Mechanistic models of human decision-making and ecological dynamics in small-scale fisheries

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2 TABLE OF CONTENTS

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3 ABSTRACT

Small scale fisheries are essential to the livelihoods of 40 million people worldwide. They are key sources of nutrients and income for these communities that rely on them. However, due to their abundance, understanding the status of these fisheries requires in-depth data collection, often in remote areas. Further, each small scale fishery is very individualized, and external groups attempting to impose fishing restrictions are often met with low compliance or are unsuccessful in their efforts to conserve fish stocks due to a lack of understanding of either fishing culture or the ecology of the harvested species. In this thesis, I employ various mechanistic models to small scale fisheries in order to better understand their underlying dynamics. In Chapter 1, I fit a Lefkovitch matrix population model to blue octopus data in the small scale fishery of Southwestern Madagascar in order to assess their life history and population health. In Chapter 2, I create a socio-ecological model with replicator dynamics and incorporated social hierarchy and space. Here, we found that collaboration between groups of people will be ineffective if only the financial gain of fishing is communicated, not the fishing strategies used to achieve high yields. Further, we found that fish movement was an extremely important parameter in these models. This work serves to exemplify the mathematical tools available when assessing small scale fisheries and highlight the need for a more substantive understanding of the status of the world's small scale fisheries.

4 Introduction

The definition of small scale fisheries is an evolving concept, but is characterized by subsistence fishing, community management, and traditional technologies (Smith 2019). 40 million people worldwide make their living off small-scale fisheries, which employs about 90% of all fishers globally. (Mills et al. 2011; FAO 2020) This metric does not include the 200-300 million people who are estimated to be employed in the processing chain of small scale fisheries, often informally (Mills et al. 2011). As many of these systems have transformed into industrial and recreational fishing, small scale fisheries are becoming increasingly associated with developing countries (Misund, Kolding, and Fréon 2002). These systems are an essential source of nutrition for these groups ("Hidden Harvest-The Global Contribution of Capture Fisheries" 2012; Chuenpagdee and Jentoft 2018; FAO 2020). Small scale fisheries have been shown to be a significant avenue of poverty alleviation through food security (Chuenpagdee and Jentoft 2018; FAO 2020). The number of fishers employed in small scale fisheries is rapidly increasing, indicating their growing importance (Jentoft and Eide 2011).

Despite the prominence of small-scale fisheries and their importance to the people who rely on them, they face many threats as they are highly susceptible to climate change (Allison et al. 2009), coastal urbanization (Kadfak and Knutsson 2017), and overfishing (Cinner et al. 2018). Because fishers are more directly reliant on these subsistence fisheries, people are more directly affected by these challenges than in large industrial fishing (Allison et al. 2009; Jentoft and Eide 2011). The issue of overfishing is also often exacerbated by large-scale industrial fishing occurring in places near small scale fisheries (Bavinck 2011). Governance of small scale fisheries is also typically difficult as different small scale fisheries often require different management styles in order to be successful (Gutiérrez, Hilborn, and Defeo 2011). Further, they are often characterized by a close connection between the ecology of the fishery and the culture of those who fish there. This means that each small scale fishery is very individualized and so there exists no "one size fits all" conservation strategy for every one. Instead, a deep understanding of both the biology of the fish being harvested and the socio-economic factors that affect fishing activity is required in order to institute effective and equitable conservation in small scale fisheries ("Saving Fish and Fishers: Toward Sustainable and Equitable Governance of the Global Fishing Sector" 2004; Kosamu 2015).

However, this in depth understanding is difficult to achieve as small scale fisheries are drastically understudied (Misund, Kolding, and Fréon 2002; Mills et al. 2011; FAO 2020). This can be partially attributed to the fact that small scale fisheries employ a large number of people over a large spatial distribution, and governments are often financially limited when surveying these sectors (Misund, Kolding, and Fréon 2002; Gutiérrez,

Hilborn, and Defeo 2011). Because a lot of employment in small scale fisheries is informal, it's difficult to understand exactly how many people are reliant on small scale fisheries, and existing metrics are likely to be underestimations (Mills et al. 2011). Data collection in small scale fisheries can be difficult and resource consuming as they often exist in remote places (Chuenpagdee et al. 2019). Also, effective conservation requires an understanding of the practices and culture of fishers. Fishers in certain areas can sometimes come from different ethnicities and speak different languages (Pomeroy et al. 2007; Barnes-Mauthe et al. 2013; Sari et al. 2021), making cross-cultural cooperation difficult. Further, conservationists have often ignored social hierarchies in small scale fisheries, and by doing so, have actually further entrench these inequalities (Baker-Médard 2017). The existence of social structures is extremely prevalent in human societies and this has been shown to alter how people interact with the environment.

Community management of fisheries has been shown to be one of the most effective forms of small scale fishery conservation while employing traditional knowledge and empowering local communities Gelcich and Donlan (2015). Small scale fisheries are typically characterized by tight social structures and strong reliance on the environment, therefore the intersection of culture and environment is extremely important in maintaining their sustainability (Grafton 2005; Thampi, Anand, and Bauch 2018; Barnes et al. 2019). Community management allows for reaching ecological goals while simultaneously maintaining the livelihood and economic and cultural goals of fishers (Govan 2010; Barnes-Mauthe et al. 2013). On the other hand, outsider institutions have typically ignored these cultural components to fisheries and either further entrenched inequalities in the community or conservation efforts have been met with low compliance (Bodin and Crona 2009; Katikiro, Macusi, and Ashoka Deepananda 2015; Kosamu 2015; Salas, Barragán-Paladines, and Chuenpagdee 2019; Prince et al. 2021).

Mechanistic models are one way in which we can study small scale fisheries despite challenges in data collection. Mechanistic models mathematically describe the underlying biological and physical processes that make up an ecological system (Grimm et al. 2005; André, Haddon, and Pecl 2010; Briggs-Gonzalez et al. 2016). Therefore, they do not require the extensive data collection needed to construct a statistical model (Crouse, Crowder, and Caswell 1987; Nowlis 2000; Gharouni et al. 2015). Mechanistic models are a prominent tool in fishery assessments (Lee et al. 2018; Free et al. 2020). In the following chapters, we utilize mechanistic models to better understand small scale fisheries and what social and ecological challenges they face.

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CHAPTER I: Using mechanistic models to assess temporary closure strategies for small scale fisheries

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1 ABSTRACT

Mechanistic models are particularly useful for understanding and predicting population dynamics in data deficient species. Data deficiency is a relevant issue in small scale fisheries as they are generally under studied and underrepresented in global fishing datasets. As overfishing remains a global issue, especially in small-scale fisheries, one commonly utilized conservation method is temporary closures. The blue octopus (Octopus cyanea) fishery off the southwest coast of Madagascar is one such system that uses temporary closures, yet lacks sufficient data collection to assess the viability of the population. This fishery is a key economic resource for the local community as blue octopus catch is sold by local fishers to international and local export markets and is a major component of fisher income. To assess the sustainability of blue octopus, we parameterize a Levkovitch population matrix model using existing catch data. In this study, 10 we show that this population was in a decline of 1.8% per month at the time of data collection. To sustain the existing population of blue octopus, our model indicates that the fishery would need to close for at least 12 three months annually. Increasing the length of closure is predicted to significantly increase the octopus population at these sites. We show that if implemented correctly, temporary closures could be used to 14 restore this population. The local communities of Madagascar have implemented various fishing restrictions 15 to ensure sustainable fishing, indicating a need for further research into the effectiveness of these fishing 16 closures. Therefore, our study provides insight into the underlying population dynamics of this fishery and 17 provides survivability estimates of this species. 18

19 Keywords: Octopus Cyanea, matrix model, small scale fisheries, Madagascar, temporary closures

$_{\scriptscriptstyle 0}$ 2 INTRODUCTION

- Mechanistic models in ecology explicitly account for species life histories, behavioral, or other mechanisms
- to describe how a population or community may change over time (André, Haddon, and Pecl 2010; Briggs-
- 23 Gonzalez et al. 2016). Mechanistic models can be important in situations without existing long-term data.
- ²⁴ when future conditions may not be similar to the past, and when different scenarios or actions need to
- be assessed (Crouse, Crowder, and Caswell 1987; Nowlis 2000; Gharouni et al. 2015). Thus, mechanistic
- 26 models play a critical role in making informed conservation decisions, such as the management of small-scale
- 27 fisheries.
- Worldwide, 32 million fishers make their livelihood in small-scale fisheries, a subsector in which 90 to 95%
- 29 of fish is distributed for local consumption. These marine products are a vital source of nutrition for these

communities ("Hidden Harvest-The Global Contribution of Capture Fisheries" 2012). The southwest region of Madagascar is one such area where subsistence fishing is an essential component to the diet and income of the local community. The ocean environments off the southwest coast of Madagascar are home to a wide variety of marine life, as sand beds, seagrass beds and coral reefs are all prominent biomes in the area. In fact, Madagascar has been calculated as a country that would benefit greatly from marine conservation given its economic reliance on marine harvests and the fact that it is a refuge to many marine species (Laroche et al. 1997). In the early 2000's, however, Madagascar began to move from local, subsistence fishing to also selling catch to export markets (Humber et al. 2006). There is evidence that up to 75% of all fish caught in select villages is now sold to outside entities for international export (Baker-Médard 2017).

Locally-managed marine areas (LMMAs) are defined as coastal and near-sore fisheries in which resources are managed almost entirely by local communities and fishery stakeholders that live in the region. Because management is conducted by those directly affected by the fishery, goals typically include maintaining the livelihood and economic and cultural goals of the local community along with environmental goals (Govan 2010). LMMAs have grown in popularity among conservationists in small scale fisheries due to this empowerment of local fishers. Because of this, LMMAs tend to have greater local participation and compliance from stakeholders when compared to top-down regulation from governing bodies (Katikiro, Macusi, and Ashoka Deepananda 2015). LMMAs have been shown to improve both fisheries and fisher livelihoods in Kenya (Kawaka et al. 2017), Pacific Islands (Govan 2010), and in Madagascar (Mayol 2013). In Madagascar, the use of LMMAs has increased significantly since 2004, and fishers in the country have seen significant improvements to fish stocks as well as have experienced economic benefits since (Benbow and Harris 2011; Gilchrist et al. 2020). In order to protect fishing resources, Madagascar has instituted various conservation programs. Marine Protected Areas (MPAs) are regions in the ocean identified as being biologically important and fishing protections are therefore enforced. Before their establishment in Madagascar, governmental bodies had bans on certain types of fishing gear, implemented seasonal fishing regulations, and criminalized 53 the harvest of endangered species. However, these strategies proved ineffective in execution and in their conservation goals (Humber et al. 2006). Both the government and nongovernmental organizations have since pledged to drastically increase the number of regions dedicated as MPAs through temporary fishing closures (Cinner et al. 2009; Oliver et al. 2015; Baker-Médard 2017).

