# **Appointments**

- Assistant Professor. Department of Applied Mathematics and Statistics. Colorado School of Mines. August 2021 - present
- Assistant Professor. Department of Computer Science. Colorado School of Mines. May 2022 - present
- Assistant Adjunct Professor. Department of Mathematics, University of California, Los Angeles. July 2019 - August 2021
- Givens Associate. MCS Division, Argonne National Laboratory. May 15, 2018 Nov 30, 2018

#### Education

- PhD. in Applied Mathematics, Emory University, Atlanta, GA, May 2019
  Advisor: Lars Ruthotto
- BSc. in Applied Mathematics, Brown University, Providence, RI, May 2014 Advisor: Johnny Guzmán
- o AA. in Mathematics, Miami Dade College, Miami, FL, May 2011

#### Research Interests

Inverse Problems, Deep Learning, Optimization, Optimal Control, Mean Field Games

# Preprints/Submitted Articles

- 1. McKenzie D, Wu Fung S, Heaton H, Yin W. Faster Predict-and-Optimize with Three-Operator Splitting, arXiv:2301.13395, 2023.
- 2. Vidal A, Wu Fung S, Tenorio L, Osher S, Nurbekyan L. Taming Hyperparameter Tuning in Continuous Normalizing Flows Using the JKO Scheme, arXiv:2211.16757, 2022.
- 3. Osher S\*, Heaton H\*, Wu Fung S\*. A Hamilton-Jacobi-based Proximal Operator, arXiv:2211.12997, 2022
- 4. Heaton H, Wu Fung S. Explainable AI via Learning to Optimize, arXiv:2204.14174, 2022

<sup>\*</sup>denotes co-first author

5. Heaton H, McKenzie D, Li Q, Wu Fung S, Osher S, Yin W. Learn to Predict Equilibra via Fixed Point Networks, arXiv:2106.00906, 2021

# Published/Accepted Articles

- 1. Chow YT, Wu Fung S, Liu S, Nurbekyan L, Osher S. A Numerical Algorithm for Inverse Problem from Partial Boundary Measurement Arising from Mean Field Game Problem, *Inverse Problems*, 39(1), 014001, 2022
- 2. Heaton H, Wu Fung S, Osher S. Global Solutions to Nonconvex Problems by Evolution of Hamilton-Jacobi PDEs, *Communications on Applied Mathematics and Computation*, accepted, 2022
- 3. Ye J<sup>†</sup>, Wan C<sup>†</sup>, Wu Fung S. Adaptive Uncertainty-Weighted ADMM for Distributed Optimization, *Journal of Applied and Numerical Optimization*, 4(2), pp. 273-290. 2022
- 4. Agrawal S, Lee W, Wu Fung S, Nurbekyan L. Random Features for High-Dimensional Nonlocal Mean-Field Games, *Journal of Computational Physics*, 459, pp. 111136. 2022
- Onken D, Nurbekyan L, Li X, Wu Fung S, Osher S, Ruthotto L. A Neural Network Approach for High-Dimensional Optimal Control, *Transactions on Control Systems Technology*, accepted, 2022
- 6. Wu Fung S\*, Heaton H\*, McKenzie D, Li Q, Osher S, Yin W. JFB: Jacobian-free Backpropagation for Implicit Networks, *AAAI Conference on Artificial Intelligence*, 36(6), 6648-6656, 2022
- 7. Heaton H\*, Wu Fung S\*, Lin AT\*, Osher S, Yin W. Wasserstein-based Projections with Applications to Inverse Problems, *SIAM Journal on Mathematics of Data Science*, 40(2), 581-603, 2022
- 8. Heaton H\*, Wu Fung S\*, Gibali A, Yin W. Feasibility-based Fixed Point Networks, Fixed Point Theory and Algorithms for Sciences and Engineering, 21, 2021
- Kan K, Wu Fung S, Ruthotto L. PNKH-B: A Projected Newton-Krylov Method for Large-Scale Bound-Constrained Optimization, SIAM Journal on Scientific Computing, 43(5), S704–S726, 2021
- Lin AT\*, Wu Fung S\*, Li W, Nurbekyan L, Osher S. Alternating the Population and Agent Control via Two Neural Networks to Solve High-Dimensional Stochastic Mean Field Games, Proceedings of the National Academy of Sciences, 118(31). 2021
- 11. Onken D, Nurbekyan L, Li X, Wu Fung S, Osher S, Ruthotto L. A Neural Network Approach Applied to Multi-Agent Optimal Control, *European Control Conference 2021 (ECC21)*, pp. 1036-1041. 2021
- 12. Onken D, Wu Fung S, Li X, Ruthotto L. OT-Flow: Fast and Accurate Continuous Normalizing Flows via Optimal Transport, *AAAI Conference on Artificial Intelligence*, 35(10), 9223-9232, 2021

