Object-oriented scientific programming with C++

Matthias Möller, Jonas Thies, Cálin Georgescu, Jingya Li (Numerical Analysis, DIAM) Lecture 2

## Task: Dot product

Write a C + + code that computes the dot product

$$a \cdot b = \sum_{i=1}^{n} a_i b_i$$

of two vectors  $a = \begin{bmatrix} a_1, a_2, ..., a_n \end{bmatrix}$  and  $b = \begin{bmatrix} b_1, b_2, ..., b_n \end{bmatrix}$  and terminates if the two vectors have different length.

# Dot product function

The main functionality without any fail-safe checks

#### Dot product function - improved version

#### First version of the dot product with exception

```
In [ ]:
#include <exception>
double dot_product(const double* a, int n, const double* b, int m)
{
    if (a == nullptr || b == nullptr) {
        // Handle null pointers by throwing an exception
            throw std::invalid_argument("Null pointer argument");
    }
    if (n != m) {
        // Handle mismatched sizes by throwing an exception
            throw std::invalid_argument("Array sizes mismatch");
    }
    // Core functionality
    double d = 0.0;
    for (int i = 0; i < n; ++i) {
          d += a[i] * b[i];
    }
    return d;
}</pre>
```

```
In [ ]:
```

```
#include <iostream>
double x[5] = { 1, 2, 3, 4, 5 };
double y[4] = { 1, 2, 3, 4 };
try {
    double d = dot_product(x, 5, y, 4);
} catch (const std::exception &e) {
    std::cout << e.what() << std::endl;
}</pre>
```

It would be much better if x and y would "know" their length internally so that the calling function cannot provide inconsistent data

# Cool! But what was the reason I enrolled in this course?



#### Flashback: Object Oriented Programming

Imagine each LEGO block as a piece of data (like an integer, string, etc.). A struct or a class is like a LEGO set that contains a variety of different blocks.

- OOP: bundle data (e.g. array) and functionality (e.g. length) into a struct or class
- Components of a struct are public (=can be accessed from outside the struct) by default
- Components of a class are private (=cannot be accessed from outside the class) by default
- Components of a struct/class are attributes and member functions (=methods)

## Class vs. struct

```
In [ ]:

class Vector {
    private: //default
    public:
        double* array;
        int length;
};

In [ ]:

struct Vector {
    public: // default
        double* array;
        int length;
    private:
};
```

#### When to use class and when to use struct?

- struct is typically used when you want to group data together without needing to restrict access to it. It is straightforward and simple. Many type traits (later in this course) are implemented as struct s.
- class is typically used when you want more control over the data and the interface through which it is accessed and manipulated, promoting the principles of encapsulation and data hiding.

#### Dot product as a member function of Vector

Second version of the dot product using Vector class or struct

Access of members of a struct or class by dot-notation (".")

Is the above implementation really OOP? How would you invoke it from the main program?

```
In [ ]:
```

The current implementation of the dot\_product function comes from functional programming and is not OOP style because it takes two input arguments x and y and returns one output argument, the dot product. In other words, it is not attached to any object (x or y).

If we want to implement a function inside a class or struct that is not attached to an object we have to define it as static

```
In [ ]:
```

static member functions are invoked with the full classname (comparable to namespaces)

In [ ]:

- It is still possible to initialise x.length by the wrong value, e.g., x.array = new double[5] {1, 2, 3, 4, 5}; x.length = 4;
- The main function is not very readable due to the lengthy declaration, initialisation and deletion of data
- OOP solution:
  - Constructor(s): method to construct a new Vector object
  - Destructor: method to destruct an existing Vector object

## Constructor

The constructor is called each time a new Vector object (=instance of the class Vector) is created

```
In [ ]:
```

```
class Vector
{
    public:
        double* array;
        int length;

    Vector() // Default constructor
    {
        array = nullptr;
        length = 0;
    }
};
```