One such class of MPAs that are currently being used in Madagascar are seasonal closures. These types of reserves have a long history of use and have been seen to successfully rehabilitate stocks (Camp, Poorten, and Walters 2015; Gnanalingam and Hepburn 2015). For example, seasonal closures have been shown to be an effective conservation strategy in increasing biomass the Atlantic sea scallop fishery in the United

States (Bethoney and Cleaver 2019), restored natural trophic interactions in coral reef fisheries in Kenya (McClanahan 2008), and successfully restored the marlin stocks in Baja California (Jensen et al. 2010). This method is flexible, logistically simple for fishers and managers to understand, and mitigates the financial loss from the fishery that can be seen with permanent closures (Nowlis 2000; Humber et al. 2006; Cohen and Foale 2013; Camp, Poorten, and Walters 2015; Gnanalingam and Hepburn 2015; Oliver et al. 2015). However, seasonal closures are not always effective in their goal of replenishing stocks and this can depend on a wide range of factors. Ecological considerations about the life history of the target species, Allee effects, and changes to community structure and species interactions all play a role in how well the seasonal closure will protect the fishery (Russ and Alcala 1998; Cohen and Foale 2013; Gnanalingam and Hepburn 2015; Gilchrist et al. 2020; Grorud-Colvert et al. 2021). Further, the characteristics of the fishery itself has been 71 seen to influence fishery recovery. Fishing method, where the effort will be redistributed to, and fishing activity upon reopening have all been factors in negating the recovery made during the closure (Hiddink et al. 2006; Humber et al. 2006; Cohen and Foale 2013). Therefore, assessments of each seasonal closure is essential to insuring that they are effective in replenishing fish stocks. Mechanistic modeling allows us to simulate different fishery scenarios and assess how populations will respond to these changes in fishing pressure. 77

Since 2003, when this marine resources in Madagascar first began to globalize, cephalopods have become one of the largest classes of exports (Humber et al. 2006; Aina 2009; Barnes-Mauthe 2013). This has since added significant fishing pressure to Madagascar's cephalopod populations and yield from this fishery has decreased in regions of this island such as the southwest Andavadoaka region (Humber et al. 2006). Cephalopods are a vital part of many ocean ecosystems and, compared to other fisheries, have a unique life history that can lead to distinct and variable population dynamics. Cephalopods act as both predators and prey in an ecosystem (Rodhouse and Nigmatullin 1996; Santos, Clarke, and Pierce 2001; Vase et al. 2021), situating them in a key role in food webs. They also provide rich nutrition and bioactive compounds to the oceanic microbial community (Fitahia et al. 2018). Further, their abundance varies drastically with a wide range of ocean conditions including sea surface and bottom temperature, salinity, currents, and sediment type (Catalán et al. 2006; Ibáñez et al. 2019; Van Nieuwenhove, Ratsimbazafy, and Kochzius 2019). Compared to other exploited marine organisms, cephalopods have a short lifespan coupled with a fast reproduction rate and high fecundity. This explains their population's ability to quickly bounce back when short term MPAs are introduced into their habitat (Humber et al. 2006; Katsanevakis and Verriopoulos 2006; Benbow et al. 2014). However, once fishing resumes, populations can suddenly and rapidly decline although in some examples, this could be attributed to heavy fishing pressure in the area right after reopening (Humber et al. 2006).

Cephalopods are therefore extremely sensitive to both protection and harvest levels, and understanding how
these volatile population dynamics will react to changes in fishing pressure is a key component to effective
conservation of this resource.

Octopus cyanea, or blue octopus, is the most abundant cephalopod species in the western Indian Ocean and is caught in about 95% of local landings in Madagascar (Humber et al. 2006; Oliver et al. 2015). Like other cephalopod species, very little is known about their life history including natural death rate, larval survivability, and how much time this species remains in each stage of maturity. Further, age is difficult to determine from size alone as they have variable growth rates up to maturity (Wells and Wells 101 1970; Heukelem 1976; Herwig et al. 2012; Raberinary and Benbow 2012). Size limits have been shown to be the most effective method of conservation for cephalopods in general as it ensures individuals will 103 breed before being harvested (Nowlis 2000; Emery, Hartmann, and Gardner 2016). To protect this species. 104 size limits have been imposed on blue octopus catch in Madagascar, but these regulations are difficult in 105 practice, as the fishing method used to harvest octopus involves spearing the octopus's den and extracting 106 the octopus from the den. Blue octopus therefore typically die before size can be assessed, so octopus too 107 small for market sale are typically harvested for household consumption (Humber et al. 2006). Further, the 108 relationship between size and maturity stage is not strongly correlated (Raberinary and Benbow 2012) and as a result, size restrictions wouldn't necessarily protect individuals ready to reproduce and would be difficult 110 to implement in the field. Therefore, temporary closures have been shown to be a more practical method of octopus conservation in that they can replenish stocks while maintaining fisher income (Benbow et al. 2014). 112 However, this requires a deeper understanding of the characteristics of Octopus cyanea in this fishery in order to be properly instituted. Instituting effective temporary closures in octopus fisheries can be difficult due to 114 their short lifespan, high mortality, and sensitivity to environmental conditions (Catalán et al. 2006; Emery, 115 Hartmann, and Gardner 2016; Ibáñez et al. 2019; Van Nieuwenhove, Ratsimbazafy, and Kochzius 2019). 116 Lack of field data and difficulty of enforcement has also been a challenge in octopus fisheries, especially in 117 Madagascar (Emery, Hartmann, and Gardner 2016; Benbow et al. 2014). This indicates that a thorough 118 understanding of the life history of O. cyanea and the harvest methods employed by fishers is necessary to 119 enact meaningful fishing restrictions. Currently, the octopus fishery in this region of Madagascar is closed for the three months between June and August on a yearly basis (Benbow and Harris 2011; Westerman and 121 Benbow 2014) which was decided in 2011. In this paper, we will also assess how this duration of closure will 122 affect Octopus cyanea stocks. 123

In this paper, we have three goals: 1) we will fit a Levkovitch matrix to the limited available data on *Octopus*cyanea populations in southwestern Madagascar, 2) as well as create a theoretical estimation of the species'

life history traits in different stages of its development and 3) determine the frequency and length in which
these temporary closures should take place to maximize population health of the fishery and maximizing
catch for the local community.

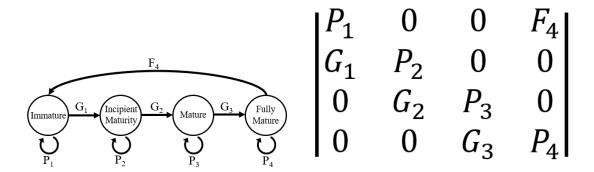


Figure 1: A graph representing the life history of O. Cyanea and the subsequent Lefkovitch Matrix where i corresponds with each of the stages of maturity (Immature, Incipient Mature, Mature, and Fully Mature individuals, respectively). P_i corresponds to probability of surviving and staying within a stage. G_i is the probability of surviving and growing to the next stage. F_i is the reproductive output of stage i.

3 METHODS

129

As O. cyanea has an extended larval phase and there is no existing data on the age structure of this population 130 of octopus, we will use a stage-based population matrix, otherwise known as a Lefkovitch matrix (Caswell 131 2001). Here, the life history of the study organism is grouped by stages (Figure 1), where each unit of 132 the matrix represents a distinct period of the organism's life where it is subject to different environments, 133 pressures, or physical attributes that would alter the survival and reproductive output at that phase, but the amount of time between each stage is variable. This would simply create different inputs for the probability 135 of remaining in the same stage, and the growth and fecundity inputs can be based on available data. 136 Lefkovitch matrices have not yet been applied to Octopus cyanea populations and therefore could be a useful 137 methodology to understand the dynamics of this population in the western Indian Ocean to better inform 138 management strategies. 130

$_{\circ}$ 3.1 Data

To inform our model, we used data collected by Raberinary and Benbow (2012) from landings ranging from the villages of Ampasilava in the south to Andragnombala in the north which spans about 30 kilometers of coastline. Here, fishers usually fish along both reef flats and deeper barrier reefs. Fishers bring catch

onshore either for household consumption or to sell to buyers for international export. This study collected 144 landing data from February 2005 to February 2006 through daily surveying fishers as they landed onshore within a two hour window. They separated each octopus into five age classes: immature, incipient maturity, 146 maturity, full maturity, and post laying. In this paper we omitted stage five, post laying, from this model as blue octopus only brood once, and stage five individuals therefore do not contribute to population growth. 148 They recorded octopus weight, weight and length of gonads, sex, and a visual assessment of maturity class. A subsample of octopus were also collected for octopus length, and laboratory assessment of gonads for a 150 confirmation of maturity class. They gathered this data on a total of 3,253 octopuses, and for the purposes 151 of this study, we will be modeling from the 1,578 females collected. Despite there being no standardization 152 for catch effort being available for this dataset, no other maturity stage study has been conducted on this 153 population of O. cyanea and is therefore the best available data to fit a Lefkovitch matrix. As there is no previous estimate of the natural death rate of this population, the Lefkovitch matrix, survivability estimates 155 and growth rate calculations for this model will also include the influence of fishing pressure. This data is reported in the appendix. 157

$$\begin{vmatrix} P_1 = 0.63 & 0 & 0 & F_4 = 26.7 \\ G_1 = 0.275 & P_2 = 0.322 & 0 & 0 \\ 0 & G_2 = 0.13 & P_3 = 0.393 & 0 \\ 0 & 0 & G_3 = 0.093 & P_4 = 0.331 \end{vmatrix}$$

Figure 2: Stage-based population matrix calculated using Wood's quadratic programming method and parameterized using data from Raberinary and Benbow (2012).

3.2 Model Parameterization

158

In order to parameterize this model, we used Wood's Quadratic Programming method (Caswell 2001).
Other methods required longer time series than were available to us, were extremely sensitive to noise in
the data, or simply resulted in matrices that had no reasonable biological interpretation (Caswell 2001).
We estimated a preliminary stage-based matrix model (Figure 2) based on Raberinary and Benbow (2012)
data and calculated using the quadprog package in R (Turlach and Weingessel 2019). Model accuracy was
assessed by comparing life history values inferred from the matrix with existing literature on *O. cyanea* life
history (Table 1). As all of our values calculated from the matrix fell within the known attributes of this
species, we were confident that this model gave an accurate mechanistic description for this population's

underlying dynamics.

