

## EE 779 Advanced topics in signal processing

### Assignment 4 simulations

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Given,  $\theta_1 = 0$  degrees. We carry out the experiment for two values of ' $\theta_2$ ' i.e 15 degrees and 7.5 degrees.

The functions:

```
function ulaData = generateULAData(numberOfSensors,
numberOfSnapshots, secondAngle)

centerFrequency = 4000;
spacing = 0.5;
firstAngle = 0;

sourceMatrix1 = getSourceMatrix(numberOfSensors,
numberOfSnapshots, firstAngle, spacing, centerFrequency);
sourceMatrix2 = getSourceMatrix(numberOfSensors,
numberOfSnapshots, secondAngle, spacing, centerFrequency);
sourceMatrix = sourceMatrix1 + sourceMatrix2;

ulaData = sourceMatrix + getErrorMatrix(numberOfSensors,
numberOfSnapshots);

end

%% make array transfer vector a(theta)

function directionVector = getDirectionVector(angle, spacing,
numberOfSensors, centerFrequency)

wavelength = 1;
speedOfPropagation = centerFrequency * wavelength;
wc = 2 * pi * centerFrequency;
angle = angle * pi / 180;
k = 1:numberOfSensors;
delay = (k - 1) .* (spacing * sin(angle) / speedOfPropagation);
directionVector = exp(-1i * wc * delay);
```

```

directionVector = directionVector(:);

end

%% get a source signal

function sourceSignal = getSourceSignal(numberOfSnapshots)

sourceSignal = wgn(1, numberOfSnapshots, 1, 'linear',
'complex');

end

%% get an error signal

function errorSignal = getErrorSignal(numberOfSnapshots)

errorSignal = wgn(1, numberOfSnapshots, 1, 'linear', 'complex');

end

%% get an error matrix

function errorMatrix = getErrorMatrix(numberOfSensors,
numberOfSnapshots)

errorSignalCell = cell(numberOfSensors, 1);
for k = 1:numberOfSensors
    errorSignalCell{k} = getErrorSignal(numberOfSnapshots);
end
errorMatrix = cat(1, errorSignalCell{:});

end

%% get a source matrix

function sourceMatrix = getSourceMatrix(numberOfSensors,
numberOfSnapshots, angle, spacing, centerFrequency)

sourceSignal = getSourceSignal(numberOfSnapshots);
directionVector = getDirectionVector(angle, spacing,
numberOfSensors, centerFrequency);
sourceMatrix = directionVector * sourceSignal;

end

```

```
function avgUlaData = getMonteCarloUlaData(numberOfRealizations,
secondAngle)
```

```
m = 10; N = 100;
```

```
avgUlaData = generateULADData(m, N, secondAngle);
for k = 1:numberOfRealizations-1
    avgUlaData = avgUlaData + generateULADData(m, N,
secondAngle);
end
avgUlaData = avgUlaData ./ numberOfRealizations;
```

```
end
```

```
function estimatedSpectrum = getSpectrum(frequencyEstimates)
```

```
N=100;
```

```
t = 1:N;
```

```
x = zeros(size(t));
```

```
for k = 1:length(frequencyEstimates)
    x = x + (exp(1i * frequencyEstimates(k) .* t));
end
```

```
% now get the spectrum using fft
```

```
M = 2 ^ nextpow2(4 * length(x));
estimatedSpectrum = 10 * log10(abs(fftshift(fft(x, M))));
L = length(estimatedSpectrum); % we want only  $-\pi/2$  to  $\pi/2$ 
estimatedSpectrum = estimatedSpectrum(round(L/4):round(3 * L/
4));
```

```
end
```

Plotting functions:

```
function plotSpectraOfUlaData(secondAngle, numberOfAngleSamples)
```

```
%% do beamforming
```

```
ULADData = getMonteCarloUlaData(50, secondAngle);
```

```

phi = beamform(ULADData, numberOfAngleSamples, 0.5);
figure;
plot(phi); axis tight;
title(['Beamforming data for ',
num2str(numberOfAngleSamples), ...
' angle samples at \theta_1 = 0 and \theta_2 = ',
num2str(secondAngle), ' degrees']);

%% do Capon beamforming

phiCapon = capon_sp(ULADData, numberOfAngleSamples, 0.5);
figure;
plot(phiCapon); axis tight;
title(['Capon beamforming data for ',
num2str(numberOfAngleSamples), ...
' angle samples at \theta_1 = 0 and \theta_2 = ',
num2str(secondAngle), ' degrees']);

%% do root MUSIC and plot spectrum

doaMusic = root_music_doa(ULADData, 2, 0.5) .* (pi/180);
rootMusicSpectrum = getSpectrum(doaMusic);
w = -(length(rootMusicSpectrum)/2):(length(rootMusicSpectrum)/
2)-1;
w = 180 * w ./ length(rootMusicSpectrum);
figure;
plot(w, rootMusicSpectrum);
axis tight;
title(['Root MUSIC spectrum for ',
num2str(numberOfAngleSamples), ...
' angle samples at \theta_1 = 0 and \theta_2 = ',
num2str(secondAngle), ' degrees']);
xlabel('Angles in degrees');

%% do ESPRIT and plot spectrum

doaESPRIT = esprit_doa(ULADData, 2, 0.5) .* (pi/180);
espritSpectrum = getSpectrum(doaESPRIT);
w = -(length(espritSpectrum)/2):(length(espritSpectrum)/2)-1;
w = 180 * w ./ length(espritSpectrum);
figure;
plot(w, espritSpectrum);
axis tight;
title(['ESPRIT spectrum for ',
num2str(numberOfAngleSamples), ...

```

```
    ' angle samples at \theta_1 = 0 and \theta_2 = ',  
num2str(secondAngle), ' degrees']);  
xlabel('Angles in degrees');
```

```
end
```

Plotting script:

```
close all; clear all;
```

```
addpath /Users/swrangsarbasumatary/Desktop/advSignalProcAsgn4/  
ch6/
```

```
addpath /Users/swrangsarbasumatary/Desktop/advSignalProcAsgn4/
```

