

MATH 118: Quiz 4

Name: key

Directions:

- * Show your thought process (commonly said as "show your work") when solving each problem for full credit.
- * If you do not know how to solve a problem, try your best and/or explain in English what you would do.
- * Good luck!

1. What is the domain of the following function?

$$f(x) = \frac{1}{x-3}$$

① Start with \mathbb{R}

② Problems: can't divide by zero

$$x-3=0$$

$$x=3 \quad \leftarrow \text{remove}$$

③ Remove problems:

$$(-\infty, 3) \cup (3, \infty)$$



2. Given $f(x) = 2x - 1$, evaluate and fully simplify the expression $f(x+h) - f(x)$.

Compare $f(x+h)$. See how $x+h$ replaces the x .

Now do that.

$$\begin{aligned} f(x+h) - f(x) &= \underbrace{2(x+h)}_{f(x+h)} - 1 - \underbrace{(2x-1)}_{f(x)} \\ &= \cancel{2x} + 2h - \cancel{1} - \cancel{2x} + \cancel{1} \\ &= 2h \end{aligned}$$

Handwritten notes:
- 2 multiplies into two terms (pointing to 2 and x+h)
- -1 multiplies into two terms (pointing to -1 and -1)
- dist (pointing to the minus sign between the two terms)

3. Draw the graph of the function $f(x) = 2x - 1$.

x	$f(x)$
-2	$2(-2) - 1 = -5$
-1	$2(-1) - 1 = -3$
0	$2 \cdot 0 - 1 = -1$
1	$2 \cdot 1 - 1 = 1$
2	$2 \cdot 2 - 1 = 3$

