This form documents the artifacts associated with the article (i.e., the data and code supporting the computational findings) and describes how to reproduce the findings.

Part 1: Data

This paper	does	not	involve	analysis	of	external	data	(i.e.,	no	data	are	used	or	the	only	data	are
generated b	by the	auth	nors via	simulatio	n i	in their co	ode).										

⊠ I certify that the author(s) of the manuscript have legitimate access to and permission to use the data used in this manuscript.

Abstract

We provide the datasets used in the experimental section, which are also available online. A detailed guide on accessing the original datasets is included in the README file.

Availability

\boxtimes	Data are publicly available.
	Data cannot be made publicly available

If the data are publicly available, see the *Publicly available data* section. Otherwise, see the *Non-publicly available data* section, below.

Publicly available data

	$\label{lem:decomposition} Data \ are \ available \ online \ at: \ https://finance.yahoo.com/lookup, \ https://www.bioconductor.org/packages/release/data/experiment/html/cancerdata.html$
\boxtimes	Data are available as part of the paper's supplementary material.
	Data are publicly available by request, following the process described here:

For the Yahoo dataset, each stock has its own dedicated webpage. For example, the page https://finance.yahoo.com/quote/MMM/history/ provides the historical data for 3M Company (MMM). To access the overall dataset, we provide the link to the Yahoo Finance Lookup page: https://finance.yahoo.com/lookup. A detailed guide on accessing the original datasets is included in the README file, and the datasets are also provided as part of the paper's supplementary material.

□ Data are or will be made available through some other mechanism, described here:

Non-publicly available data

Description

File format(s)

\boxtimes	CSV or other plain text.
	Software-specific binary format (.Rda, Python pickle, etc.): pkcle
	Standardized binary format (e.g., netCDF, HDF5, etc.):
	Other (please specify):

Data dictionary

 ☑ Provided by authors in the following file(s): all_stocks_5yr.csv, stock_data_elliptical.csv, elliptical_breast_cancer.csv ☐ Data file(s) is(are) self-describing (e.g., netCDF files) ☐ Available at the following URL:
We described the process of obtaining the combined historical stock data file, all_stocks_5yr.csv in the README file. The columns of all_stocks_5yr.csv include prices, volume, and stock names, as defined in the README file. The code in stock_preprocessing.R preprocesses the all_stocks_5yr.csv datase

README file. The columns of all_stocks_5yr.csv include prices, volume, and stock names, as defined in the README file. The code in stock_preprocessing.R preprocesses the all_stocks_5yr.csv dataset to generate the testing dataset, stock_data_elliptical.csv. The dataset stock_data_elliptical.csv is organized such that each row corresponds to a specific datetime, and each column represents a stock.

The breast capacity dataset is available in the P_pressure capacitate, with a detailed description pre-

The breast cancer dataset is available in the R package cancerdata, with a detailed description provided in the documentation cancerdata.pdf or online at https://bioconductor.org/packages/release/data/experiment/manuals/cancerdata/man/cancerdata.pdf. For our analysis, we use the VIJVER dataset from the package. The original data is a 24481 × 295 matrix, where each row represents a gene and each column corresponds to a tumor sample. The code in breast_cancer_preprocessing.R is used to load and preprocess the VIJVER dataset, generating the testing dataset elliptical_breast_cancer.csv. The dataset elliptical_breast_cancer.csv is structured such that each row represents a specific tumor sample, and each column corresponds to a gene.

Additional Information (optional)

Part 2: Code

Abstract	
Abstract	

Description

Code format(s)

$\hfill\Box$ Script files	
\boxtimes R \square Python \boxtimes Matlab \square Other:	
$\hfill\Box$ Package	
☐ R ☐ Python ☐ MATLAB too ☐ Other:	olbox
\square Reproducible repo	rt
□ R Markdown□ Jupyter notel□ Other:	oook
☐ Shell script☐ Other (please spec	eify):

Supporting software requirements

Version of primary software used R 4.4.1, Matlab R2023a

Libraries and dependencies used by the code We used the following R packages: psych 2.4.12, tilting 1.1.1, Matrix 1.5.3, foreach 1.5.2, wordspace 0.2.8, mnormt 2.1.1, Rlab 4.0, gTests 0.2, expm 0.999.9, MASS 7.3.58.2, normwhn.test 1.0, mvtnorm 1.2.4, mvShapiroTest 1.0, ade4 1.7.22, ggplot2 3.5.1, scales 1.3.0

Supporting system/hardware requirements (optional)
Parallelization used
 □ No parallel code used □ Multi-core parallelization on a single machine/node
Number of cores used:
⊠ Multi-machine/multi-node parallelization
- Number of nodes and cores used: 12
License
 □ MIT License (default) □ BSD □ GPL v3.0 □ Creative Commons □ Other: (please specify)
Additional information (optional)
Part 3: Reproducibility workflow
Scope
The provided workflow reproduces:
 □ Any numbers provided in text in the paper ☑ The computational method(s) presented in the paper (i.e., code is provided that implements the method(s)) □ All tables and figures in the paper □ Selected tables and figures in the paper, as explained and justified below:

The real data results of the proposed test can be reproduced, but the normality test involves some random-

Workflow

Location

The workflow is available:
 ☑ As part of the paper's supplementary material. ☐ In this Git repository: ☐ Other (please specify):
$\mathbf{Format}(\mathbf{s})$
 ⊠ Single master code file □ Wrapper (shell) script(s) □ Self-contained R Markdown file, Jupyter notebook, or other literate programming approach □ Text file (e.g., a readme-style file) that documents workflow □ Makefile □ Other (more detail in <i>Instructions</i> below)
Instructions
The code in elliptical_test.m and tests.R can be used to calculate the test statistic and p-value. A detailed description is provided in the README file.
Expected run-time
Approximate time needed to reproduce the analyses on a standard desktop machine:
 ☐ < 1 minute ☐ 1-10 minutes ☐ 10-60 minutes ☐ 1-8 hours ☐ > 8 hours ☐ Not feasible to run on a desktop machine, as described here:
Additional information (optional)
Notes (optional)