<sup>†</sup>undergraduate student at time of publication

- 13. Ruthotto L, Osher S, Li W, Nurbekyan L, Wu Fung S. A Machine Learning Framework for Solving High-Dimensional Mean Field Game and Mean Field Control Problems, *Proceedings of the National Academy of Sciences*, 117(17), 2019-22204, 2020 †
- Wu Fung S, Tyrväinen S, Ruthotto L, Haber E. ADMM-Softmax: An ADMM Approach for Multinomial Logistic Regression, *Electronic Transactions on Numerical Analysis*, 52, 214-229, 2020
- 15. Wu Fung S, Di Z. Multigrid Optimization for Large-Scale Ptychographic Phase Retrieval, SIAM Journal on Imaging Sciences, 13(1), 214–233. 2020
- Wu Fung S, Ruthotto L. An Uncertainty-Weighted Asynchronous ADMM Method for Large-Scale PDE Parameter Estimation, SIAM Journal on Scientific Computing, 41(5),S129-S148, 2019
- 17. Wu Fung S, Ruthotto L. A Multiscale Method for Model Order Reduction in PDE Parameter Estimation, *Journal of Computational and Applied Mathematics*, 350, 19-34, 2019

# Contributed and Invited Research Presentations

- Using Hamilton Jacobi PDEs in Optimization
  - invited talk at the Center for Mathematics and Artificial Intelligence, George Mason University. February 24, **2023**.
  - invited talk at the Center for Research in Signals and Networks Seminar, Colorado School of Mines. February 11, **2023**.
  - invited talk at the Applied and Computational Mathematics Division Seminar Series. National Institute of Standards and Technology. Boulder, CO, January 24, **2023**
- o Global Solutions to Nonconvex Problems by Evolution of Hamilton-Jacobi PDEs
  - invited talk at the Spatial Statistics and Kernel Club. Colorado School of Mines. Golden,
    CO, October 12, 2022
  - invited talk at the Optimal Transport and Mean Field Game Seminar at University of South Carolina. April 7, 2022.
  - invited talk at Level Set Collective Seminar, Department of Mathematics, UCLA, Los Angeles, Ca. September, 20, **2022**
  - invited talk at the Early Career Math Colloquium at The University of Arizona. September 21, **2022**.
- A Deep Learning Approach for Real-Time High-Dimensional Optimal Control
  - invited talk at Colorado School of Mines, Math Club/SIAM Student Chapter. March 16, 2022.
  - invited talk at the Center for Research in Signals and Networks Seminar, Colorado School of Mines. February 18, **2022**.

<sup>&</sup>lt;sup>†</sup>Author contributions: L.R., S.J.O., W.L., L.N., and S.W.F. designed research; L.R., L.N., and S.W.F. performed research; and L.R., S.J.O., W.L., L.N., and S.W.F. wrote the paper.