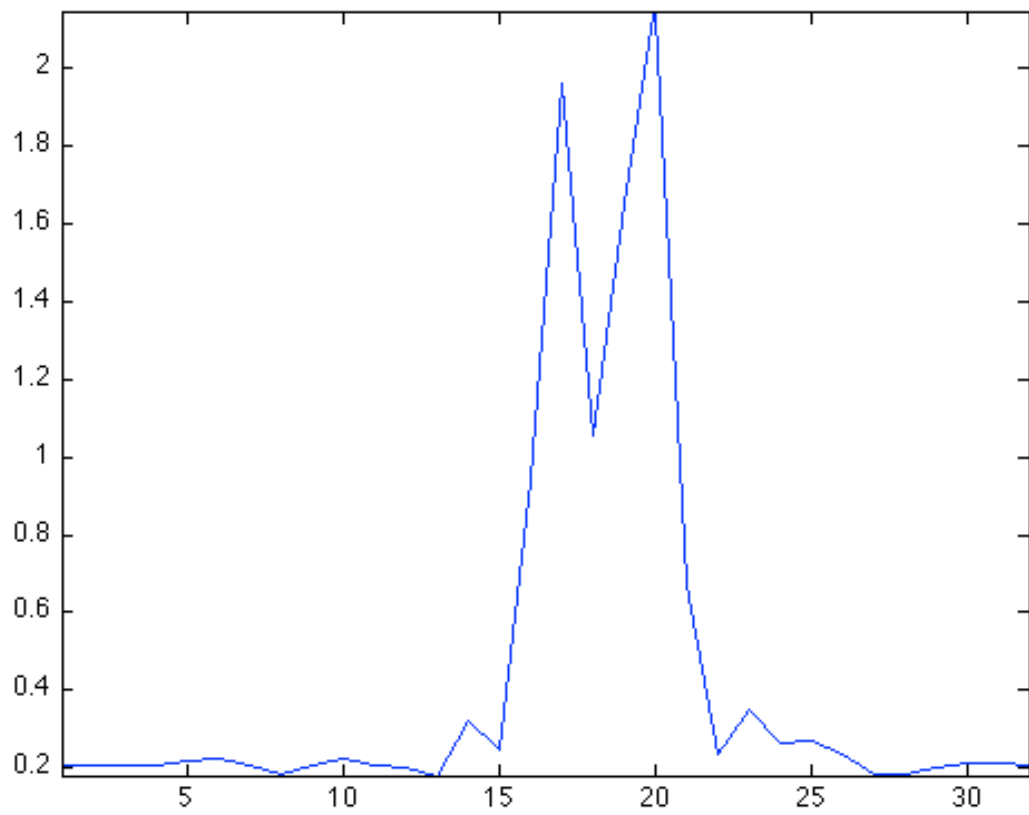
```
plotSpectraOfUlaData(15, 32);  
plotSpectraOfUlaData(15, 64);  
plotSpectraOfUlaData(7.5, 64);  
plotSpectraOfUlaData(7.5, 512);
```

```
rmpath /Users/swrangsarbasumatary/Desktop/advSignalProcAsgn4/  
rmpath /Users/swrangsarbasumatary/Desktop/advSignalProcAsgn4/  
ch6/
```

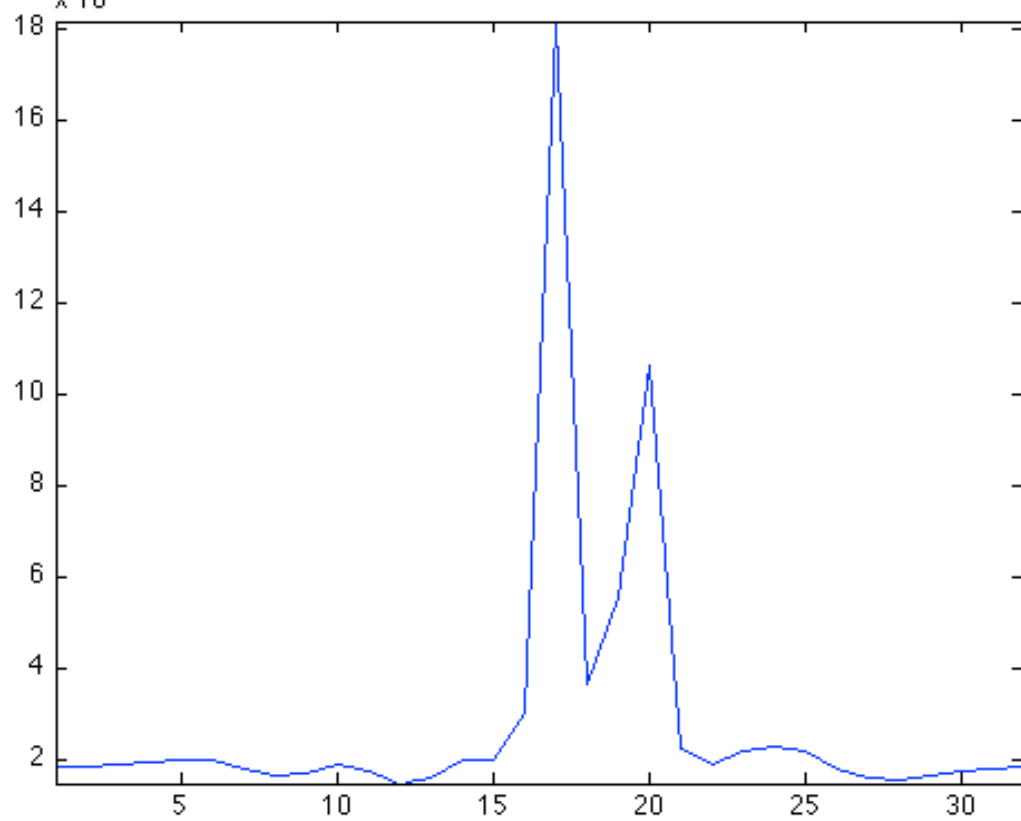
The plots:

For 32 samples of angles in [-90, 90] (in degrees) and  $\theta_2 = 15$  degrees

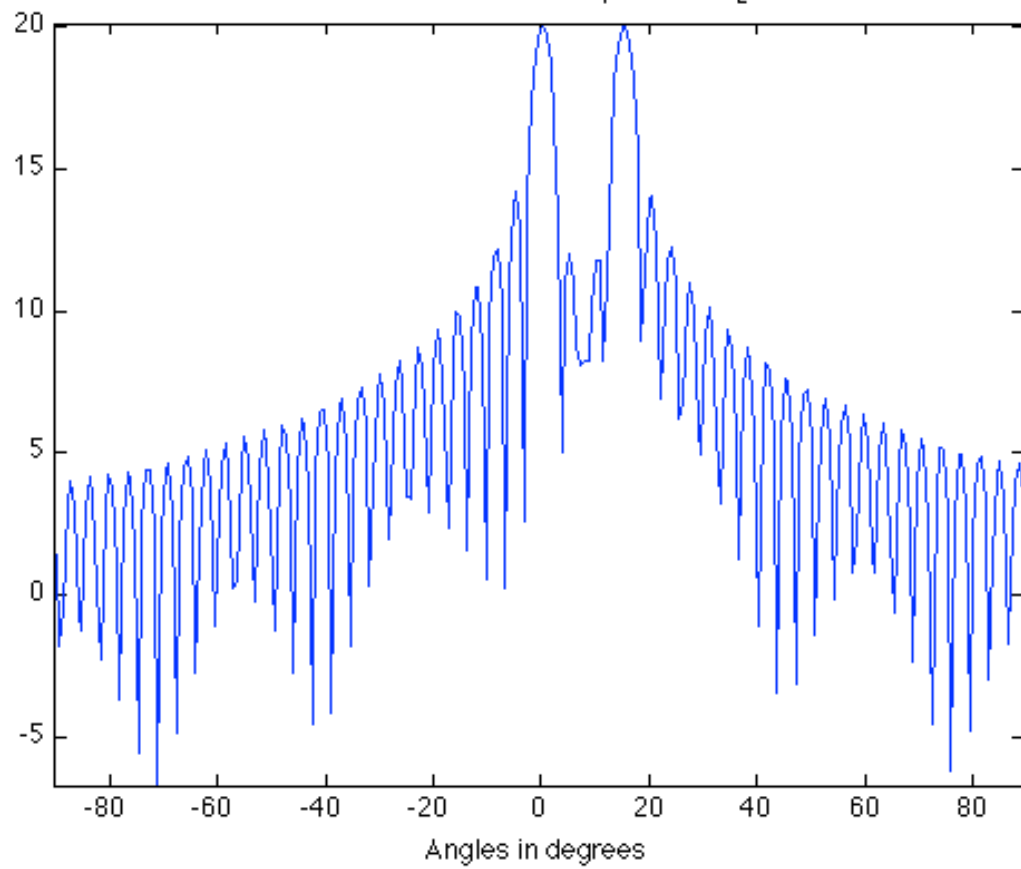
Beamforming data for 32 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 15$  degrees



