CHAPTER II: Social-ecological models with social hierarchy and space applied to small scale fisheries

Sophie Wulfing 1* and Easton R. White 1

¹Department of Biological Sciences, University of New Hampshire, 03824, NH, USA

^{*} Corresponding authors: Sophie Wulfing (Sophie
Wulfing@gmail.com) and Dr. Easton White (Easton.White@unh.edu)

1 ABSTRACT

Socio-ecological models combine ecological systems with human social dynamics in order to better understand human interactions with the environment. One such model of human behavior is replicator dynamics. Replicator dynamics are derived from evolutionary game theory and model how societal influence and financial costs can change opinions about resource extraction. Previous research on replicator dynamics have shown how evolving opinions on conservation can change how humans interact with their environment and therefore change population dynamics of the harvested species. However, these models have all assumed that human societies are homogeneous with no social structure. Extending off of previously existing models, we develop a two-patch socio-ecological model with social hierarchy in order to study the effect that social inequity has on decision making. We also analyzed the spatial components of this two-patch model and observed the effect of species movement on decision making and population dynamics. We found that this movement is a major driver of model dynamics when the two patches are asymmetrical and the linear aspects of these movement terms can overcome the non-linear components of the socio-ecological model. Further, we found that the societal influence between groups of harvesters was essential to ensuring stable fishery dynamics. Next, we developed a case-study of a co-managed fishery where one group fishes sustainable while another was over-harvests, resulting in a fishery collapse of both patches. SAY A LITTLE MORE ABOUT RESULTS OF THIS BIT. This study indicates the importance of including spatial components to socio-ecological models and highlights the importance of understanding species movements when making conservation decisions. Further, we demonstrate how incorporating fishing methods from outside sources can result in higher stability of the harvested population, indicating a need for diversified information when managing resources.

Keywords: two-patch model, replicator dynamics, social hierarchy, socio-ecological model, species movement

2 INTRODUCTION

The study of social ecological models is a growing field in ecology as they treat human behavior as a variable as opposed to a set parameter. This allows for the study of how human decision making can change in response to environmental factors and in turn, change how humans interact with resources and profits (Bauch, 2005; Ostrom, 2009; Innes et al., 2013; Oraby et al., 2014; Bauch et al., 2016; Sigdel et al., 2017; Thampi et al., 2018). As human societies grow increasingly intricate and interconnected, these models can help us to analyze how our social structures can influence the environment around us (Liu et al., 2007). These models provide important insight not only into how human decision making can influence ecological patterns but they can also show hidden processes, reveal regime shifts that would otherwise be hidden, and identify vulnerabilities of systems that do not exist within the purely social or ecological models (Liu et al., 2007; Young et al., 2007; Ostrom, 2009; Lade et al., 2013). Socio-ecological models have even showed different dynamics at different scales and different amounts of human connectivity (Cumming et al., 2017). They can also be used in systems where data are difficult to collect, as parameters can be changed in order to analyze different hypothetical scenarios. Socio-ecological models can also inform effective policy decisions. Conservation plans often do not reach their conservation goals, and these setbacks are often attributed to a lack of stakeholder participation (Crona & Bodin, 2006; Salas et al., 2019; Prince et al., 2021). This can be due to an emergence of conflict for stakeholders, where the conservation plan in place directly hinders their practices, therefore deterring them from participating in the restorative efforts. Socio-ecological models can identify where these areas of potential conflict can arise, compromises that can be made in the system, and alternative conservation practices that encourages participation from all stakeholder groups (Ban et al., 2013). Further, as these models are simulations of human and environmental interactions, they allow flexibility in that they can be adapted to fit the specific system of study and improve place-based management practices (Young et al., 2007; Liu et al., 2007; Felipe-Lucia et al., 2022)

Due to their adaptability, socio-ecological models can use a wide range of strategies to represent human decision making. One such method is replicator dynamics, which model human decision making where an individual makes conservation choices based on weighing the perceived benefits of conservation with the costs, as well as the social pressure to conform to the group's stance on conservation. Individuals will therefore "replicate" the behavior of their peers by changing their harvest practices based on the opinion of the majority (Bauch & Bhattacharyya, 2012). Models that employ replicator dynamics have been used to show how this social learning is a key component to vaccination uptake in public health, and preexisting social norms can actually suppress vaccine uptake despite frequent disease outbreaks (Bauch & Bhattacharyya, 2012; Oraby et al., 2014). They can also have conservation applications as pest invasion models have shown ways to simultaneously mitigate pest outbreaks and the cost to address them in the timber industry (Barlow et al., 2014). Further, land use changes have been modeled to have completely different dynamics when human decision making was added to these models (Innes et al., 2013). However, all previous models of human behavior have assumed that human societies are homogeneous, and all people are subject to the same social influence and ecological dynamics. No existing replicator-dynamics model has incorporated social hierarchy, despite the fact the most human societies have varying levels of social order within them.

Instituting effective conservation strategies can be especially difficult if the organism being protected has a migratory pattern that crosses over multiple management jurisdictions such as country borders (Ogburn et al., 2017; Garrone-Neto et al., 2018; Ramírez-Valdez et al., 2021). Borders can also create challenges when gathering population data that require extensive fieldwork (Cozzi et al., 2020; Hebblewhite & Whittington, 2020). The fragmentation of management can also result in a mismatch of conservation strategies that become ineffective when these management bodies do not coordinate efforts (Siddons et al., 2017). Research on the importance of coordinated research efforts has been conducted on many terrestrial

species with large migratory ranges and have consistently shown that cooperation among government bodies is essential to protecting the health of highly migratory species or species whose native ranges expand across multiple countries (Plumptre et al., 2007; Gervasi et al., 2015; Meisingset et al., 2018). Because fish are generally migratory, this issue is especially relevant in international waters or waters where different government bodies share jurisdiction (Mchich et al., 2000). For this reason, research on two-patch fishing models is a commonly used method as different management strategies can be modeled in each patch. Previous research on two-patch fishing models has shown that movement rates between patches can affect population stability when there are different fishing pressures in each patch (Mchich et al., 2000; Cai et al., 2008). Economic output can also be maximized in multi-patch fishing models as high dispersal can result in a higher overall yield of the system than the yield of each patch combined (Auger et al., 2022). High dispersal across patches is commonly found to be an essential component to maximizing population health and economic gain from fishing (Freedman & Waltman, 1977; Moeller & Neubert, 2015; Auger et al., 2022). Two-patch models help us to understand the population dynamics of fish species better who face different pressures in each patch and have even resolved conflicts between fishing groups (Mchich et al., 2000).