A class can have multiple constructors if they have a different interface (=different parameters)

```
In [ ]:
```

```
class Vector
{
   public:
        double* array;
        int length;

   Vector() // Default constructor
   {
        array = nullptr;
        length = 0;
   }

   Vector(int len) // Another constructor
   {
        array = new double[len];
        length = len;
   }
};
```

What if a parameter has the same name as an attribute?

```
In [ ]:
```

```
class Vector
{
   public:
        double* array;
        int length;

   Vector(int length) // Another constructor
{
        // this pointer refers to the object itself,
        // hence this->length is the attribute and length
        // is the parameter passed to the constructor

        array = new double[length];
        this->length = length;
   }
};
```

#### Destructor

The destructor is called implicitly at the end of the lifetime of a Vector object, e.g., at the end of its scope

```
class Vector
{
   public:
        double* array;
        int length;

   ~Vector() // Destructor (and there can be only one!)
   {
        delete[] array;
        length = 0;
   }
};
```

## Uniform initialisation constructors (C++11)

```
Remember this double x[5] = \{ 1, 2, 3, 4, 5 \}; It would be cool to simply write Vector x = \{ 1, 2, 3, 4, 5 \}; C++11 solution: initializer lists Vector(const std::initializer_list&ltdouble&gt&amp list) { length = (int)list.size(); array = new double[length]; std::uninitialized_copy(list.begin(), list.end(), array); }
```

```
In [ ]:
```

```
#include <initializer list>
#include <memory>
class Vector {
private:
    double* array;
    int length;
public:
    // Constructor with initializer list
    Vector(const std::initializer list<double>& list)
        length = (int)list.size();
        array = new double[length];
        std::uninitialized copy(list.begin(), list.end(), array);
    // Destructor
    ~Vector() {
        delete[] array;
};
```

#### Dot product – close to perfection

Third version of the dot product using Vector class with uniform initialisation constructor (C++11) and exceptions

```
int main() { Vector x = \{ 1, 2, 3, 4, 5 \}; Vector y = \{ 2, 4, 6, 8, 10 \}; try { double dot_product(x, y); } catch (const std::exception &e) { std::cout &lt&lt e.what() &lt&lt std::endl; } }
```

# Delegating constructor (C++11)

Can we delegate some of the work

```
In [ ]:
```

```
#include <memory>
#include <initializer_list>

class Vector {
    private:
        double* array;
        int length;

public:
        Vector(int length)
        {
            this->length = length;
            array = new double[length];
        }

        Vector(const std::initializer_list<double>& list)
        {
            length = (int)list.size();
            array = new double[length];
            std::uninitialized_copy(list.begin(), list.end(), array);
        }
}
```

Delegating constructors delegate part of the work to another constructor of the same or another class

Vector(int length) : length(length), array(new double[length]) { }

- Here, delegation is not really helpful but more a question of coding style, e.g., some programmers use delegation in all situation where this is technically possible
- It is no longer necessary to distinguish between the **attribute** (this->length) and the **argument** (length) if both have the same name. But be careful with the order in which delegated objects are constructed!

## Quiz

```
    Vector(int len)

            length(len),
            array(new double[len])
            Vector(int len)
            array(new double[len]),
            length(len)

    {}
```

```
    Vector(int len)

            length(len),
            array(new double[lengh])
            Vector(int len)
            array(new double[length]),
            length(len)

    {}
```

If you have multiple constructors with increasing functionality, delegating constructors can be really helpful to remove duplicate code, e.g.

```
Vector(const std::initializer_list&ltdouble>& list) : Vector((int)list.size()) {
  std::uninitialized_copy(list.begin(), list.end(), array); }
```

#### Function -> member function

```
Function that computes the sum of a Vector static double sum(const Vector& a) { double s = 0; for (auto i=0; i<a.length; <math>i++) s += a.array[i]; return s; }
This is not really OOP-style!
int main() { Vector x = \{ 1, 2, 3, 4, 5 \}; std::cout &lt< sum(x) &lt< std::endl; }
```