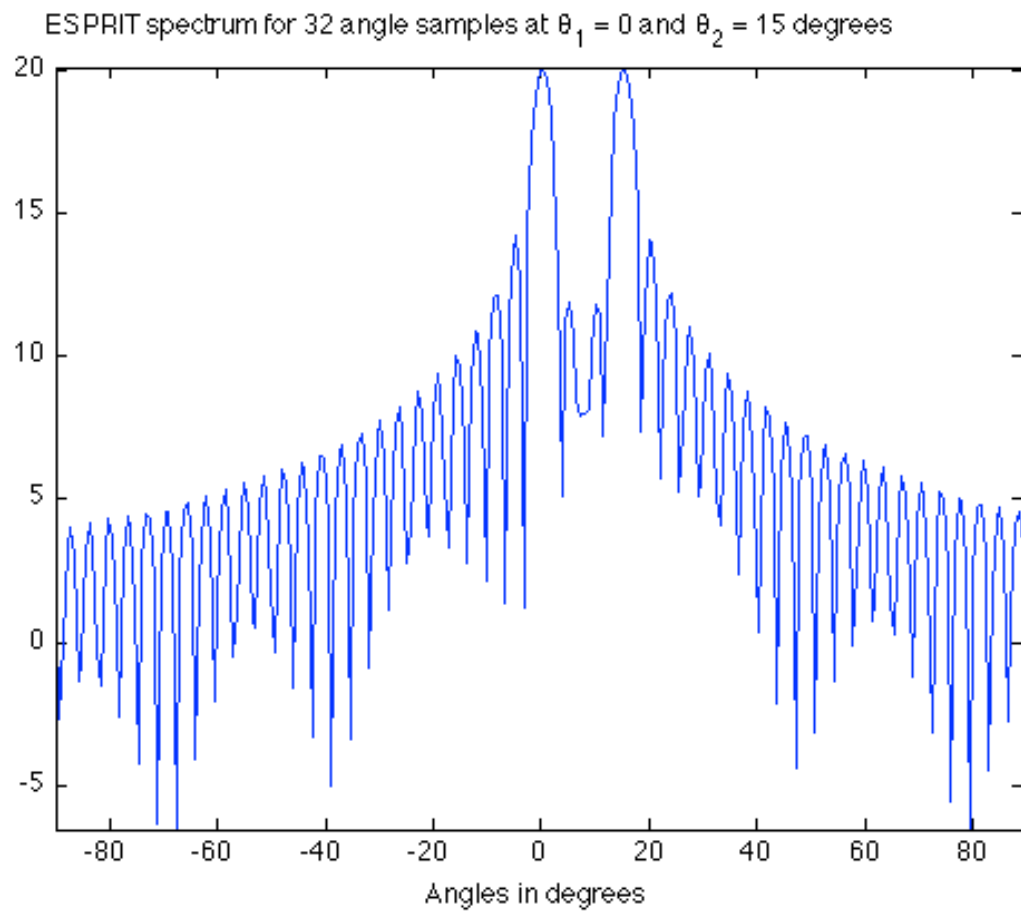
Capon beamforming data for 32 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 15$  degrees  
 $\times 10^4$



RootMUSIC spectrum for 32 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 15$  degrees

