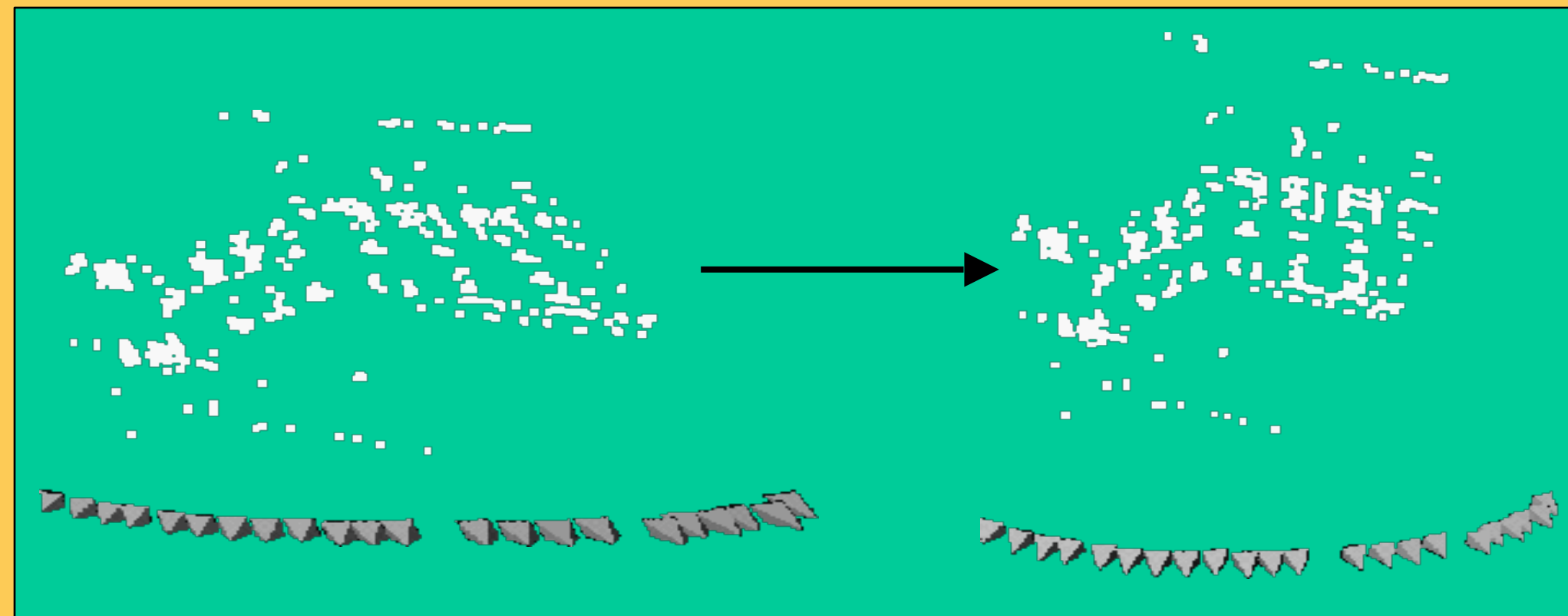
Compute T from

$$\tilde{\mathbf{I}} = \mathbf{T}\Omega_{\infty}^*\mathbf{T}^{\top} \text{ or } \mathbf{T}^{-1}\tilde{\mathbf{I}}\mathbf{T}^{-\top} = \Omega_{\infty}^* \text{ with } \tilde{\mathbf{I}} = \begin{bmatrix} \mathbf{I} & 0 \\ 0^{\top} & 0 \end{bmatrix}$$

using eigenvalue decomposition of Ω_{∞}^*

and then obtain metric reconstruction as

\mathbf{PT}^{-1} and \mathbf{TM}



CRITICAL MOTION SEQUENCES

(Sturm, CVPR'97, Kahl, ICCV'99, Pollefeys, PhD'99)

- Self-calibration depends on camera motion
- Motion sequence is not always general enough
- **Critical Motion Sequences** have more than one potential absolute conic satisfying all constraints
- Possible to derive classification of CMS