168 3.3 Model Analysis

Eigenvalues (λ) were then calculated from the matrix and future populations can be predicted by multiplying a population vector to incrementally higher powers of our matrix where the power of the matrix corresponds 170 to the time length of the projection. We performed sensitivity analysis on the population matrix and 171 eigenvalues using the r package popbio (Stubben and Milligan 2007). Further, as all of the parameters 172 are scaled to a value between 0 and 1 except F_4 , a unit change in these parameters will have a greater 173 proportional effect on the eigenvalue than F_4 . To address this, we also conducted elasticity analysis using 174 the popbio package (Stubben and Milligan 2007). This will allow us to identify the groups within this 175 octopus population whose protection will most benefit population growth, essentially creating focus points of conservation. The results of sensitivity and elasticity analysis will be included in the supplementary 177 material. Other life history traits that can be calculated from this matrix are stable stage distribution, reproductive value of each stage, and per-stage survivability. We will also use the R package Rage (Jones 179 et al. 2021) to calculate the age in each stage, life expectancy and longevity, the age and probability of 180 reaching maturity, and generation time of this population. We then used the rage package in R to analyze 181 various life history traits of this matrix, the output of which is included in the supplementary material. 182 Finally, we calculated the minimum survivability increase necessary per stage to result in an increase of the overall population. We did this by increasing the P_i and G_i parameters by increasing percentages in each 184

3.4 Management Scenarios

stage i until the overall eigenvalue (λ) became greater than one.

In order to determine optimal conservation strategies, we altered the survivability of *O. cyanea* by different rates from 0-10% survival increase of the species. Then, we simulated different closure scenarios for each survival increase, by altering the length of annual closures by month. We then multiplied higher powers of the original matrix during months that were simulated to be "open fishing" and then when a closure was simulated, the matrix with increased survival was multiplied to the population for that month. We simulated these different scenarios in order to analyze all combinations of conservation strategies that result in stable *O. cyanea* populations including the three month closure that is currently being instituted.

Table 1: Existing research and information on the per-stage lifespan of *O. Cyanea*. All existing estimates are from Heukelem (1976), Heukelem (1976), Guard and Mgaya (2003), Humber et al. (2006), Aina (2009). Note: Heukelem and Fred (1976) estimate the time to maturity to be 10-13 months (i.e. stages 1-3 combined).

| Stage | Existing Estimate | Estimate from Lefkovitch Matrix | Variance |
|-------------------------------|----------------------|---------------------------------|-----------|
| Egg | 20-35 days | NA | NA |
| Larval | 28-56 days | NA | NA |
| 1: Immature | No existing estimate | 2.699666 | 4.5885318 |
| 2: Incipient Maturity | No existing estimate | 1.474724 | 0.7000867 |
| 3: Mature | No existing estimate | 1.646790 | 1.0651277 |
| 4: Fully Mature | No existing estimate | 1.494651 | 0.7393301 |
| 5: Post Laying | 45-61 days | NA | NA |
| Post larval Phase (stage 1-5) | 9-18 months | NA | NA |

$_{\scriptscriptstyle 94}$ 4 RESULTS

The resulting eigenvalue of our matrix was 0.982, indicating a population decline of 1.8% per month with fishing pressure included (Figure 3). The stable stage distribution (Table 2) shows that 65% of the makeup 196 of this population is immature individuals, while actively breeding individuals (fully mature) only make up less than 1% of the naturally occurring population. However, the reproductive output per stage (Table 2) 198 shows that on average, an individual in this fully mature population is expected to have 41 times the number of offspring as those in stage 1. Larval survivability of 0.0001328 was calculated by dividing our estimated 200 number of larvae surviving back to stage 1 (F_4) by 201,000 - the average estimated reproductive output of O. 201 cyanea by (Guard 2009). The life expectancy of this population was calculated by the Rage package to be 202 4.06 months with a variance of 5.87 months. The calculated age of maturity is 6.82 months with probability 203 of reaching maturation of 0.022. The longevity of this population (the amount of months for only 1\% of the 204 population to remain) is 12 months with a generation time of 7.38 months. 205

Changing the survivability of each stage (Figure 4) showed that immature individuals (Stage 1) would need
the smallest amount (5%) of survival increase in order to result in overall population growth. Stage 4, on
the other hand, would require a survivability increase of 25% in order to create a viable population.

Our analysis of different closure scenarios (Figure 5) indicates closures two months in length or shorter will
be ineffective in ensuring a stable population, regardless of how much these closures decreased the death rate
of the species. Further, as our baseline growth rate was close to stable (-0.0184), it took a maximum of a
7.5% increase in the survivability of the population to ensure a sustainable population when utilizing three
month closures. This analysis (Figure 5) provides all the possible combinations of increased survival rates
and frequency of closures that will result in a stable population. Suggested changes in overall survivability

range from 2-7.5%, and the ranges of frequencies of closures span from permanent closure (every month) to once every three months.

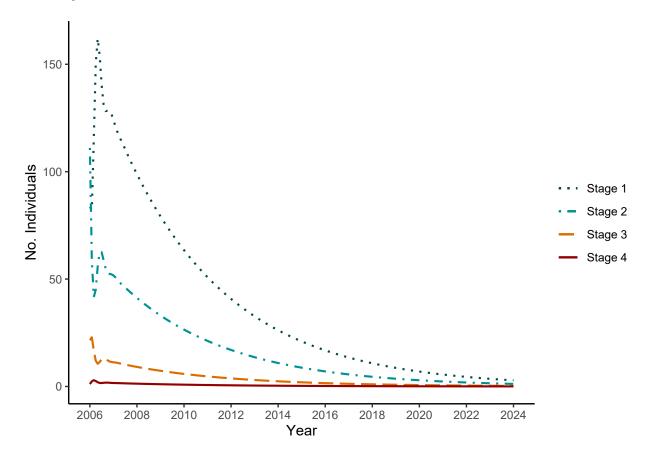


Figure 3: Projection of *O. cyanea* population based off of our calculated Lefkovitch matrix through the present.

5 DISCUSSION

Our calculated growth rate of -0.0184 and resulting population projection supports previous reports of overfishing (Humber et al. 2006; Benbow et al. 2014). Decline in population presents an economical issue for individual fishers as their catch will become less lucrative and a recovery of this population will also result in economic gains from fishers in this community (Humber et al. 2006; Benbow et al. 2014; Oliver et al. 2015). Our model provides other information about the life history of this population as well, beyond its overall growth rate. As each column in the matrix represents a proportion of individuals within a stage either growing or staying within a stage (with the exception of the F_4 parameter), it also shows a per-stage survivability estimate (Table 2) and stage duration (Table 1), life history parameters on which there has been no previous research. However, as the immature stage has a high survivability of 90.4% and a longer

Table 2: Stable stage distribution and reproductive value of each stage of this blue octopus population matrix given in Figure 2. The survivability (i.e. the proportion of individuals who survive from stage i to stage i+1) in each stage includes death rate from fishing. Stages 1-4 survivability were calculated by summing up the proportion of individuals surviving and staying within a stage every month (P_i) and the proportion of individuals surviving and growing every month (G_i) . Larval survivability of 0.0001328 was calculated by dividing our estimated number of larvae surviving back to stage 1 (F_4) by the average estimated reproductive output of O. cyanea.

| Stage | Stable Stage Distribution (Dominant Eigenvector) | Reproductive Value (Left Eigenvector) | Survivability |
|----------------------|---|--|---------------|
| 1 Immature | 0.657 | 1.000 | 0.9048003 |
| 2 Incipient Maturity | 0.274 | 1.279 | 0.4519657 |
| 3 Mature | 0.061 | 6.491 | 0.4859363 |
| 4 Fully Mature | 0.009 | 41.029 | 0.3309474 |

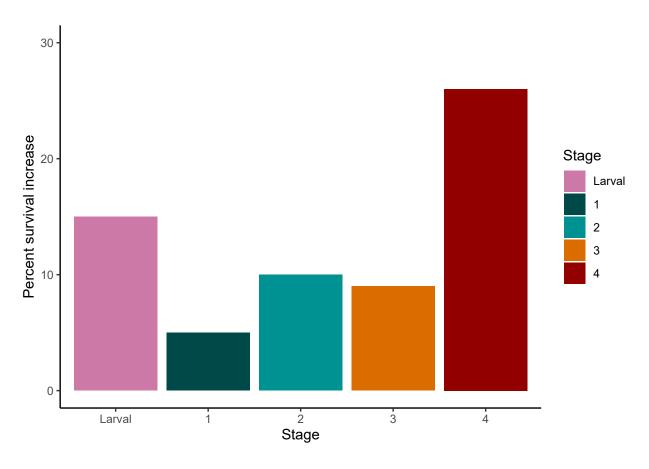


Figure 4: Minimum percent of per-stage survivability change needed to create population increase. Each stage was increased by higher percentages until the eigenvalue of the overall system became greater than zero.

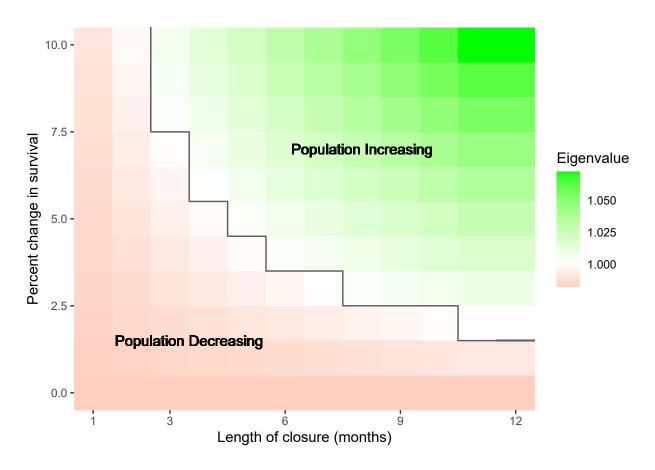


Figure 5: Analysis of different management scenarios. The black line separates the scenarios that succeed in sustaining the population from the scenarios that don't. Green and white squares indicate theoretically successful management scenarios where red refers to the strategies that will not result in overall population growth.

duration than the other stages of 2.7 months, this could indicate that although the fishing method employed 227 in this region does not distinguish by octopus size, fishers may not be bringing this smaller catch to landing due to size limits preventing them from selling immature individuals (Humber et al. 2006). Therefore, this 229 challenges our assumption of the data being properly stratified by size. Further, as O. Cyanea have an approximately one to two month larval stage (Guard and Mgaya 2003), the fecundity parameter does not 231 indicate the overall reproductive output of mature individuals, but the number of hatched offspring that will survive its larval stage and back the immature stage. This gives an estimation for larval survivability as 233 female octopus have a fecundity ranging between 27,000 and 375,000 eggs (Guard 2009), our model indicates 234 that only an average of 26.7 individuals will survive back into immaturity, which indicates a survivability 235 of 0.0001328. There is no other larval survivability estimation that currently exists for this species, which 236 would be a useful further study as this could indicate a recruitment rate for this population. Further, an 237 average lifespan of 4.06 months and an age of maturation of 6.82 months indicates that most individuals die 238 before reaching maturation.