Contrary to this assumption made by previous models that human groups are homogeneous, the vast majority of real-world societies exhibit some form of hierarchy or inequality. Societies with different social subgroups can often exhibit an "us vs. them" mentality and compete for resources (Borgatti, 2003). This is because social status can greatly alter peoples' interaction with the environment. Competition over resources has been shown to be exacerbated by social hierarchies and 'top-down' regulation whereas when social connectivity is considered in management plans, management outcomes are not only improved, but costs are reduced as well (Krackhardt & Stern, 1988; Grafton, 2005; Bodin & Crona, 2009). Further, members of social networks have been shown to have varying levels of connectivity with others in their groups based on attributes such as ethnicity, and this can in turn alter

an individual's relationship with the environment and their views on conservation (Barnes-Mauthe, 2013; Sari et al., 2021). Barnes-Mauthe (2013) showed that fishing communities can exhibit homophily, which is the tendency for people to obtain information and opinions from those who are similar to themselves before seeking views from those who are perceived as different. Therefore, people in different social groups may be receiving different information and opinions about conservation and acting accordingly (McPherson et al., 2001). For example, in Kenya, communication among fishers has been shown to stay within groups using the same gear type which has inhibited successful regulation of the whole fishery (Crona & Bodin, 2006). Further, in the southwest Madagascar octopus fishery, fishing method and location typically falls along gendered lines. When fishing restrictions were imposed on tidal flats, this affected fishing access for women while maintaining this livelihood for male fishers, who typically fished in deeper waters (Baker-Médard, 2017). In Thailand, ethnicity has been shown to be a source of fishing conflict which has exacerbated resource depletion (Pomeroy et al., 2007). The existence of social structures is extremely prevalent in human societies and this has been shown to alter how people interact with the environment. However, there is little existing research that uses replicator dynamics study to study how social hierarchies alter harvest practices.

Small-scale fisheries are a particularly relevant system to apply replicator dynamics as fishing practices and policies are often made by communal decision makers. Research on small-scale fisheries is a growing and essential field as they are drastically understudied yet affect many people around the globe. Worldwide, about 32 million fishers make their livelihood in small-scale fisheries, a subsector in which 90 to 95% of harvest is distributed for local consumption. These marine products are a vital source of nutrition for these communities (The World Bank, 2012). Due to tight social structures, community decision making and strong reliance on the environment, small-scale fisheries are systems that are well represented by socio-ecological models and replicator dynamics (Grafton, 2005; Thampi et al., 2018; Barnes et al., 2019). Governmental bodies or third parties instituting conservation efforts in small-scale fisheries

have often been unsuccessful, especially when the social and economic components of the industry have been ignored (Salas et al., 2019; Prince et al., 2021). However, even when human interactions and decision making have been considered, socio-ecological models have often treated individuals in human societies equal in their social standing. As human societies are often complex and hierarchical, this simplifying assumption that everyone interacts with the environment and within their community equally can lead to lack of participation in conservation by some groups within a community (Barnes-Mauthe, 2013; Cumming et al., 2017). Mismanagement of fisheries have even been shown to exacerbate these inequalities (Cinner et al., 2012; Baker-Médard, 2017). Further, the specific dynamics of the fishery in question have been shown to be important components to models, as models with multiple patches can actually mitigate overfishing if there is high movement of the harvested species between patches (Cressman et al., 2004). No previous research has combined two-patch fishing models with a hierarchical human decision making model in order to study how space and social dynamics affect fishery dynamics.

In this study, we couple a human-decision replicator dynamics model with social hierarchies with a two-patch resource model in order to understand how decision making is affected by spatial and hierarchical factors. The objectives of this study were: 1) to compare the output of previous replicator dynamics studies with this two-patch model to understand the affect of species movement on harvesting decisions, 2) understand the effect of social hierarchy and communication across groups and how this changes the dynamics of this model, 3) use a co-managed small-scale fishery as a case study to understand how fishery dynamics are driven when one group fishes sustainably while the other overharvests. We hypothesized that higher cooperation between groups would benefit fish stocks overall and that increased fish movement would increase the health of fish populations.

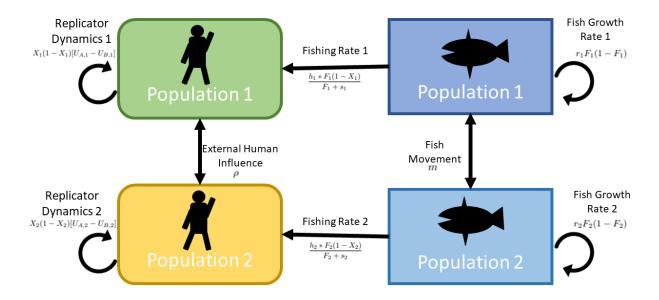


Figure 1: A conceptual representation of our model as a two-patch extension of Bauch et al. (2016). Here, each fish population (F_i) in each patch i increase through natural growth and movement of fish into the patch. Fish populations are decreased through emigration out of the patch and fishing mortality. The number of fishers (X_i) in each patch i change in response to fish population levels, the cost of stopping fishing activity, and the opinions of those in the patch and those in the other patch.

3 METHODS

3.1 Model Construction

We build on the work of Bauch et al. (2016) by extending their old-growth forest model to a two-patch model (Figure 1). The resource population models adapted from Bauch et al. (2016) are as follows:

$$\frac{dF_i}{dt} = r_i F_i (1 - F_i) - \frac{h_i * F_i}{F_i + s_i} - m_j F_i + m_i F_j \tag{1}$$

where the change in resource populations F_i is dependent on r_i , the net population growth of each patch i, and both populations follow logistic growth. The second term: $\frac{h_i*F_i}{F_i+s_i}$, denotes population lost to human activity. h_i is the harvesting efficiency of the respective human population and s_i controls the supply and demand of the system. Because we extend this to a two-patch model, the m_i parameter denotes the movement of the harvested species out of patch i and into patch j. In this study, we assume a closed population between the two patches. Therefore, individuals move directly from patch to patch and do not disperse elsewhere, nor are they immigrating from outside areas.

For the model of human activity and opinion, we use replicator dynamics from evolutionary game theory to simulate societal influence on an individual's opinion. Humans in this population can either be harvesters (therefore participating in harvesting activity) or conservationists (who do not partake in resource extraction), but can change from their current opinion to the other based on the perceived values and costs of each stance. Social dynamics are represented by the proportion of conservationists in a population (X) and the proportion of harvesters (1-X). These two groups interact with one another using the term (X)(1-X) which simulates individuals "sampling" the opinions other individuals in the population. If one opinion dominates in the population (i.e. X >> (1-X) or (1-X) >> X), the rate of changing opinions will be slow as the power of societal pressure makes it challenging for

the other opinion to gain traction. However, if X and (1 - X) are close, the rate of change in opinion will be fast as society has a split opinion on conservation versus harvest, so individuals will be quick to take up the opinions of others. In this model, each person holds an opinion (conservation or harvest) by weighing the benefits of conservation (U_A) against the benefits of harvest (U_B) . This gives the replicator equation:

$$\frac{dX_i}{dt} = k_i X_i (1 - X_i) [U_{A,i} - U_{B,i}]$$
 (2)

