## MATH 119: Midterm 1

Name:	

## Directions:

- \* Show your thought process (commonly said as "show your work") when solving each problem for full credit.
- \* If you do not know how to solve a problem, try your best and/or explain in English what you would do.
- \* Good luck!

Problem	Score	Points
1		10
2		10
3		10
4		10
5		10
6		10

60

- 1. Short answer questions:
  - (a) Suppose you write

$$(x+y)^2 z^2 = x^2 + y^2 z^2$$

What are the two errors you made?

- 1) x and y are terms. can only manipulate exponents (exponent laws) across factors.
- (2) everything to the left of 2° should be encopsulated in parentheses since you are multiplying 2° into = 2 terms
- (b) True or false: We can simplify  $\frac{x^2 + x 2}{x 1}$  by crossing out the x's to become  $\frac{x^2 2}{-1}$ . If not, properly simplify the expression.

False; x is both a term in the context of the entire numerature and dinaminator.

$$\frac{x^{2} + x - 2}{x - 1} = \frac{(x - 1) \cdot (x + 2)}{(x - 1)} = x + 2$$

(c) Bob has a function f(x). It is not one-to-one. However, he goes ahead and finds the inverse  $f^{-1}$ . What is the problem with  $f^{-1}$  and why?

fis not a function because one input is sent

to at least two different outputs.

(d) If 
$$f(x) = \frac{x}{1-x}$$
, find  $f(x^2 - 1)$ .  

$$\int (x^2 - 1) = \frac{x^2 - 1}{1 - (x^2 - 1)} = \frac{x^2 - 1}{x^2 + 2}$$

(e) Suppose we have a base function  $f(x) = x^3$  and we have

$$g(x) = (x+2)^3 + 4$$
  $h(x) = \left(\frac{1}{2}x + 2\right)^3 + 4$ 

Does g(x) have the same horizontal shift as h(x)? If not, state what **both** g(x) and h(x)'s horizontal shift are.

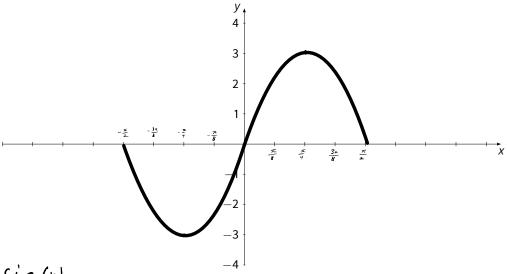
No. g(x) is 2 unils to the left of f(x) while h(x) is I unit to the left of f(x).

## 2. Suppose

$$f(x) = -3\sin(2x + \pi) = -3\sin\left(2\left(x + \frac{\pi}{2}\right)\right)$$

Do two things:

- (a) Graph at least one period of f(x) using transformations. Label the x-axis tick marks you are using.
- (b) Write out the blueprint of transformations starting with  $g(x) = \sin x$  to end up at f(x).



$$h(x) = -g(x) = -\sin(x)$$

reflection around x-axis

$$j(x) = 3h(x) = -3\sin(x)$$

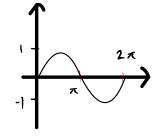
V. Stretch 3 unils

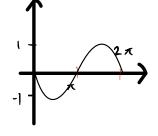
$$\frac{1}{2}(x) = \int (2x) = -3\sin(2x)$$

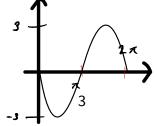
h. shink factor of 1/2

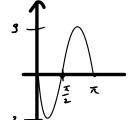
$$\int (x) = k \left( x + \frac{\pi}{2} \right) = -3 \sin \left( 2 \left( x + \frac{\pi}{2} \right) \right) \quad h. \quad Shidt \quad \frac{\pi}{2} \quad kdf$$

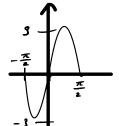












3. Let

$$f(x) = 2x^2 - 7x + 3$$
  $g(x) = \sin(x) - \frac{1}{x - 1}$ 

(a) Factor f(x).

$$(2x-1)(x-3)$$

(b) Find and simplify f(x) - g(x) and it's domain given in interval notation.

$$f(x) - g(x) = 2x^{2} - 7x + 3 - \left(s \ln(x) - \frac{1}{x - 1}\right)$$

$$= 2x^{2} - 7x + 1 - \sin(x) + \frac{1}{x - 1}, \quad (-\infty, 1) \cup (1, \infty)$$

(c) Evaluate and simplify f(x+h) - f(x) (you should be able to factor out h at the end).