Implementation of sum as an OOP-style member function

```
In [ ]:
```

```
#include <memory>
#include <initializer list>
class Vector {
    private:
        double* array;
        int length;
    public:
        Vector(const std::initializer list<double>& list) {
            length = static cast<int>(list.size());
            array = new double[length];
            std::uninitialized copy(list.begin(), list.end(), array);
        ~Vector() {
            delete[] array;
        double sum() {
            double s = 0;
            for (int i = 0; i < length; i++) {
                s += array[i];
            return s;
};
```

This is good OOP-style Vector  $v = \{1.0, 2.0, 3.0\}$ ; std::cout &lt< v.sum() &lt< std::endl; Can we implement the dot\_product function as a member function?

```
In [ ]:
```

This is good OOP-style int main() { Vector  $x = \{1,2,3\}$ ; Vector  $y = \{2,4,6\}$ ; std::cout &lt< x.dot\_product(y) &lt< std::endl; std::cout &lt< y.dot\_product(x) &lt< std::endl; } Formally, the dot product is an operation between two Vector objects and not a member function of one Vector object that needs another Vector object for calculation

#### Operator overloading

C++ allows to overload (=redefine) the standard operators

- Unary operators: ++a, a++, --a, a--, ~a, !a
- Binary operators: a+b, a-b, a\*b, a/b
- Relational operators: a==b, a!=b, a<b, a<=b, a>b, a>=b

#### Interfaces:

return\_type operator() [const] return\_type operator(const Vector& other) [const]

**Complete list:https://en.cppreference.com/w/cpp/language/operators** 

Implementation of dot product as overloaded \*-operator double operator(const Vector&amp other) const { if (length != other.length) throw  $std::invalid\_argument("Vector lengths mismatch"); double d=0.0; for (auto i=0; i<length; i++) d += array[i]other.array[i]; return d; }$ 

Now, the dot product is implemented as \*-operator that maps two Vector objects to a scalar value

int main() { Vector  $x = \{1,2,3\}$ ; Vector  $y = \{2,4,6\}$ ; std::cout &lt< x \* y &lt< std::endl; std::cout &lt< y \* x &lt< std::endl; }

The const specifier indicates that the Vector reference other must not be modified by the \*-operator

The trailing const specifier indicates that the this pointer (aka, the object whose function is invoked) must not be modified by the \*-operator double operator\*(const Vector&amp other) const { ... }

#### Assignment by operator overloading

Implementation of assignment as overloaded =-operator

Vector& operator=(const Vector& other) { if (this != &other) { length = other.length; delete[] array; array = new double[length]; for (auto i=0; i<length; ++i) array[i] = other.array[i]; } return \*this; }

- Usage: Vector x, y; x = y;
- Note that the this pointer is modified so there must not be a trailing const

Implementation of incremental assignment as overloaded =-operator
Vector&amp operator+=(const Vector&amp other) { if(length != other.length) throw
std::invalid\_argument("Vector lengths mismatch"); for (auto i=0; i<length; i++) array[i]
+= other.array[i]; return \*this; }</pre>

- Usage: Vector x, y; x += y;
- Note that the this pointer is modified so there must not be a trailing const

#### Container class

```
class Container {
  private:
      double* data;
    int length;
public:
      Container(int length)
      : length(length), data(new double[length])
      { }
      Container(const std::initializer_list<double>& l)
      : Container( (int)l.size() )
      {
            std::uninitialized_copy(l.begin(), l.end(), data);
      }
};
```

#### Conversion constructors

Both constructors convert a single input argument into a Container object, hence, they are called conversion constructors. They can be called in two different ways

Using the regular construction form

```
Container a( 4 );
Container a( {1,2,3,4} );
```