$$\frac{dX_i}{dt} = k_i X_i (1 - X_i) [\Delta U_i] \tag{3}$$

where k_i refers to the rate of interaction within a group. As individuals "sample" the opinions of others in their group, they can switch from A to B if $U_B > U_A$ and vice versa. In our model, we adapted U_A , the percieved benefit of conservation, from Bauch et al. (2016) with the added influence of the other population's opinion. U_A is therefore given by:

$$U_{A,i} = \frac{1}{(F_i + c_i)} + d_i X_i + \rho_i X_j \tag{4}$$

where $\frac{1}{(F_i+c_i)}$ represents the perceived rarity of the harvested population within a patch. As F_i and c_i (the rarity valuation parameter) decrease, this term will increase, therefore adding to the perceived benefit of protecting resources. d_i refers to the social influence that each population has on itself, and as an individual encounters a conservationist in their own population (X_i) , the social benefit of also being a conservationist is shown in d_i . ρ_i has this similar effect, but denotes the social effect of the opposite population on decision making (X_j) . Individuals in each population i are receiving information about the conservation practices of the other population j, and the influence that this has on each population is encapsulated by ρ_i .

 U_B (the perceived benefits of harvest) is:

$$U_{B,i} = \omega_i + d_i(1 - X_i) + \rho_i(1 - X_i) \tag{5}$$

where ω_i is the cost of conservation (i.e. revenue lost by not harvesting) where now, d_i is the within-population social benefit of switching to harvesting $(1 - X_i)$ and ρ_i is the other population's $(1 - X_j)$ ability to change the opinion of an individual to be a harvester.

Plugging equations (4) and (5) into equation (2) gives:

$$\frac{dX_1}{dt} = k_1 X_1 (1 - X_1) \left[\frac{1}{F_1 + c_1} - \omega_1 + d_1 (2X_1 - 1) + \rho_1 (2X_2 - 1) \right]$$
 (6)

$$\frac{dX_2}{dt} = k_2 X_2 (1 - X_2) \left[\frac{1}{F_2 + c_2} - \omega_2 + d_2 (2X_2 - 1) + \rho_2 (2X_1 - 1) \right]$$
 (7)

where specifics of the derivation are outlined in the supplementary material. Coupling the resource population and human opinion models gives:

$$\frac{dF_1}{dt} = r_1 F_1 (1 - F_1) - \frac{h_1 * F_1 (1 - X_1)}{F_1 + s_1} - m_2 F_1 + m_1 F_2 \tag{8}$$

$$\frac{dF_2}{dt} = r_2 F_2 (1 - F_2) - \frac{h_2 * F_2 (1 - X_2)}{F_2 + s_2} - m_1 F_2 + m_2 F_1 \tag{9}$$

$$\frac{dX_1}{dt} = k_1 X_1 (1 - X_1) \left[\frac{1}{F_1 + c_1} - \omega_1 + d_1 (2X_1 - 1) + \rho_1 (2X_2 - 1) \right]$$
(10)

$$\frac{dX_2}{dt} = k_2 X_2 (1 - X_2) \left[\frac{1}{F_2 + c_2} - \omega_2 + d_2 (2X_2 - 1) + \rho_2 (2X_1 - 1) \right]$$
(11)

where the harvesting pressure is now a function of the number of harvesters in a population $\left(\frac{h_i F_i(1-X_i)}{F_i+s_i}\right)$. Further, the opinion of each population will shift based on the perceived population

lation health of their respective patch weighed against the costs and benefits of conservation. As resources decrease, individuals will sway more toward conservation, thereby relieving this harvest pressure. However, we now have an external influence in this model: the opinions of people in population j. The strength of this external influence is ρ , and in this study, we plan to simulate inequalities in human societies with this parameter.

Table 1: Default parameter values used in this analysis taken from Bauch et al. (2016) where oscillations are observed.

Parameter	Population 1	Population 2	Definition
r	0.16	0.16	Fish net growth
S	0.8	0.8	Supply and demand
h	0.25	0.25	Harvesting efficiency
k	0.17	0.17	Rate of sampling opinions or social interaction
ω	1.44	1.44	Conservation cost
c	0.5	0.5	Rarity valuation
d	0.3	0.3	Strength of social influence (within population)
m	0	0	Fish movement (from opposite patch)
ρ	0	0	Strength of social influence (opposite population)

The default parameters used to analyze the resources movement and human hierarchy parameters were taken from an analyses done in Bauch et al. (2016) and given in Table 1. Here, Bauch et al. (2016) found an oscillatory behavior where decreased forest cover resulted in decreased harvest due to the replicator dynamics of the human system. This therefore allows forest recovery and humans to begin high harvest once again.

3.2 Parameter Analyses

In order to understand how resource movement $(m_1 \text{ and } m_2)$ affects dynamics, we first compare how the system will change when both patches are equal (i.e. all of the parameters in each patch is the same) by increasing both m_1 and m_2 incrementally and running the model for 1000 years. We then compare this to the asymmetrical case, where we just increase the m_1 parameter and see how this affects the model for the next 1000 years. We also construct bifurcation curves of the m_1 parameter when compared to resource populations in order to understand their effect on dynamics. Further, to analyze the human hierarchy parameters ρ_1 and ρ_2 , we constructed this same analyses of increasing ρ_2 , or the amount of influence of human population 2 (X_2) has on the dynamics of human population 1 (X_1) . We also compared this to the effect of the d_1 parameter by also incrementally increasing this and comparing this affect to that of ρ_2 .

3.3 Co-Managed Small Scale Fishery Case Study

For a small scale fishery, we choose to model a two-patch fishery where patch 1 is fishing sustainably while patch 2 is overharvesting. The harvested fish species has a mid-range growth rate and regularly diffuses across the two patches, such as the parrot fish modeled in Thampi et al. (2018), which uses a fish growth rate of is 0.35 fish per year, but alter patch 1's growth rate to be 0.4 fish per year. For the harvesting efficiency, we choose a maximal fishing rate of 0.5. These numbers were adapted from a coral reef fishing model Thampi et al. (2018) where r = 0.35 and h = 0.5 are the mid-level growth rate and max fishing rates analyzed by this paper. For the movement parameters m, we chose 0.2 for each as these are the values used in the two-patch fishing model described in Cai et al. (2008). We used the s parameter described in the Bauch et al. (2016) model of s = 0.8. For the purposes of this study, we are assuming a constant net growth rate of fish populations and that reproduction happens locally within each patch. The rate at which humans interact

with one another is described by the parameter k. In our default model, we use k=1.014 as adapted from the Thampi et al. (2018) default model. Here, they calculated this parameter by fitting conservation opinion data in the United States from 1965 to 1990 to coral health data at that time (Thampi et al., 2018). We used the default rarity valuation parameter c from Thampi et al. (2018) where c=1.68. The cost of conservation default parameter is $\omega=0.35$ from Bauch et al. (2016). Further, as our default model has no human social hierarchy, we set $d=\rho=0.5$ for our social norm strengths as adapted from Bauch et al. (2016) which models social decision making regarding deforestation.

