

MATH 119: Quiz 7

Name: key

Directions:

- * Show your thought process (commonly said as "show your work") when solving each problem for full credit. **Remember to fully simplify.**
- * If you do not know how to solve a problem, try your best and/or explain in English what you would do.
- * Good luck!

1. Draw an accurate graph of

$$x^2 + 4y^2 = 16$$

Include the foci.

$$\frac{x^2 + 4y^2}{16} = \frac{16}{16}$$

$$\frac{x^2}{16} + \frac{4y^2}{4} = 1$$

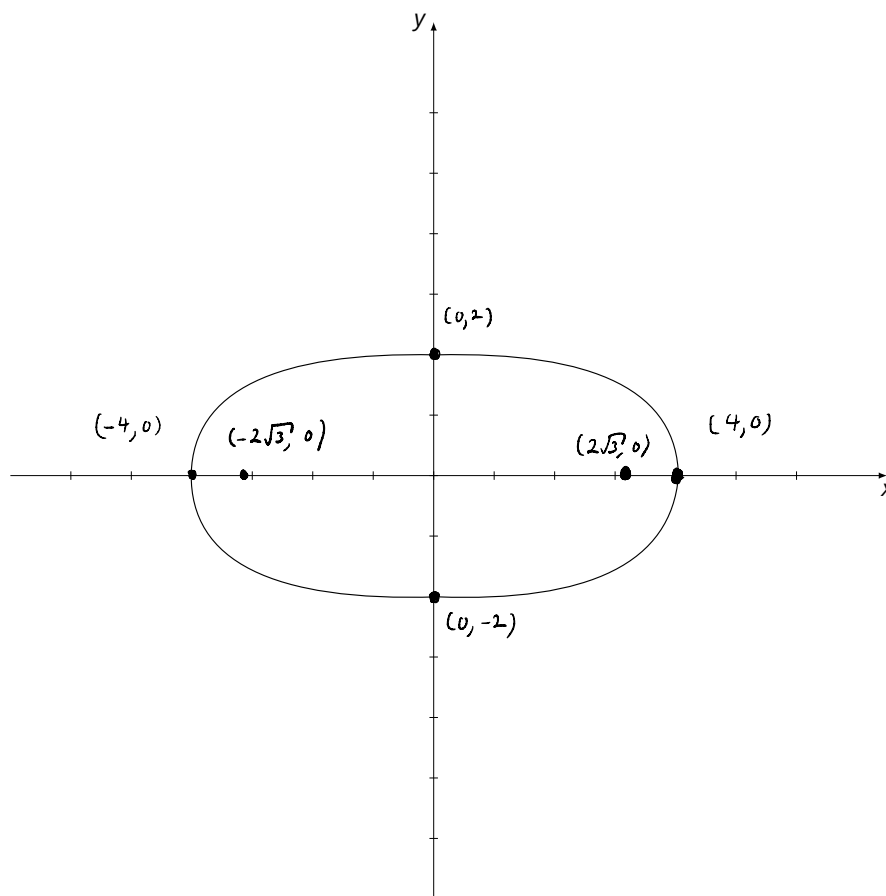
\uparrow \uparrow
 a^2 b^2

So $a=4, b=2$.

Foci: $(\pm c, 0)$

$$\begin{aligned} c^2 &= a^2 - b^2 \\ &= 16 - 4 \\ &= 12 \end{aligned}$$

$$c = \pm \sqrt{12} = \pm \sqrt{4 \cdot 3} = \pm 2\sqrt{3}$$



2. Find the equation of an ellipse with foci $(\pm 2, 0)$ and vertices $(\pm 3, 0)$ or state it's impossible to.

Foci / vertices on x -axis. Use $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.

vertices : $(\pm a, 0)$ so $a = 3$.

foci : $(\pm c, 0)$ where $c^2 = a^2 - b^2$.

$$\text{So } 2^2 = 3^2 - b^2$$

$$4 = 9 - b^2$$

$$b^2 = 9 - 4 = 5$$

$$\text{Equation: } \frac{x^2}{9} + \frac{y^2}{5} = 1$$

3. What type of conic section is

$$x^2 - 9y^2 + 1 = 0$$

$$1 = 9y^2 - x^2$$

Hyperbola!