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## syakesaba / deep-learning-from-scratch

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ch01	Bactch Normalizationまで	4 months ago
ch02	日本語が入ると駄目っぽい→latex	4 months ago
ch03	日本語が入ると駄目っぽい→latex	4 months ago
ch04	日本語が入ると駄目っぽい→latex	4 months ago
ch05	日本語が入ると駄目っぽい→latex	4 months ago
ch06	ch6 end	4 months ago
ch07	Ch07.End	5 days ago
ch08	ch08.end	5 days ago
common	Add delta(1e-7) for cross_entropy_error	9 months ago
dataset	fixfix	5 months ago
.gitignore	added gitignore	9 months ago
LICENSE.md	updated to DOT graphviz	9 months ago
README.md	a	5 days ago

README.md



## ゼロから作る Deep Learning

syakesabaの勉強用ノートのリポジトリ。それぞれのチャプターに合わせてipynbファイルを作成し JupyterNotebookで実際にコードを動かしてグラフを出したりします。

以下、オリジナルの方のREADME.md

## ゼロから作る Deep Learning



本リポジトリはオライリー・ジャパン発行書籍『[ゼロから作る Deep Learning](#)』のサポートサイトです。

## ファイル構成

フォルダ名	説明
ch01	1章で使用するソースコード
ch02	2章で使用するソースコード
...	...
ch08	8章で使用するソースコード
common	共通で使用するソースコード
dataset	データセット用のソースコード

ソースコードの解説は本書籍をご覧ください。

## 必要条件

ソースコードを実行するには、下記のソフトウェアがインストールされている必要があります。

- Python 3.x
- NumPy
- Matplotlib

※Pythonのバージョンは、3系を利用します。

## 実行方法

各章のフォルダへ移動して、Pythonコマンドを実行します。

```
$ cd ch01  
$ python man.py  
  
$ cd ../ch05  
$ python train_neuralnet.py
```

## ライセンス

本リポジトリのソースコードは[MITライセンス](#)です。 商用・非商用問わず、自由にご利用ください。

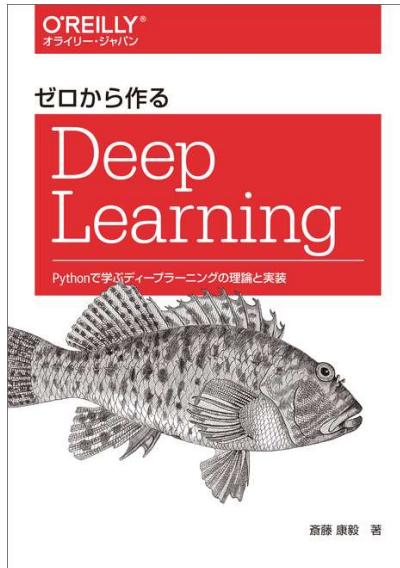
## 正誤表

本書の正誤情報は以下のページで公開しています。

<https://github.com/oreilly-japan/deep-learning-from-scratch/wiki/errata>

本ページに掲載されていない誤植など間違いを見つけた方は、[japan@oreilly.co.jp](mailto:japan@oreilly.co.jp)までお知らせください。

# SYA-KE Deep Learning Training



## Parent Repository URL

<https://github.com/oreilly-japan/deep-learning-from-scratch> (<https://github.com/oreilly-japan/deep-learning-from-scratch>)

## Pythonに慣れる

In [1]:

```
!python --version
```

Python 3.6.5

In [2]:

```
#もう何年もやってるので省略
```

## Numpyに慣れる

## 参考URL

<http://www.sist.ac.jp/~kanakubo/research/hosoku/gyoretu.html>  
(<http://www.sist.ac.jp/~kanakubo/research/hosoku/gyoretu.html>)

## 配列、行列

In [3]:

```
import numpy as np
```

In [4]:

```
np.__version__
```

Out[4]:

```
'1.14.3'
```

In [5]:

```
x = np.array([1.0, 2.0, 3.0])
```

In [6]:

```
y = np.array([2.0, 4.0, 6.0])
```

In [7]:

```
x + y
```

Out[7]:

```
array([3., 6., 9.])
```

In [8]:

```
x - y
```

Out[8]:

```
array([-1., -2., -3.])
```

In [9]:

```
x * y
```

Out[9]:

```
array([ 2.,  8., 18.])
```

In [10]:

```
x / y
```

Out[10]:

```
array([0.5, 0.5, 0.5])
```

In [11]:

```
x / 2.0
```

Out[11]:

```
array([0.5, 1. , 1.5])
```

In [12]:

```
A = np.array([[1, 2], [3, 4]])
```

In [13]:

```
print(A)
```

```
[[1 2]
 [3 4]]
```

In [14]:

```
A.shape
```

Out[14]:

```
(2, 2)
```

In [15]:

```
A.dtype
```

Out[15]:

```
dtype('int32')
```

In [16]:

```
B = np.array([[3, 0], [0, 6]])
```

In [17]:

```
A + B
```

Out[17]:

```
array([[ 4,  2],
       [ 3, 10]])
```

In [18]:

```
A * B
```

Out[18]:

```
array([[ 3,  0],
       [ 0, 24]])
```

In [19]:

```
A*10
```

Out[19]:

```
array([[10, 20],
       [30, 40]])
```

参考 (<http://www.scipy-lectures.org/intro/numpy/operations.html>)

In [20]:

```
X = np.array([[51, 55], [14, 19], [0, 4]])
X
```

Out[20]:

```
array([[51, 55],
       [14, 19],
       [0, 4]])
```

In [21]:

```
X[0] #0行目
```

Out[21]:

```
array([51, 55])
```

In [22]:

```
X[0][1] #(0, 1) => (0行1列)
```

Out[22]:

```
55
```

In [23]:

```
for row in X:
    print(row)
```

```
[51 55]
[14 19]
[0 4]
```

In [24]:

```
AX = X.flatten() #行列を配列に
AX
```

Out[24]:

```
array([51, 55, 14, 19, 0, 4])
```

In [25]:

```
AX[AX>15] #配列から条件の値を抽出
```

Out[25]:

```
array([51, 55, 19])
```

In [26]:

```
X>15
```

Out[26]:

```
array([[ True,  True],
       [False,  True],
       [False, False]])
```

In [27]:

```
X[X>15] #行列でもできる。
```

Out[27]:

```
array([51, 55, 19])
```

ニューラルネットワークにおいては行列は 行数 = 入力数 列数 = 重み数

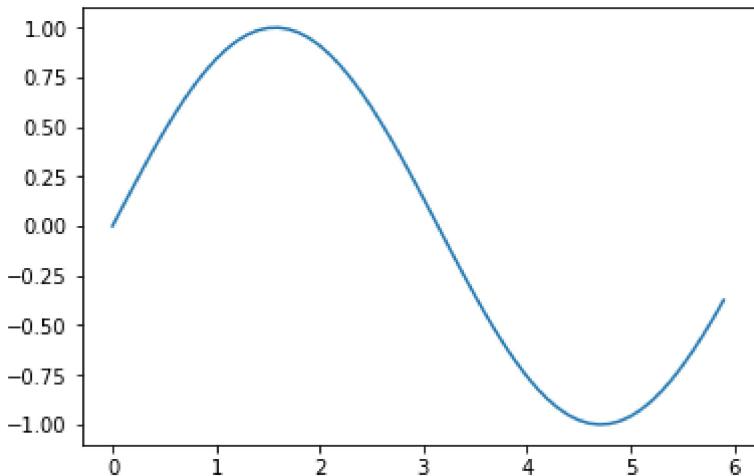
## Matplotlibに慣れる

参考URL (<http://qiita.com/hik0107/items/de5785f680096df93efa>)

In [28]:

```
%matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

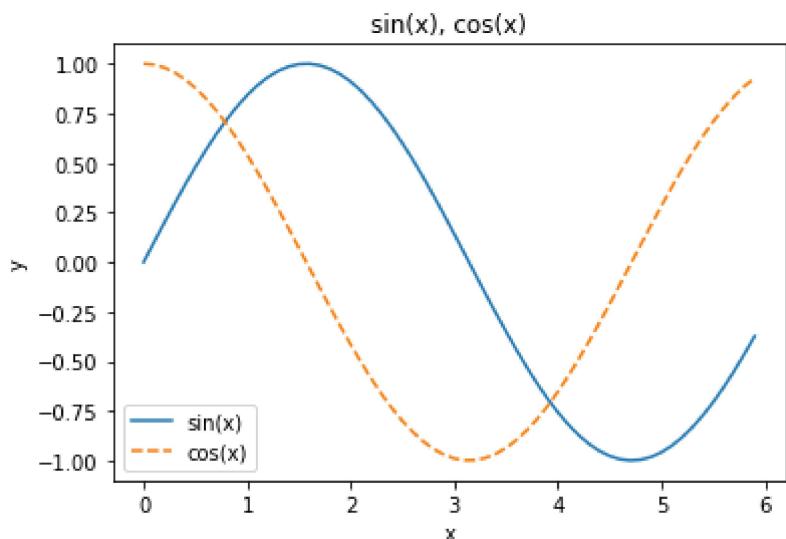
x = np.arange(0, 6, 0.1) #0to6 by 0.1 => sin(0to6)
y = np.sin(x)
plt.plot(x,y)
plt.show()
plt.close()
```



