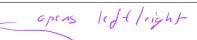
## MATH 119: Some Practice Final Problems

Here are problems that cover the last two weeks of our class.

The final is cumulative; you should look at Practice Midterm 1+2 and Midterm 1+2 as well.

1.	Answer	the	fol	lowing
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(a) Find a hyperbola with foci  $(\pm 5, 0)$  and vertices  $(\pm 3, 0)$ , if possible.

for i: 
$$(\pm c, 0) \rightarrow c = 5$$

Virtics:  $(\pm a, 0) \rightarrow a = 3$ 

For b:  $c^2 = a^2 + b^2$ 

$$b^2 = 25 - 9 = 16$$

So  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ 

$$\frac{x^2}{9} - \frac{y^2}{16}$$

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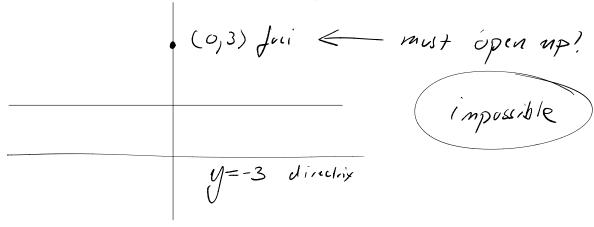
(b) Find an ellipse with eccentricity 0.5 and vertices  $(\pm 4, 0)$ , if possible.

 $Vertices: (\pm a, 0) \rightarrow a = 4 \quad For \ b: \ c^2 = a^2 - b^2$ eccentricity:  $\frac{c}{a} = \frac{1}{2}$  $b^2 = a^2 - c^2 = 4^2 - 2^2 = 17$  $C = \frac{a}{2} = \frac{4}{2} = 2$ 

$$= \frac{4}{2} = 2$$

$$50 \quad \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \implies \boxed{\frac{x^2}{16} + \frac{y^2}{12}} = 1$$

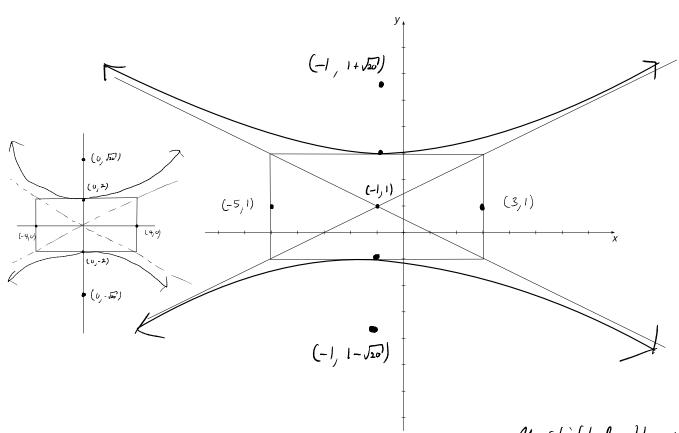
(c) Find a parabola with directrix y = -3 and opens right, if possible.



## 2. Consider the hyperbola

$$4(y-1)^2 - (x+1)^2 = 16$$

Find the foci, vertices, and sketch an accurate graph.



$$\frac{4(y-1)^{2} - (x+1)^{2}}{16} = \frac{16}{16}$$

$$4(y-1)^{2} - \frac{(x+1)^{2}}{16} = 1$$

$$\frac{4(y-1)^{2}}{16} - \frac{(x+1)^{2}}{16} = 1$$

$$\frac{(y-1)^2}{4} - \frac{(x+1)^2}{16} = 1$$

$$Shift up | left |$$

unshifted 
$$\#s$$
:  
 $\alpha^2 = 4 \implies \alpha = 2$   
 $b^2 = 16 \implies b = 4$ 