CRITICAL MOTION SEQUENCES: ALGORITHM DEPENDENT

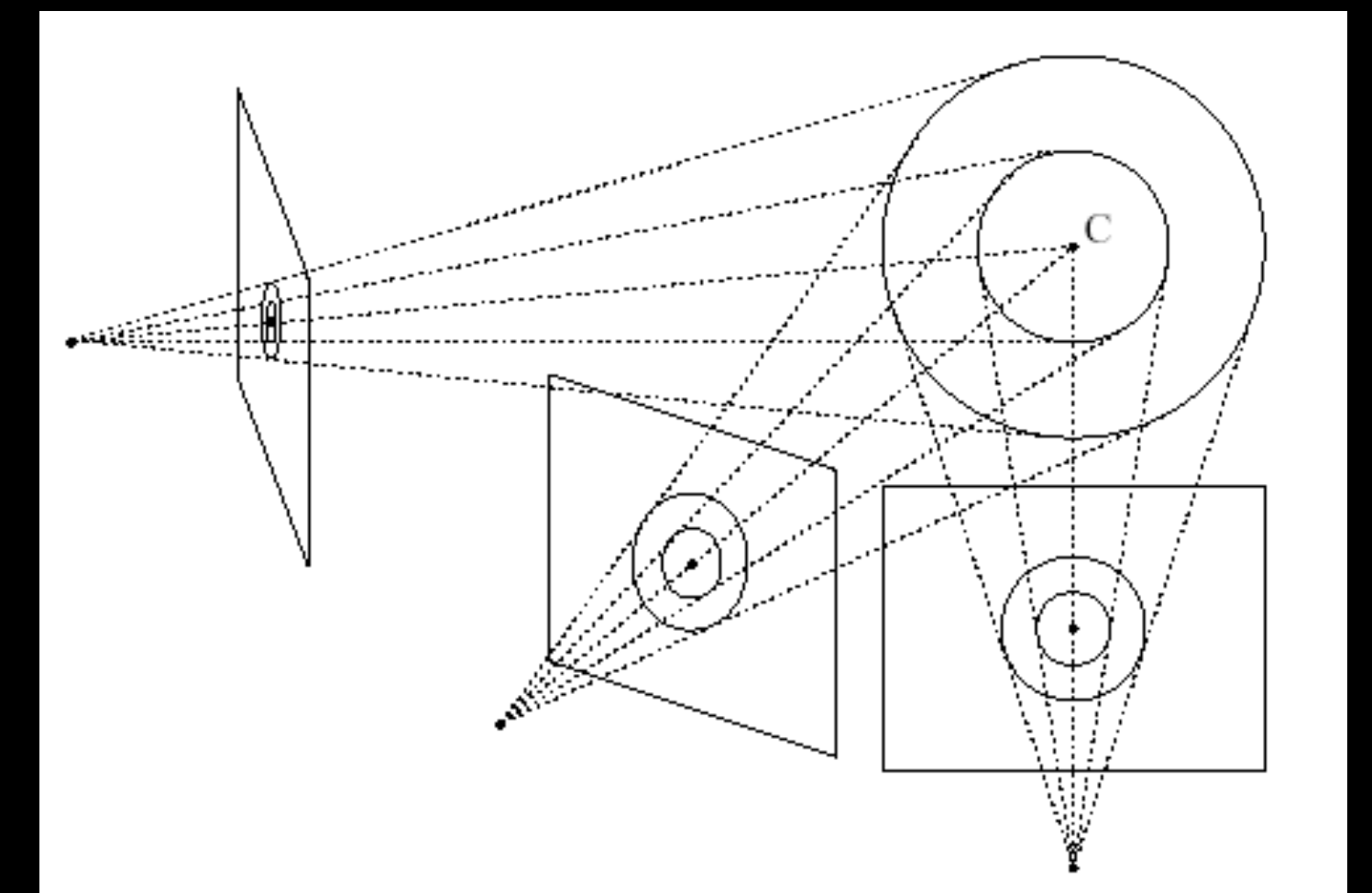
Additional critical motion sequences
can exist for some specific
algorithms

- ▶ when not all constraints are enforced

(e.g. not imposing rank 3 constraint)