• Using copy initialisation

```
Container a = 4;  // -> Container a(4)
Container a = \{1,2,3,4\}; // -> Container a(\{1,2,3,4\})
Container a = \{4\}; // which constructor is called?
```

#### Explicit specifier

The explicit specifier prevents the use of the constructor as conversion constructor explicit Container(int length): length(length), data(new double[length])  $\{\ \}$  Now, copy-initialisation (Container a = 4;) is no longer possible but explicit constructor (Container a(4);) has to be used

# Constructors summary

Constructor	Description	Usage
Default	Constructor with no parameters.	Used to create an object with default values.
Parameterized	Constructor with parameters to initialize an object with specific values.	Used to create an object with specified attributes.
Сору	A constructor that initializes an object using another object of the same class.	Used to create a copy of an object.
Explicit	Constructor with the explicit keyword to prevent implicit conversions or copyinitialization.	Used to enforce explicit object creation with constructor.

#### Task: Numerical integration

• Approximate a one-dimensional integral by numerical quadrature

$$\int_{a}^{b} f(x)dx \approx \sum_{i=1}^{n} w_{i} f(x_{i})$$

ullet Choice of quadrature weights  $w_i$  and points  $x_i$  determines the concrete numerical integration rule

#### Simple integration rules

• Midpoint rule

$$\int_{a}^{b} f(x)dx \approx (b-a) \cdot f\left(\frac{a+b}{2}\right)$$

• Simpson rule

$$\int_{a}^{b} f(x)dx \approx \frac{b-a}{6} \left[ f(a) + 4f\left(\frac{a+b}{2}\right) + f(b) \right]$$

• Rectangle rule

$$\int_{a}^{b} f(x)dx \approx h \sum_{n=0}^{N-1} f(x_n), \quad h = \frac{b-a}{N}, \quad x_n = a + nh$$

## Gauss integration rules

- Zoo of Gauss integration rules with quadrature weights and points tabulated for the reference interval [-1,1]
- Complete list of weights/points is available, e.g., at Wikipedia

	n	$\xi_i$	$w_{i}$
ł	1	0	2
	2	-0.57735026919	2
		0.57735026919	1
	3	-0.774596669241	5/9
		0.0	8/9
		0.774596669241	5/9
	4	-0.861136311594053	0.3478548451374
		-0.339981043584856	0.6521451548625
		0.774596669241	0.6521451548625
		0.861136311594053	0.3478548451374

• Change of variable theorem

$$\int_{a}^{b} f(x)dx = \int_{-1}^{1} f(\phi(t))\phi^{i}(t)dt$$

• Mapping from interval [a,b] to interval [-1,1]

$$\phi(t) = \frac{b-a}{2}t + \frac{a+b}{2}, \phi'(t) = \frac{b-a}{2}$$

• Numerical quadrature rule

$$\int_{a}^{b} f(x)dx \approx \phi \sum_{n=1}^{n} w_{i} f(\phi(\xi_{i}))$$

### Program design

#### We need...

- A strategy to ensure that all numerical quadrature rules (=classes) provide an **identical interface** for evaluating integrals
- A standard way to **pass user-definable function** f(x) from outside (=main routine) to the evaluation function

- A strategy to ensure that all numerical quadrature rules (=classes) provide an **identical interface** for evaluating integrals
  - Polymorphism: Base class Quadrature provides common attributes and member functions (at least their interface declaration); derived classes implement specific quadrature rule (reusing common functionality of the base class, where this is possible and makes sense)

- A standard way to **pass user-definable function** f(x) from outside (=main routine) to the evaluation function
  - Function pointers (traditional approach)
  - Lambda expressions (recommended approach since C++11)

#### Function pointers

Define a function to be integrated
 const double myfunc1(double x){ return x; }

Define interface of the integrate function
 double integrate(const double (\*func)(double x), double a, double b) { ... }

• Usage: integrate(myfunc1, 0, 1);

