

Question 10

→ From the given Question, there are two labels, \bullet & \times . Considering \bullet as 1 and \times as 0. So the feature values and labels ^{or classes} are as below.

f	class
1	1
2	1
3	0
6	0
6	0
7	1
10	1
11	1

① Since we need to divide the data equally into two parts. Splitting the data into train & test data.

Train data $\rightarrow \{1, 2, 3, 6\}$

class $\rightarrow \{1, 1, 0, 0\}$

Test data $\rightarrow \{6, 7, 10, 11\}$

class $\rightarrow \{0, 1, 1, 1\}$

Confusion matrix for Test data will be as

Actual \downarrow		0	1	\leftarrow Predicted
	0	TN	FP	
1	FN	TP		

Using Euclidean distance, find the distance between the Test sample 6 and Train samples 1, 2, 3, 6, we get

$$d_1 = \sqrt{(6-1)^2} = 5$$

$$d_2 = \sqrt{(6-2)^2} = 4$$

$$d_3 = \sqrt{(6-3)^2} = 3$$

$$d_4 = \sqrt{(6-6)^2} = 0$$

So ~~train~~ Using 3-NN classifier, train samples nearer to the test sample 6 are 6, 3, 2 & their labels/classes are 0, 0, 1.

Taking the maximum out of them, the predicted output is 0.

So ~~it is~~ Actual is 0 & Predicted is 0. So it is TN

Now for Test samples 7, 10 & 11 we get

for 7 ^{3-NN are} $\rightarrow 0, 0, 1$ So FN since actual is 1 & Predicted is 0

10 ^{3-NN are} $\rightarrow 0, 0, 1$ So FN since actual is 1 & Predicted is 0

11 ^{3-NN are} $\rightarrow 0, 0, 1$ So FN since actual is 1 & Predicted is 0

② So, Confusion matrix is

	0	1
0	1	0
1	3	0

$$\Rightarrow TN = 1$$

$$FP = 0$$

$$FN = 3$$

$$TP = 0$$

$$\text{So, Accuracy} = \frac{TP + TN}{P + N} = \frac{TP + TN}{TN + FP + FN + TP} = \frac{1}{4} = 0.25$$

$$\text{Sensitivity} = \frac{TP}{TP + FN} = \frac{TP}{P} = \frac{0}{0+3} = 0$$

$$\text{Specificity} = \frac{TN}{FP + TN} = \frac{TN}{N} = \frac{1}{0+1} = 1$$