EE 610 Image Processing Project 2

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Implementing the 'A' matrix

The plots the initial image estimates (the data) and the final image estimates (the output after carrying out the TV constraint and so on) are as follows:

Initial image estimate using 8 spokes

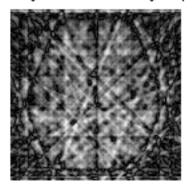
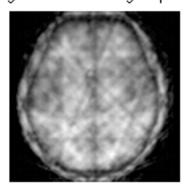


Image estimate using 8 spokes



Initial image estimate using 16 spokes

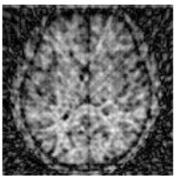
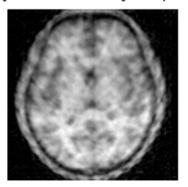


Image estimate using 16 spokes



Initial image estimate using 32 spokes

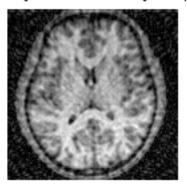
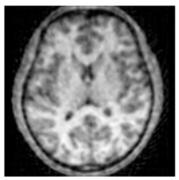


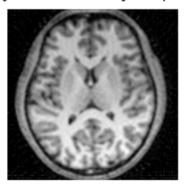
Image estimate using 32 spokes



Initial image estimate using 64 spokes



Image estimate using 64 spokes



The functions:

```
function [x, repetitionCounter] = fnlCg(x0,numberOfSpokes,data,
param)
%------
%------
% the nonlinear conjugate gradient method
disp('running fnlcg');
x = x0;
```

```
% line search parameters - Dont touch..leave alone
maxlsiter = 150;
qradToll = 1.0000e-030;
alpha = 0.0100;
beta = 0.6000;
t0 = 1;
Itnlim = 16;
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repetitionCounter = 0;
previousObjective = 0;
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k = 0;
% copmute q0 = qrad(Phi(x))
g0 = wGradient(x,numberOfSpokes,data, param);
dx = -q0;
% iterations
while(1)
% backtracking line-search
    % pre-calculate values, such that it would be cheap to
compute the objective
    % many times for efficient line-search
    f0 = objective(x,dx, 0, numberOfSpokes,data, param);
    t = t0;
        [f1] = objective(x,dx, t,numberOfSpokes,data, param);
    lsiter = 0;
    while (f1 > f0 - alpha*t*abs(q0(:)'*dx(:)))^2 &
(lsiter<maxlsiter)
        lsiter = lsiter + 1;
        t = t * beta;
        [f1] = objective(x,dx, t,numberOfSpokes,data, param);
    end
    if lsiter == maxlsiter
        disp('Reached max line search,.... not so good... might
have a bug in operators. exiting... ');
```

```
return;
    end
    % control the number of line searches by adapting the
initial step search
    if lsiter > 2
        t0 = t0 * beta;
    end
    if lsiter<1</pre>
        t0 = t0 / beta;
    end
   x = (x + t*dx);
    %---- uncomment for debug purposes
    disp(sprintf('%d , obj: %f ', k,f1));
    %conjugate gradient calculation- Dont touch
    g1 = wGradient(x,numberOfSpokes,data, param);
    bk = g1(:)'*g1(:)/(g0(:)'*g0(:)+eps);
    q0 = q1;
    dx = -g1 + bk* dx;
    k = k + 1;
    %TODO: need to "think" of a "better" stopping criteria ;-)
    if f1 == previousObjective
        repetitionCounter = repetitionCounter + 1;
    else
        repetitionCounter = 0;
    end
    previousObjective = f1;
    if (k > Itnlim) | (norm(dx(:)) < gradToll)</pre>
        break:
    end
    if repetitionCounter > 7
        break:
    end
```

```
repetitionCounter
return;
end
%% the objective function
function [res] = objective(x,dx,t,numberOfSpokes,data, param)
%DEFINE obj
x = x + (t * dx);
b = data;
Ax = getDataMatrix(x, numberOfSpokes);
obj = (Ax - b);
res= (obj(:)'*obj(:)) + (param.TVWeight * getTotalVariation(x))
+ ...
    (param.FOVWeight * fov(x)) + (param.POSWeight *
getPosResidual(x)) + ...
    (param.LaplacianWeight * getLaplacianResidual(x));
end
%% the grad function
function grad = wGradient(x,numberOfSpokes,data, param)
%Define this function
gradObj=gOBJ(x,numberOfSpokes,data);
grad = (gradObj) + (param.TVWeight * gradTotalVariation(x))
+ ...
    (param.FOVWeight * gradFOV(x)) + (param.POSWeight *
getPosGradient(x)) ...
    + (param.LaplacianWeight * getLaplacianGradient(x));
end
%% calculating the gradient of the Objective
function gradObj = gOBJ(x,numberOfSpokes,data)
% computes the gradient of the data consistency
b = data;
inputSize = size(x, 1);
```

```
Ax = getDataMatrix(x, numberOfSpokes);