Based on our calculations of growth rate over different closure scenarios, any closure less than three months 240 will not be effective in preserving blue octopus stocks, but the strictness of the closure (i.e. allowing some 241 limited fishing) can be altered depending on how frequently these restricted fishing periods are implemented. There is no literature on the survivability of O. cyanea throughout their lifetime, particularly in this region. 243 Therefore, the changes to survivability suggested by our analysis is in relation to their overall death rate not fishing rate, indicating a need for further research on the natural mortality rate of O. cyanea before 245 concluding if the three month closure is effective in sustaining fish stocks. Three month closures began to be implemented in the region in 2011 as this length of time was shown to improve octopus yield and had 247 limited negative effects on fisher income (Benbow and Harris 2011). As we don't have a current assessment of 248 Octopus cyanea stocks in this fishery, this indicates a need to understand how effective these closures are in 249 preserving the blue octopus of this region. Our analysis of different closure scenarios suggests a range of the 250 simplest actions needed in order to ensure stability of this population. As all combinations of survivability 251 increase and frequency of closure suggested by the analysis will result in stable O. cyanea populations, the 252 specific strategy chosen should be decided based on which is most convenient and economically feasible to the 253 local fisher community of southwest Madagascar. Among conservationists, there is a growing understanding 254 that decision making is best left to those directly involved with resource extraction and implementing fishing 255 restrictions upon a community without understanding their cultural practices can have detrimental effects 256 upon the community, as well as be less effective in actually protecting natural resources (Humber et al. 2006; 257 Baker-Médard 2017).

When implemented deliberately, establishing periodic closures is an effective and commonly-used strategy in sustainable fishing practices (Humber et al. 2006; Oliver et al. 2015). As Madagascar has been committed to protecting its marine natural resources through increasing the number of marine parks, this study serves 261 to highlight some of the available strategies to make population predictions and conservation strategies with limited data sources (Westlund 2017). Implementing fishing restrictions without regard for social norms 263 can undermine cultural practices and in turn be detrimental to both the people and fishery, and halts the dissemination of traditional ecological knowledge (Okafor-Yarwood et al. 2022). For this reason, both 265 the Madagascar government and scientific community has found a new emphasis on studying the complex 266 social structures within the community in question in order to more effectively preserve resources along with 267 peoples' livelihoods (Billé and Mermet 2002; Baker-Médard, Gantt, and White 2021). This has been shown 268 to increase participation in conservation practices, therefore making them more effective.

The mechanistic methods used in this study allowed us to gain a baseline understanding of the growth rate 270 and mortality of this population despite the limited data used to parameterize the model. Limitations of this 271 study include the data collection process. Even though daily collections occurred daily within a two-hour 272 window, catch was not standardized by effort and therefore there could be catch fluctuations between months 273 that are not captured in the data. As stage 1 had a high survival rate yet low duration, this challenges the assumption that the octopus caught are an accurate ratio of the octopus at each stage in the wild. Further, 275 matrix population models will converge or diverge based on their dominant eigenvalue, regardless of the initial population inputted in the model. Therefore, we can still conclude that the population at this time 277 was in an overall decline, despite not knowing the exact number of individuals in this population. Another shortcoming of this study is that the only available stage data for this species and region was collected in 279 2006, and the community of southwest Madagascar has implemented several strategies since that time to 280 improve the sustainability of their fish stocks in the region (Humber et al. 2006; Raberinary and Benbow 281 2012). Due to the time of data collection, this study does not reflect the current status of Octopus cyanea, but 282 outlines the underlying population dynamics and serves to indicate the need for a more current assessment 283 of *O. cyanea* stocks in the region. 284

Finally, as we are using a Lefkovitch matrix to simulate population fluctuations, these models inherently
make simplifying assumptions about the biology of the study species. For example, these models assume
that all individuals within a stage are subject to the same growth and mortality rates. As this study uses
data collected from a large geographic range (Raberinary and Benbow 2012), different individuals nesting in
different regions may be subject to different selective pressures. Further, this population of blue octopus has
been shown to exhibit spatial variability depending on their life stage. Younger individuals tend to live in the

shallow inner zone of the reef and larger individuals, who are more able to withstand stronger currents, move to deeper waters for more suitable habitats for nesting (Raberinary 2007). Despite these limitations, the data provided is the best data available for fitting a Lefkovitch matrix to this species. Future extensions of this 293 work could include exploring the dynamics of both sexes in the population (Gerber and White 2014) as male octopus have different growth rates and spatial dynamics (Heukelem 1976). Further, a better understanding 295 of the seasonal breeding dynamics of this population of blue octopus could give better insight into the health of this fishery (White and Hastings 2020). Cephalopod juveniles (a key life stage in understanding future 297 population dynamics) often have two seasonal peaks per year, indicating biannual spawning periods (Humber 298 et al. 2006; Katsanevakis and Verriopoulos 2006). This is related to seasonal fluctuations in temperature. 299 as cephalopod growth is related to environmental temperature (Domain, Jouffre, and Caverivière 2000). 300 However, this relationship is subject to a lot of variation (Heukelem 1976; Herwig et al. 2012). Further, as Madagascar is a tropical climate, this trend may be different in our region of study, as suggested by 302 Raberinary and Benbow (2012), where all life stages of O. cyanea were observed year round, suggesting continuous breeding. 304

With a short generation time, cephalopod species respond more quickly to new management strategies. 305 Future work on other fished species in the region is necessary to understand the effectiveness of temporary closures. This study also highlights the need for further research into the life history patterns of Octopus 307 cyanea. Specifically, studies on the natural mortality rate of this species, both in the larval and benthic stages, could better inform both our model and the greater understanding of how populations of this species 309 grow. Further, a more contemporary study on the status of the octopus fishery of southwest Madagascar 310 will paint a more accurate picture of how this population is faring under the current fishing pressure. These 311 studies can also be used to build off of this one as more in depth data collection could be used to add spatial 312 variability to our model, where we then can evaluate the accuracy of the assumption that every individual 313 within a stage is subject to the same selective pressure. Finally, as the people of southwestern Madagascar 314 are actively taking steps to preserve the health of their fisheries, we hope that studies such as these can serve 315 to facilitate informed decision making when choosing how and when to impose fishing restrictions. 316

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Data Availability - All supplemental material and code for this project are available at https://github.com/
swulfing/OCyanea. All data used to parameterize this model was collected in Raberinary and Benbow (2012)

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CHAPTER II: Social-ecological models with social hierarchy and space applied to small scale fisheries

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$_{\scriptscriptstyle 1}$ 1 ABSTRACT

- Socio-ecological models combine ecological systems with human social dynamics in order to better understand human interaction with the environment. One such model of human behavior is replicator dynamics. Replicator dynamics are derived from evolutionary game theory and model how societal influence and financial costs can change opinions about resource extraction. Previous research on replicator dynamics have shown how evolving opinions on conservation can change how humans interact with their environment and therefore change population dynamics of the harvested species. However, these models have all assumed that human societies are homogeneous with no social structure. Using co-managed fisheries as a case study, we develop a two-patch socio-ecological model with social hierarchy in order to study the effect that social inequity has on decision making. We also analyzed the spatial components of this two-patch model and 10 observed the effect of fish movement on decision making and fish population dynamics. We found that, contrary to our hypothesis, social influences became less significant in our two patch model. Instead, we found 12 that fish movement across patches was a major driver of changes to population dynamics. This indicates the 13 importance of including spatial components to socio-ecological models. Further, this study highlights the 14 importance of understanding species movements when making conservation decisions. 15
- ¹⁶ Keywords: two-patch model, replicator dynamics, social hierarchy, socio-ecological model, species movement

$_{\scriptscriptstyle 17}$ 2 INTRODUCTION

The study of social ecological models is a growing field in ecology as they treat human behavior as a variable as opposed to a set parameter. This allows for the study of how human decision making can change in response to environmental factors and in turn, change how humans interact with resources and profits (Bauch 2005; Innes, Anand, and Bauch 2013; Oraby, Thampi, and Bauch 2014; Bauch et al. 2016; Sigdel, Anand, and Bauch 2017; Thampi, Anand, and Bauch 2018). As human societies grow increasingly intricate and interconnected, these models can help us to analyze how our social structures can influence the environment around us (Liu et al. 2007). These models provide important insight not only into how human decision making can influence ecological patterns but it can also show hidden processes, reveal regime shifts that would otherwise be hidden, and identify vulnerabilities of systems that don't exist within the purely social or ecological models (Liu et al. 2007; Young et al. 2007; Lade et al. 2013). Socio-ecological models have even showed different dynamics at different scales and different amounts of human connectivity (Cumming, Morrison, and Hughes 2017). They can also be used in systems where data is difficult to collect.

as parameters can be changed in order to analyze different hypothetical scenarios. Socio-ecological models
can also inform effective policy decisions. Conservation plans often do not reach their conservation goals,
and these setbacks are often attributed to a lack of stakeholder participation (Crona and Bodin 2006; Salas,
Barragán-Paladines, and Chuenpagdee 2019; Prince et al. 2021). This can be due to an emergence of conflict
for stakeholders, where the conservation plan in place directly hinders their practices, therefore deterring
them from participating in the restorative efforts. Socio-ecological models can identify where these areas
of potential conflict can arise, compromises that can be made in the system, and alternative conservation
practices that encourages participation from all stakeholder groups (Ban et al. 2013). Further, as these
models are simulations of human and environmental interactions, they allow flexibility in that they can be
adapted to fit the specific system of study and improve place-based management practices (Young et al.
2007; Liu et al. 2007; Felipe-Lucia et al. 2022)

Due to their adaptability, socio-ecological models can use a wide range of strategies to represent human decision making. One such method is replicator dynamics, which model human decision making where an individual makes conservation choices based on weighing the perceived benefits of conservation with the costs, as well as the social pressure to conform to the group's stance on conservation. Individuals will therefore "replicate" the behavior of their peers by changing their harvest practices based on the opinion of the majority (Bauch and Bhattacharyya 2012). They have been used to show how social learning is a key component to vaccination uptake public health, and preexisting social norms can actually suppress vaccine uptake despite frequent disease outbreaks (Bauch and Bhattacharyya 2012; Oraby, Thampi, and Bauch 2014). They can also have conservation applications as pest invasion models have shown ways to simultaneously mitigate pest outbreaks and the cost to address them in the timber industry (Barlow et al. 2014). Further, land use changes have been modeled to have completely different dynamics when human decision making was added to these models (Innes, Anand, and Bauch 2013). However, all previous models of human behavior have assumed that human societies are homogeneous, and all people are subject to the same social influence and 53 ecological dynamics. No replicator-dynamics model has incorporated social inequality or hierarchy, despite the fact the most human societies have varying levels of social influence within them.

