

Lab Task: Linear Regression: To find relationship between two variables

Task:

Build an excel worksheet calculates a linear regression equation. First two columns will contain two integers on each row and multiple rows in worksheet.

Regression Definition:

A regression is a statistical analysis assessing the association between two variables. It is used to find the relationship between two variables.

Regression Formula:

Regression Equation(y) = $w_0 + w_1x$

Slope(w_1) = $(N\sum XY - (\sum X)(\sum Y)) / (N\sum X^2 - (\sum X)^2)$

Intercept(w_0) = $(\sum Y - b(\sum X)) / N$

where

x and y are the variables.

w_1 = The slope of the regression line

w_0 = The intercept point of the regression line and the y axis.

N = Number of values or elements

X = First Score

Y = Second Score

$\sum XY$ = Sum of the product of first and Second Scores

$\sum X$ = Sum of First Scores

$\sum Y$ = Sum of Second Scores

$\sum X^2$ = Sum of square First Scores

Regression Example: To find the Simple/Linear Regression of

| X Values | Y Values |
|----------|----------|
| 60 | 3.1 |
| 61 | 3.6 |
| 62 | 3.8 |
| 63 | 4 |
| 65 | 4.1 |

To find regression equation, we will first find slope, intercept and use it to form regression equation.

Step 1: Count the number of values. $N = 5$

Step 2: Find XY , X^2 See the below table

| X Value | Y Value | $X*Y$ | $X*X$ |
|---------|---------|--------------------|------------------|
| 60 | 3.1 | $60 * 3.1 = 186$ | $60 * 60 = 3600$ |
| 61 | 3.6 | $61 * 3.6 = 219.6$ | $61 * 61 = 3721$ |
| 62 | 3.8 | $62 * 3.8 = 235.6$ | $62 * 62 = 3844$ |
| 63 | 4 | $63 * 4 = 252$ | $63 * 63 = 3969$ |
| 65 | 4.1 | $65 * 4.1 = 266.5$ | $65 * 65 = 4225$ |

Step 3: Find ΣX , ΣY , ΣXY , ΣX^2 .

$$\Sigma X = 311$$

$$\Sigma Y = 18.6$$

$$\Sigma XY = 1159.7$$

$$\Sigma X^2 = 19359$$

Step 4: Substitute in the above slope formula given.

$$\begin{aligned} \text{Slope}(w_1) &= (N\Sigma XY - (\Sigma X)(\Sigma Y)) / (N\Sigma X^2 - (\Sigma X)^2) \\ &= ((5)*(1159.7) - (311)*(18.6)) / ((5)*(19359) - (311)^2) \\ &= (5798.5 - 5784.6) / (96795 - 96721) \\ &= 13.9 / 74 \\ &= 0.19 \end{aligned}$$

Step 5: Now, again substitute in the above intercept formula given.

$$\begin{aligned} \text{Intercept}(w_1) &= (\Sigma Y - w_1 (\Sigma X)) / N \\ &= (18.6 - 0.19(311)) / 5 \\ &= (18.6 - 59.09) / 5 \\ &= -40.49 / 5 \\ &= -8.098 \end{aligned}$$

Step 6: Then substitute these values in regression equation formula

$$\begin{aligned} \text{Regression Equation (y)} &= w_0 + w_1x \\ &= -8.098 + 0.19x. \end{aligned}$$

Suppose if we want to know the approximate y value for the variable $x = 64$. Then we can substitute the value in the above equation.

$$\begin{aligned} \text{Regression Equation(y)} &= w_0 + w_1x \\ &= -8.098 + 0.19(64). \\ &= -8.098 + 12.16 \\ &= 4.06 \end{aligned}$$

This example will guide you to find the relationship between two variables by calculating the Regression from the above steps.

Data Set:

Year end foreign exchange rate Pak Rupees per US \$ taken from State Bank of Pakistan [1].

| YEAR | YEAR # | PKRS PRICE PER USD |
|------|--------|--------------------|
| 1981 | 1 | 13 |
| 1982 | 2 | 14 |
| 1983 | 3 | 14 |
| 1984 | 4 | 17 |
| 1985 | 5 | 17 |

| | | |
|------|----|----|
| 1986 | 6 | 18 |
| 1987 | 7 | 19 |
| 1988 | 8 | 22 |
| 1989 | 9 | 22 |
| 1990 | 10 | 25 |
| 1991 | 11 | 26 |
| 1992 | 12 | 28 |
| 1993 | 13 | 31 |
| 1994 | 14 | 32 |
| 1995 | 15 | 36 |
| 1996 | 16 | 41 |
| 1997 | 17 | 47 |
| 1998 | 18 | 52 |
| 1999 | 19 | 53 |
| 2000 | 20 | 65 |
| 2001 | 21 | 61 |
| 2002 | 22 | 58 |
| 2003 | 23 | 59 |
| 2004 | 24 | 60 |
| 2005 | 25 | 61 |
| 2006 | 26 | 61 |
| 2007 | 27 | 69 |
| 2008 | 28 | 82 |
| 2009 | 29 | 86 |
| 2010 | 30 | 86 |
| 2011 | 31 | 95 |
| 2012 | 32 | 99 |

Submission Procedure

Submit your excel sheet file like [NAME].[xlsx] for example ALI.xlsx etc. in an email with subject title “[ALI]-LABWORK-01” at swjaffry@pucit.edu.pk.

[1] <http://www.sbp.org.pk/ecodata/HER-USDollar.xls>