AhAx = getImageMatrix(Ax, numberOfSpokes, inputSize);
Ahb = getImageMatrix(b, numberOfSpokes, inputSize);
qradObj = 2 * (AhAx - Ahb);
end
%% the function implementing system matrix A
function dataMatrix = getDataMatrix(imageMatrix, numberOfSpokes)
theta = 0:numberOfSpokes-1;
theta = theta .* (180/numberOfSpokes);
dataMatrix = radon(imageMatrix, theta);
dataMatrix = fft(dataMatrix, [], 1); % column fft of the matrix
end
%% function implementing the adjoint system matrix A*
function imageMatrix = getImageMatrix(dataMatrix,
numberOfSpokes, inputSize)
theta = 0:numberOfSpokes-1;
theta = theta .* (180/numberOfSpokes);
imageMatrix = ifft(dataMatrix, [], 1);
imageMatrix = iradon(imageMatrix, theta, 'linear', 'Ram-Lak', 1,
inputSize);
end
%% the total variation penalty function
function totalVariation = getTotalVariation(imageMatrix)
variationX = filter2([1 -1 0], imageMatrix);
variationY = filter2([1; -1; 0], imageMatrix);
mag = sqrt( (abs(variationX) .^ 2) + abs((variationY) .^ 2));
totalVariation = sum(mag(:));
end
%% gradient of the total variation
```

```
function gradTV = gradTotalVariation(imageMatrix)
gradTV=filter2([0 -1 1],filter2([1 -1 0], imageMatrix))
+filter2([0;-1;1],filter2([1; -1; 0], imageMatrix));
end
%% the FOV Mask function
function fovMask = fovMask(inputMatrix)
[rows, cols] = size(inputMatrix);
xRadius = ceil(rows/2);
yRadius = ceil(cols/2);
[X, Y] = meshgrid(-(xRadius):(rows-(xRadius+1)), -yRadius:(cols-
(yRadius + 1));
a = 4;
b = 5;
term1 = (X./a).^2;
term2 = (Y./b).^2;
radius = sqrt(term1 + term2);
normalizer = sqrt((xRadius/a)^2 + (0/b)^2);
normalizedRadius = radius/normalizer;
mask = normalizedRadius < 0.93;</pre>
inputMatrix(mask) = 0;
fovMask = inputMatrix;
end
%% the FOV penalty function
function fov = fov(x)
x = fovMask(x);
mag = abs(x) \cdot ^2;
fov = sum(mag(:));
end
%% the gradient of the FOV function
function gradFOV = gradFOV(x)
```

```
x = fovMask(x);
gradFOV = 2 .* x;
end
%% the POS function
function posResidual = getPosResidual(x)
mask = x < 0;
posMatrix = (x .* mask) .^ 2;
posResidual = sum(posMatrix(:));
end
%% gradient of the POS function
function posGradient = getPosGradient(x)
mask = x < 0;
posGradient = 2 * (x .* mask);
end
%% the laplacian function
function laplacianResidual = getLaplacianResidual(imageMatrix)
laplacianX = filter2([1 -2 1], imageMatrix);
laplacianY = filter2([1; -2; 1], imageMatrix);
mag = sqrt( (abs(laplacianX) .^ 2) + abs((laplacianY) .^ 2));
laplacianResidual = sum(mag(:));
end
%% the gradient of the laplacian
function laplacianGradient = getLaplacianGradient(imageMatrix)
laplacianGradient = filter2([0 -1 1],filter2([1 -2 1],
imageMatrix))+filter2([0;-1;1],filter2([1; -2; 1],
imageMatrix));
end
```

```
The script:
close all; clear all;
addpath /Users/swrangsarbasumatary/Desktop/
imageProcessingProject2/
load sim 8ch data
disp('data loaded');
inputImage = anatomy orig;
numberOfSpokes = 8;
% generating the data vector
theta = 0:numberOfSpokes-1;
theta = theta .* (180/numberOfSpokes);
dataMatrix = radon(inputImage, theta);
dataMatrix = fft(dataMatrix, [], 1);
imageMatrix = ifft(dataMatrix, [], 1);
imageMatrix = iradon(imageMatrix, theta, 'linear', 'Ram-Lak', 1,
size(inputImage, 1));
% Reconstruction Parameters
param.TVWeight = 0.0001; % Weight for TV penalty
param.FOVWeight = 1;
param.POSWeight = 5;
param.LaplacianWeight = 0.23;
res = imageMatrix; %Initial degraded image supplied to fnlcq
function
figure(300), imshow(abs(res), []);
title(['Initial image estimate using ', num2str(numberOfSpokes),
' spokes']);
% do iterations
```

```
tic
for n=1:5
    [res, repetitionCounter] =
fnlCg(res,numberOfSpokes,dataMatrix, param); %initialize fnlcg
    im_res = res;
    figure(100), imshow(abs(im_res),[]), drawnow;
    title(['Image estimate using ', num2str(numberOfSpokes), '
spokes']);

    if repetitionCounter > 7
        break;
    end;
end
toc

rmpath /Users/swrangsarbasumatary/Desktop/
imageProcessingProject2/
```