Contrary to this assumption made by previous models that human groups are homogeneous, the vast majority of real-world societies exhibit some form of hierarchy or inequality. Societies with different social subgroups can often exhibit an "us vs. them" mentality and compete for resources (Borgatti 2003). This is because social status can greatly alter peoples' interaction with the environment. Competition over resources has been shown to be exacerbated by social hierarchies and 'top-down' regulation whereas when social connectivity is considered in management plans, this can not only improve management outcomes, but reduce costs as well

(Krackhardt and Stern 1988; Grafton 2005; Bodin and Crona 2009). Further, members of social networks have been shown to have varying levels of connectivity with others based on attributes such as ethnicity, and this can in turn alter an individual's relationship with the environment and their views on conservation (Barnes-Mauthe 2013; Sari et al. 2021). Barnes-Mauthe (2013) also showed that fishing communities can exhibit homophily, which is the tendency for people to obtain information and opinions from those who are similar to themselves before seeking views from those who are perceived as different. Therefore, people in different social groups may be receiving different information and opinions about conservation and acting accordingly (McPherson, Smith-Lovin, and Cook 2001). For example in Kenya, communication among fishers has been shown to stay within groups using the same gear type which has inhibited successful regulation of the whole fishery (Crona and Bodin 2006). Further, in the southwest Madagascar octopus fishery, fishing 71 method and location typically falls along gendered lines. When fishing restrictions were imposed on tidal flats, this affected fishing access for women while maintaining this livelihood for male fishers, who typically fished in deeper waters (Baker-Médard 2017). In Thailand, ethnicity has been shown to be a source of fishing conflict which has exacerbated resource depletion (Pomeroy et al. 2007). The existence of social structures is extremely prevalent in human societies and this has been shown to alter how people interact with the environment. However, there has been no previous replicator dynamics study that considers how social hierarchies alters harvest practices.

Small scale fisheries are a particularly relevant system to apply replicator dynamics as fishing practices and policies are often made by communal decision makers. Research on small-scale fisheries is a growing and essential field as they are drastically understudied yet affect many people around the globe. Worldwide, about 32 million fishers make their livelihood in small-scale fisheries, a subsector in which 90 to 95% of fish is distributed for local consumption. These marine products are a vital source of nutrition for these communities ("Hidden Harvest-The Global Contribution of Capture Fisheries" 2012). Due to tight social structures, community decision making, and strong reliance on the environment, small scale fisheries are systems that are well represented by socio ecological models and replicator dynamics (Grafton 2005; Thampi, Anand, and Bauch 2018; Barnes et al. 2019). Conservation efforts in small scale fisheries have often been unsuccessful, especially when the social and economic components of the industry have been ignored (Salas, Barragán-Paladines, and Chuenpagdee 2019; Prince et al. 2021). However, even when human interactions and decision making have been considered, socio-ecological models have often treated individuals in human societies homogeneous. As human societies are often complex and hierarchical, this simplifying assumption that everyone interacts with the environment and within their community equally can lead to lack of participation in conservation by some groups within a community (Barnes-Mauthe 2013; Cumming, Morrison, and Hughes

2017). Mismanagement of fisheries have even been shown to exacerbate these inequalities (Cinner et al. 2012;
Baker-Médard 2017). Further, the specific dynamics of the fishery in question have been shown to be an

important component to models, as models with multiple patches can actually mitigate overfishing if there

97 is a high migratory ability of the harvested species (Cressman, Křivan, and Garay 2004).

Instituting effective conservation strategies can be especially difficult if the organism being protected has a migratory pattern that crosses over multiple management jurisdictions such as country borders (Ogburn et al. 2017; Garrone-Neto et al. 2018; Ramírez-Valdez et al. 2021). Borders can also create challenges when gathering population data that requires extensive fieldwork (Cozzi et al. 2020; Hebblewhite and Whittington 101 2020). The fragmentation of management can also result in a mismatch of conservation strategies that become ineffective when these management bodies do not coordinate efforts (Siddons, Pegg, and Klein 103 2017). Research on the importance of coordinated research efforts has been conducted on many species 104 of terrestrial animals with large migratory ranges and have consistently shown that cooperation among 105 government bodies is essential to protecting population health of highly migratory species or species whose 106 native ranges expand across multiple countries (Plumptre et al. 2007; Gervasi et al. 2015; Meisingset et al. 107 2018). Because fish are generally highly migratory, this issue is especially relevant in international waters 108 or waters where different government bodies share jurisdiction (Mchich, Auger, and Raïssi 2000). For this reason, research on two patch fishing models is a commonly used method as different management strategies 110 can be modeled in each patch. Previous research on two-patch fishing models has shown that movement rates between patches can effect population stability when there is different fishing pressures in each patch 112 (Mchich, Auger, and Raïssi 2000; Cai, Li, and Song 2008). Economic output can also be maximized in multipatch fishing models as high dispersal can result in a higher overall yield of the system than the yield of each 114 patch combined (Auger, Kooi, and Moussaoui 2022). High dispersal across patches is commonly found to 115 be an essential component to maximizing population health and economic gain from fishing (Freedman and 116 Waltman 1977; Moeller and Neubert 2015; Auger, Kooi, and Moussaoui 2022). Two patch models help us 117 to understand better the population dynamics of fish species who face different pressures in each patch and 118 have even resolved conflicts between fishing groups (Mchich, Auger, and Raïssi 2000). However, no previous 119 research has combined two patch fishing models with a hierarchical human decision making model in order to study how space and social dynamics affect fishery dynamics. 121

In this study, we couple a human-decision replicator dynamics model with social hierarchies with a two-patch fishing model in order to understand how decision making is affected by spatial and hierarchical factors. The objectives of this study are: 1) to compare the output of this model with that of previous replicator dynamics studies without spatial or social hierarchical components, 2) Find the effects of social hierarchies in decision

making and how that effects fishing dynamics 3) determine the significance of fish dispersal in our two patch model. We hypothesize that higher cooperation between groups will benefit fish stocks overall and that increased fish movement will increase the health of fish populations.

3 METHODS

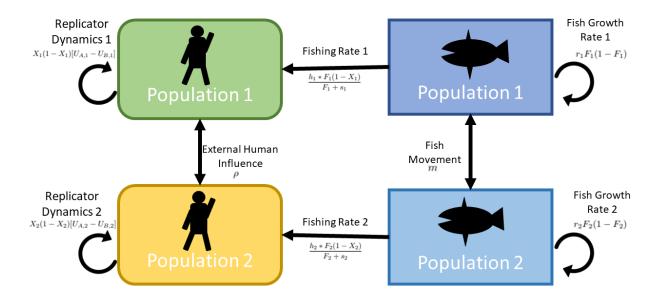


Figure 1: A conceptual representation of our model as a two-patch extension of Bauch et al. (2016). Here, each fish population (F_i) in each patch i increase through natural growth and movement of fish into the patch. Fish populations are decreased through emigration out of the patch and human fishing activity. The number of fishers (X_i) in each patch i change in response to fish population levels, the cost of stopping fishing activity, and the opinions of those in the patch and those in the other.

3.1 Model Construction

We build on the work of Bauch et al. (2016) by extending their approach to a two-patch model (Figure 1).

The fish population models are as follows:

$$\frac{dF_i}{dt} = r_i F_i (1 - F_i) - \frac{h_i * F_i}{F_i + s_i} - m_j F_i + m_i F_j \tag{1}$$

Where the change in fish populations is dependent on r_i , the net population growth of each patch i, and

both populations follow logistic growth. The second term: $\frac{h_i * F_i}{F_i + s_i}$, denotes fish lost to human activity. h_i is
the harvesting efficiency of the respective human population and s_i controls the supply and demand of the
fishery. Because we are now working with a two-patch model, the m_i parameter denotes the movement of
fish out of patch i and into patch j. In this study, we are assuming a closed population between the two
patches. Therefore, fish move directly from patch to patch and do not disperse elsewhere.

For the model of human activity and opinion, we used replicator dynamics from evolutionary game theory 139 to simulate societal influence on an individual's opinion. Social dynamics are represented by the proportion of conservationists in a population (X) and the proportion of harvesters (1-X). These two groups interact 141 with one another using the term (X)(1-X) which simulates individuals "sampling" other individuals in the population. If one opinion dominates in the population (i.e. X >> (1 - X) or (1 - X) >> X), the rate of 143 changing opinions will be slow as the power of societal pressure makes it challenging for the other opinion to gain traction. However, if X and (1-X) are close, the rate of change in opinion will be high as society has 145 a split opinion on conservation versus harvest. In this model, each person holds an opinion (conservation or harvest) by weighing the benefits of conservation (U_A) against the benefits of harvest (U_B) . This gives the 147 replicator equation: 148

$$\frac{dX_i}{dt} = k_i X_i (1 - X_i) [U_{A,i} - U_{B,i}]$$
 (2)

$$\frac{dX_i}{dt} = k_i X_i (1 - X_i) [\Delta U_i] \tag{3}$$

Where k_i refers to the rate of interaction within a group. As individuals "sample" the opinions of others in their group, they can switch from A to B if $U_B > U_A$ and vice versa. In our model, we adapt U_A from Bauch et al. (2016) with the added influence of the other population's opinion. U_A is therefore given by:

$$U_{A,i} = \frac{1}{(F_i + c_i)} + d_i X_i + \rho_i X_j \tag{4}$$

Where $\frac{1}{(F_i+c_i)}$ represents the perceived rarity of fish populations within a patch. As F_i and c_i (the rarity valuation parameter) decrease, this term will increase, therefore adding to the perceived benefit of protecting fish populations. d_i refers to the social influence that each population has on itself, and as an individual encounters a conservationist (X_i) , the social benefit of also being a conservationist is shown in d_i . ρ_i has this similar effect, but denotes the social effect of the opposite population on decision making (X_j) . Individuals

in each population i are receiving information about the conservation practices of the other population j, and the influence that this has on each population is encapsulated by ρ_i .

 U_B (the perceived benefits of harvest) is:

$$U_{B,i} = \omega_i + d_i(1 - X_i) + \rho_i(1 - X_j) \tag{5}$$

Where ω_i is the cost of conservation (i.e. revenue lost by not fishing) where now, d_i is the within-population social benefit of switching to harvesting $(1 - X_i)$ and ρ_i is the other population's $(1 - X_j)$ ability to change the opinion of an individual to be a harvester.

Plugging equations (4) and (5) into equation (2) gives:

$$\frac{dX_1}{dt} = k_1 X_1 (1 - X_1) \left[\frac{1}{F_1 + c_1} - \omega_1 + d_1 (2X_1 - 1) + \rho_1 (2X_2 - 1) \right]$$
 (6)

$$\frac{dX_2}{dt} = k_2 X_2 (1 - X_2) \left[\frac{1}{F_2 + c_2} - \omega_2 + d_2 (2X_2 - 1) + \rho_2 (2X_1 - 1) \right]$$
 (7)

Where specifics of the derivation are outlined in the supplementary material. Coupling the fish population and human opinion models gives:

$$\frac{dF_1}{dt} = r_1 F_1 (1 - F_1) - \frac{h_1 * F_1 (1 - X_1)}{F_1 + s_1} - m_2 F_1 + m_1 F_2 \tag{8}$$

$$\frac{dF_2}{dt} = r_2 F_2 (1 - F_2) - \frac{h_2 * F_2 (1 - X_2)}{F_2 + s_2} - m_1 F_2 + m_2 F_1 \tag{9}$$

$$\frac{dX_1}{dt} = k_1 X_1 (1 - X_1) \left[\frac{1}{F_1 + c_1} - \omega_1 + d_1 (2X_1 - 1) + \rho_1 (2X_2 - 1) \right]$$
(10)

$$\frac{dX_2}{dt} = k_2 X_2 (1 - X_2) \left[\frac{1}{F_2 + c_2} - \omega_2 + d_2 (2X_2 - 1) + \rho_2 (2X_1 - 1) \right]$$
(11)

Where the fishing pressure is now a function of the number of harvesters in a population $(\frac{h_i F_i(1-X_i)}{F_i+s_i})$.