#### Lambda expressions

- Introduced in C++11, **lambda expressions** provide an elegant way to write userdefined callback functions
- General syntax

```
auto name = [&ltcaptures>] (&ltparameters>) {&ltbody>};
```

• Lambda expressions can be inlined (anonymous functions)

```
integrate([&ltcaptures>](&ltparameters>) {&ltbody>});
```

• Define function to be integrated

```
auto myfunc2 = [](double x) { return x; };
```

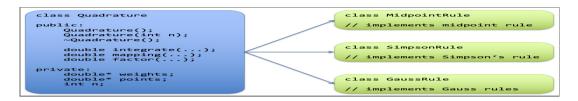
• Define interface of the integration function

```
double integrate(std::function&ltdouble(double)> func, double a, double b) const { ... }
```

• Usage:

```
integrate(myfunc2, 0, 1);
integrate([](double x){ return x; }, 0, 1);
```

## Program design, revisited



## Base class **Quadrature**

```
In [ ]:

class Quadrature
{
    public:
        Quadrature()
        : n(0), weights(nullptr), points(nullptr) {};
        Quadrature(int n)
        : n(n), weights(new double[n]), points(new double[n]) {};
        ~Quadrature()
        { delete[] weights; delete[] points; n=0; }
    private:
        double* weights;
```

double\* points;

n;

int

};

• Scenario I: We want to **declare the interface** of the integrate function but we want to *force* the user to implement each integration rule individually

// pure (=0) virtual member function virtual double integrate(double (\*func)(double x), double a, double b) const = 0;

```
// pure (=0) virtual member function
virtual double integrate(std::function&ltdouble(double)> func, double a,
double b) const = 0;
```

- Keyword virtual ... = 0; declares the function to be **pure virtual**
- That is, each class that is derived from the **abstract class** Quadrature must(!!!) implement this function explicitly
- Otherwise, the compiler complains when the programmer forgets to implement a pure virtual function and tries to create an object of the derived but not fully implemented class

#### Base class **Quadrature**

• Scenario II: We provide a generic implementation but allow the user to override it explicitly in a derived class

```
virtual double integrate(double (*func)(double x), double a, double b) const {...}
virtual double integrate(std::function&ltdouble(double)> func, double
a, double b) const{...}
```

• Keyword virtual declares the function virtual. Virtual functions can be overridden in a derived class. If no overriding takes place, then the function implementation from the base class is used

```
In [ ]:
```

```
class Ouadrature {
    private:
        double* weights;
        double* points;
        int
                n;
    public:
        Ouadrature()
        : n(0), weights(nullptr), points(nullptr) {};
        Ouadrature(int n)
        : n(n), weights(new double[n]), points(new double[n]) {};
        ~Quadrature()
        { delete[] weights; delete[] points; n=0; }
    // ** pure virtual functions (implemented in derived class) ** /
    virtual double mapping(double xi, double a, double b) const = 0;
    virtual double factor(double a, double b) const = 0;
    // ** virtual integration function (generic implementation) ** /
    virtual double integrate(double (*func)(double x), double a, double b) const {
        double integral(0.0);
        for (auto i=0; i<n; i++)
            integral += weights[i]*func(mapping(points[i],a,b));
        return factor(a,b)*integral;
};
```

- The virtual integrate function makes use of the pure virtual functions factor and mapping
- Both functions are **not** implemented in class Quadrature
- It is therefore obvious that class Quadrature must be an **abstract class** (and cannot be instantiated) since some of its functions (here: integrate) are still unavailable
- Virtual functions make it is possible to call functions in the base class which will be implemented in the derived class

### Class MidpointRule

• **Derive** class MidpointRule from base class Quadrature

```
class MidpointRule : public Quadrature
{
    // Implement pure virtual functions (not used but need to be implemented!)
    virtual double mapping(double xi, double a, double b) const { return 0; }
    virtual double factor(double a, double b) const { return 1; }

    // Override the implementation of the virtual integrate
    // function from class Quadrature with own implementation
    virtual double integrate(double (*func)(double x), double a, double b) const
    {
        return (b-a) * func( 0.5 * (a+b) );
    }
};
```