- invited talk at the Hamilton-Jacobi PDEs Reunion Conference I, at the Institute for Pure and Applied Mathematics, Los Angeles, California, January 13, **2022**.
- Efficient Training and Design of Implicit Networks with Applications in Contextual Games
  - invited talk at the Center for Research in Signals and Networks Seminar, Colorado School of Mines. December 10, **2021**.
- Efficient Training of Infinite-depth Neural Networks via Jacobian-free Backpropagation
  - invited talk at Sacred Heart University. Fairfield, CT. October 3, 2022.
  - invited talk at SIAM Conference on Mathematics of Data Science. San Diego, CA. September 30, **2022**.
  - invited talk at the CS@Mines Seminar at Colorado School of Mines. Golden, CO. May 3, 2022.
  - invited talk at SIAM Conference on Uncertainty Quantification. Atlanta, Ga. April 14, 2022.
  - invited talk at the Math Colloquium Series, at University of Colorado, Colorado Springs, March 31, 2022.
  - invited talk at the Los Alamos National Lab ML Seminar, February 17, 2022.
  - invited talk at the The Carl Heiland Lecture Series, at the Department of Geophysics, Colorado School of Mines, February 9, **2022**.
  - invited talk at the Applied Math/Inverse Problems Seminar, at Colorado State University, February 3, 2022.
  - invited talk at the The Scientific Al Research Group, at the University of Texas at Austin, January 28, **2022**.
  - invited talk at the Center for Wave Phenomena Seminar, Colorado School of Mines.
    December 6, 2021
  - invited talk at the AMS Fall Western Sectional Meeting, at University of New Mexico.
    October 23, 2021.
  - invited talk at the PDE and Applied Math Seminar at the University of California, Riverside.
    October 20, 2021.
  - invited talk at the Statistics, Optimization and Machine Learning Seminar at University of Colorado, Boulder. October 12, 2021.
  - contributed talk at the Applied Math and Statistics Colloquium at Colorado School of Mines. September 10, 2021.
- Wasserstein-based Projections for Inverse Problems
  - invited talk at the Applied and Computational Mathematics Seminar at Dartmouth College.
    January 26, 2021.
  - invited talk at the PDE and Applied Math Seminar at the University of California, Riverside.
    January 20, 2021.
  - invited talk at the Deep Learning Seminar at University of South Carolina. December 1, 2020.

- invited talk at the Optimal Transport and Mean Field Game Seminar at University of South Carolina. October 14, 2020.
- invited talk at the Mathematics and Deep Learning Collective at Iowa State University.
  October 2, 2020.
- o A GAN-based Approach for High-Dimensional Stochastic Mean Field Games, held at
  - invited talk at the Spatial Statistics and Kernel Club. Colorado School of Mines. Golden,
    CO, March 11, 2022
  - invited talk at the SIAM Virtual Conference on Mathematics of Data Science. June 25,
    2020
  - invited talk at the Laboratory for Applied Mathematics, Numerical Software, and Statistics (LANS) Seminar at Argonne National Laboratory. June 17, **2020**.
  - invited talk at the Numerical Analysis and Scientific Computing Seminar at Emory University. Atlanta, Ga. March 27, **2020**.
- o A Machine Learning Framework for High-Dimensional Mean Field Games, held at
  - invited talk at the Optimal Transport and Applications to Machine Learning and Statistics workshop at MSRI, Berkeley, Ca, May 5, **2020** (Online Recording)
  - invited talk (joint with Stanley Osher) at the High Dimensional Hamilton-Jacobi Methods in Control and Differential Games workshop at IPAM, Los Angeles, Ca, April 1, 2020 (Online Recording)
  - contributed poster in the Intersections between Control, Learning and Optimization workshop at IPAM, Los Angeles, Ca, February 24, **2020**
  - invited talk at the Level Set Collective Seminar, Department of Mathematics, UCLA, Los Angeles, Ca. December 3, 2019
- Adaptive Multiscale and Asynchronous Optimization Methods for Large-Scale PDE Parameter Estimation, held at
  - invited talk at the Level Set Collective Seminar, Department of Mathematics, UCLA, Los Angeles, Ca. July 30, 2019
  - invited talk at AMS Spring Southeastern Sectional Meeting, Auburn, AL, March 17, 2019
  - invited talk at SIAM Conference on Computational Science and Engineering, Spokane, Wa. February 27, 2019.
- Large-Scale Classification using Multinomial Regression and ADMM
  - contributed poster at Georgia Scientific Computing Symposium. Atlanta, Ga. February 16, **2019**
- Multilevel Algorithms for Ptychographic Phase Retrieval, held at various occasions:
  - contributed talk at the Summer Argonne Student Symposium at Argonne National Laboratory. Lemont, II. July 26, 2018
  - invited talk at the Advanced Photon Source at Argonne National Laboratory. Lemont, II.
    July 16, 2018