Further, the opinion of each population will shift based on the perceived fish stock health of their respective patch weighed against the costs and benefits of conservation. As fish stocks decrease, individuals will sway

more toward conservation, thereby relieving this fishing pressure. However, we now have an external influence in this model: the opinions of people in population j. The strength of this external influence is ρ , and in this study, we plan to simulate inequalities in human societies with this parameter.

Table 1: "Parameter values used to simulate sustainable fishing practices in patch 1 and overfishing in patch 2"

| Parameter | Population 1 | Population 2 | Definition |
|-----------|--------------|--------------|-------------------------------------|
| r | 0.4 | 0.35 | Fish net growth |
| s | 0.8 | 0.8 | Supply and demand |
| h | 0.25 | 0.5 | Harvesting efficiency |
| k | 1.014 | 1.014 | Social learning rate |
| ω | 0.2 | 0.35 | Conservation cost |
| c | 1.5 | 1.5 | Rarity valuation |
| d | 0.5 | 0.5 | Social norm strength (within pop) |
| m | 0.2 | 0.2 | Fish movement (from opposite patch) |
| ho | 0.5 | 0.1 | Social norm strength (opposite pop) |

3.2 Fish Parameters

For our basic analysis, we chose to model a two-patch fishery where the harvested fish species has a midrange growth rate and regularly diffuses across the two patches, such as the parrot fish modeled in Thampi,
Anand, and Bauch (2018). From the human side, the two groups of fishers have the same social influence on
one another, representing a non-hierarchical social structure. The default fish growth rate of both patches is
0.35 fish per year. For the harvesting efficiency, we chose a maximal fishing rate of 0.5. These numbers were
adapted from a coral reef fishing model Thampi, Anand, and Bauch (2018) where r = 0.35 and h = 0.5 are
the mid-level growth rate and max fishing rates analyzed by this paper. For the movement parameters m,
we chose 0.2 for each as these are the values used in the two-patch fishing model described in Cai, Li, and
Song (2008). We used the s parameter described in the Bauch et al. (2016) model of s = 0.8.

3.3 Human Parameters

The rate at which humans interact with one another is described by the parameter k. In our default model, we used k=1.014 as adapted from the Thampi, Anand, and Bauch (2018) default model. We used the default rarity valuation parameter c from Thampi, Anand, and Bauch (2018) where c=1.68. The cost of conservation default parameter is $\omega=0.35$ from Bauch et al. (2016). Further, as our default model will have no human social hierarchy, we set $d=\rho=0.5$ for our social learning rate as adapted from Bauch et al. (2016) which models social decision making regarding deforestation.

Based off of this default model, we then changed parameters such that patch 1 is fished sustainably, and patch 2 is overfished (Table 1). Further, we added a social hierarchical component where patch 2 has a higher social influence on patch 1.

192 3.4 Analyses

First, we compared the model from Bauch et al. (2016) to that of our model by setting our parameters $m_1 = m_2 = \rho_1 = \rho_2 = 0$ and comparing the results. We then ran different simulations of this model with different parameterizations in order to understand how fish population dynamics are affected by 2-patch socio-ecological models with social hierarchy. Next, we incrementally increased the parameters m and ρ and simulated this system for 100 years in order to assess how increasing each new parameter would affect the overall dynamics of the system. Sensitivity analysis was conducted with the R package FME on these parameters (Soetaert and Petzoldt 2010). Finally, we created parameter planes of each pair of variables in order to assess how altering two parameters at a time would affect the system.

$_{201}$ 4 RESULTS

4.1 Model Comparisons

We first compared the output of our model to that of Bauch et al. (2016) in order to see how the addition
of social hierarchy and two-patch fishing affects the replicator dynamics of a fishery. We found that, while
the model in Bauch et al. (2016) had multiple states where oscillations occurred (Figure 2 a), there were no
scenarios with our model in which we tested that resulted in oscillatory behavior (Figure 2 b).

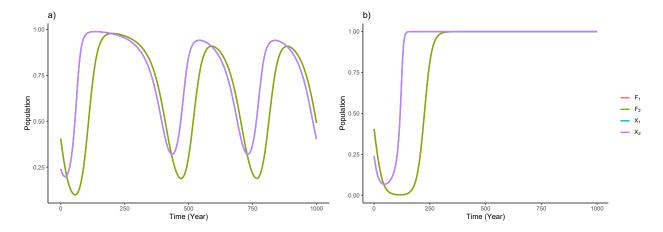


Figure 2: a) Oscillatory behavior of the model in Bauch et al. (2016) where r = 0.06, s = 0.8, h = 0.1, k = 0.17, $\omega = 1$, c = 0.6, d = 0.3. This is compared to our model, b) which used the same parameter values with the addition of m = 0.2, $\rho = 0.3$.

4.2 Model Analysis

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We then modeled a hypothetical scenario where patch 1 is fished sustainably whereas patch 2 is experiencing overfishing and has a higher social sway than patch 1 (Table 1). Here, the unsustainable practices of human population 2 are so exploitative, that both fish populations eventually collapse (Figure 3). We used this parameterization for the rest of the analysis, however the conclusions from each analyses are consistent with the other parameterizations we tested.

Next, we ran our model with incrementally higher ρ values in both populations and observed how this affected the final population of each fish patch (Figure 4). We found that under different parameterizations, ρ rarely had an effect on the final fish populations. However, there were some instances where ρ acted as a tipping point for population dynamics where instead of continuously changing the final fish populations, the ρ parameter either resulted in stable fish populations or both stocks collapsed once ρ increased past this point.

We then ran the same analysis with the fish dispersal parameter, m. Contrary to the effect ρ had on the model, dispersal had a more direct and continuous effect on the final population of fish in each patch. For example, as fish movement from patch 2 to patch 1 increased (i.e. from the unsustainable patch to the sustainable patch), this actually maintained low fish populations in both patches (Figure 5 a). However, if the fish movement was increased from patch 1 to patch 2 (from the sustainable fishing to unsustainable), both patches eventually collapsed to zero (Figure 5 b).

We then conducted sensitivity analysis on the m and ρ parameters to confirm the conclusions from the previous two analyses and further test if the fish diffusion parameter has a higher influence on fish population

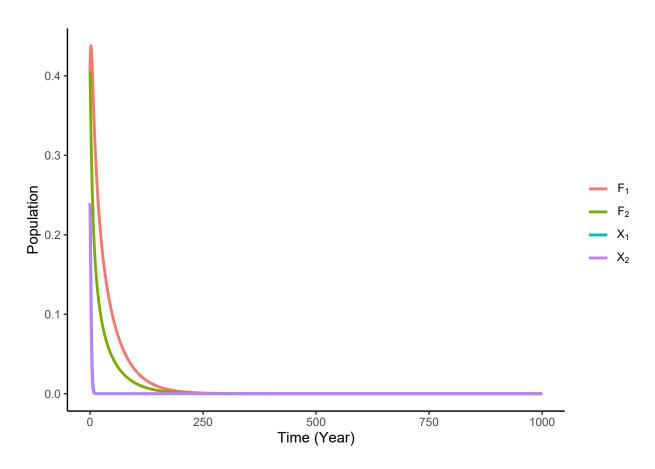


Figure 3: Representation of dynamics with parameters from table 1

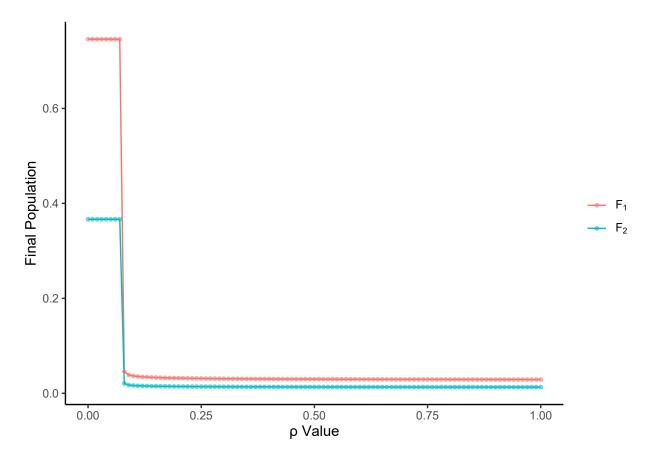


Figure 4: Final fish populations after 100 years in the two patch fishing model where patch 1 is fished sustainably but human population 1 has a lower social influence than patch 2, which is being fished unsustainably. Both ρ_1 and ρ_2 were increased simultaneously.

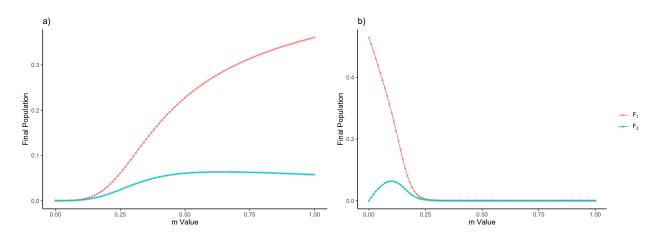


Figure 5: Final fish populations after 100 years in the two patch fishing model where patch 1 is fished sustainably but human population 1 has a lower social influence than patch 2, which is being fished unsustainably. a) shows how increases in m_1 affect final populations and b) shows how increases in m_2 affect final populations.

dynamics than the outside social influence parameter (Table 2). We used the R package FME (Soetaert and Petzoldt 2010) and found that F_1 and F_2 dynamics are consistently more sensitive to perturbations in the m parameter than to perturbations in the ρ parameter. This table shows the L1 sensitivity as it is less sensitive to outliers, however all measures of sensitivity taken showed that the F_1 and F_2 variables are more sensitive to the m parameters than the ρ .

Table 2: L1 Sensitivity analysis of the m and ρ parameters on F_1 and F_2 variables

| Sensitivity |
|-------------|
| 0.0072569 |
| 0.0072569 |
| 0.0010693 |
| 0.0010693 |
| |

Finally, to confirm that ρ has a small effect on the overall dynamics of the fish population model, we generated a series of parameter planes, which show how dynamics change based on variations of two different parameters (Figure 6). Each axis represents a new value for parameter and then the final dynamics of the system were analyzed. If the final fish population was greater than .2, this was considered stable whereas below .2 was considered population collapse (Pinsky et al. 2011). The corresponding color in the graph represents how each patch fared after 100 years under each parameter combination. The result of this analysis showed that ρ had little direct effect on the final fish population's sustainability.

