

Topic 9 Statistical Testing

1. Introduction

Hypothesis testing is the process of using sample data to test a claim about the value of a population parameter

2. P-value and alpha

- If $p_value \leq \alpha$, we reject H_0
- If $p_value > \alpha$, we fail to reject H_0

notes:

The P-value is a statement about the probability that the sample mean takes on specific values.

It is not a statement about the probability that the population mean has a certain value.

It is not a statement about the probability that the null hypothesis is true.

Type I and II error

Type I error: Reject H_0 while H_0 is true

If the null hypothesis is true and $\alpha = 0.05$

- There really is no relationship and the extremity of the test statistic is due to chance.
- About 5% of all samples from this population will lead us to wrongly reject chance and conclude significance.

Type II error: Fail to reject H_0 while H_0 is false

- This is an incorrect decision only if H_a is true.
- The probability of this incorrect decision β is computed as $1 - \text{Power}(\text{test})$

One sample t test

```
ods graphics on; # requests graphical output
proc ttest h0=80 plots(showh0) sides=u alpha=0.1;
var time;
run;
ods graphics off;
```

- $h_0 = 80$: the value of null hypothesis
- `plots(showh0)` = null value be displayed on all relevant graphs.
- `sides = u`: greater than

if the alternative hypothesis is larger, use "sides=u".

if the alternative hypothesis is smaller, use "sides=l".

if the alternative hypothesis is not equal, use "sides=2".