In [29]:

```
%matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

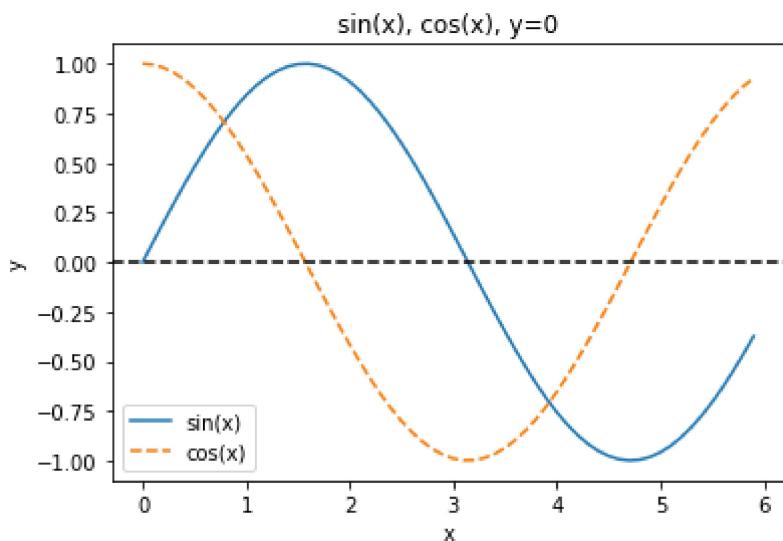
x = np.arange(0, 6, 0.1) #0to6 by 0.1 => sin(0to6)
y1 = np.sin(x)
y2 = np.cos(x)
plt.plot(x, y1, label="sin(x)")
plt.plot(x, y2, label="cos(x)", linestyle="--")
plt.xlabel("x")
plt.ylabel("y")
plt.title("sin(x), cos(x)")
plt.legend() #show label box
plt.show()
plt.close()
```



In [30]:

```
%matplotlib inline
#plt.show()をinlineにて表示する
#Esc+Lで行番号を表示する
import matplotlib.pyplot as plt
import numpy as np

x = np.arange(0, 6, 0.1) #0to6 by 0.1 => sin(0to6)
y1 = np.sin(x)
y2 = np.cos(x)
plt.plot(x, y1, label="sin(x)")
plt.plot(x, y2, label="cos(x)", linestyle="--")
plt.axhline(color='black', linestyle="--")
plt.xlabel("x")
plt.ylabel("y")
plt.title("sin(x), cos(x), y=0")
plt.legend() #show label box
plt.show()
plt.close()
```

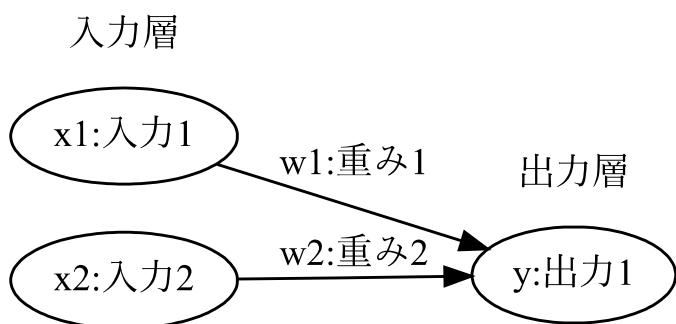


パーセプトロンに慣れる

In [31]:

```
from graphviz import Digraph
dot = Digraph(comment="単純パーセプトロン")
dot.attr(rankdir="LR")
dot.attr(splines="line")
dot.attr(fixedsize="true")
with dot.subgraph(name="cluster_x") as x:
    x.attr(label="入力層")
    x.attr(color="white")
    x.node("x1", "x1:入力1")
    x.node("x2", "x2:入力2")
with dot.subgraph(name="cluster_y") as y:
    y.attr(label="出力層")
    y.attr(color="white")
    y.node("y", "y:出力1")
dot.edge("x1", "y", label="w1:重み1")
dot.edge("x2", "y", label="w2:重み2")
#print(dot)
dot
```

Out[31]:

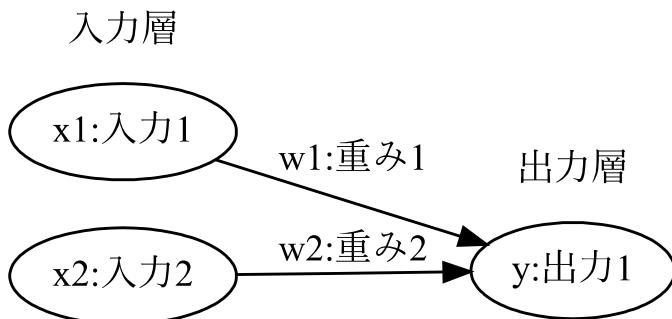


# パーセプトロンに慣れる

In [1]:

```
from graphviz import Digraph
dot = Digraph(comment="単純パーセプトロン")
dot.attr(rankdir="LR")
dot.attr(splines="line")
dot.attr(fixedsize="true")
with dot.subgraph(name="cluster_x") as x:
    x.attr(label="入力層")
    x.attr(color="white")
    x.node("x1", "x1:入力1")
    x.node("x2", "x2:入力2")
with dot.subgraph(name="cluster_y") as y:
    y.attr(label="出力層")
    y.attr(color="white")
    y.node("y", "y:出力1")
dot.edge("x1", "y", label="w1:重み1")
dot.edge("x2", "y", label="w2:重み2")
#dot
dot
```

Out[1]:



今、 $x_1$ :入力1と $x_2$ :入力2を0~1の変数と仮定すると、以下のように発火判定をして任意のCPU処理を実装することが可能になる。

つまり、パーセプトロンは**チューリング完全**であり、電子コンピュータで出来ることがパーセプトロンでも出来ることを示している。

$$AND \quad y = \begin{cases} 0 & (0.5x_1 + 0.5x_2 \leq 0.6) \\ 1 & (0.5x_1 + 0.5x_2 > 0.6) \end{cases}$$

In [2]:

```
def AND(x1, x2):
    w1, w2, theta = 0.5, 0.5, 0.6 #0001
    tmp = x1*w1 + x2*w2
    if tmp <= theta:
        return 0
    else:
        return 1
```

$$OR \quad y = \begin{cases} 0 & (0.5x_1 + 0.5x_2 \leq 0.4) \\ 1 & (0.5x_1 + 0.5x_2 > 0.4) \end{cases}$$

In [3]:

```
def OR(x1, x2):
    w1, w2, theta = 0.5, 0.5, 0.4 #0111
    tmp = x1*w1 + x2*w2
    if tmp <= theta:
        return 0
    else:
        return 1
```

$$NAND \quad y = \begin{cases} 0 & (0.5x_1 + 0.5x_2 > 0.6) \\ 1 & (0.5x_1 + 0.5x_2 \leq 0.6) \end{cases}$$

In [4]:

```
def NAND(x1, x2):
    w1, w2, theta = 0.5, 0.5, 0.6 #1110
    tmp = x1*w1 + x2*w2
    if tmp > theta:
        return 0
    else:
        return 1
```

$$NOR \quad y = \begin{cases} 0 & (0.5x_1 + 0.5x_2 > 0.4) \\ 1 & (0.5x_1 + 0.5x_2 \leq 0.4) \end{cases}$$

In [5]:

```
def NOR(x1, x2):
    w1, w2, theta = 0.5, 0.5, 0.4 #1000
    tmp = x1*w1 + x2*w2
    if tmp > theta:
        return 0
    else:
        return 1
```

$$XOR \quad y = \begin{cases} 0 & AND(NAND, OR) \\ 1 & AND(NAND, OR) \end{cases}$$

In [1]:

```
def XOR(x1, x2):
    AND_x1x2 = AND(x1, x2) # 0001
    OR_x1x2 = OR(x1, x2) #0111
    AND_x1x2 = NAND(x1, x2) #1110
    return AND(NAND_x1x2, OR_x1x2) #0110
```

# 活性化関数

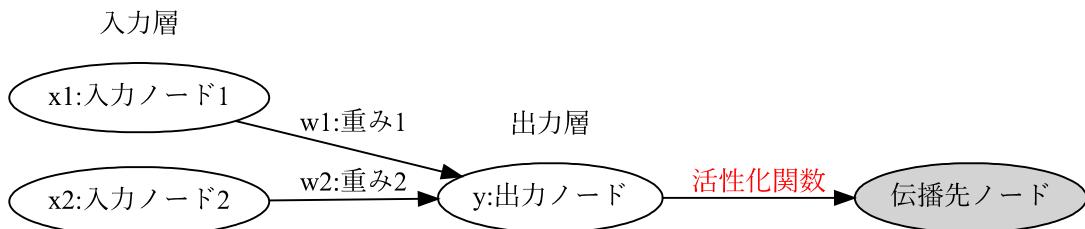
発火するか、しないか or 発火するならどのくらいの発火なのかを定める

In [1]:

```
from graphviz import Digraph
dot = Digraph(comment="単純パーセプトロン")
dot.attr(rankdir="LR")
dot.attr(splines="line")
dot.attr(fixedsize="true")
with dot.subgraph(name="cluster_x") as x:
    x.attr(label="入力層")
    x.attr(color="white")
    x.node("x1", "x1:入力ノード1")
    x.node("x2", "x2:入力ノード2")
with dot.subgraph(name="cluster_y") as y:
    y.attr(label="出力層")
    y.attr(color="white")
    y.node("y", "y:出力ノード")
with dot.subgraph(name="cluster_a") as a:
    a.attr(color="white")
    a.node("a", "伝播先ノード", style="filled")

dot.edge("x1", "y", label="w1:重み1")
dot.edge("x2", "y", label="w2:重み2")
dot.edge("y", "a", label="活性化関数", fontcolor="red")
#print(dot)
dot
```