5 DISCUSSION

We extended previous models on replicator dynamics to two patch fishing scenarios with social hierarchy in the human population. Firstly, we compared the results of our model to previous replicator equation models such as Thampi, Anand, and Bauch (2018) and Bauch et al. (2016) (Figure 2 a). Mainly, both models found oscillations under certain parameterizations. This is in contrast to our model, where we found no scenarios that exhibit this behavior (Figure 2 b). This is likely due to the fact that the linear aspects of the fish dispersal term eventually overpowers the non-linear components of the model. Further, because of the outside human influence term, ρ_i , people are not responding directly to their respective fishing patch, but also to the conservation opinion of the other group. This indicates that the inclusion of the immigration

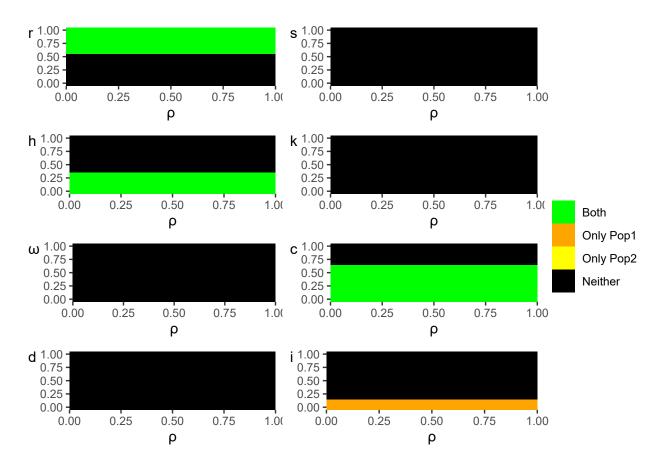


Figure 6: Parameter plans of perturbations of each parameter compared to perturbations in ρ . Each fish population was evaluated after 100 years and if the final population was under 0.2, this patch's stocks were considered to be collapsed.

term from each patch overcame the non-linear components of the model because this is a linear term that 248 had a major effect on the dynamics of the model. This shows that adding a spatial component to socioecological models can greatly change their dynamics and therefore how people are expected to act under 250 certain environmental conditions. In our model, this shows that the dispersion of fish populations must be well understood in order to institute effective conservation practices. This is also because any decision made 252 by one group of people to conserve resources may be rendered ineffective if this species is highly migratory and the other group of harvesters is using unsustainable conservation practices. Further, because of the 254 outside influences from the other human patch, fishers are no longer responding directly to fish levels in their 255 respective patch, i, but are also influenced by the number of fishers in the other patch, j. In a scenario where 256 fish is abundant in one patch, this will also encourage fishing in the other patch because this will increase 257 the incentive to fish from the outside influence parameter. Past research has exemplified how multi-patch models and the addition of spatial components have been shown to change dynamics of systems, especially in 259 fisheries (Mchich, Auger, and Raïssi 2000; Cai, Li, and Song 2008; Moeller and Neubert 2015; Auger, Kooi, and Moussaoui 2022). This highlights the importance of including spatial components to socio-ecological 261 models. 262

For the remainder of the analyses, we simulated a scenario where patch 1 was being fished sustainably and patch 2 was experiencing overfishing with social hierarchy, which resulted in the whole system experiencing 264 collapse (Table 1 and Figure 3). Next, we tested the effect of external social influence on this model and how social hierarchy in decision making would influence dynamics. Contrary to our hypothesis, this parameter 266 often had very little overall effect on the model (Figure 6). Figure 4 showed how fish population dynamics typically crashed when ρ passed a tipping point, showing that high levels of cooperation between groups actually crashed both populations of fish. Instead of modeling a cohesive system where communication 269 fostered effective conservation, we created a tragedy of the commons scenario, where each community raced 270 to fish each patch as opposed to coming to common understanding of sustainable fishing practices. This 271 is because in our model, the only information being passed on to the outside group is the general opinion 272 regarding fishing versus conservation instead of what sustainable fishing practices were used in order to 273 achieve this benefit. As a result, when one patch i is overfished and the other patch j is fished sustainably, 274 the group i will continue to overfish their own resources because the opposite patch j is encouraging this group 275 to continue fishing. Therefore, this further highlights that the content of the information being disseminated 276 matters in successful conservation (Gray et al. 2012). This confirms previous research on co-management 277 strategies in that despite the fact they are a growing method in meeting social and ecological goals in small 278 scale fisheries, they are prone to fail and groups can come to management decisions that are unsuccessful 279

(Cinner et al. 2012). This aligns with previous social-ecological research that shows that the structure of a social network should be taken into consideration when the community manages a resource (Grafton 2005; Newman and Dale 2007; Bodin et al. 2014). This is because people who interact differently with the environment or within a society have to consider different tradeoffs in conservation (Cumming, Morrison, and Hughes 2017).

Instead of social norms controlling a lot of the dynamics of this model, we found that the dispersal of fish 285 between patches was a major driver of population sustainability or collapse (Table 2). As we increased the movement of fish into the sustainable patch (Figure 5 a), this increased populations in that respective patch 287 because humans in population 1 continued to fish sustainably. Further, as those in population 2 decreased fishing rates, this influenced population 1 to also decrease their number of fishers. As a result, population 1 289 maintained high fishing levels while population 2 had low stocks. On the contrary, as fish immigrated from 290 the sustainable patch 1 to the unsustainable patch 2 (Figure 5 b), both fish populations collapsed as m₂ 291 increased. This is because fish movement from patch 1 eventually grew to be too great for human population 292 1 to fish sustainably and human population 2 continued to overfish. High migration has been shown to be 293 an essential part of maximizing economic benefit from fishing in multi-patch models (Moeller and Neubert 294 2015). Because fish are highly migratory and therefore difficult to track, constraining fishing to one group of people is more challenging (Grafton 2005). This is especially important for fish species that migrate based 296 on life stage, and requires more management coordination (Siddons, Pegg, and Klein 2017).

The decision to include the external social influence term in our model within the injunctive social norms X(1-X) implies that external influence can still change an opinion for or against conservation. However, 299 an individual's willingness to take up a new opinion is still dictated by the overall opinion of their own population. This exemplifies homophily, a concept in sociology where humans tend to take information 301 and the opinions from subgroups similar to them before listening to subgroups of different social standing (Brechwald and Prinstein 2011). Social network based conservation, like in our model, can replace 'top-303 down' regulation which can exclude stakeholders. However, this method of conservation has been shown to be susceptible to homophily (Newman and Dale 2007). Conservation has been shown to be more effective when human populations are more cohesive and that those with subgroups experience more barriers to 306 effective conservation (Bodin and Crona 2009). Solutions to this issue could be to institute some form of actor that serves as cross-group communicators (Guerrero, Mcallister, and Wilson 2015). 308

Further research on this model could look at an open system, where fish diffusion doesn't necessarily have to pass between patches and could diffuse into non-fished areas. Also, stronger social networks have been shown to be more adaptable to environmental change (Grafton 2005), therefore further studies could look at

the effect of climate change or extreme events on this social system. The specific way we chose to incorporate 312 social hierarchy into the model could be changed as well, for example testing a model that includes the outside 313 social influence outside of the X(1-X) term. There are many ways to model social systems so another 314 further application of this study would be to compare different models that incorporate social hierarchy to 315 the results of this one. Finally, further work on parameterizing this model to a real-world system could 316 help understand if this model is properly capturing the underlying dynamics of two patch fishing systems 317 with social hierarchy. Next, this model assumed that the uptake of opinions happens solely through social 318 networks and weighing costs of conservation against the benefits. In reality, there may be more factors that 319 influence one's harvesting decisions such as governing bodies or media consumption. Further research could 320 look into the other components that form decision-making. 321

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1 CONCLUSION

In these two chapters, we demonstrated how mechanistic modeling can be used to assess the status of small scale fisheries when available data is limited. In chapter 1, we were able to take monthly landing data to assess the health of the small scale blue octopus fishery in southwest Madagascar. We were also able to assess various life history traits of this species such as per-stage duration, reproductive value, survivability as well as the stable stage distribution of this population. Finally, we showed how different closure scenarios would affect this population's sustainability. We were able to infer more about the biology of this important species as well as provide various management scenarios that should be effective in preserving stocks. In chapter 2, we created a socio-ecological model where we coupled a human decision-making system with social hierarchy with a two patch fish model in order to understand how the addition of space and human inequality 10 affects fishing and fishery dynamics. We found that the fish movement parameter had a large effect on the dynamics of the system and that the parameter that symbolized the social pressure from the outside group 12 had more of a "tipping point" effect on the model where low values maintained stable fish populations but 13 once this parameter reached a certain point, the whole system crashed. This exemplified the importance of 14 fish movement when instituting conservation strategies. Further, this shows how important the content of 15 information is when collaborating with other groups to make management choices. 16 Further extensions of this work would firstly be to collect data to confirm or enhance the results of these 17 studies. For example, understanding how much fishing pressure is affecting the overall death rate of blue octopus would allow us to better understand how these closures are affecting this population. Next, spatial 19 variability could be an important factor in blue octopus dynamics so research into how space affects selective 20 pressure would provide further insight into the status of this species. As for the socio-ecological model, we conducted an exploratory analysis of the underlying dynamics of this model, but future research could parameterize this model into a real-world system. This would involve assessing the biology of the harvest 23 species in question, but also conducting user surveys about fishing perception, fishing rates, and the amount 24 of interconnectivity between people in these groups. Data collection can also produce a valuable check into the accuracy of mechanistic models. However, mechanistic models do provide insight into ecological and social dynamics and allow us to conduct hypothetical experiments that would otherwise be impossible or costly to conduct empirically.

