

Directions:

- * Show your thought process (commonly said as "show your work") when solving each problem for full credit.
- * If you do not know how to solve a problem, try your best and/or explain in English what you would do.
- * Good luck!

Find the following limits: $1. \lim_{n \to \infty} 5^{-n} = \lim_{n \to \infty} \frac{1}{5^n} = \lim_{n \to \infty} \left(\frac{1}{5}\right)^n = 0$

$$2. \lim_{n \to \infty} \frac{e^{2n} - e^n}{e^{3n} + 1} = \lim_{n \to \infty} \frac{e^{3n} - e^{3n}}{e^{3n}}$$

$$= \lim_{n \to \infty} \frac{e^{3n} + \frac{1}{e^{3n}}}{1 + \frac{1}{e^{3n}}}$$

$$= \lim_{n \to \infty} \frac{e^{-n} - e^{-2n}}{1 + \frac{1}{e^{3n}}}$$

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3.
$$\lim_{x \to \infty} \left[x^3 - x^2 + x \right] = \lim_{x \to \infty} \left[x^2 \left(x - 1 \right) + x \right]$$

$$= \left[\lim_{x \to \infty} x^2 \right] \cdot \left[\lim_{x \to \infty} x - 1 \right] + \left[\lim_{x \to \infty} x \right]$$

$$= \infty \cdot \infty + \infty$$

$$= \infty + \infty = \infty$$

$$4. \lim_{x \to \infty} \frac{1 - 3^{x}}{e^{x} - 2^{-x}}$$

$$= \lim_{x \to \infty} \frac{\frac{1}{e^{x}} - \frac{3}{e^{x}}}{\frac{e^{x}}{e^{x}} - \frac{2^{-x}}{e^{x}}}$$

$$= \lim_{x \to \infty} \frac{\left(\frac{1}{e}\right)^{x} - \left(\frac{3}{e}\right)^{x}}{\left(\frac{1}{e}\right)^{x} - \left(\frac{3}{e}\right)^{x}}$$

$$= \lim_{x \to \infty} \frac{\left(\frac{1}{e}\right)^{x} - \left(\frac{3}{e}\right)^{x}}{\left(\frac{1}{e}\right)^{x} - \left(\frac{1}{e}\right)^{x}}$$

$$= \lim_{x \to \infty} \left(\frac{1}{e}\right)^{x} - \lim_{x \to \infty} \left(\frac{3}{e}\right)^{x}$$

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$$=\frac{\bigcirc-\bigcirc}{\bigcirc-\bigcirc}$$

$$=$$
 $\left[-\infty\right]$