- An Uncertainty-Weighted ADMM Method for Large-Scale PDE Parameter Estimation, held at various occasions:
  - invited talk at SIAM Conference on Uncertainty Quantification. Garden Grove, Ca. April 19, 2018
  - contributed talk at Fifteen Copper Mountain Conference on Iterative Methods. Copper Mountain, Co. March 26, 2018
  - invited talk at Spelman College. Atlanta, Ga, February 26, 2018
  - contributed poster at Georgia Scientific Computing Symposium. Atlanta, Ga. February 24, 2018
  - contributed talk at the Scientific Computing Seminar at Emory University. Atlanta, Ga, USA, October 13, 2017
- o jInv A Flexible Julia Package for Parallel PDE Parameter Estimation, held at various occasions:
  - contributed e-poster at SIAM Conference on Computer Science and Engineering, Atlanta, GA, March 1, 2017
  - contributed poster, Georgia Scientific Computing Symposium. Atlanta, Ga. February 20, 2016
- o PDE-Constrained Optimization with Multiscale Methods, held at various occasions:
  - invited talk at SIAM Annual Meeting Conference. Pittsburgh, Pa, USA. July 10 14,
    2017
  - invited talk at SIAM Conference on Computational Science and Engineering. Atlanta, Ga, USA, March 3, 2017
  - contributed talk at the Scientific Computing Seminar at Emory University. Atlanta, Ga, USA, February 17, 2017

#### Teaching

- o Fall 2022
  - MATH 307: Intro to Scientific Computing, Section A, Colorado School of Mines
- o Spring 2022
  - MATH 307: Intro to Scientific Computing, Section A, Colorado School of Mines
- o Fall 2021
  - MATH 307: Intro to Scientific Computing, Section A, Colorado School of Mines
  - CSCI 499: Independent Study
- Spring 2021
  - MATH199: Directed Research in Mathematics, Section 9, UCLA (online)

- MATH 151A: Applied Numerical Methods I, Sections 1 & 2, UCLA (online)
- o Winter 2021
  - MATH 270C: Computational Linear Algebra (Graduate Level), Section 1, UCLA (online)
- o Fall 2020
  - MATH 151B: Applied Numerical Methods II, Section 1, UCLA (online)
- o Spring 2020
  - MATH 151A: Applied Numerical Methods I, Sections 1 & 2, UCLA (online)
- O Winter 2020
  - MATH 151B: Applied Numerical Methods II, Section 1, UCLA
- o Fall 2019
  - MATH 151A: Applied Numerical Methods I, Section 3, UCLA
- o Fall 2016
  - MATH 111: Introductory Calculus, Emory University
- o Spring 2016
  - MATH 111: Introductory Calculus, Emory University
- o Fall 2015
  - MATH 111: Introductory Calculus, Emory University
- O Spring 2015
  - MATH 351: Partial Differential Equations, Emory University (TA)
- o Fall 2014
  - MATH 212: Ordinary Differential Equations, Emory University (TA)

# Mentoring

- Graduate Student Supervision
  - Michael Ivanitsky. Project: Reinforcement Learning Informed by Biological Processes. Co-advised with Cecilia Diniz-Behn, Colorado School of Mines, since January 2022.
  - Soraya Terrab. Project: Data-Driven Multiwavelet Methods for Discontinuity Detection. Co-advised with Jennifer Ryan, Colorado School of Mines, since January 2022.
  - Alexander Vidal. Project: Optimal Transport-based Continuous Normalizing Flows, since August 2022.