Based off of this default model, we then change parameters such that patch 1 is fished sustainably, meaning the fish population in patch 1 is able to persist regardless of the fishing pressure from human population 1. We then set patch 2 to be overfished, meaning human patch 2 is fishing at too high a rate for the fish population to survive over time (Table 2). Further, we add a social hierarchical component where patch 2 has a higher social influence on patch 1. To analyze this scenario, we incrementally increase the parameters m and ρ and simulated this system for 100 years in order to assess how increasing each new parameter would affect the overall dynamics of the system.

Table 2: Parameter values used to simulate sustainable fishing practices in patch 1 and overfishing in patch 2.

Parameter	Population 1	Population 2	Definition
r	0.4	0.35	Fish net growth
S	0.8	0.8	Supply and demand
h	0.25	0.5	Harvesting efficiency
k	1.014	1.014	Rate of sampling opinions or social interaction
ω	0.2	0.35	Conservation cost
c	1.5	1.5	Rarity valuation

Parameter	Population 1	Population 2	Definition
d	0.5	0.5	Strength of social influence (within population)
m	0.2	0.2	Fish movement (from opposite patch)
ho	0.5	0.1	Strength of social influence (opposite population)

4 RESULTS

5 Model Comparisons

6 MOVEMENT

7 SOCIAL INFLUENCE STUFF

7.1 Scenario Analysis

We then modeled a hypothetical scenario where patch 1 is fished sustainably whereas patch 2 is experiencing overfishing and has a higher social sway than patch 1. We did this by altering fish new growth rates (r), harvesting efficiencies (h), costs of conservation (ω), and external social norm strengths (ρ) (Table 2). Here, the unsustainable practices of human population 2 are so exploitative, that both fish populations eventually collapse (Figure 5). We used this parameterization for the rest of the analysis, however the conclusions from each analyses are consistent with the other parameterizations we tested.

Next, we ran our model with incrementally higher external social influence values (ρ) in both populations and observed how this affected the final population of each fish patch (Figure 7). We found that under different parameterizations, ρ rarely had an effect on the final

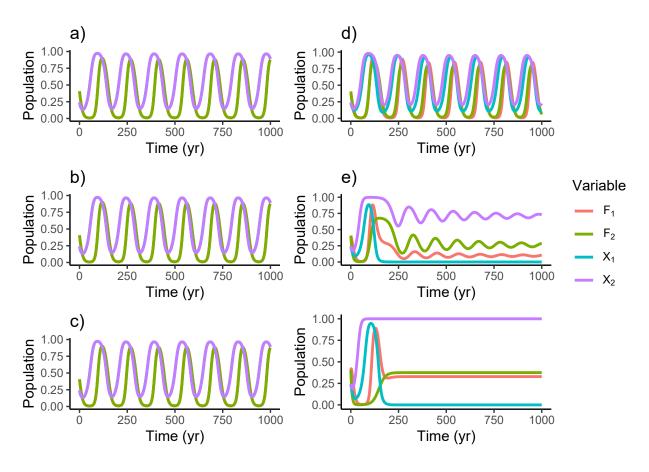


Figure 2: Showing that movement only matters when there is asymmetry. This can be asymmetry in other params. When this is the case, high movement dampens oscillatory effects

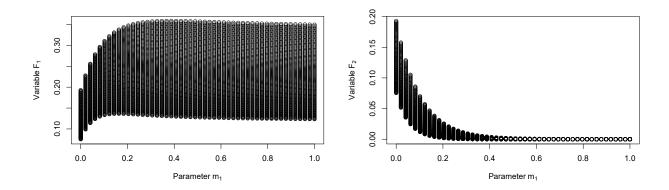


Figure 3: Bifurcation curves of fish pops in response to changes in m1 paramter. Shows how high m parameters eliminates oscillations.

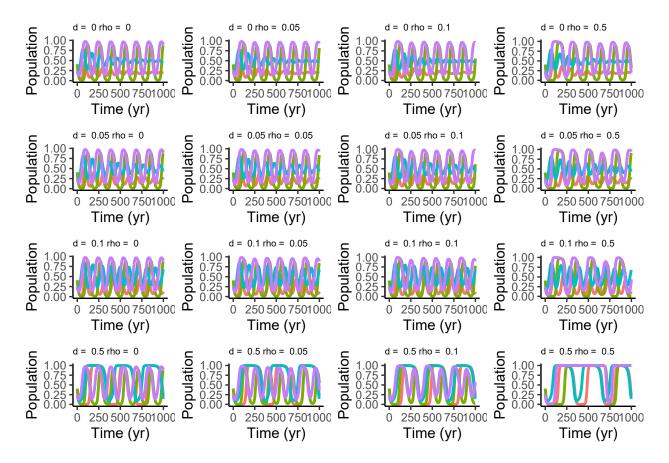


Figure 4: This shows the difference between a pop 1 listening to themselves vs. other pop. Looking at red line (which is fish in pop 1), this demonstrates that a portfolio effect can smooth over variation in dynamics. See how red line levels out when rho is high but with a low d. high d and low rho results in high fluctuations in stocks

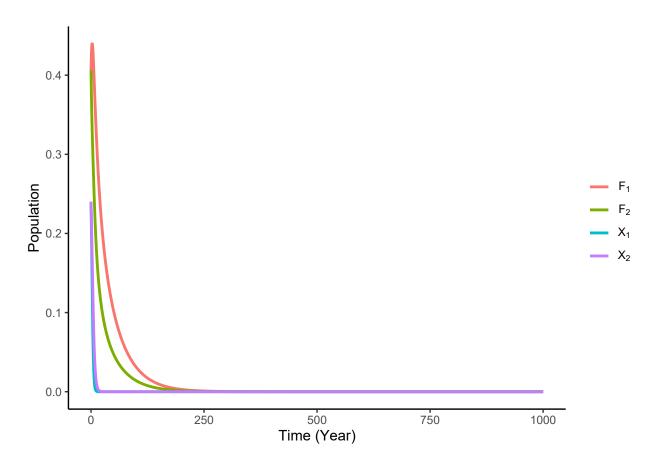


Figure 5: Representation of the dynamics of both the fish populations (F_i) and human conservationists (X_i) in each patch with default parameters from table 1 after 1000 years.

fish populations. However, there were some instances where ρ acted as a tipping point for population dynamics where instead of continuously changing the final fish populations, the ρ parameter either resulted in stable fish populations or both stocks collapsed once ρ increased past this point.