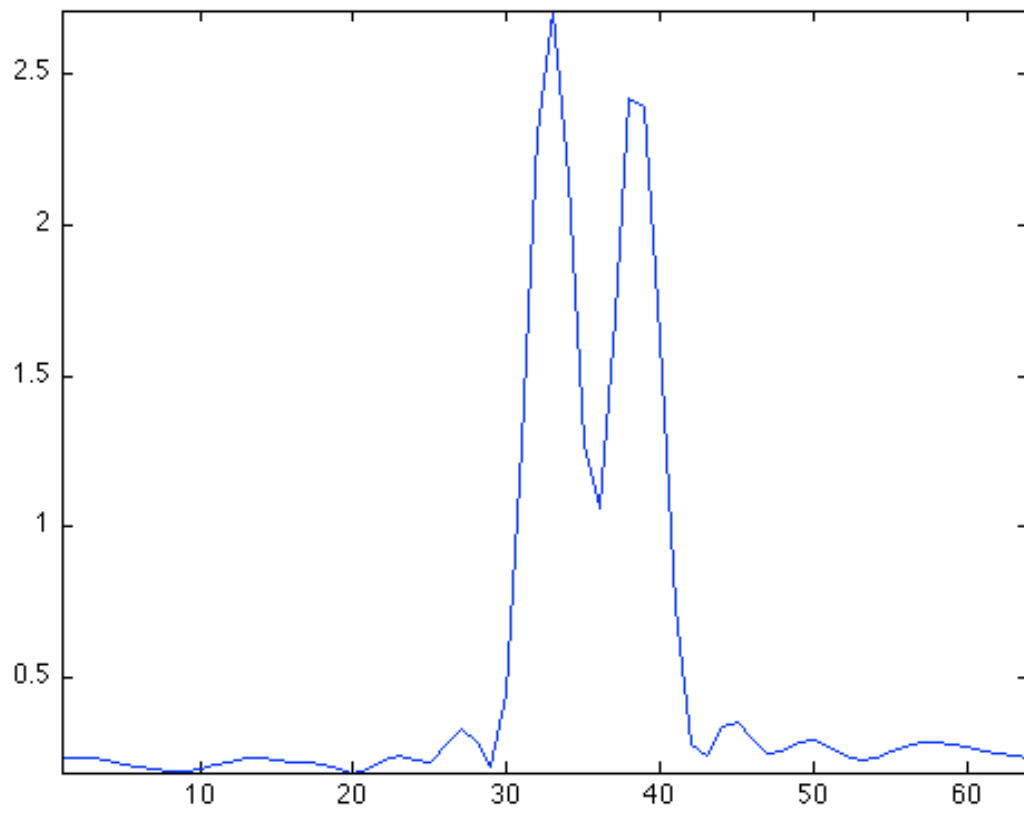




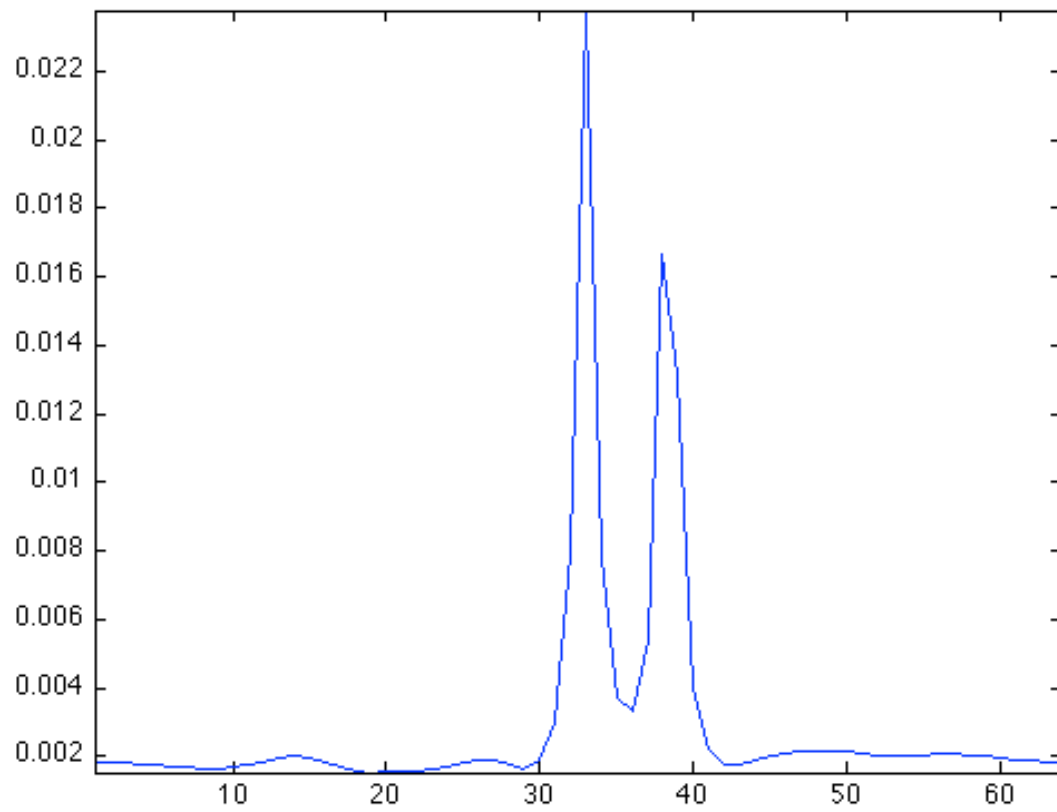


For 64 samples of angles in  $[-90, 90]$  (in degrees) and  $\theta_2 = 15$  degrees

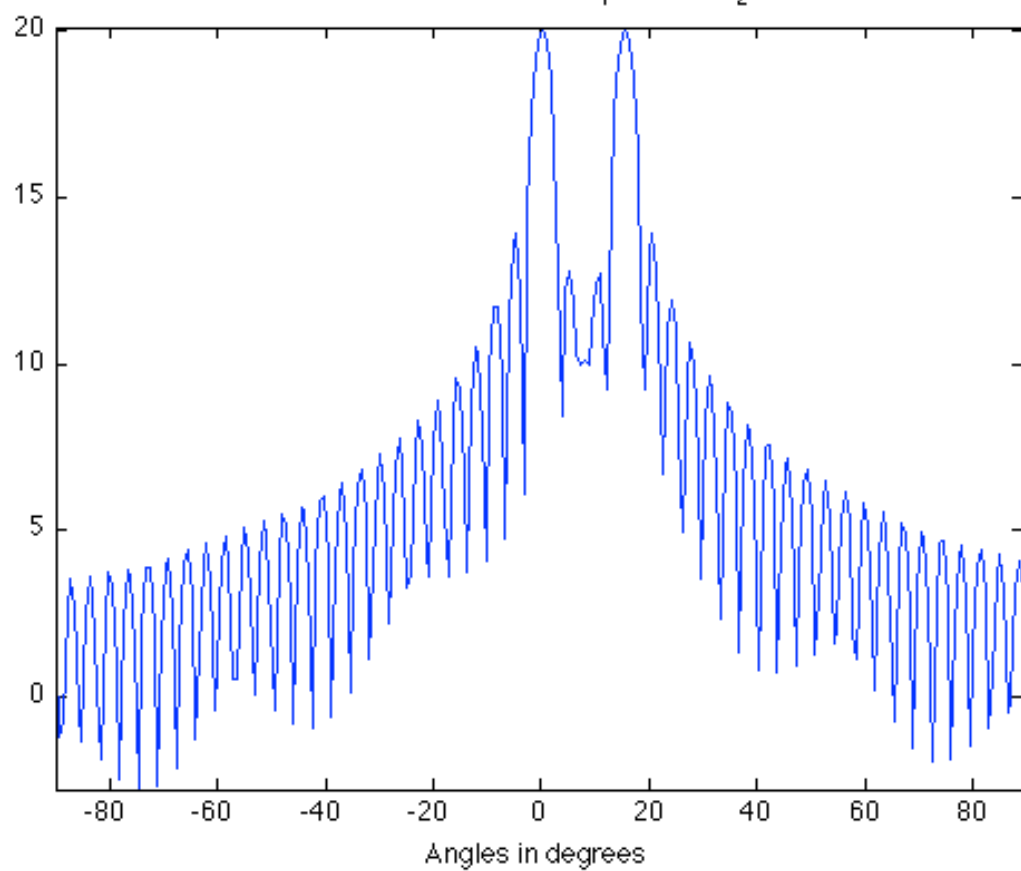
Beamforming data for 64 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 15$  degrees