## Class SimpsonRule

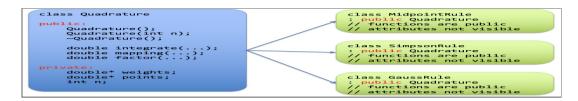
• **Derive** class SimpsonRule from base class Quadrature

```
class SimpsonRule : public Quadrature
{
    // Implement pure virtual functions (not used but need to be implemented!)
    virtual double mapping(double xi, double a, double b) const { return 0; }
    virtual double factor(double a, double b) const { return 1; }

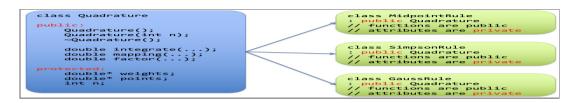
    // Override the implementation of the virtual integrate
    // function from class Quadrature with own implementation
    virtual double integrate(double (*func)(double x), double a, double b) const
    {
        return (b-a)/6.0 * ( func(a) + 4.0 * func( 0.5*(a+b) ) + func(b) );
    }
};
```

## Class GaussRule

# Program design, revisited



# Program design, revisited



#### Class GaussRule

- Attributes from base class are now visible in derived class
- Class GaussRule implements functions factor and mapping
- Class GaussRule inherits the virtual function integrate from class Quadrature

```
In [ ]:
```

```
class GaussRule : public Quadrature
{
    virtual double factor(double a, double b) const
    { return 0.5 * (b-a); }

    virtual double mapping(double xi, double a, double b) const
    { return 0.5 * (b-a) * xi + 0.5 * (a+b); }
};
```

#### Keyword: override (C++11)

• With the override keyword you can force the compiler to explicitly check that the function in a derived class overrides a (pure) virtual function from the base class

```
class GaussRule : public Quadrature
{
    virtual double factor(double a, double b) const override
    {
        return 0.5 * (b - a);
    }
};
```

• If the base class Quadrature does not specify a (pure) virtual function factor an error will be thrown

### Keyword: final (C++11)

 With the final keyword you can force the compiler to explicitly prevent further overriding of functions

```
class GaussRule : public Quadrature
{
    virtual double factor(double a, double b) const final
    { return 0.5*(b-a); }
};
```