- Undergraduate Student Supervision
  - Amandin Chyba and Jordan Pettyjohn. Project: Logical Extrapolation via Implicit Deep Learning. Colorado School of Mines, since August 2022.
  - Ibrohim Nosirov. Project: *Deep Learning Methods for Signal Processing*. Colorado School of Mines, September 2021 December 2021. Co-advised with Mike Wakin
  - Sudhanshu Agrawal. Project: *Machine Learning for High-Dimensional Non-Local Mean Field Games*. UCLA, January 2020 February 2022. Co-advised with Levon Nurbekyan
  - Richard Yim. Project: Learned Inverse Scale Space Flows. UCLA, January 2020 June 2020.
  - Caleb Wan and Jiangping Ye. Project: Adaptive Uncertainty-Weighted ADMM Methods for Machine Learning. UCLA, July 2020 - December 2021.
- Emory 2022 REU/RET Program on Model Meets Data. Project: Implicit Deep Learning for Inverse Problems.
  - Linghai Liu, Brown University
  - Allen Tong, UCLA
  - Lisa Zhou, UC Berkeley
- Research in Industrial Projects for Students (RIPS). Institute for Pure and Applied Mathematics, UCLA. June 2020 Aug 2020. Project: *Large-Scale Inventory Optimization* 
  - Miranda Kaiser, Rensselaer Polytechnic Institute
  - Julia Balukonis, Providence College
  - Rachel Fan, Vanderbilt University
  - Rong (Hugh) Jiang, UC Berkeley

#### Other Skills

- o Programming Languages: Python, Julia, Matlab
- Languages: Spanish (native), English (fluent), French (fluent), Cantonese (fluent)

# Workshop and Minisymposium Organization

- Co-organizer of mini-symposium on Advances in Learning to Optimize and Optimizing to Learn at SIAM Conference on Mathematics of Data Science, San Diego, California. September 2022
- Co-organizer of mini-symposium on Deep Learning Methods for Optimization at SIAM Conference on Uncertainty Quantification, Atlanta, Georgia, USA. April 2022
- Co-organizer of mini-symposium on Advances in Regularization Techniques for Ill-Posed Problems at the SIAM Conference on Imaging Sciences, Toronto, Canada. July, 2020

- Co-organizer of mini-symposium on Advances in Optimal Control for and with Machine Learning at the SIAM Conference on Mathematics of Data Science, Cincinnati, Ohio. May, 2020
- Co-organizer of mini-symposium on Mathematical Advances in Deep Learning at the SIAM Conference on Computational Science and Engineering, Spokane, Washington. February, 2019

### Professional Activities and Affiliations

- Reviewer for the following journals and conferences:
  - SIAM Journal on Numerical Analysis
  - SIAM Journal on Scientific Computing
  - SIAM Journal on Imaging Sciences
  - Frontiers in Applied Mathematics and Statistics
  - Mathematical and Scientific Machine Learning Conference (MSML)
  - Journal of Applied and Numerical Optimization (JANO)
  - Inverse Problems
- Board Member for the Emory SIAM Student Chapter. Aug 2014 May 2019
- Member of the Brown University Immigrant Rights Coalition. Aug 2011 May 2014
- o Member of Students Working for Equal Rights. Aug 2009 May 2011

#### Honors and Awards

- 2022 SIAM Early Career Travel Award for the SIAM Conference on Mathematics of Data Science
- 2022 MGB-SIAM Early Career (MSEC) Fellowship
- o 2021 Open Access Mini Grant Award, Colorado School of Mines
- o 2019 Emory Graduate Student Research Award
- Brown University Dean's Grant. 06/2013 07/2013
- Second Place Team Placement: 2011 Florida State Math Olympics
- o 2010 Miami Dade Honors Convocation Award in Economics