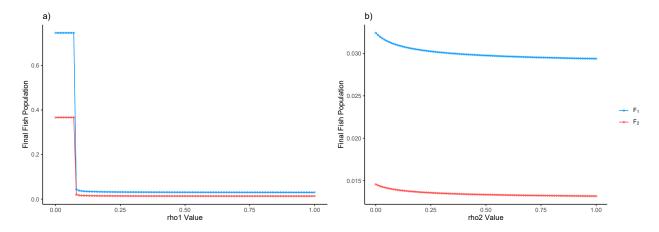


Figure 6: Each rho individually. Ok so here's my confusion, above in ??influenceasym I say that incorporating new information will increase stability but here, as pop 2 (which is unsustainable) listens to pop 1 more, the whole thing crashes. Earlier we said this was because pop 1 is continuing to fish, so therefore encouraging pop 2 to fish more (looking at graph a)

We then ran the same analysis with the fish dispersal parameter, m, by changing m_1 and m_2 individually. Contrary to the effect external social influence (ρ) had on the model, dispersal had a more direct and continuous effect on the final population of fish in each patch. For example, as fish movement from patch 2 to patch 1 increased (i.e. from the unsustainable patch to the sustainable patch), this actually maintained low fish populations the sustainable patch, but resulted in crashed populations in the unsustainable (Figure 8 a). However, if the fish movement was increased from patch 1 to patch 2 (from the sustainable fishing to unsustainable), both patches eventually collapsed to zero (Figure 8 b).

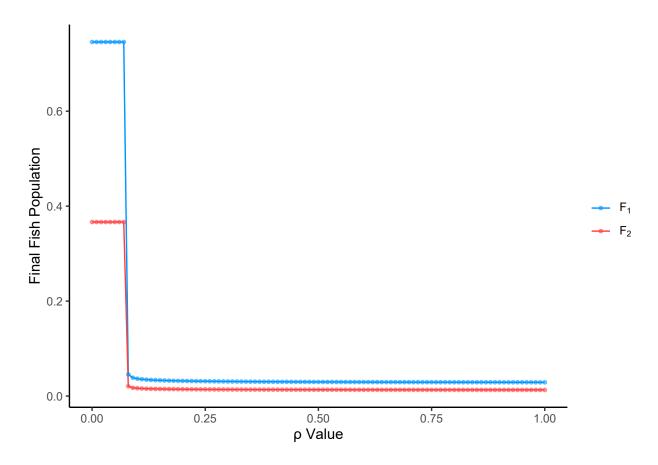


Figure 7: Final fish populations after 100 years in the two-patch fishing model where the F_1 population in patch 1 is fished sustainably but human population 1 has a lower social influence than humans in patch 2, where F_2 is being fished unsustainably. Both ρ_1 and ρ_2 were increased simultaneously.

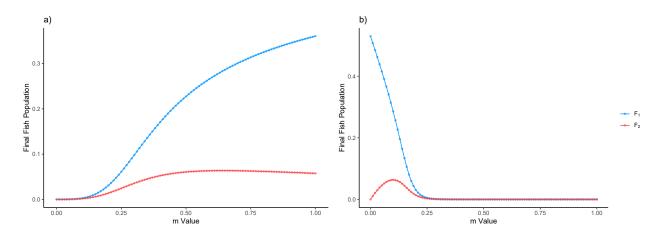


Figure 8: Final fish populations after 100 years in the two-patch fishing model where patch 1 (F_1) is fished sustainably but human population 1 has a lower social influence than patch 2, where F_2 is being fished unsustainably. a) shows how increases in fish movement into patch 1 (m_1) affect final populations and b) shows how increases in fish movement into patch 2 (m_2) affect final populations.

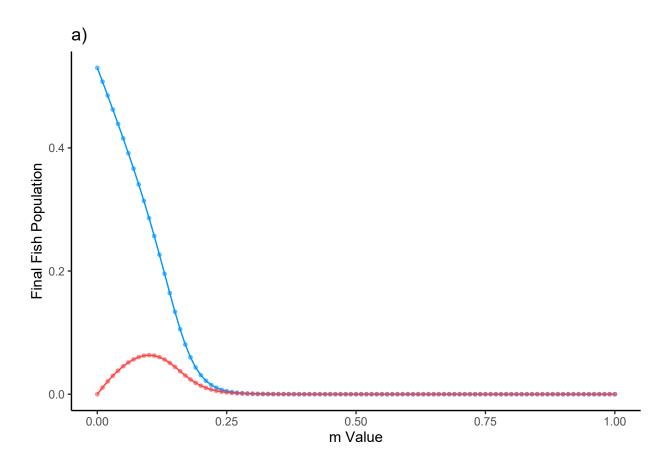


Figure 9: Both ms changing. Increasing both ms results in fishery crashes. Probably due to more fish entering F2 to be overfished more?

8 DISCUSSION

We extended previous models on replicator dynamics to two-patch fishing scenarios with social hierarchy in the human population. Firstly, we compared the results of our model to previous replicator equation models such as Thampi et al. (2018) and Bauch et al. (2016) (Figure ?? a). Mainly, both models found oscillations under certain parameterizations. This is in contrast to our model, where we found no scenarios that exhibit this behavior (Figure?? b). This is likely due to the fact that the linear aspects of the fish dispersal term eventually overpowers the non-linear components of the model. Further, because of the outside human influence term, ρ_i , people are not responding directly to their respective fishing patch, but also to the conservation opinion of the other group. This indicates that the inclusion of the immigration term from each patch overcame the non-linear components of the model because this is a linear term that had a major effect on the dynamics of the model. This shows that adding a spatial component to socio-ecological models can greatly change their dynamics and therefore how people are expected to act under certain environmental conditions. In our model, this shows that the dispersion of fish populations must be well understood in order to institute effective conservation practices. This is also because any decision made by one group of people to conserve resources may be rendered ineffective if this species is highly migratory and the other group of harvesters is using unsustainable conservation practices. Further, because of the outside influences from the other human patch, fishers are no longer responding directly to fish levels in their respective patch, i, but are also influenced by the proportion of fishers in the other patch, j. In a scenario where fish is abundant in one patch, this will also encourage fishing in the other patch because this will increase the incentive to fish from the outside influence parameter. Past research has exemplified how multi-patch models and the addition of spatial components change the dynamics of systems, especially in fisheries (Mchich et al., 2000; Cai et al., 2008; Moeller & Neubert, 2015; Auger et al., 2022). This highlights the importance of including spatial components to socio-ecological models.