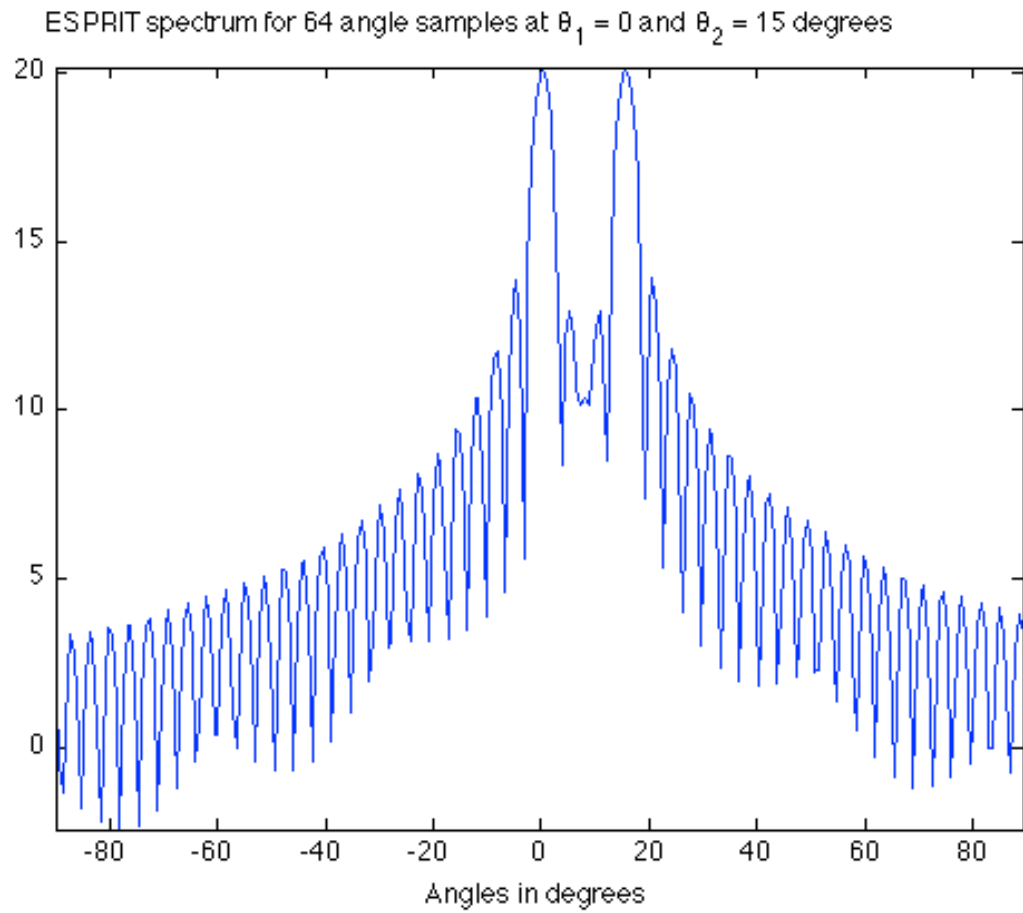


Capon beamforming data for 64 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 15$  degrees



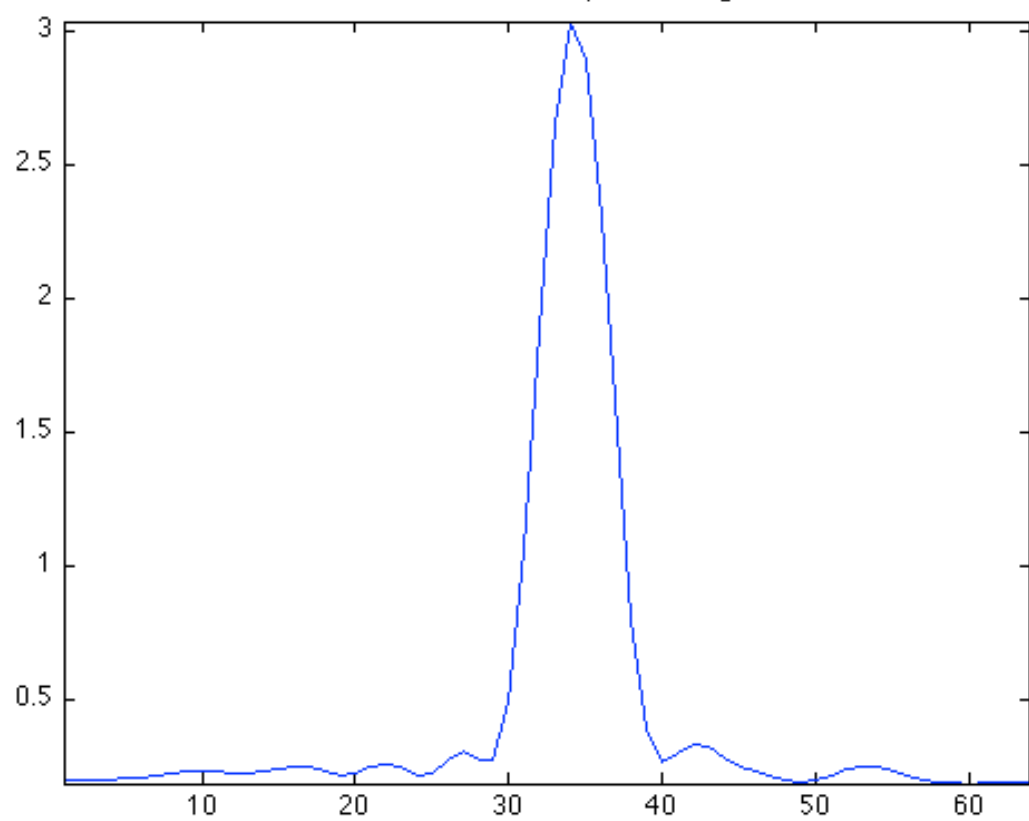
RootMUSIC spectrum for 64 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 15$  degrees



