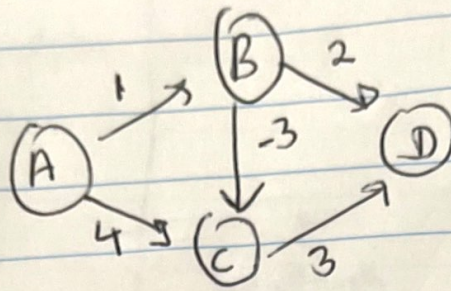


# Bellman Ford Algorithm works with cyclic graph

I/P -



Output Distances = {0, 1, -2, 1}   
 A B C D

Idea - to find shortest path of edge length 1 first, shortest path of edge length 2 second and so on

Note: Edge length is defined as no. of nodes pointing towards it

Algorithm - we relax all edges V-1 times

if  $d[u] > d[v] + \text{weight}(u, v)$   
 $d[v] = d[v] + \text{weight}(u, v)$

Why?

$v \rightarrow v \dots v_{n-1} \rightarrow v_n$   
 $v_{n-1} \rightarrow v_n$   
 $v_{n-2} \rightarrow v_{n-1}$   
 $v_{n-3} \rightarrow v_{n-2}$

Algorithm -

$d[v] = \{\infty, \infty, \infty, \dots, \infty\}$

$d[\text{src}] = 0$

for (count = 0; count < V-1; count++)

for every edge (u, v)

if  $d[u] > d[v] + w(u, v)$

$d[v] = d[v] + w(u, v)$

after V-1 iterat  
 $v_n$  will be  
 updated

Time complexity  $\rightarrow O(V \cdot E)$



Order  
doesn't  
matter

Order of edges

B-C

B-D

C-D

A-B

A-C

1st  
shortest path  
2nd shortest path  
3rd

A	B	C	D
0	$\infty$	$\infty$	$\infty$
0	1	<del>4</del>	$\infty$
0	1	-2	3
0	1	-2	1

Note  $\rightarrow$  If we do one more iteration, we  
can find negative cycle

for Every edge  $(u, v)$

if  $(d[u] > d[v] + \text{weight}(u, v))$   
print ("Negative cycle")