We also simulated a scenario where patch 1 was being fished sustainably and patch 2 was experiencing overfishing, and also included social hierarchy by increasing ρ_1 , or the social influence that human population 2 has on the human population in the first patch. This resulted in the whole system collapsing (Table 1 and Figure 5). Next, we tested the effect of external social influence (ρ) on this model and how increasing social influence between human groups would influence the model's dynamics. Contrary to our hypothesis, increasing this parameter did not result in higher fish populations (Figure ??). Figure 7 shows how fish population dynamics typically crashed when ρ passed a tipping point, showing that high levels of cooperation between groups actually overharvested both populations of fish. At high levels of external social influence, sustainable fishing practices were not achieved because the only information being passed on to the other human population is the number of fishers as opposed to what sustainable fishing practices were used in order to achieve sustainable fishing yields. As a result, when one patch i is overfished and the other patch j is fished sustainably, the group i will continue to overfish their own resources because the opposite patch i is influencing this group to continue fishing through the high external social influence (ρ) . Instead of modeling a cohesive system where communication fostered effective conservation, we created a scenario where each community raced to fish each patch as opposed to coming to common understanding of sustainable fishing practices. Therefore, this further highlights that the content of the information being disseminated matters in successful conservation (Gray et al., 2012). This confirms previous research on co-management strategies where despite the fact they are a growing method in meeting social and ecological goals in smallscale fisheries, they are prone to fail and groups can come to management decisions that are unsuccessful, especially with ineffective conservation (Cinner et al., 2012). This aligns with previous social-ecological research that shows that social structures should be taken into consideration when the community manages a resource (Grafton, 2005; Newman & Dale, 2007; Bodin et al., 2014). This is because people who interact differently with the environment or within a society have to consider different tradeoffs in conservation, and these tradeoffs must be understood in order to institute sustainable practices (Cumming et al., 2017).

Instead of social norms controlling a lot of the dynamics of this model, we found that the movement of fish between patches (m) was a major driver of population sustainability or collapse (Table??). As we increased the movement of fish into the sustainable patch (Figure 8 a), this increased populations in that respective patch because humans in population 1 continued to fish sustainably. Further, as those in population 2 decreased fishing rates, this influenced population 1 to also decrease their number of fishers. As a result, population 1 maintained high fish stocks while population 2 had low stocks. On the contrary, as fish moved from the sustainable patch 1 to the unsustainable patch 2 (Figure 8 b), both fish populations collapsed as m_2 increased. This is because fish movement away from patch 1 eventually grew to be too great for human population 1 to fish sustainably and human population 2 continued to overfish in their own patch. High migration has been shown to be an essential part of maximizing economic benefit from fishing in multi-patch models (Moeller & Neubert, 2015). Because fish are generally migratory and therefore can be difficult to track, constraining fishing to one group of people is more challenging (Grafton, 2005). This is especially important for fish species that exhibit different movement patterns based on life stage, and requires more management coordination (Siddons et al., 2017).

The decision to include the external social influence term in our model within the injunctive social norms X(1-X) implies that external influence can still change an opinion for or against conservation. However, an individual's willingness to take up a new opinion is still dictated by the overall opinion of their own population. This exemplifies homophily, a concept in sociology where humans tend to take information and the opinions from subgroups similar to them before listening to subgroups of different social standing (Brechwald & Prinstein, 2011). Social network based conservation, like in our model, can replace 'top-down' regulation which can exclude stakeholders. However, this method of conservation has been shown to be susceptible to homophily (Newman & Dale, 2007). Conservation has been shown to be

more effective when human populations are more cohesive and that those with subgroups experience more barriers to effective conservation (Bodin & Crona, 2009). Solutions to this issue could be to institute some form of liason that serves as cross-group communicators (Guerrero et al., 2015).

Further research on this model could consider an open system, where fish diffusion doesn't necessarily have to pass between patches and could diffuse into non-fished areas. Further, extensions of this work could observe model dynamics with fish species with a long lifespan or fast reproduction rates. Also, stronger social ties have been shown to be more adaptable to environmental change (Grafton, 2005), therefore further studies could evaluate the effect of climate change or extreme events on this social system. The specific way we chose to incorporate social hierarchy into the model could be changed as well, for example by testing a model that includes the outside social influence outside of the X(1-X) term. There are many ways to model social systems so another further application of this study would be to compare different models that incorporate social hierarchy to the results of this one. Next, further work on parameterizing this model to a real-world system could help understand if this model is properly capturing the underlying dynamics of two-patch fishing systems with social hierarchy. This model is limited in that it only incorporates public opinion, fishing rates, and financial gains from fisheries as aspects that could cause fishery failure. In practice, other issues such as non-compliance to fishing regulations, hyper-stability, and regulation lag time could all be additional factors that result in fishery collapse but are not incorporated in this model (Erisman et al., 2011; Pinsky & Fogarty, 2012; Belhabib et al., 2014). Finally, this model assumed that the uptake of opinions happens solely through social networks and weighing costs of conservation against the benefits. In reality, there may be more factors that influence one's harvesting decisions such as governing bodies or media consumption. Further research could look into the other components that form decision-making.

References

- Auger, P., Kooi, B., & Moussaoui, A. (2022). Increase of maximum sustainable yield for fishery in two patches with fast migration. *Ecological Modelling*, 467, 109898. https://doi.org/10.1016/j.ecolmodel.2022.109898
- Baker-Médard, M. (2017). Gendering Marine Conservation: The Politics of Marine Protected Areas and Fisheries Access. *Society & Natural Resources*, 30(6), 723–737. https://doi.org/10.1080/08941920.2016.1257078
- Ban, N. C., Mills, M., Tam, J., Hicks, C. C., Klain, S., Stoeckl, N., Bottrill, M. C., Levine, J., Pressey, R. L., Satterfield, T., & Chan, K. M. (2013). A social–ecological approach to conservation planning: Embedding social considerations. Frontiers in Ecology and the Environment, 11(4), 194–202. https://doi.org/10.1890/110205
- Barlow, L.-A., Cecile, J., Bauch, C. T., & Anand, M. (2014). Modelling Interactions between Forest Pest Invasions and Human Decisions Regarding Firewood Transport Restrictions. *PLoS ONE*, 9(4), e90511. https://doi.org/10.1371/journal.pone.0090511
- Barnes, M. L., Bodin, Ö., McClanahan, T. R., Kittinger, J. N., Hoey, A. S., Gaoue, O. G., & Graham, N. A. J. (2019). Social-ecological alignment and ecological conditions in coral reefs. *Nature Communications*, 10(1), 2039. https://doi.org/10.1038/s41467-019-09994-1
- Barnes-Mauthe, M. (2013). The total economic value of small-scale fisheries with a characterization of post-landing trends: An application in Madagascar with global relevance.