Out[1]:



## Sigmoid関数 (シグモイド関数)

便利な非線形関数

$$h_\theta(x) = \frac{1}{1+e^{-\theta x}}$$

これは $\theta = 1$ の時、標準シグモイド関数となる。

$$h_1(x) = \frac{1}{1+e^{-x}}$$

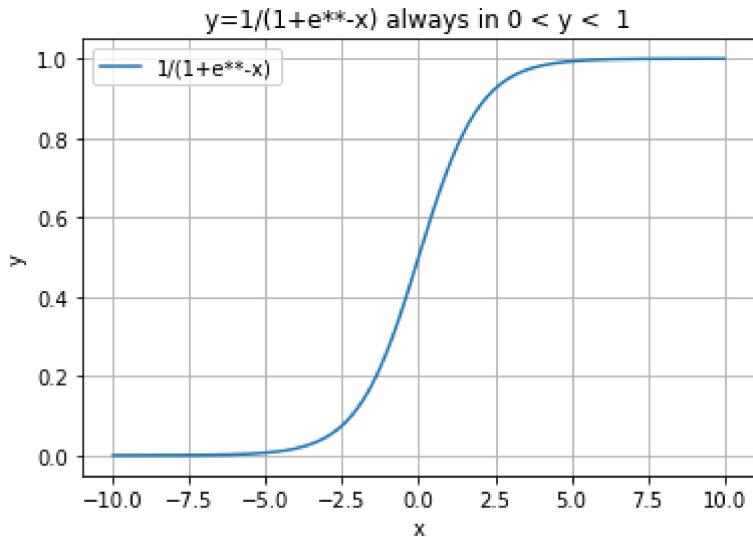
標準シグモイド関数は $x$ の値がいかなる数値であっても結果は $0 < h_1(x) < 1$ となる

In [2]:

```
%matplotlib inline
# plt.show()をinlineにて表示する
# Esc+Lで行番号を表示する
import matplotlib.pyplot as plt
import numpy as np

x = np.arange(-10, 10, 0.001) # -10 to 10 by 0.001
y = 1.0/(1.0 + np.e ** (-1.0*x))

plt.plot(x, y, label="1/(1+e**-x)", linestyle="-")
plt.xlabel("x")
plt.ylabel("y")
plt.title("y=1/(1+e**-x) always in 0 < y < 1")
plt.legend() #show label box
plt.grid()
plt.show()
plt.close()
```



## ステップ関数

$x$ がどの値であっても0か1を指す非線形関数

In [3]:

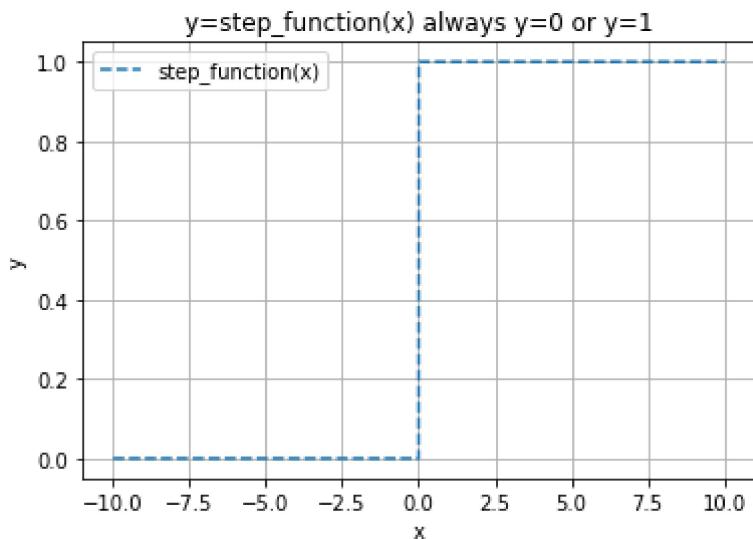
```
import numpy as np
def step_function(x):
    """x: numpy.Array"""
    y = x > 0
    # x(int)がboolに変換されるので、またintに直す
    return y.astype(np.int)
```

In [4]:

```
%matplotlib inline
#plt.show()をinlineにて表示する
#Esc+Lで行番号を表示する
import matplotlib.pyplot as plt
import numpy as np

import numpy as np
def step_function(x):
    y = x > 0
    return y.astype(np.int)

x = np.arange(-10, 10, 0.001) # -10 to 10 by 0.001
y = step_function(x)
plt.plot(x, y, label="step_function(x)", linestyle="--")
plt.xlabel("x")
plt.ylabel("y")
plt.title("y=step_function(x) always y=0 or y=1")
plt.legend() #show label box
plt.grid()
plt.show()
plt.close()
```



## シグモイド関数とステップ関数の関係

ステップ関数では情報量が欠ける

In [5]:

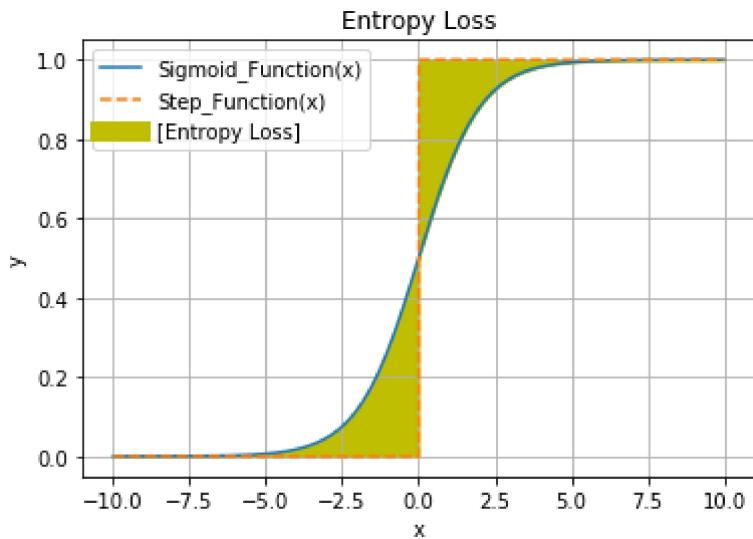
```
%matplotlib inline
#plt.show()をinlineにて表示する
#Esc+Lで行番号を表示する
import matplotlib.pyplot as plt
import numpy as np

x = np.arange(-10, 10, 0.001) # -10 to 10 by 0.001
y1 = 1.0/(1.0 + np.e ** (-1.0*x))

def step_function(x):
    y = x > 0
    return y.astype(np.int)

y2 = step_function(x)

plt.plot(x, y1, label="Sigmoid_Function(x)", linestyle="--")
plt.plot(x, y2, label="Step_Function(x)", linestyle=":")
plt.fill_between(x, y1, y2, color="y")
plt.plot([], [], color="y", linewidth=10, label="[Entropy Loss]")
plt.title("Entropy Loss")
plt.xlabel("x")
plt.ylabel("y")
plt.legend() #show label box
plt.grid()
plt.show()
plt.close()
```



## 活性関数は非線形関数でなければならない

活性関数が線形関数の場合は計算結果が予測可能となり計算式も因数分解が可能となる(=一瞬で演算が収束する)。そうなった場合多層パーセプトロンは組む意味がない。今後は非線形(パーセプトロンやシグモイドのような)になることを意識しなければならない。活性化関数に線形関数を使っても得られる情報は価値(情報量、エントロピー)が少ない。

## 活性関数の特徴

- ステップ関数：劇的な信号の変化を発生させる
- シグモイド関数：緩やかな信号の変化を発生させる
- RELU：発火しないものに関して逆伝搬をさせなくする（ニューロンの無効化）