$$\int (x+h) - \int (x) = 2(x+h)^{2} - 7(x+h) + 3 - (2x^{2} - 7x + 3)$$

$$= 2(x^{2} + 2xh + h^{2}) - 7x - 7h + 3 - 2x^{2} + 7x - 3$$

$$= 2x^{2} + 4xh + 2h^{2} - 7h - 2x^{2}$$

$$= h \cdot (4x + 2h - 7)$$

4. Given 
$$ax - bx(c+d) - ex = gx$$
, isolate  $x$ .  
 $ax - bcx - bdx - cx = gx$ 

$$ax - bcx - bdx - ex - gx = 0$$

$$\frac{x \cdot (a - bc - bd - e - g)}{a - bc - bd - e - g} = 0$$

$$\frac{10}{x} - \frac{12}{x - 3} + 4 = 0$$

$$X\left(x-3\right)\left(\frac{10}{x}-\frac{12}{x-3}+4\right)=O\cdot X\left(x-J\right)$$

$$\frac{10 \times (x-3)}{X} - \frac{12 \times (x-3)}{(x-3)} + 4 \times (x-3) = 0$$

$$10x - 30 - 12x + 4x^2 - 12x = 0$$

$$4x^2 - 12x - 30 = 0$$

$$(2x+3)(2x-10)=0$$

$$= 0 \qquad 2 \times -10 = 0$$

x = 5

 $=-\frac{20}{3}-\frac{12}{-\frac{9}{2}}+4$ 

 $= -\frac{20}{3} + 12^{\frac{7}{2}} + 4$ 

 $= -\frac{20}{3} + \frac{8}{3} + \frac{12}{3}$ 

 $\frac{10}{5} - \frac{12}{5-3} + 4 = 2 - \frac{12}{2} + 4 = 2 - 6 + 4 = 0$ 

$$\frac{3}{2} \qquad \qquad 2 \times = 10$$

$$2x + 3 = 0$$

$$2x - 10 = 0$$

 $\frac{10}{-\frac{3}{2}} - \frac{12}{-\frac{3}{2} - 3} + 4 = 10 \cdot \left(-\frac{2}{3}\right) - \frac{12}{-\frac{3}{2} - \frac{6}{2}} + 4$ 

$$2x + 3 = 0$$

$$2x - 10 - 0$$

$$x = -\frac{3}{2}$$

$$2x = 10$$

 $\chi = -\frac{3}{2}$ 

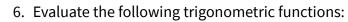
Check x=- =

Check x = 5

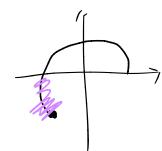
$$2x + 3 = 0$$
  $2x - 10 = 0$ 

$$2x + 3 = 0$$
  $2x - 10 =$ 

$$2x + 3 = 0$$
  $2x - 10 = 0$ 



(a) 
$$\sin\left(\frac{5\pi}{4}\right)$$



$$\operatorname{Sin}\left(\frac{5\pi}{4}\right) = -\operatorname{Sin}\left(\frac{\pi}{7}\right) = \boxed{\frac{\sqrt{2}}{2}}$$

(b) 
$$\cos\left(\frac{-7\pi}{6}\right)$$



& cos negativa in I

$$\cos\left(-\frac{7\pi}{6}\right) = -\cos\left(\frac{\pi}{6}\right) = \sqrt{\frac{3}{2}}$$

(c) 
$$\tan\left(\frac{-40\pi}{3}\right) = \tan\left(-\frac{39\pi}{3} - \frac{\pi}{3}\right)$$

$$= \cot \left(-13\pi - \frac{\pi}{3}\right)$$

(d) 
$$\csc\left(10000000000000\pi - \frac{4\pi}{3}\right)$$
 ignore
$$-\left(5\left(-\frac{4\pi}{3}\right)\right)$$

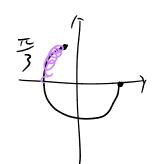
$$ton\left(-\frac{40z}{3}\right) = -ton\left(\frac{z}{3}\right)$$

$$= -\frac{\sqrt{3}}{2} = -\frac{\sqrt{3}}{2}$$

$$= CSC\left(-\frac{4\pi}{3}\right)$$

$$\widehat{U} = \frac{\pi}{3}$$

$$=\overline{\left[ -\sqrt{3}\right] }$$



$$\operatorname{Csc}\left(-\frac{4\pi}{3}\right) = \operatorname{Csc}\left(\frac{\pi}{3}\right) = \frac{2}{\sqrt{3}} = \frac{2}{\sqrt{3}}$$