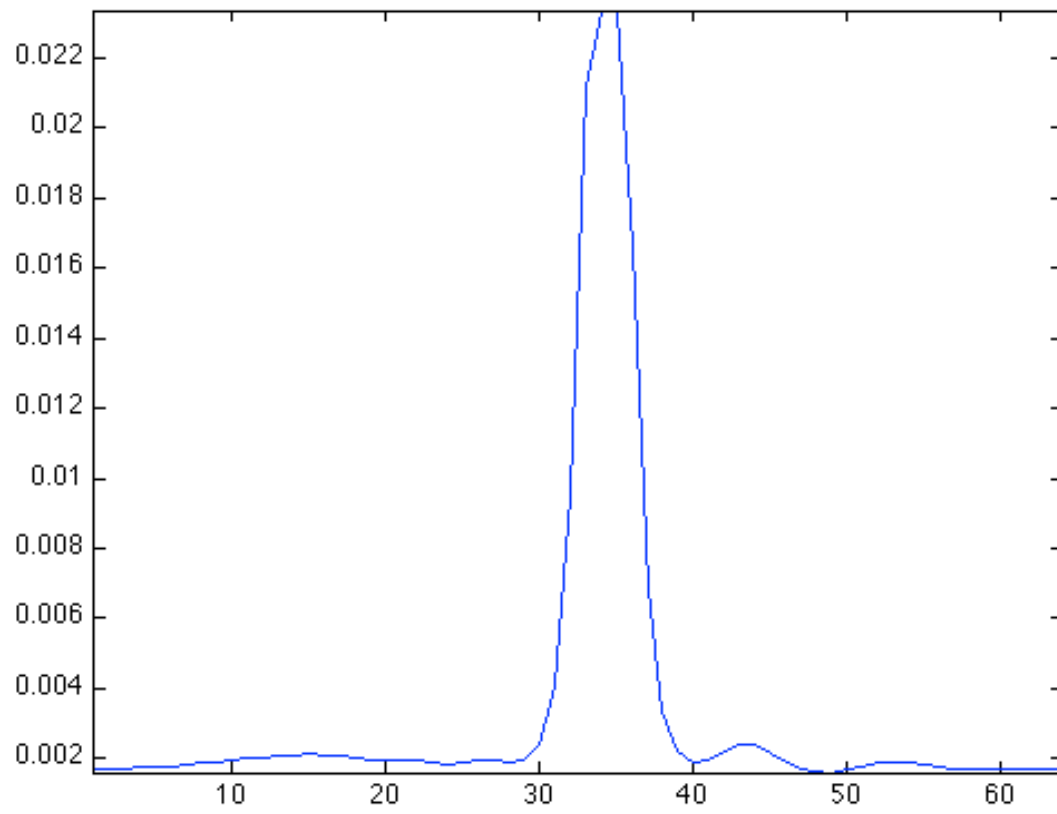


For 64 samples of angles in  $[-90, 90]$  (in degrees) and  $\theta_2 = 7.5$  degrees

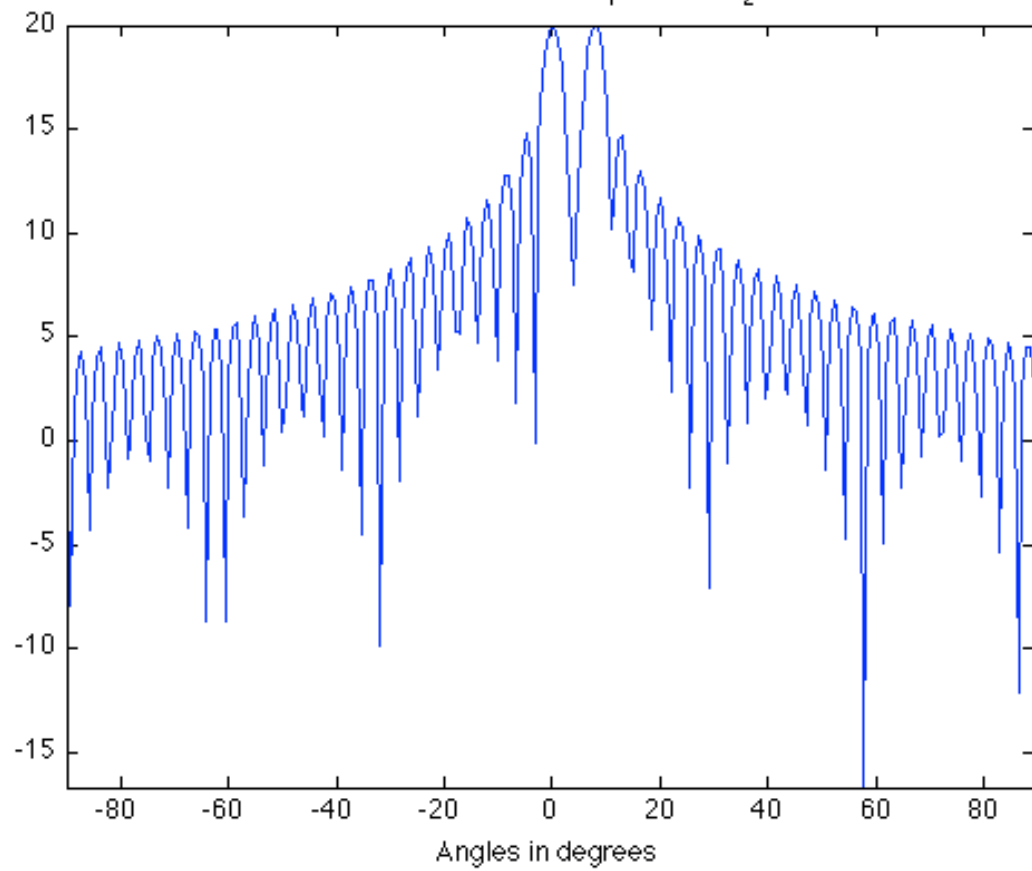
Beamforming data for 64 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 7.5$  degrees



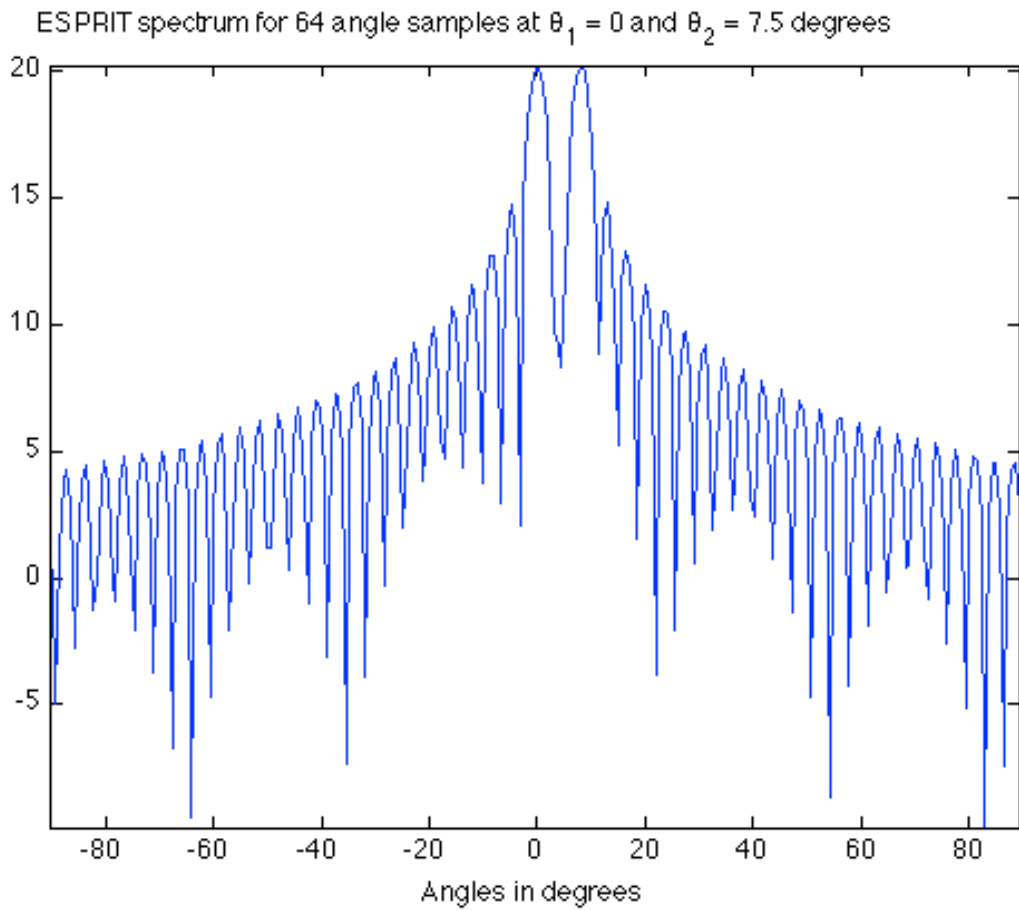
Capon beamforming data for 64 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 7.5$  degrees