## ReLU関数 (Rectified Liner Unit)

$$h(x) = \begin{cases} x & (x > 0) \\ 0 & (x \leq 0) \end{cases}$$

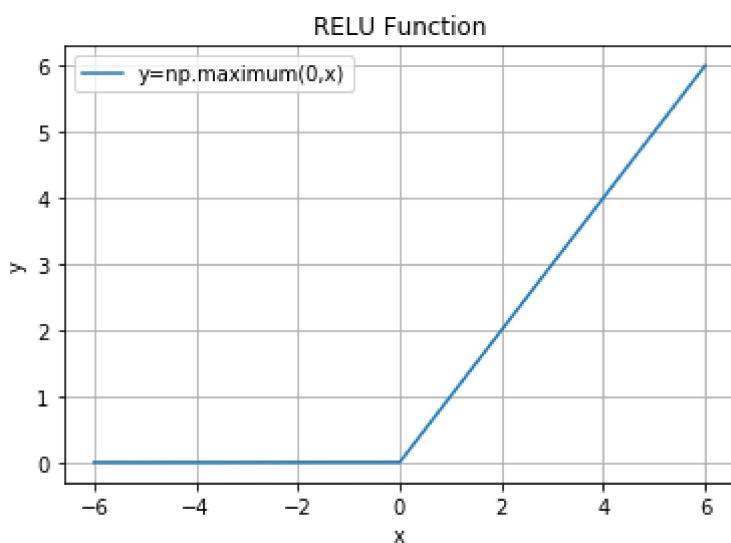
In [6]:

```
%matplotlib inline
# plt.show() をinlineにて表示する
# Esc+Lで行番号を表示する1
import matplotlib.pyplot as plt
import numpy as np

x = np.arange(-6, 6, 0.001) #-6 to 6 by 0.001

def relu(x):
    return np.maximum(0, x)

plt.plot(x, relu(x), label="y=np.maximum(0,x)", linestyle="--")
plt.xlabel("x")
plt.ylabel("y")
plt.title("ReLU Function")
plt.xlabel("x")
plt.ylabel("y")
plt.legend() #show label box
plt.grid()
plt.show()
plt.close()
```



## 多次元配列に慣れる

In [7]:

```
import numpy as np
A = np.array([1, 2, 3, 4])
print(A)
print("何次元配列→", A.ndim)
print("何行、何列→", A.shape)
```

```
[1 2 3 4]
何次元配列→ 1
何行、何列→ (4, )
```

In [8]:

```
import numpy as np
A = np.array([[1, 2, 3, 4], [5, 6, 7, 8]])
print(A)
print("何次元配列→", A.ndim)
print("何行、何列→", A.shape)
```

```
[[1 2 3 4]
 [5 6 7 8]]
何次元配列→ 2
何行、何列→ (2, 4)
```

In [9]:

```
import numpy as np
A = np.array([[1, 2, 3, 4], [5, 6, 7, 8], [0, -1, -2, -3]])
print(A)
print("何次元配列→", A.ndim)
print("何行、何列→", A.shape)
```

```
[[ 1  2  3  4]
 [ 5  6  7  8]
 [ 0 -1 -2 -3]]
何次元配列→ 2
何行、何列→ (3, 4)
```

## 内積(ドット積)

In [10]:

```
import numpy as np
A = np.array([[1, 2, 3, 4], [5, 6, 7, 8], [0, -1, -2, -3]])
B = np.array([[1, 2, 3], [5, 6, 7], [0, -1, -2], [4, 5, 6]])
print("何次元配列→", A.ndim)
print("何行、何列→", A.shape)
print(A)
print("x")
print("何次元配列→", B.ndim)
print("何行、何列→", B.shape)
print(B)
print("=")
C=np.dot(A, B)
print(C)
print("何次元配列→", C.ndim)
print("何行、何列→", C.shape)
```

何次元配列→ 2  
何行、何列→ (3, 4)

```
[[ 1  2  3  4]
 [ 5  6  7  8]
 [ 0 -1 -2 -3]]
```

x

何次元配列→ 2  
何行、何列→ (4, 3)

```
[[ 1  2  3]
 [ 5  6  7]
 [ 0 -1 -2]
 [ 4  5  6]]
```

=

```
[[ 27  31  35]
 [ 67  79  91]
 [-17 -19 -21]]
```

何次元配列→ 2  
何行、何列→ (3, 3)

## ニューラルネットワークにおける内積(ドット積)

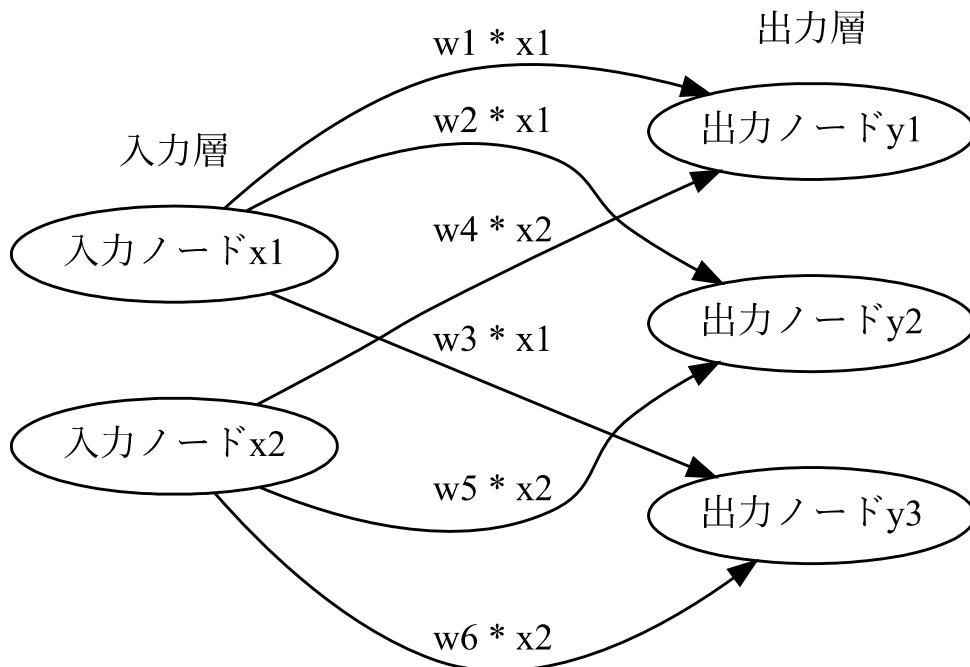
行列に見立てる事により、一度に計算が可能となり、なおかつ行列計算式が使用可能となる

一層ニューラルネットワークの場合（バイアス無し）

In [11]:

```
from graphviz import Digraph
dot = Digraph(comment="単純パーセプトロン")
dot.attr(rankdir="LR")
dot.attr(ranksep="1.0")
dot.attr(nodesep="0.5")
with dot.subgraph(name="cluster_x") as x:
    x.attr(label="入力層")
    x.attr(color="white")
    x.node("x1", "入力ノードx1")
    x.node("x2", "入力ノードx2")
with dot.subgraph(name="cluster_y") as y:
    y.attr(label="出力層")
    y.attr(color="white")
    y.node("y1", "出力ノードy1")
    y.node("y2", "出力ノードy2")
    y.node("y3", "出力ノードy3")
dot.edge("x1", "y1", label="w1 * x1")
dot.edge("x1", "y2", label="w2 * x1")
dot.edge("x1", "y3", label="w3 * x1")
dot.edge("x2", "y1", label="w4 * x2")
dot.edge("x2", "y2", label="w5 * x2")
dot.edge("x2", "y3", label="w6 * x2")
dot
```

Out[11]:



In [12]:

```
import numpy as np
x1 = 1
x2 = 2
X = np.array([x1, x2])
x1_W = [1, 3, 5]
x2_W = [2, 4, 6]
W = np.array([x1_W, x2_W])
Y = np.dot(X, W)
print("入力")
print(X)
print("出力重み")
print(W)
print("出力")
y1, y2, y3 = Y
print("y1=", y1)
print("y2=", y2)
print("y3=", y3)
#np.dotの一行で各行列の計算ができた→ニューラルネットワークの伝搬計算がすぐさま可能に
```

入力

[1 2]

出力重み

[[1 3 5]

[2 4 6]]

出力

y1= 5

y2= 11

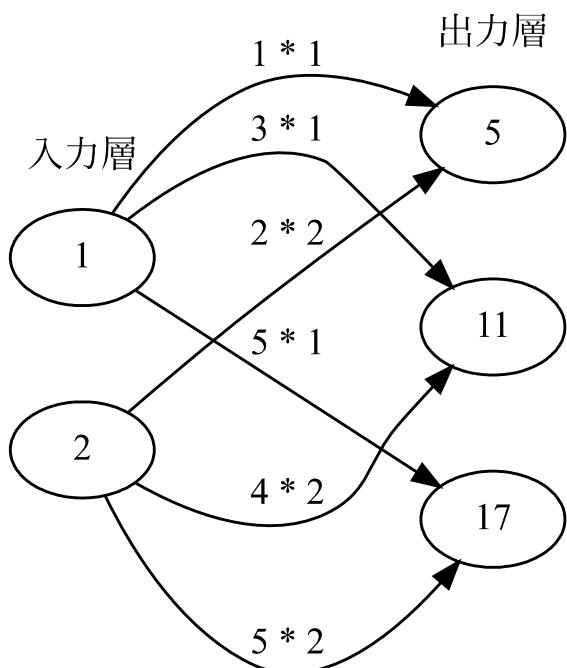
y3= 17

In [13]:

```
import numpy as np
x1 = 1
x2 = 2
X = np.array([x1, x2])
x1_W = [1, 3, 5]
x2_W = [2, 4, 6]
W = np.array([x1_W, x2_W])
Y = np.dot(X, W)
y1, y2, y3 = Y

from graphviz import Digraph
dot = Digraph(comment="単純パーセプトロン")
dot.attr(rankdir="LR")
dot.attr(ranksep="1.0")
dot.attr(nodesep="0.5")
with dot.subgraph(name="cluster_x") as x:
    x.attr(label="入力層")
    x.attr(color="white")
    x.node("x1", "1")
    x.node("x2", "2")
with dot.subgraph(name="cluster_y") as y:
    y.attr(label="出力層")
    y.attr(color="white")
    y.node("y1", "5")
    y.node("y2", "11")
    y.node("y3", "17")
dot.edge("x1", "y1", label="1 * 1")
dot.edge("x1", "y2", label="3 * 1")
dot.edge("x1", "y3", label="5 * 1")
dot.edge("x2", "y1", label="2 * 2")
dot.edge("x2", "y2", label="4 * 2")
dot.edge("x2", "y3", label="5 * 2")
dot
```