 If a class GaussRuleImproved derived from GaussRule tries to override the function factor an error will be thrown

```
In []:

import asyncio
import os
import tempfile

from subprocess import PIPE, Popen
from pyppeteer import launch

import concurrent.futures

async def html_to_pdf(html_file, pdf_file, pyppeteer_args=None):
    """Convert a HTML file to a PDF"""
    browser = await launch(
```

```
handleSIGINT=False,
    handleSIGTERM=False.
    handleSIGHUP=False,
    headless=True,
    args=["--no-sandbox"],
page = await browser.newPage()
await page.setViewport(dict(width=994, height=768))
await page.emulateMedia("screen")
await page.goto(f"file://{html file}", {"waitUntil": ["networkidle2"]})
page margins = {
    "left": "20px",
    "right": "20px",
    "top": "30px",
    "bottom": "30px",
dimensions = await page.evaluate(
    """() => {
    return {
        width: document.body.scrollWidth,
        height: document.body.scrollHeight,
        offsetWidth: document.body.offsetWidth,
        offsetHeight: document.body.offsetHeight,
        deviceScaleFactor: window.devicePixelRatio,
3 " " "
width = dimensions["width"]
height = dimensions["height"]
await page.pdf(
        "path": pdf file,
        "format": "A4",
        "printBackground": True,
        "margin": page margins,
await browser.close()
```

```
if __name__ == "__main__":
    html_input_file = "http://localhost:8888/notebooks/Desktop/Cpp-slides/OospCpp/notebooks/lecture2.ipynb#
/slide-0-0?print-pdf"
    pdf_output_file = "slides.pdf"

pool = concurrent.futures.ThreadPoolExecutor()
    pool.submit(
        asyncio.run,
        html_to_pdf(
            html_input_file,
            pdf_output_file
        ),
    ).result()
```

```
NetworkError
                                          Traceback (most recent call last)
Cell In[3], line 72
     63 pdf output file = "slides.pdf"
     65 pool = concurrent.futures.ThreadPoolExecutor()
     66 pool.submit(
            asyncio.run,
     67
            html to pdf(
     68
     69
                html input file,
                pdf output file
     70
           ),
     71
---> 72 ).result()
File ~/anaconda3/lib/python3.11/concurrent/futures/ base.py:456, in Future.result(self, timeout
            raise CancelledError()
    454
    455 elif self. state == FINISHED:
            return self. get result()
--> 456
    457 else:
            raise TimeoutError()
    458
File ~/anaconda3/lib/python3.11/concurrent/futures/ base.py:401, in Future. get result(self)
    399 if self. exception:
    400
            try:
                raise self. exception
--> 401
            finally:
    402
                # Break a reference cycle with the exception in self. exception
    403
```

```
404
                self = None
File ~/anaconda3/lib/python3.11/concurrent/futures/thread.py:58, in WorkItem.run(self)
     55
            return
     57 trv:
---> 58
            result = self.fn(*self.args, **self.kwargs)
     59 except BaseException as exc:
            self.future.set exception(exc)
File ~/anaconda3/lib/python3.11/asyncio/runners.py:190, in run(main, debug)
            raise RuntimeError(
    186
                "asyncio.run() cannot be called from a running event loop")
    187
    189 with Runner(debug=debug) as runner:
            return runner.run(main)
--> 190
File ~/anaconda3/lib/python3.11/asyncio/runners.py:118, in Runner.run(self, coro, context)
    116 self. interrupt count = 0
    117 try:
--> 118
            return self. loop.run until complete(task)
    119 except exceptions.CancelledError:
    120
            if self. interrupt count > 0:
File ~/anaconda3/lib/python3.11/asyncio/base events.py:650, in BaseEventLoop.run until complete
(self, future)
    647 if not future.done():
            raise RuntimeError('Event loop stopped before Future completed.')
--> 650 return future.result()
Cell In[3], line 24, in html to pdf(html file, pdf file, pyppeteer args)
     21 await page.setViewport(dict(width=994, height=768))
     22 await page.emulateMedia("screen")
---> 24 await page.goto(f"file://{html file}", {"waitUntil": ["networkidle2"]})
     26 page margins = {
            "left": "20px".
     27
            "right": "20px",
     28
     29
            "top": "30px",
     30
            "bottom": "30px",
     31 }
     33 dimensions = await page.evaluate(
            """() => {
     34
     35
            return {
   (\ldots)
     42 }"""
     43 )
```

```
File ~/anaconda3/lib/python3.11/site-packages/pyppeteer/page.py:829, in Page.goto(self, url, op
tions. **kwarqs)
    826 timeout = options.get('timeout', self. defaultNavigationTimeout)
    827 watcher = NavigatorWatcher(self. frameManager, mainFrame, timeout, options)
--> 829 result = await self. navigate(url, referrer)
    830 if result is not None:
            raise PageError(result)
    831
File ~/anaconda3/lib/python3.11/site-packages/pyppeteer/page.py:843, in Page. navigate(self, ur
l, referrer)
    842 async def navigate(self, url: str, referrer: str) -> Optional[str]:
            response = await self. client.send('Page.navigate', {'url': url, 'referrer': referr
--> 843
er})
            if response.get('errorText'):
    844
                return f'{response["errorText"]} at {url}'
    845
NetworkError: Protocol error (Page.navigate): Cannot navigate to invalid URL
```

```
In [ ]:
```