RootMUSIC spectrum for 64 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 7.5$  degrees

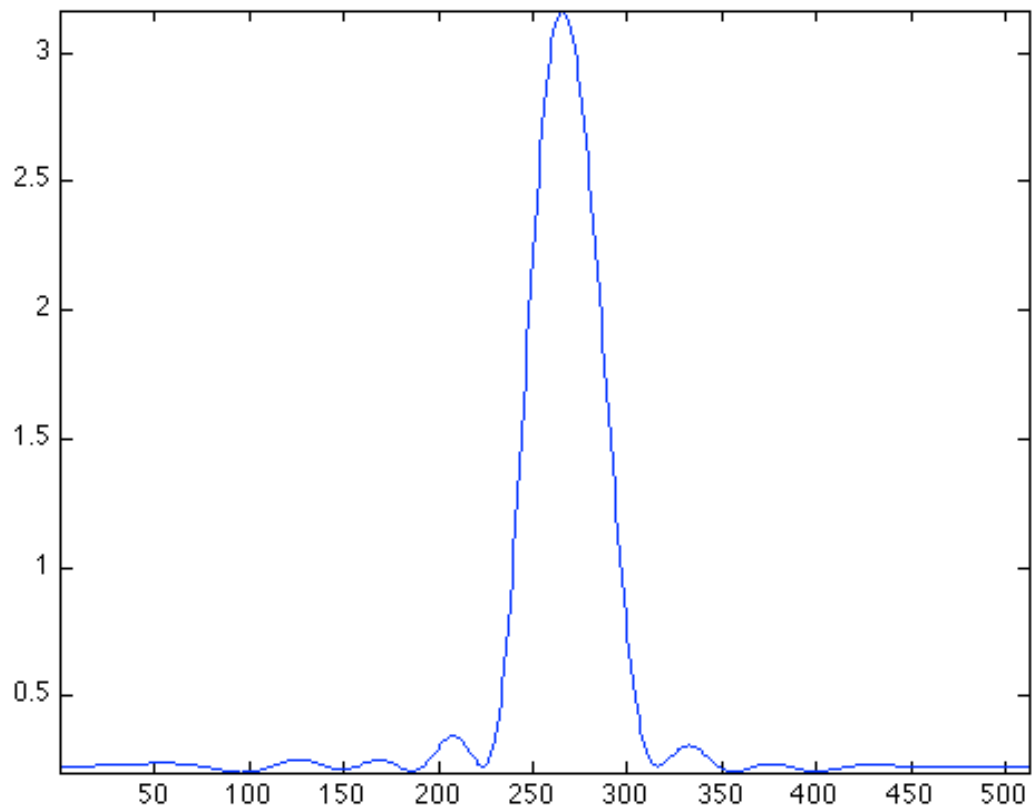




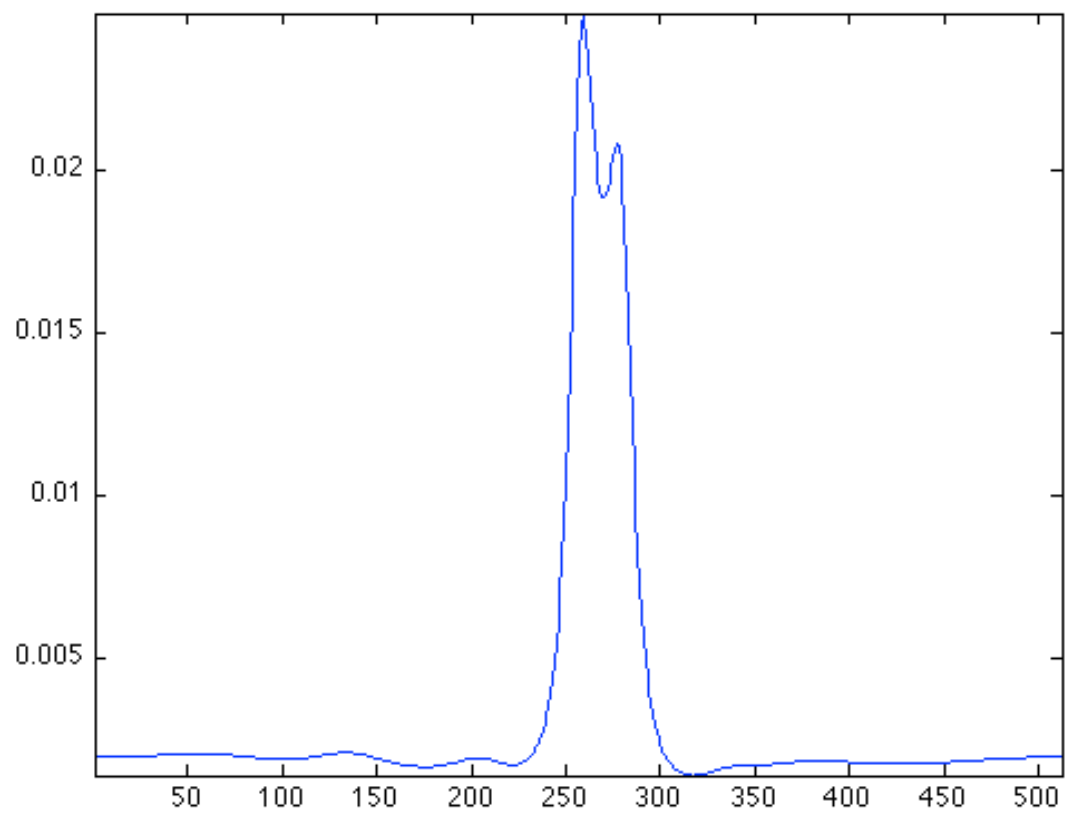


For 512 samples of angles in  $[-90, 90]$  (in degrees) and  $\theta_2 = 15$  degrees