Out[13]:



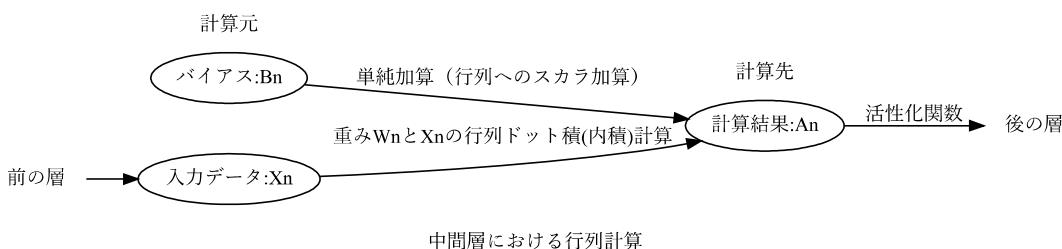
# 多層ニューラルネットワーク

In [14]:

```
from graphviz import Digraph
dot = Digraph()
dot.attr(label="中間層における行列計算")
dot.attr(rankdir="LR")
dot.attr(ranksep="0.5")
dot.attr(nodesep="0.5")
with dot.subgraph(name="cluster_in") as x:
    x.attr(label="")
    x.attr(color="white")
    x.node("in1", "前の層", color="white")
with dot.subgraph(name="cluster_x") as x:
    x.attr(label="計算元")
    x.attr(color="white")
    x.node("b1", "バイアス:Bn")
    x.node("x1", "入力データ:Xn")
with dot.subgraph(name="cluster_y") as y:
    y.attr(label="計算先")
    y.attr(color="white")
    y.node("y1", "計算結果:An")
with dot.subgraph(name="cluster_out") as y:
    y.attr(label="")
    y.attr(color="white")
    y.node("out1", "後の層", color="white")

dot.edge("in1", "x1", label="")
dot.edge("b1", "y1", label="単純加算（行列へのスカラ加算）")
dot.edge("x1", "y1", label="重みWnとXnの行列ドット積(内積)計算")
dot.edge("y1", "out1", label="活性化関数")
dot
```

Out[14]:



$$\text{Calc } A^n = XW^n + B^n \text{ Result } A^n = (a^1, a^2, a^3, \dots, a^n) \text{ Input } X^n = (x^1, x^2, \dots, x^n) \text{ Bias } B^n = (b^1, b^2, b^3, \dots, b^n) \text{ Weight } W^n = \left\{ \begin{array}{l} W_{(1,1)}, W_{(1,2)}, W_{(1,3)}, \dots \\ W_{(2,1)}, W_{(2,2)}, W_{(2,3)}, \dots \\ W_{(3,1)}, W_{(3,2)}, W_{(3,3)}, \dots \\ \dots \\ W_{(N,1)}, W_{(N,2)}, W_{(N,3)}, \dots \end{array} \right\}$$

In [15]:

```
X = np.array([1.0, 0.5])
W1 = np.array([[0.1, 0.3, 0.5], [0.2, 0.4, 0.6]])
B1 = np.array([0.1, 0.2, 0.3])
A1 = np.dot(X, W1) + B1
print("入力層の列数", X.shape)
print("中間層の入力層側行数、中間層の出力層側の列数", W1.shape)
print("出力層の行数", B1.shape)
print(A1)
```

```
入力層の列数 (2,)
中間層の入力層側行数、中間層の出力層側の列数 (2, 3)
出力層の行数 (3,)
[0.3 0.7 1.1]
```

層と層の間で要素数が異ならなければ、Xの要素数とW1の行数は合致することになるので行列の計算が可能。つまり、ただ一度も途中でニューロンの数が変わらない前提となるので入力層の数 = 計算結果の数となる。この場合、入力層を増やさなければ、計算結果も増えないため、入力層の数だけの特徴量しか持つことができない。

## 出力層の設計

### ソフトマックス関数

In [16]:

```
import numpy as np
def softmax(array):
    """一つの行列を0~1に直します。"""
    return np.exp(array) / np.sum(np.exp(array))
```

In [17]:

```
a1, a2, a3 = softmax([1, 2, 3])
print("a1, a2, a3=", a1, a2, a3)
print("SUM=", a1+a2+a3)
```

```
a1, a2, a3= 0.09003057317038046 0.24472847105479767 0.6652409557748219
SUM= 1.0
```

### 注意点

In [18]:

```
print(np.exp([1, 2, 100000])) #eの100000乗は64bit以上になるので、無限大と扱われてしまう。
```

```
[2.71828183 7.3890561 inf]
```

```
c:\Users\4037554\AppData\Local\Programs\Python\Python36-32\lib\site-packages\ipykernel_launcher.py:1: RuntimeWarning: overflow encountered in exp
    """Entry point for launching an IPython kernel.
```

In [19]:

```
import numpy as np
def softmax(array):
    """一つの行列を0~1に直します。inf簡易対策バージョン。"""
    array = array - np.max(array)
    return np.exp(array) / np.sum(np.exp(array))
```

In [20]:

```
a1, a2, a3 = softmax([1, 2, 3])
print("a1, a2, a3=", a1, a2, a3)
print("SUM=", a1+a2+a3)
```

```
a1, a2, a3= 0.09003057317038046 0.24472847105479764 0.6652409557748218
SUM= 0.9999999999999999
```

In [21]:

```
a1, a2, a3 = softmax([1, 2, 1000000])
print("a1, a2, a3=", a1, a2, a3)
print("SUM=", a1+a2+a3)
```

```
a1, a2, a3= 0.0 0.0 1.0
SUM= 1.0
```

ニューラルネットワークでは定数の大きさではなく影響力の大きさで計算するので、このオーバーフロー対策は不要

## ニューラルネットワーク層に関する注意点

- 入力層のニューロン数 = テストケースをベクトル化した際の種類の数、ただし異常値やNullを除去したもの
- 中間層のニューロン数 = ハイパー parameter
- 出力層のニューロン数 = 分類問題であるなら、分類されるべき種類の数、ただし確実にそれ以外の種類が出ないという保証があるもの

## MNIST 0-9画像データセット

利用の前にmnist.pyの中身を参照して元々の画像データがどういう形式で、どういう形に変換されたかを確認すること。例えば、訓練画像と全く同じデータがテスト画像の中に含まれていないかどうか、外れ値が無いかどうか、Nullが無いかどうか、など。（今回は入っていない）データのチェック及び加工処理がほとんどの工数を占める

In [22]:

```
import sys, os
sys.path.append(os.pardir) #mnist.pyを呼び出すための設定
from dataset.mnist import load_mnist

#flattenで行列ではなく配列にする
#normalizeで0~1に正規化する
(x_train, t_train), (x_test, t_test) = load_mnist(flatten=True, normalize=False)
#1画素 = 0~256

print(x_train.shape) # 784画素 x 6万件の学習データ
print(t_train.shape) # 6万件の学習ラベルデータ
print(x_test.shape) # 784画素 x 1万件のテストデータ
print(t_test.shape) # 1万件のテスストラベルデータ
```

```
(60000, 784)
(60000, )
(10000, 784)
(10000, )
```

- 今回は0~9の分類になるため、10個の出力層が必要となる
- 入力層は画素数になるので、784個
- 中間層は不明だが、10個以上でなければならない。

In [23]:

```
%matplotlib inline
#plt.show()をinlineにて表示する
#Esc+Lで行番号を表示する
import numpy as np
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
from dataset.mnist import load_mnist
from PIL import Image

(x_train, t_train), (x_test, t_test) = load_mnist(flatten=True, normalize=False)
img = x_train[0]
label = t_train[0]
img = img.reshape(28, 28)
print("行、列", img.shape)
print("とりあえず画像の表示=>", label)
img_data = Image.fromarray(np.uint8(img))
img_data
```

```
行、列 (28, 28)
とりあえず画像の表示=> 5
```

Out[23]:



In [24]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import pickle
from dataset.mnist import load_mnist
from common.functions import sigmoid, softmax

def init_network():
    """学習済の推論モデル(ただの重みとゲタの行列)を読み込む。"""
    with open("sample_weight.pkl", 'rb') as f:
        network = pickle.load(f)
    return network

network = init_network()