- ▶ Kruppa equations/linear algorithm:
fixating a point

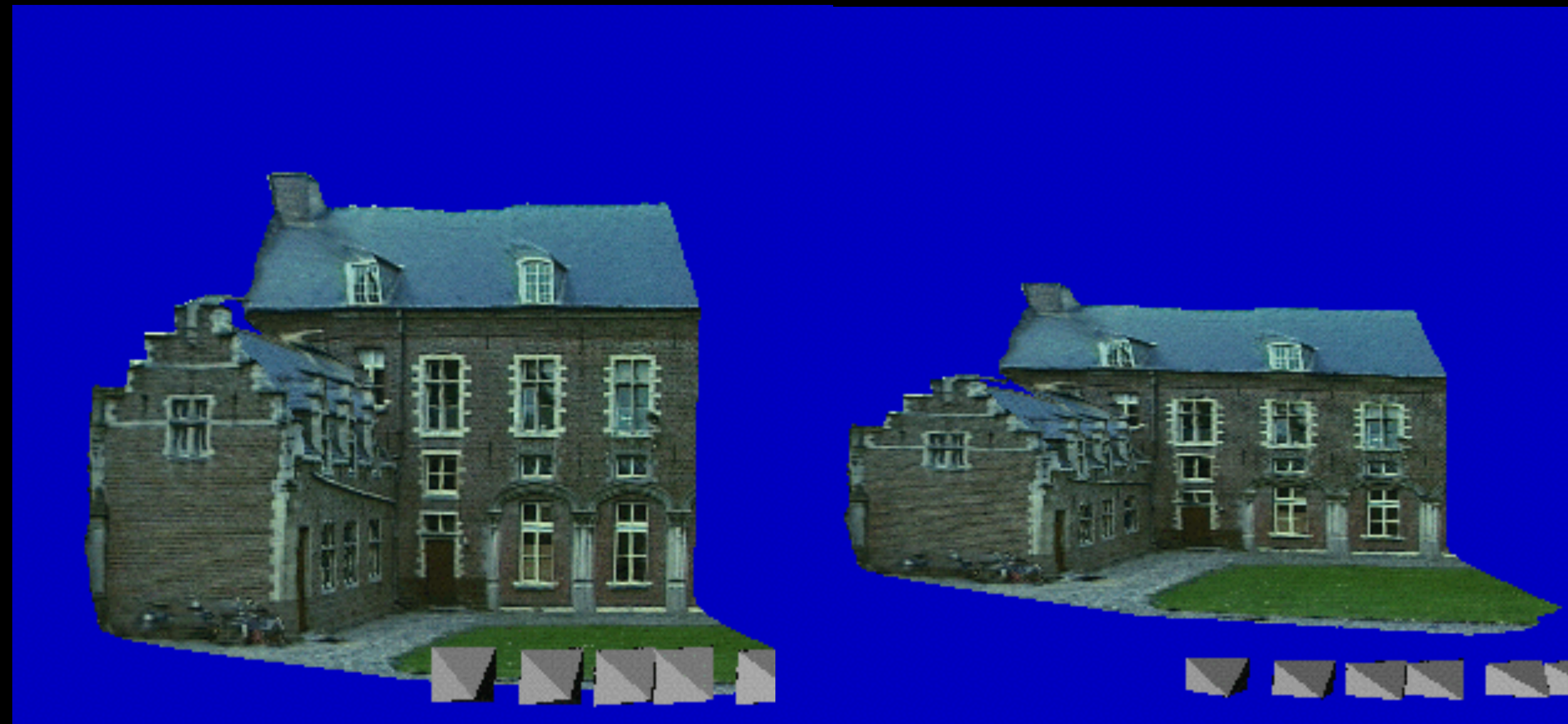
Some spheres also project to circles
located in the image and hence
satisfy all the linear/kruppa self-
calibration constraints



NON-AMBIGUOUS NEW VIEWS FOR CMS

(Pollefeys, ICCV'01)

- restrict motion of virtual camera to CMS
- use (wrong) computed camera parameters



REFERENCES

- ▶ <http://www.cs.unc.edu/~marc/tutorial/node76.html>
- ▶ R. Hartley and A. Zisserman, Multiple View Geometry in Computer Vision, chapter 19.