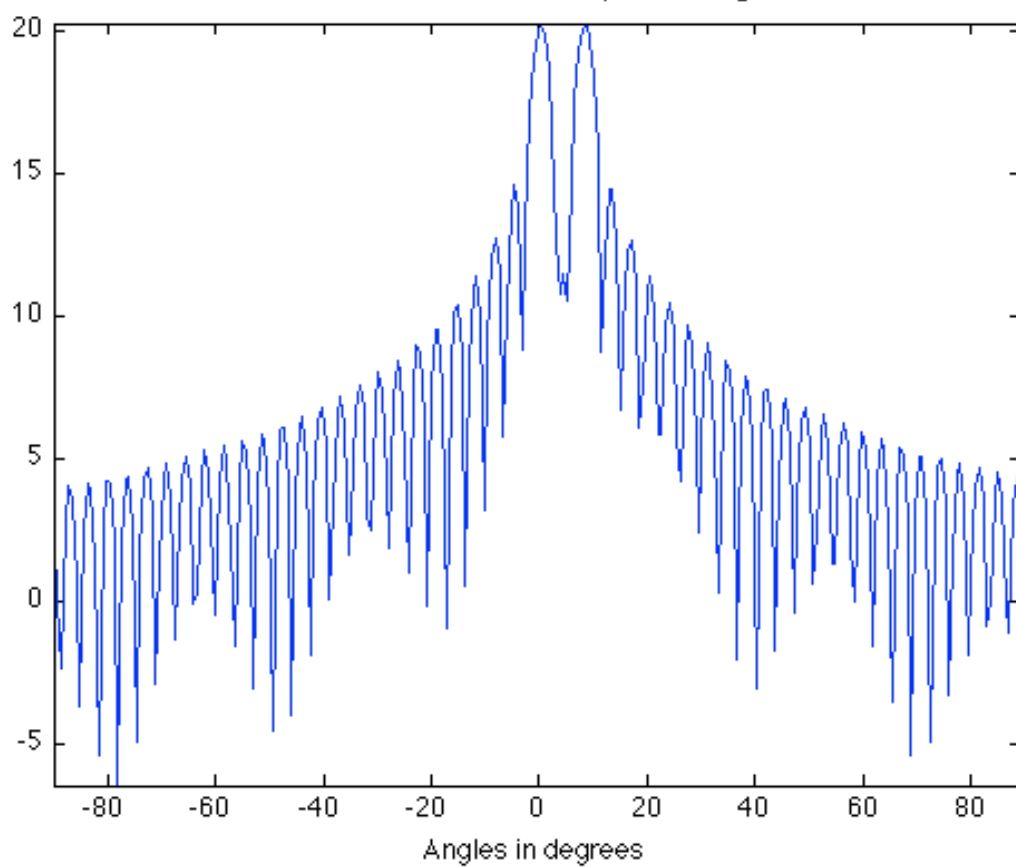
Beamforming data for 512 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 7.5$  degrees

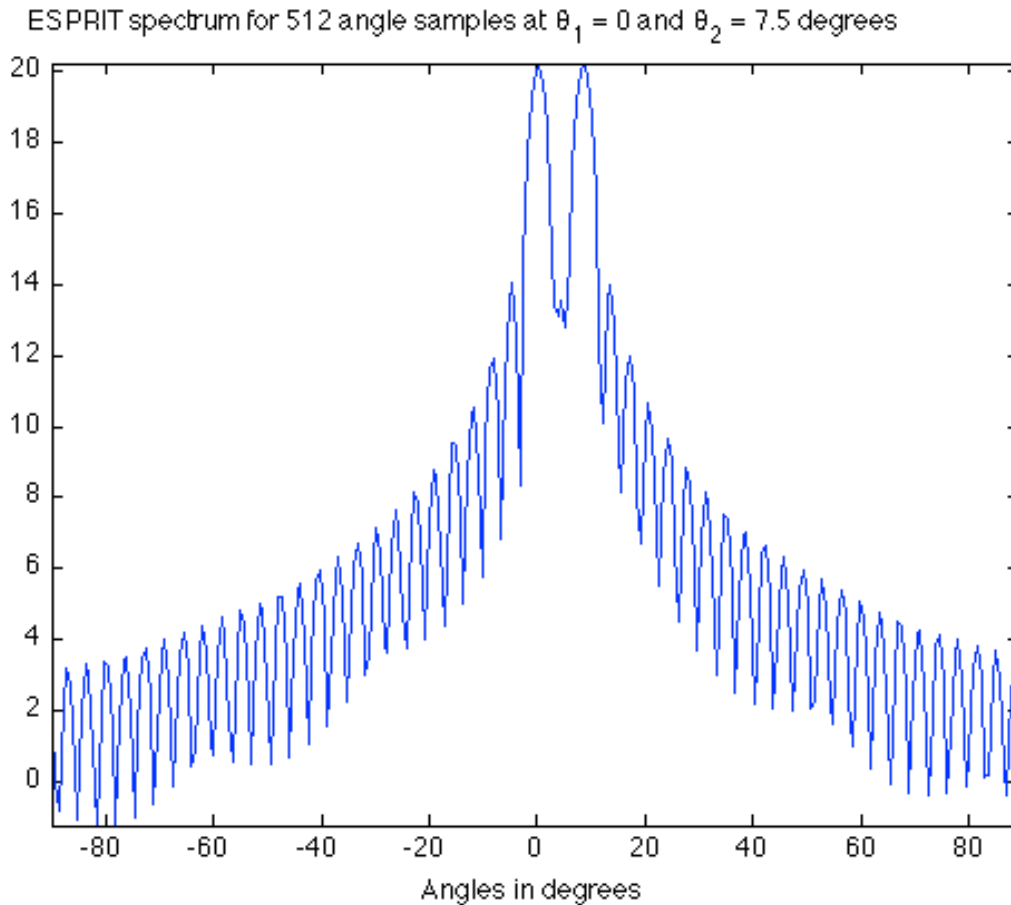


Capon beamforming data for 512 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 7.5$  degrees



RootMUSIC spectrum for 512 angle samples at  $\theta_1 = 0$  and  $\theta_2 = 7.5$  degrees





### Discussion:

For  $\theta_2 = 15$  the two spatial frequencies are resolved well for angle samples of 32 and more. '32' is not the minimum but if we keep decreasing the number of angle samples the two different sources cannot be resolved because the peaks start to merge into a single peak.

For  $\theta_2 = 7.5$  the two spatial frequencies(signal sources) are not resolved by both Beamforming method and the Capon beamforming method even at 32 angle samples. But at 512 angle samples atleast the Capon beamforming method atleast begins to be able to resolve the two sources.

So Capon can be considered more powerful than the normal beamforming method. But MUSIC method is better than them both because at the above number of angle samples and  $\theta_2$  values under discussion the MUSIC method is able to resolve the two sources. The ESPRIT method is even better. We know

that the ESPRIT method is better than the MUSIC method from the previous assignments.