W1, W2, W3 = network['W1'], network['W2'], network['W3']
b1, b2, b3 = network['b1'], network['b2'], network['b3']
network = init_network()

def predict(network, x):
    a1 = np.dot(x, W1) + b1
    z1 = sigmoid(a1)
    a2 = np.dot(z1, W2) + b2
    z2 = sigmoid(a2)
    a3 = np.dot(z2, W3) + b3
    y = softmax(a3)
    return y

def get_data():
    """正規化済、配列化済のテストデータを読み込む"""
    (x_train, t_train), (x_test, t_test) = load_mnist(normalize=True, flatten=True, one_hot_label=False)
    return x_test, t_test

x, t = get_data()
accuracy_cnt = 0
for i in range(len(x)):
    y = predict(network, x[i])
    p= np.argmax(y) # 最も確率の高い要素のインデックスを取得
    if p == t[i]:
        accuracy_cnt += 1
print("正解率:" + str(float(accuracy_cnt) / len(x)) + "(" + str(int(accuracy_cnt))+"/"+str(len(x)) + ")")
```

正解率:0.9352 (9352 /10000)

In [25]:

W1.shape

Out[25]:

(784, 50)

In [26]:

W2.shape

Out[26]:

(50, 100)

In [27]:

W3.shape

Out[27]:

(100, 10)

入力層：入力の数と一致している。行数は固定。  
中間層：前の行列の列数と後の行列の行数が一致している。  
行数・列数は固定ではない。50と100の数字は適当に決めることもできるが大きいほど計算も増える。  
出力層：出力の数と一致している。列数は固定。

## バッチ処理

行列にスカラを掛けても同一の計算式になるため、入力層を100個にして出力層も100個にすることで同時計算することも可能

In [28]:

```
x, t = get_data()
network = init_network()

batch_size = 100
accuracy_cnt = 0
for i in range(0, len(x), batch_size):
    x_batch = x[i:i+batch_size]
    y_batch = predict(network, x_batch)
    p = np.argmax(y_batch, axis=1)
    accuracy_cnt += np.sum(p == t[i:i+batch_size])

print("正確さ：" + str(int(accuracy_cnt) / len(x)))
```

正確さ : 0.9352

正確さに変動が無いことを確認すること。

# ニューラルネットワークの学習

## 用語の説明

- データ駆動：人の意識なく集められたデータのみを信用する考え方
- 人駆動：人の意識によって集められた特徴量（ベクトル）、人の意識によって集められた分類法によって得られたデータを使用する考え方
- 教師データ：ニューラルネットワークでいう、学習データ。学習データはディープラーニングにおいてデータ駆動として扱う都合テストデータと一致してはならない。

## 過学習(overfitting)

ディープラーニングにおいて特定個人・個別のデータの特徴量のみ意識してしまい汎化能力に欠けてしまうこと。ディープラーニングに置いては 学習データ≠テストデータ≠将来的なデータ でなければならない。

## 損失関数(loss function)

出力における、テスト結果における正解との誤差のこと。平均二乗誤差(mean squared error)と交差エントロピー誤差 (cross entropy error) の二つが代表的にある。この損失関数の値が小さいほど正解に近いということになる。

### 平均二乗誤差

$$E = \frac{1}{2} \sum_k ((y_k - t_k)^2)$$

In [1]:

```
import numpy as np
import pandas as pd
def mean_squared_error(y, t):
    return 0.5 * np.sum((y-t)**2)
a1, a2 = np.asarray([1, 2, 3]), np.asarray([1, 2, 4])
print(mean_squared_error(a1, a2))
a1, a2 = np.asarray([1, 2, 3]), np.asarray([1, 2, 10])
print(mean_squared_error(a1, a2))
a1, a2 = np.asarray([1, 2, 3]), np.asarray([1, 2, 3])
print(mean_squared_error(a1, a2))
```

0.5  
24.5  
0.0

### 交差エントロピー誤差

$$E = -\sum_k (p_k \log q_k)$$
$$(0 \leq p \leq 1, 0 \leq q \leq 1)$$

## log(x)の関数の特徴

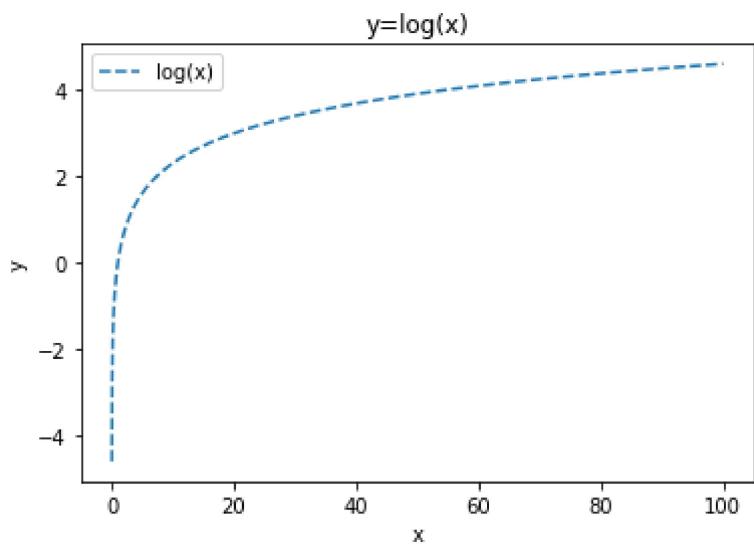
In [2]:

```
%matplotlib inline
# plt.show()をinlineにて表示する
# Esc+Lで行番号を表示する
import matplotlib.pyplot as plt
import numpy as np

import numpy as np
def log(x):
    return np.log(x)
x = np.arange(0.01, 100, 0.01)
y = log(x)

plt.plot(x, y, label="log(x)", linestyle="--")
plt.xlabel("x")
plt.ylabel("y")

plt.title("y=log(x)")
plt.legend() #show label box
plt.show()
plt.close()
```



## 交差エントロピー誤差の関数

In [3]:

```
def softmax(array):
    return np.exp(array) / np.sum(np.exp(array))
def cross_entropy_error(y, t):
    delta = 1e-7 #Avoid log(0) => Inf
    return -np.sum(t * np.log(y + delta))
```

In [4]:

```
t = [0, 0, 1, 0, 0, 0, 0, 0, 0] #One-Shot配列 (正解=1、不正解=0に正規化したもの)
y = [0.1, 0.05, 0.6, 0.0, 0.05, 0.1, 0.0, 0.1, 0.0, 0.0] #SoftMax関数により正規化済
print("SUM t =", np.sum(np.array(t)))
print("SUM y =", np.sum(np.array(y)))
print("交差エントロピー誤差 =", cross_entropy_error(np.array(y), np.array(t)))
t = [0, 0, 1, 0, 0, 0, 0, 0, 0] #One-Shot配列 (正解=1、不正解=0に正規化したもの)
y = [0.1, 0.05, 0.1, 0.0, 0.05, 0.1, 0.0, 0.6, 0.0, 0.0] #SoftMax関数により正規化済
print("SUM t =", np.sum(np.array(t)))
print("SUM y =", np.sum(np.array(y)))
print("交差エントロピー誤差 =", cross_entropy_error(np.array(y), np.array(t)))
```

SUM t = 1  
SUM y = 1.0  
交差エントロピー誤差 = 0.510825457099338  
SUM t = 1  
SUM y = 1.0  
交差エントロピー誤差 = 2.302584092994546

## ミニバッチ学習（サンプリング）

損失関数を行列横断的に実施するためには、以下の関数を用いる

$$E = -\frac{1}{N} \sum_n \sum_k (t_{nk} \log y_{nk})$$

関数は難しいが単純に損失関数を各配列ごとにやって最後に足しているだけ。それぞれの配列の内容や要素数はもちろん異なるため、それぞれ正規化されていることが条件。最後に誤差を平均化するため配列数で割る。（これにより、それぞれのバッチのパーセプトロンの数（=配列数）や次元数（=配列の長さ）を変動させてても互いに損失関数として比較可能とすることが出来る。） → 膨大なデータの中から任意の数のデータのみをサンプリングして機械学習に流し込むことができる、計算量を削減できる。しかも、サンプリングパーセンテージはその配列毎に変えることができる。（batch\_size）

## MNISTデータを使ってミニバッチ学習を実践

In [5]:

```
# MNISTデータのロード
import sys, os
sys.path.append(os.pardir) #mnist.pyを呼び出すための設定
from dataset.mnist import load_mnist

#flattenで行列ではなく配列にする
#normalizeで0~1に正規化する
(x_train, t_train), (x_test, t_test) = load_mnist(normalize=False, one_hot_label=True)
#1画素 = 0~256

print(x_train.shape) # 784画素 x 6万件の学習データ
print(t_train.shape) # 6万件の学習ラベルデータ
print(x_test.shape) # 784画素 x 1万件のテストデータ
print(t_test.shape) # 1万件のテストラベルデータ

(60000, 784)
(60000, 10)
(10000, 784)
(10000, 10)
```

In [6]:

```
#MNISTデータからランダムサンプリング
batch_size = 10
np.random.choice(x_train.shape[0], batch_size) #0~60000の配列のうち、どの配列を使うか選んで数字
でインデックスを返す
```

Out [6]:

```
array([11357, 23726, 38963, 48357, 18302, 45106, 47393, 21141, 52581,
       30185])
```

### ミニバッチ対応版（交差エントロピー誤差 損失関数の実装）

In [7]:

```
def cross_entropy_error(y, t):
    if y.ndim == 1:
        t = t.reshape(1, t.size)
        y = y.reshape(1, y.size)

    batch_size = y.shape[0]
    # One-Hot表現の場合、0 or 1なので、
    return -np.sum(np.log(y[np.arange(batch_size), t])) / batch_size
```

## 認識精度よりも損失度を認識度の指標とする理由

- 認識精度はどのレベルまで認識できれば良いのか上限が見えず、たまたま100%になる（微分し傾きが0になる場所が多く存在する）ことがありデータ表現として0~1の間で表せられないことが多い。（機械が扱うには少し弱いデータ）
- 誤差精度は滅多に100%になることがなく、ゆるやかに収束する（微分し傾きが0になる場所が滅多に存在しない）ため微細なパラメータ調整の結果得られる誤差移動率（=微分した際の傾き）が算出可能となり0~1の間で表せられる。（機械が扱いやすい）

In [8]:

```
%matplotlib inline
#plt.show()をinlineにて表示する
#Esc+Lで行番号を表示する
import matplotlib.pyplot as plt
import numpy as np

x1 = np.arange(-10, 10, 0.01) # -10 to 10 by 0.01
y1 = 1.0/(1.0 + np.e ** (-1.0*x1))

x2 = x1
y2 = x2*0

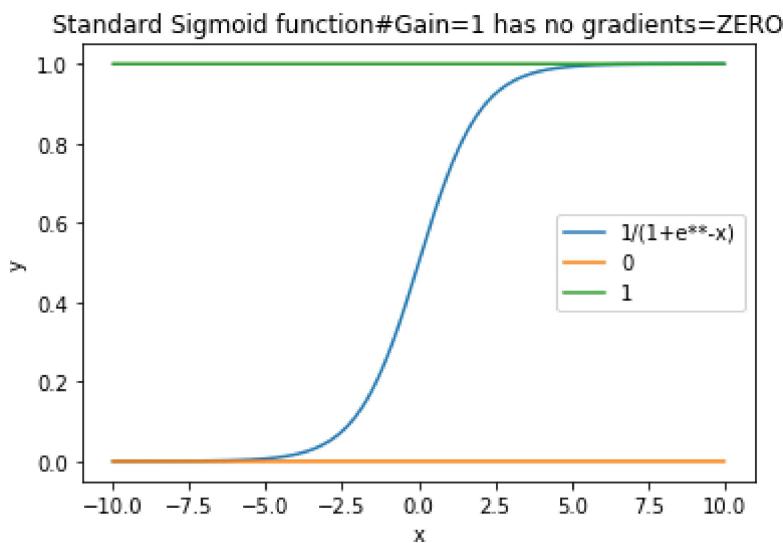
x3 = x1
y3 = x3*0+1

plt.plot(x1, y1, label="1/(1+e**-x)", linestyle="--")
plt.plot(x2, y2, label="0", linestyle="--")
plt.plot(x3, y3, label="1", linestyle="--")

plt.xlabel("x")
plt.ylabel("y")

plt.title("Standard Sigmoid function#Gain=1 has no gradients=ZERO")
plt.legend() #show label box

plt.show()
plt.close()
```



## 誤差の遷移に傾き（微分）を使う際の丸め誤差

In [9]:

```
np.float32(1e-50)
```

Out[9]:

```
0.0
```

## 微分方程式

$$f'(x) = \frac{d}{dx} f(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

## 数値微分プログラム

In [10]:

```
def numerical_diff(f, x):
    h = 10e-4
    return (f(x+h) - f(x)) / 2*h
```

## 解析的な微分と数値微分

- 数値的微分：最小の微動値(h)を+-し、結果の計算結果の差分を2で割る
- 解析的微分：微分方程式を使用し変数を残した状態で算出する

In [11]:

```
# coding: utf-8
import numpy as np
import matplotlib.pyplot as plt

def numerical_diff(f, x):
    h = 1e-4 # 0.0001
    return (f(x+h) - f(x-h)) / (2*h)

def function_1(x):
    return 0.01*x**2 + 0.1*x

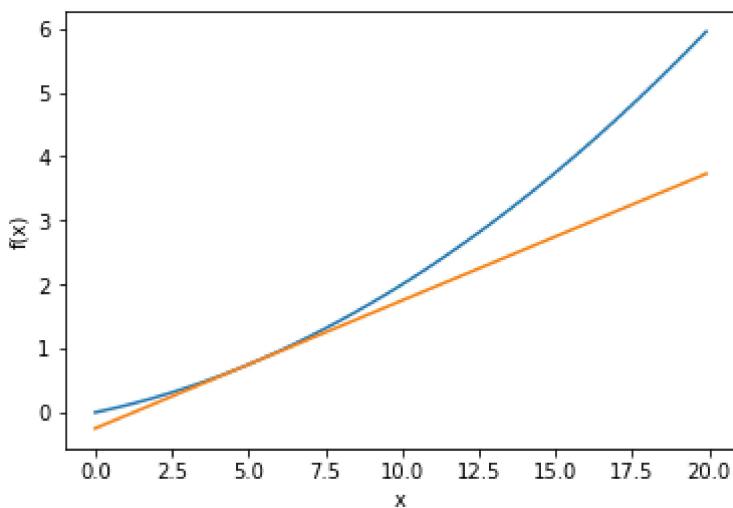
def tangent_line(f, x):
    d = numerical_diff(f, x)
    print(d)
    y = f(x) - d*x
    return lambda t: d*t + y

x = np.arange(0.0, 20.0, 0.1)
y = function_1(x)
plt.xlabel("x")
plt.ylabel("f(x)")

tf = tangent_line(function_1, 5)
y2 = tf(x)

plt.plot(x, y)
plt.plot(x, y2)
plt.show()
#傾きが0.2になっていない!
```

0.199999999990898



- 傾きが0.2になっていないが、接線にはなっているように見えることに着目する

## 偏微分

略（微分が対象軸（=変数）ごとに実施できることと、複数の微分演算子が微分の順番を変えても最終的に成り立つということが示されていること）

## 勾配

行列式において、全ての値についての偏微分を求めてベクトル化したものを勾配と呼ぶ。

In [12]:

```
def numerical_gradient(f, x):
    """f関数におけるx配列の数値微分をし、それぞれの値の勾配（微分した際の傾きを返します）をxと同じ列数の配列で返します。"""
    h = 1e-4 # 0.0001 (微動)
    grad = np.zeros_like(x) # 0 * xと同義

    for idx in range(x.size):

        #一旦退避。
        tmp_val = x[idx]

        #もしプラスの方向に微動した場合の結果は？
        x[idx] = float(tmp_val) + h
        fxh1 = f(x) # f(x+h)

        #もしマイナスの方向に微動した場合の結果は？
        x[idx] = tmp_val - h
        fxh2 = f(x) # f(x-h)

        #配列を数値微分
        grad[idx] = (fxh1 - fxh2) / (2*h)

        #傾きの計算が終わったので、一旦値を戻す
        x[idx] = tmp_val

    return grad
```

勾配降下のイメージ図（2次元関数の場合）→傾きが0に収束するためのベクトルがプロットされる

In [13]:

```
# coding: utf-8
# cf. http://d.hatena.ne.jp/white_wheels/20100327/p3
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

def _numerical_gradient_no_batch(f, x):
    h = 1e-4 # 0.0001
    grad = np.zeros_like(x)

    for idx in range(x.size):
        tmp_val = x[idx]
        x[idx] = float(tmp_val) + h
        fxh1 = f(x) # f(x+h)

        x[idx] = tmp_val - h
        fxh2 = f(x) # f(x-h)
        grad[idx] = (fxh1 - fxh2) / (2*h)

        x[idx] = tmp_val # 値を元に戻す

    return grad

def numerical_gradient(f, X):
    if X.ndim == 1:
        return _numerical_gradient_no_batch(f, X)
    else:
        grad = np.zeros_like(X)

        for idx, x in enumerate(X):
            grad[idx] = _numerical_gradient_no_batch(f, x)

        return grad

def function_2(x):
    if x.ndim == 1:
        return np.sum(x**2)
    else:
        return np.sum(x**2, axis=1)

def tangent_line(f, x):
    d = numerical_gradient(f, x)
    print(d)
    y = f(x) - d*x
    return lambda t: d*t + y

if __name__ == '__main__':
    x0 = np.arange(-2, 2.5, 0.25)
    x1 = np.arange(-2, 2.5, 0.25)
    X, Y = np.meshgrid(x0, x1)

    X = X.flatten()
    Y = Y.flatten()

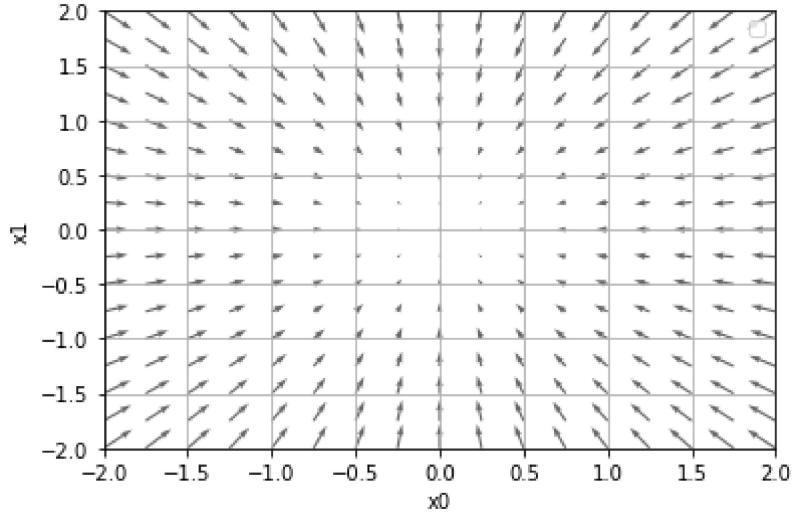
    grad = numerical_gradient(function_2, np.array([X, Y]) )
```