Supplementary Material for:

Using mechanistic models to assess temporary closure strategies for small scale fisheries

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Table 1: Data collected in Raberinary and Benbow 2012.

| Τ | Stage1 | Stage2 | Stage3 | Stage4 | Total |
|----|-----------|------------|-----------|-----------|-----------|
| 1 | 10.40119 | 5.200594 | 0.000000 | 1.1144131 | 16.71620 |
| 2 | 76.52303 | 27.860327 | 2.228826 | 1.8573551 | 108.46954 |
| 3 | 57.57801 | 37.890045 | 1.857355 | 0.0000000 | 97.32541 |
| 4 | 40.49034 | 50.891531 | 3.343239 | 0.0000000 | 94.72511 |
| 5 | 71.69391 | 16.716196 | 8.172363 | 1.1144131 | 97.69688 |
| 6 | 121.09955 | 28.974740 | 5.572065 | 2.2288262 | 157.87519 |
| 7 | 119.98514 | 52.005944 | 6.686478 | 0.7429421 | 179.42051 |
| 8 | 78.75186 | 41.604755 | 14.487370 | 1.1144131 | 135.95840 |
| 9 | 118.87073 | 53.491828 | 14.487370 | 1.1144131 | 187.96434 |
| 10 | 119.98514 | 39.004458 | 10.772660 | 1.1144131 | 170.87667 |
| 11 | 73.55126 | 26.374443 | 4.457652 | 2.2288262 | 106.61218 |
| 12 | NA | NA | NA | NA | NA |
| 13 | 83.58098 | 111.069837 | 21.545320 | 1.1144131 | 217.31055 |

1 Data

- ² Table 1 shows data used to parameterize matrix model from Raberinary and Benbow (2012). Data was
- ³ extracted from Figure 7 of this paper using WebPlotDigitizer (https://automeris.io/WebPlotDigitizer/)

₄ 2 Stability and Elasticity analysis

- Sensitivity analysis (Figure 1) showed that within each stage, the growth parameters $(G_1 G_3)$ had the largest
- effect on this growthrate compared to the parameters indicating staying within a stage (P_1-P_4) . However, as
- $_{7}$ all the parameters represent proportions of individuals in a stage and must necessarily be between 0 and 1
- 8 with the exception of the F_4 parameter, elasticity analysis provides an interpretation that weights all stages
- 9 equally. The result of this analysis shows that percent changes in the fecundity metric can be as beneficial
- to the overall population growth as changes in the G parameters (Figure 2). Further, this analysis indicates
- that of all the stages, stage 1 has the most overall influence on the overall population growth.
- 12 Elasticity analysis shows that conservation of both the growth and reproductive parameters would have equal

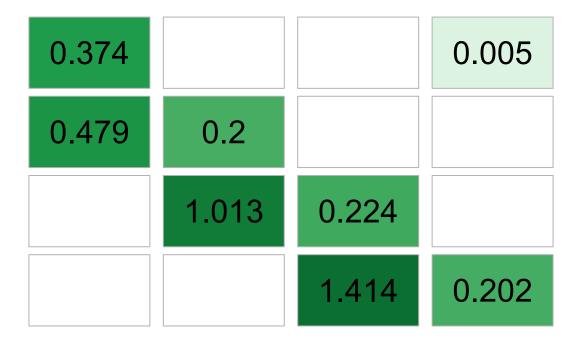


Figure 1: Sensitivity analysis of our matrix model - the change in the eigenvalue (λ) as a result of a unit change of each parameter in the model.

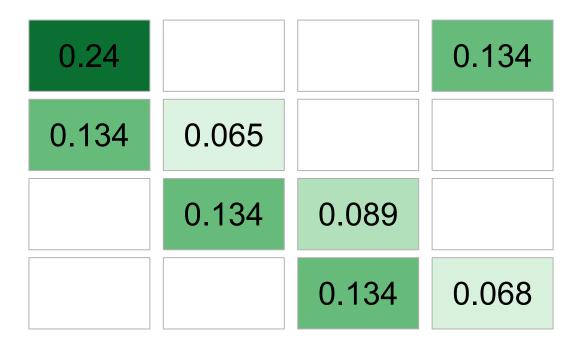


Figure 2: Elasticity analysis of our matrix model - the change in the eigenvalue (λ) as a result of a proportional change of each parameter in the model.

effect on the overall population growth, with the most influential parameter being the survival of stage 1 individuals. The sensitivity and elasticity analysis indicate which stages will have the greatest effect on the population if they are targeted for preservation practices. Previous research has indicated that catch size limits are very effective in preserving stocks of species with rapid growth and high death rates, but this is only if individuals do not enter the fishery until they have reached maturity (Nowlis 2000). However, the fishing method most commonly employed by the local people is spearfishing, where harvesters will search out octopus dens and spear the den to probe out the octopus (Benbow et al. 2014). Because of this, fishing method does not discriminate based on stage, this is not an applicable suggestion for conservation practices. For this reason, even though our analysis of different stage survivabilities indicates that conserving immature individuals would be an effective tool for fostering population growth, this is not a realistic management practice in this fishery for most harvesters.

24 3 Per-stage management scenarios

$_{\scriptscriptstyle 25}$ 3.1 METHODS

Examined how increasing the chance of survival of individuals in each stage class would contribute to population health. This was achieved by isolating the growth (G_i) and in-stage survival (P_i) for each stage i. We then increased these parameters by 1% and recalculated the overall eigenvalue of the matrix. We then incorporated into different scenarios with different frequencies of fishing restrictions to examine how temporary closures on blue octopus in certain stages would affect the population.

31 3.2 RESULTS

Our within stage analysis showed that Stage 1 needed the smallest percent increase in survival to result in overall population growth (Figure 3). Stage 4 and larval survivability would be the highest needed increase, with stage 4 needing a 25% increase and larval needing a 15% increase in order for the overall population to be stable. Further, when examining the different frequencies of fishing closures, we found that, for any scenario, no closure would be effective if it was less frequent than every other month. As exemplified by the previous analysis, closures focusing on either stage 4 or larval individuals required the most increase in survivorship and highest frequencies of closures in order to result in population growth.

33 DISCUSSION

The results of our per-stage analysis showed that focusing on protecting individuals in stage 1 would be the most effective form of management if size could be determined before capture in this fishery. It is a common trend that individuals that survive long larval stages that have high death rates are the most valuable in terms of contributions to overall population growth. However, this is not a realistic management suggestion, as it is difficult to assess the size of octopus before catch, which is often fatal to the individual. This could suggest, however, that the establishment of aquaculture of *Octopus cyanea* could have benefits to the overall population if octopus are reared until passing this first stage of development. However, further research is needed on cephalopod aquaculture in order to be effective and reduce pollutants in the surrounding waters (Jacquet et al. 2023).

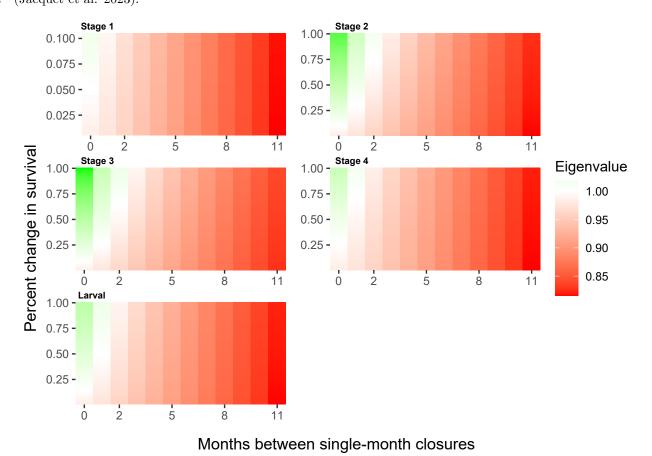


Figure 3: Different fishing scenarios based on increasing survivability of one stage.

Table 2: Life table of O. cyanea as calculated from our Lefkovitch matrix.

| Age (months) | Survivorshi | ipProportion of orginal cohort dying | Mortality hazard | Probability of death | Probability of survival | Remaining life expectancy | Per- capita reproduc- tion rate | Expected number of offspring |
|--------------|-------------|---|---------------------|-------------------------|-------------------------------|---------------------------|--|------------------------------|
| 0 | 1.0000000 | 0.0951997 | 0.0999577 | 0.0951997 | 0.9048003 | 3.546039 | 0.00000000 | 0.0000000 |
| 1 | 0.9048003 | 0.2107642 | 0.2636471 | 0.2329401 | 0.7670599 | 2.866532 | 0.0000000 | 0.0000000 |
| 2 | 0.6940360 | 0.1996469 | 0.3359857 | 0.2876607 | 0.7123393 | 2.585199 | 0.0000000 | 0.0000000 |
| 3 | 0.4943891 | 0.1567056 | 0.3766632 | 0.3169681 | 0.6830319 | 2.427255 | 0.1801271 | 0.0890529 |
| 4 | 0.3376835 | 0.1130954 | 0.4022801 | 0.3349152 | 0.6650848 | 2.321617 | 0.4417776 | 0.1491810 |
| 5 | 0.2245882 | 0.0778436 | 0.4192659 | 0.3466059 | 0.6533941 | 2.238925 | 0.7077949 | 0.1589624 |
| 6 | 0.1467446 | 0.0520106 | 0.4307673 | 0.3544291 | 0.6455709 | 2.161373 | 0.9405289 | 0.1380175 |
| 7 | 0.0947340 | 0.0340773 | 0.4386006 | 0.3597150 | 0.6402850 | 2.073494 | 1.1279077 | 0.1068513 |
| 8 | 0.0606568 | 0.0220360 | 0.4439266 | 0.3632896 | 0.6367104 | 1.957489 | 1.2709528 | 0.0770919 |
| 9 | 0.0386208 | 0.0141236 | 0.4475285 | 0.3656983 | 0.6343017 | 1.789093 | 1.3761398 | 0.0531476 |
| 10 | 0.0244972 | 0.0089981 | 0.4499474 | 0.3673119 | 0.6326881 | 1.532303 | 1.4513443 | 0.0355539 |
| 11 | 0.0154991 | 0.0057097 | 0.4515599 | 0.3683858 | 0.6316142 | 1.131614 | 1.5039407 | 0.0233097 |
| 12 | 0.0097895 | 0.0097895 | 2.0000000 | 1.0000000 | 0.0000000 | 0.500000 | 1.5400772 | 0.0150765 |

4 Rage package analysis

50 4.1 Age specific Calculations

- Table 2 shows age specific life-history traits of *Octopus cyanea* as calculated by the Rage package from our
- matrix. Expected number of offspring is reported per original cohort number.

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Supplementary Material for:

Social-ecological models with social hierarchy and space applied to small scale fisheries

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¹Department of Biological Sciences, University of New Hampshire, 03824, NH, USA * Corresponding authors: Sophie Wulfing (SophieWulfing@gmail.com) and Dr. Easton White (Easton.White@unh.edu) Equations 2), 4), and 5) are as follows:

$$\frac{dX_i}{dt} = k_i X_i (1 - X_i) [U_{A,i} - U_{B,i}]$$
(2)

$$U_{A,i} = \frac{1}{(F_i + c_i)} + d_i X_i + \rho_i X_j \tag{4}$$

$$U_{B,i} = \omega_i + d_i(1 - X_i) + \rho_i(1 - X_j)$$
(5)

² Substituting equations 4) and 5) into equation 2 Gives:

$$\text{3} \quad \frac{dX_i}{dt} = k_i X_i (1-X_i) [\frac{1}{(F_i+c_i)} + d_i X_i + \rho_i X_j - \omega_i - d_i (1-X_i) - \rho_i (1-X_j)]$$

$$4 \quad \frac{dX_i}{dt} = k_i X_i (1 - X_i) \left[\frac{1}{(F_i + c_i)} - \omega_i + d_i (X_i - 1 + X_i) + \rho_i (X_j - 1 + X_j) \right]$$

s
$$\frac{dX_i}{dt} = k_i X_i (1-X_i) [\frac{1}{F_i + c_i} - \omega_i + d_i (2X_i - 1) + \rho_i (2X_j - 1)]$$