 Fisheries Research, 11.
- Bauch, C. T. (2005). Imitation dynamics predict vaccinating behaviour. *Proceedings of the Royal Society B: Biological Sciences*, 272(1573), 1669–1675. https://doi.org/10.1098/rspb.2005.3153

- Bauch, C. T., & Bhattacharyya, S. (2012). Evolutionary Game Theory and Social Learning Can Determine How Vaccine Scares Unfold. PLoS Computational Biology, 8(4), e1002452. https://doi.org/10.1371/journal.pcbi.1002452
- Bauch, C. T., Sigdel, R., Pharaon, J., & Anand, M. (2016). Early warning signals of regime shifts in coupled human–environment systems. *Proceedings of the National Academy of Sciences*, 113(51), 14560–14567. https://doi.org/10.1073/pnas.1604978113
- Belhabib, D., Koutob, V., Sall, A., Lam, V. W. Y., & Pauly, D. (2014). Fisheries catch misreporting and its implications: The case of Senegal. *Fisheries Research*, 151, 1–11. https://doi.org/10.1016/j.fishres.2013.12.006
- Bodin, Ö., & Crona, B. I. (2009). The role of social networks in natural resource governance: What relational patterns make a difference? *Global Environmental Change*, 19(3), 366–374. https://doi.org/10.1016/j.gloenvcha.2009.05.002
- Bodin, Ö., Crona, B., Thyresson, M., Golz, A.-L., & Tengö, M. (2014). Conservation Success as a Function of Good Alignment of Social and Ecological Structures and Processes: Social-Ecological Fit and Conservation. *Conservation Biology*, 28(5), 1371–1379. https://doi.org/10.1111/cobi.12306
- Borgatti, S. (2003). The Network Paradigm in Organizational Research: A Review and Typology. *Journal of Management*, 29(6), 991–1013. https://doi.org/10.1016/S0149-2063(03)00087-4
- Brechwald, W. A., & Prinstein, M. J. (2011). Beyond Homophily: A Decade of Advances in Understanding Peer Influence Processes: Beyond Homophily. *Journal of Research on Adolescence*, 21(1), 166–179. https://doi.org/10.1111/j.1532-7795.2010.00721.x
- Cai, L., Li, X., & Song, X. (2008). Modeling and analysis of a harvesting fishery model in a two-patch environment. *International Journal of Biomathematics*, 01(03), 287–298.

- Cinner, J. E., McClanahan, T. R., MacNeil, M. A., Graham, N. A. J., Daw, T. M., Mukminin,
 A., Feary, D. A., Rabearisoa, A. L., Wamukota, A., Jiddawi, N., Campbell, S. J., Baird,
 A. H., Januchowski-Hartley, F. A., Hamed, S., Lahari, R., Morove, T., & Kuange, J.
 (2012). Comanagement of coral reef social-ecological systems. *Proceedings of the National Academy of Sciences*, 109(14), 5219-5222. https://doi.org/10.1073/pnas.1121215109
- Cozzi, G., Behr, D. M., Webster, H. S., Claase, M., Bryce, C. M., Modise, B., Mcnutt, J. W., & Ozgul, A. (2020). African Wild Dog Dispersal and Implications for Management. The Journal of Wildlife Management, 84(4), 614–621. https://doi.org/10.1002/jwmg.21841
- Cressman, R., Křivan, V., & Garay, J. (2004). Ideal Free Distributions, Evolutionary Games, and Population Dynamics in Multiple-Species Environments.
- Crona, B., & Bodin, Ö. (2006). What You Know is Who You Know? Communication Patterns Among Resource Users as a Prerequisite for Co-management. *Ecology and Society*, 11(2), art7. https://doi.org/10.5751/ES-01793-110207
- Cumming, G. S., Morrison, T. H., & Hughes, T. P. (2017). New Directions for Understanding the Spatial Resilience of Social–Ecological Systems. *Ecosystems*, 20(4), 649–664. https://doi.org/10.1007/s10021-016-0089-5
- Erisman, B. E., Allen, L. G., Claisse, J. T., Pondella, D. J., Miller, E. F., & Murray, J. H. (2011). The illusion of plenty: Hyperstability masks collapses in two recreational fisheries that target fish spawning aggregations. Canadian Journal of Fisheries and Aquatic Sciences, 68(10), 1705–1716. https://doi.org/10.1139/f2011-090
- Felipe-Lucia, M. R., Guerrero, A. M., Alexander, S. M., Ashander, J., Baggio, J. A., Barnes,
 M. L., Bodin, Ö., Bonn, A., Fortin, M.-J., Friedman, R. S., Gephart, J. A., Helmstedt,
 K. J., Keyes, A. A., Kroetz, K., Massol, F., Pocock, M. J. O., Sayles, J., Thompson, R.

- M., Wood, S. A., & Dee, L. E. (2022). Conceptualizing ecosystem services using social—ecological networks. *Trends in Ecology & Evolution*, 37(3), 211–222. https://doi.org/10.1016/j.tree.2021.11.012
- Freedman, H. I., & Waltman, P. (1977). Mathematical Models of Population Interactions with Dispersal. I: Stability of Two Habitats with and without a Predator. SIAM Journal on Applied Mathematics, 32(3), 631–648. https://doi.org/10.1137/0132052
- Garrone-Neto, D., Sanches, E. A., Daros, F. A. L. de M., Imanobu, C. M. R., & Moro, P. S. (2018). Using the same fish with different rules: A science-based approach for improving management of recreational fisheries in a biodiversity hotspot of the Western South Atlantic. Fisheries Management and Ecology, 25(4), 253–260. https://doi.org/10.1111/fme.12288
- Gervasi, V., Brøseth, H., Nilsen, E. B., Ellegren, H., Flagstad, Ø., & Linnell, J. D. C. (2015). Compensatory immigration counteracts contrasting conservation strategies of wolverines (Gulo gulo) within Scandinavia. *Biological Conservation*, 191, 632–639. https://doi.org/10.1016/j.biocon.2015.07.024
- Grafton, R. Q. (2005). Social capital and fisheries governance. Ocean & Coastal Management, 48(9-10), 753-766. https://doi.org/10.1016/j.ocecoaman.2005.08.003
- Gray, S., Chan, A., Clark, D., & Jordan, R. (2012). Modeling the integration of stakeholder knowledge in social–ecological decision-making: Benefits and limitations to knowledge diversity. *Ecological Modelling*, 229, 88–96. https://doi.org/10.1016/j.ecolmodel.2011. 09.011
- Guerrero, A. M., Mcallister, R. R. J., & Wilson, K. A. (2015). Achieving Cross-Scale Collaboration for Large Scale Conservation Initiatives: Cross-scale collaboration in conservation.

