Sum manising, we expect the total verpower 
$$u(x,t) \Rightarrow y$$
,

 $u(x,t) = u_{st}(x,t) + u_{f}(x,t)$  (2)

where,  $u_{st}(0,t) = u_{g_1}(t)$  and  $u_{st}(1,t) = u_{g_2}(t)$ 
 $u_{f}(0,t) = 0$  and  $u_{f}(1,t) = 0$ 

Solving for  $u_{st}(x,t)$ 

Reconsider the varie equation,  $EA$   $\frac{\partial u}{\partial x_1} = u \frac{\partial u}{\partial t} \Rightarrow \text{Neglecting the inertial faces (i.e., treating the string is non-flexible), } EA  $\frac{\partial u_{st}}{\partial x_1} = 0 \Rightarrow 0$ 
 $\Rightarrow u_{st}(x,t) = c_1(t) \times + c_2(t) \Rightarrow u_{g_1}(t) = c_1(t)$ 

Put  $u_{st}(0,t) = u_{g_1}(t)$ 
 $\Rightarrow u_{st}(x,t) = u_{g_1}(t) \Rightarrow u_{g_2}(t) = c_1(t) + u_{g_1}(t) \Rightarrow 0$ 
 $\Rightarrow u_{st}(x,t) = u_{g_1}(t) \Rightarrow u_{g_2}(t) - u_{g_1}(t) \Rightarrow 0$ 
 $\Rightarrow u_{st}(x,t) = u_{g_1}(t) \Rightarrow u_{g_2}(t) - u_{g_1}(t) \Rightarrow 0$ 
 $\Rightarrow u_{st}(x,t) = u_{g_1}(t) \Rightarrow u_{g_2}(t) - u_{g_1}(t) \Rightarrow 0$ 
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Solving for 4f(x1+1) Substitute (2) mb the governing equixion (1) =>  $(EA \frac{\partial u_st}{\partial x^2} + EA \frac{\partial u_f}{\partial x^2} = m \frac{\partial^2 u_st}{\partial t^2} + m \frac{\partial^2 u_f}{\partial t^2} \Rightarrow$  $\frac{\partial u_f}{\partial x^2} - m \frac{\partial u_f}{\partial t^2} = m \frac{\partial u_{st}}{\partial t^2} = f(x,t)$ (3)

He problem for known smotore Standard Justern of x and t (33) Uf(0,t)=0, Uf(1,+)=0= with simple BCs. = we get 'simple' bound any auditions! Note on the initial conditions:  $u(x,0) = g(x) \rightarrow u_{s+}(x,0) + u_{f}(x,0) = g(x) \rightarrow$ \*(uf(x,0)=g(x)-us+(x,0)) Similarly ne campute the other initial and that up (4,0)= h(x)-1. Hence, (3), (32) and (36) fam a standard publicus that we can role.