$$c^{2} = a^{2} + b^{2} = 2^{2} + 4^{2}$$

$$= 2$$

$$C = \sqrt{20}$$

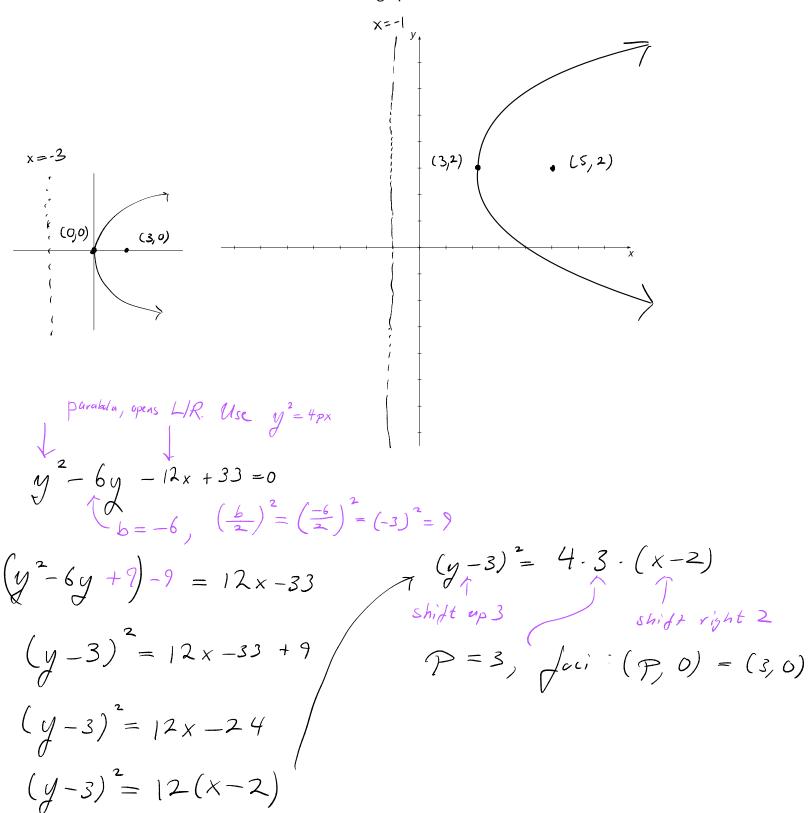
$$\int_{0}^{\infty} ci \, one \, \left(0, \pm \sqrt{20}\right)$$

$$Shifted \int_{0}^{\infty} ci \, one \, \left(0-1, 1\pm\sqrt{20}\right) = \left(-1, 1\pm\sqrt{20}\right)$$

## 3. Consider the parabola

$$y^2 - 6y - 12x + 33 = 0$$

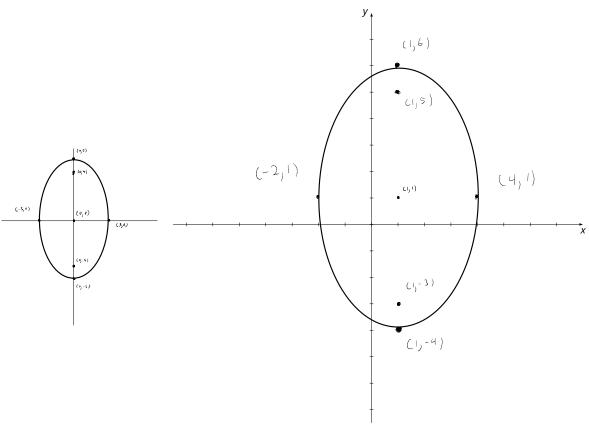
Find the foci and sketch an accurate graph.



## 4. Consider the ellipse

$$25(x-1)^2 + 9(y-2)^2 = 25 * 9$$

Find the foci, vertices and sketch an accurate graph.



$$\frac{25(x-1)^{2} + 9(y-1)^{2}}{25\cdot 9} = \frac{25\cdot 9}{25\cdot 9}$$

$$\frac{25(x-1)^{2}}{25\cdot 9} + \frac{9(y-1)^{2}}{25\cdot 9} = 1$$

$$\frac{(x-1)^{2}}{9 + \frac{(y-1)^{2}}{25\cdot 9}} = 1$$
Shift eight 1

unshifted info:  

$$a^{2}=25 \rightarrow a=5$$
  
 $b^{2}=9 \rightarrow b=3$   
vertices:  $(0,\pm a)=(0,\pm 5)$   
 $foci:(0,\pm c)=(0,\pm 4)$   
 $c^{2}=a^{2}-b^{2}=25-9=16$   
 $c=4$