 Conservation Letters, 8(2), 107–117. https://doi.org/10.1111/conl.12112

- Hebblewhite, M., & Whittington, J. (2020). Wolves without borders: Transboundary survival of wolves in Banff National Park over three decades. *Global Ecology and Conservation*, 24, e01293. https://doi.org/10.1016/j.gecco.2020.e01293
- Innes, C., Anand, M., & Bauch, C. T. (2013). The impact of human-environment interactions on the stability of forest-grassland mosaic ecosystems. *Scientific Reports*, 3(1), 2689. https://doi.org/10.1038/srep02689
- Krackhardt, D., & Stern, R. N. (1988). Informal Networks and Organizational Crises: An Experimental Simulation. Social Psychology Quarterly, 51(2), 123. https://doi.org/10. 2307/2786835
- Lade, S. J., Tavoni, A., Levin, S. A., & Schlüter, M. (2013). Regime shifts in a social-ecological system. *Theoretical Ecology*, 6(3), 359–372. https://doi.org/10.1007/s12080-013-0187-3
- Liu, J., Redman, C. L., Schneider, S. H., Ostrom, E., Pell, A. N., Lubchenco, J., Taylor, W. W., Ouyang, Z., Deadman, P., Kratz, T., & Provencher, W. (2007). Coupled Human and Natural Systems.
- Mchich, R., Auger, P., & Raïssi, N. (2000). The dynamics of a fish stock exploited in two fishing zones. *Acta Biotheoretica*, 48, 201–218.
- McPherson, M., Smith-Lovin, L., & Cook, J. M. (2001). Birds of a Feather: Homophily in Social Networks. *Annual Review of Sociology*, 27(1), 415–444. https://doi.org/10.1146/annurev.soc.27.1.415
- Meisingset, E. L., Loe, L. E., Brekkum, Ø., Bischof, R., Rivrud, I. M., Lande, U. S., Zimmermann, B., Veiberg, V., & Mysterud, A. (2018). Spatial mismatch between management units and movement ecology of a partially migratory ungulate. *Journal of Applied Ecology*, 55(2), 745–753. https://doi.org/10.1111/1365-2664.13003

- Moeller, H. V., & Neubert, M. G. (2015). Economically optimal marine reserves without spatial heterogeneity in a simple two-patch model: Economically optimal marine reserves.

 Natural Resource Modeling, 28(3), 244–255. https://doi.org/10.1111/nrm.12066
- Newman, L., & Dale, A. (2007). Homophily and Agency: Creating Effective Sustainable Development Networks. *Environment, Development and Sustainability*, 9(1), 79–90. https://doi.org/10.1007/s10668-005-9004-5
- Ogburn, M. B., Harrison, A.-L., Whoriskey, F. G., Cooke, S. J., Mills Flemming, J. E., & Torres, L. G. (2017). Addressing Challenges in the Application of Animal Movement Ecology to Aquatic Conservation and Management. Frontiers in Marine Science, 4. https://doi.org/10.3389/fmars.2017.00070
- Oraby, T., Thampi, V., & Bauch, C. T. (2014). The influence of social norms on the dynamics of vaccinating behaviour for paediatric infectious diseases. *Proceedings of the Royal Society B: Biological Sciences*, 281(1780), 20133172. https://doi.org/10.1098/rspb.2013.3172
- Ostrom, E. (2009). A General Framework for Analyzing Sustainability of Social-Ecological Systems. *Science*, 325 (5939), 419–422. https://doi.org/10.1126/science.1172133
- Pinsky, M. L., & Fogarty, M. (2012). Lagged social-ecological responses to climate and range shifts in fisheries. *Climatic Change*, 115(3-4), 883–891. https://doi.org/10.1007/s10584-012-0599-x
- Plumptre, A. J., Kujirakwinja, D., Treves, A., Owiunji, I., & Rainer, H. (2007). Transboundary conservation in the greater Virunga landscape: Its importance for landscape species. Biological Conservation, 134(2), 279–287. https://doi.org/10.1016/j.biocon.2006.08.012
- Pomeroy, R., Parks, J., Pollnac, R., Campson, T., Genio, E., Marlessy, C., Holle, E., Pido, M., Nissapa, A., Boromthanarat, S., & Thu Hue, N. (2007). Fish wars: Conflict and

- collaboration in fisheries management in Southeast Asia. *Marine Policy*, 31 (6), 645–656. https://doi.org/10.1016/j.marpol.2007.03.012
- Prince, J., Lalavanua, W., Tamanitoakula, J., Tamata, L., Green, S., Radway, S., Loganimoce, E., Vodivodi, T., Marama, K., Waqainabete, P., Jeremiah, F., Nalasi, D., Naleba, M., Naisilisili, W., Kaloudrau, U., Lagi, L., Logatabua, K., Dautei, R., Tikaram, R., ... Mangubhai, S. (2021). Spawning potential surveys in Fiji: A new song of change for small-scale fisheries in the Pacific. Conservation Science and Practice, 3(2). https://doi.org/10.1111/csp2.273
- Ramírez-Valdez, A., Rowell, T. J., Dale, K. E., Craig, M. T., Allen, L. G., Villaseñor-Derbez, J. C., Cisneros-Montemayor, A. M., Hernández-Velasco, A., Torre, J., Hofmeister, J., & Erisman, B. E. (2021). Asymmetry across international borders: Research, fishery and management trends and economic value of the giant sea bass (Stereolepis gigas). Fish and Fisheries, 22(6), 1392–1411. https://doi.org/10.1111/faf.12594
- Salas, S., Barragán-Paladines, M. J., & Chuenpagdee, R. (Eds.). (2019). Viability and Sustainability of Small-Scale Fisheries in Latin America and The Caribbean (Vol. 19). Springer International Publishing. https://doi.org/10.1007/978-3-319-76078-0
- Sari, I., Ichsan, M., White, A., Raup, S. A., & Wisudo, S. H. (2021). Monitoring small-scale fisheries catches in Indonesia through a fishing logbook system: Challenges and strategies. *Marine Policy*, 134, 104770. https://doi.org/10.1016/j.marpol.2021.104770
- Siddons, S. F., Pegg, M. A., & Klein, G. M. (2017). Borders and Barriers: Challenges of Fisheries Management and Conservation in Open Systems: Challenges of Fisheries Management and Conservation in Open Systems. *River Research and Applications*, 33(4), 578–585. https://doi.org/10.1002/rra.3118
- Sigdel, R. P., Anand, M., & Bauch, C. T. (2017). Competition between injunctive social

- norms and conservation priorities gives rise to complex dynamics in a model of forest growth and opinion dynamics. *Journal of Theoretical Biology*, 432, 132–140. https://doi.org/10.1016/j.jtbi.2017.07.029
- Thampi, V. A., Anand, M., & Bauch, C. T. (2018). Socio-ecological dynamics of Caribbean coral reef ecosystems and conservation opinion propagation. *Scientific Reports*, 8(1), 2597. https://doi.org/10.1038/s41598-018-20341-0
- The World Bank. (2012). HIDDEN HARVEST-The Global Contribution of Capture Fisheries (66469-GLB). The World Bank. https://documents1.worldbank.org/curated/en/515701468152718292/pdf/664690ESW0P1210120HiddenHarvest0web.pdf
- Young, O. R., Osherenko, G., Ekstrom, J., Crowder, L. B., Ogden, J., Wilson, J. A., Day, J. C., Douvere, F., Ehler, C. N., McLeod, K. L., Halpren, B. S., & Peach, R. (2007). Solving the Crisis in Ocean Governance: Place-Based Management of Marine Ecosystems. Environment: Science and Policy for Sustainable Development, 49(4), 20–32. https://doi.org/10.3200/ENVT.49.4.20-33