```

plt.figure()
plt.quiver(X, Y, -grad[0], -grad[1], angles="xy", color="#666666") #, headwidth=10, scale=40, color="#444444")
plt.xlim([-2, 2])
plt.ylim([-2, 2])
plt.xlabel('x0')
plt.ylabel('x1')
plt.grid()
plt.legend()
plt.draw()
plt.show()

```

No handles with labels found to put in legend.



関数が収束する方向にベクトルが向いていることに注意。

## 勾配法

関数の傾きが0となる点を目指して関数の値を徐々に収束させる手法。今回の場合は損失関数を0に収束させるため、勾配降下法と呼ぶ。

## 勾配法

$$x_1 = x_0 - \eta \frac{\partial f}{\partial x_0}, \quad x_2 = x_1 - \eta \frac{\partial f}{\partial x_1}, \dots$$

$\eta = \text{learning rate} (\text{e.g., } 0.1, 0.001, \dots)$

## 勾配法プログラム

In [14]:

```
import numpy as np
import matplotlib.pyplot as plt
from gradient_2d import numerical_gradient

def gradient_descent(f, init_x, lr=0.01, step_num=100):
    """f : 最適化が必要な関数, init_xは初期値, lrは学習率, step_numは勾配降下回数. fの傾きが最小となるような"""
    x = init_x
    x_history = []

    for i in range(step_num):
        x_history.append( x.copy() )

        grad = numerical_gradient(f, x)
        x -= lr * grad

    return x, np.array(x_history)
```

$$f(x_0, x_1) = x_0^2 + x_1^2$$

の最小値を勾配法プログラムによって求める。

In [15]:

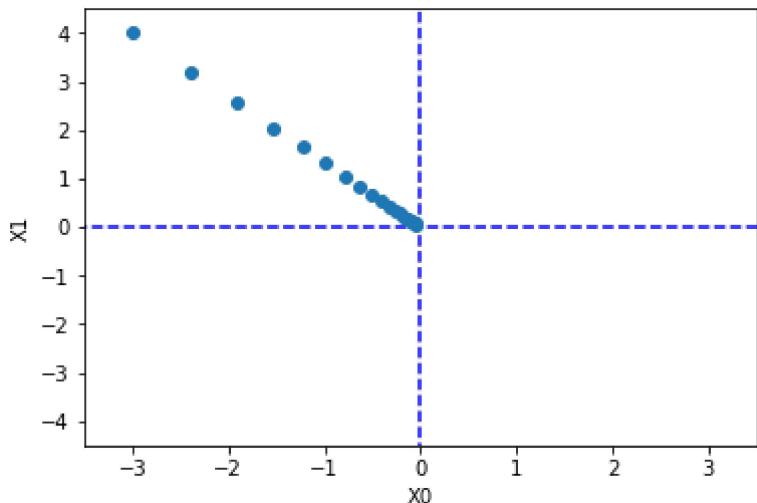
```
def function_2(x):
    return x[0]**2 + x[1]**2

init_x = np.array([-3.0, 4.0])

lr = 0.1
step_num = 20
x, x_history = gradient_descent(function_2, init_x, lr=lr, step_num=step_num)

plt.plot([-5, 5], [0, 0], '--b')
plt.plot([0, 0], [-5, 5], '--b')
plt.plot(x_history[:, 0], x_history[:, 1], 'o')

plt.xlim(-3.5, 3.5)
plt.ylim(-4.5, 4.5)
plt.xlabel("X0")
plt.ylabel("X1")
plt.show()
```



$$\begin{aligned}(kf_x) &= kf_x \\(f \pm g)_x &= f_x \pm g_x \\(f \cdot g)_x &= f_x \cdot g + f \cdot g_x \\ \left(\frac{f}{g}\right)_x &= \frac{f_x \cdot g - f \cdot g_x}{g^2} \\ \frac{\partial f}{\partial x} &= \frac{df}{du} \frac{\partial u}{\partial x} \\ \frac{\partial f}{\partial y} &= \frac{df}{du} \frac{\partial u}{\partial y}\end{aligned}$$

## ニューラルネットワーク（行列式）における勾配降下プログラム

In [16]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
from common.functions import softmax, cross_entropy_error
from common.gradient import numerical_gradient

class simpleNet:
    def __init__(self):
        self.W = np.random.randn(2, 3) # 2行x3列の行列として作成
        # ガウス分布で初期化

    def predict(self, x):
        """内積をとる（自身のW（重み）を積算）"""
        return np.dot(x, self.W)

    def loss(self, x, t):
        """x = 入力データ、t = テストデータ"""
        z = self.predict(x)
        y = softmax(z) # 0~1の値へと汎化
        loss = cross_entropy_error(y, t) # tはone-shot行列とする（正解=1、不正解=0）

        return loss

x = np.array([0.6, 0.9]) # 1行2列
t = np.array([0, 0, 1]) # 1行3列

net = simpleNet()
f = lambda w: net.loss(x, t)
dW = numerical_gradient(f, net.W)

print("W=", net.W)
print("dW=", dW)
print("WをdWを下げるようベクトルを向ける必要がある")

W= [[-0.29987897 -2.12317372  0.47065595]
 [-0.39304798 -0.98756266 -0.75852701]]
dW= [[ 0.25654033  0.05031211 -0.30685244]
 [ 0.38481049  0.07546816 -0.46027865]]
WをdWを下げるようベクトルを向ける必要がある
```

## 学習アルゴリズムの実装

## 1. ミニバッチ（訓練データサンプリング）

- 訓練データの中からランダムに一部のデータを選びだす。その選ばれたデータをミニバッチと言い、ここでは、そのミニバッチの損失関数の値を減らすことを目的とする。（ミニバッチは無作為サンプリングの手法のため、**確率的勾配降下法(stochastic gradient descent, SGD)**と呼ばれる）

## 2. 勾配算出

- ミニバッチの損失関数を減らすために、各重みのパラメータの勾配を求める。勾配は損失関数の値をもっとも減らす方向を示す。

## 3. パラメータの更新

- 重みパラメータを勾配方向に微小量だけ更新する。

## 4. 繰り返し

- 1 ~ 3 の繰り返し

In [17]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
from common.functions import *
from common.gradient import numerical_gradient

class TwoLayerNet:
    """
    2層ニューラルネットワークの実装
    """

    def __init__(self, input_size, hidden_size, output_size, weight_init_std=0.01):
        """input_size = 入力の数(MNISTの場合、28 x 28の画素=784), hidden_size = 隠れ層の数(ハイパー-パラメータ), output_size = 出力の数(MNISTの場合、0~9の数字=10), weight_init_std = 重みの標準化引数(?)"""
        # 重みの初期化
        self.params = {}
        self.params['W1'] = weight_init_std * np.random.randn(input_size, hidden_size) #ガウス分布による重みパラメータの初期化
        self.params['b1'] = np.zeros(hidden_size) #一様分布によるバイアスパラメータの初期化
        self.params['W2'] = weight_init_std * np.random.randn(hidden_size, output_size) #ガウス分布による重みパラメータの初期化
        self.params['b2'] = np.zeros(output_size) #一様分布によるバイアスパラメータの初期化

    def predict(self, x):
        """入力に対する出力を確率配列として返す"""
        W1, W2 = self.params['W1'], self.params['W2']
        b1, b2 = self.params['b1'], self.params['b2']

        a1 = np.dot(x, W1) + b1
        z1 = sigmoid(a1)
        a2 = np.dot(z1, W2) + b2
        y = softmax(a2)

        return y

    # x:入力データ, t:教師データ
    def loss(self, x, t):
        """誤差を交差エントロピー誤差関数によって返す(y = 確率配列, t = one-hot配列)"""
        y = self.predict(x)
        return cross_entropy_error(y, t)

    def accuracy(self, x, t):
        """正確度を返す。x = 入力データ、t = テストデータ、accuracy = **%"""
        y = self.predict(x)
        y = np.argmax(y, axis=1)
        t = np.argmax(t, axis=1)

        accuracy = np.sum(y == t) / float(x.shape[0])
        return accuracy

    # x:入力データ, t:教師データ
    def numerical_gradient(self, x, t):
        loss_W = lambda W: self.loss(x, t)

        grads = {}
        grads['W1'] = numerical_gradient(loss_W, self.params['W1'])
        grads['b1'] = numerical_gradient(loss_W, self.params['b1'])
        grads['W2'] = numerical_gradient(loss_W, self.params['W2'])
```

```

grads['b2'] = numerical_gradient(loss_W, self.params['b2'])

return grads

def gradient(self, x, t):
    W1, W2 = self.params['W1'], self.params['W2']
    b1, b2 = self.params['b1'], self.params['b2']
    grads = {}

    batch_num = x.shape[0]

    # forward
    a1 = np.dot(x, W1) + b1
    z1 = sigmoid(a1)
    a2 = np.dot(z1, W2) + b2
    y = softmax(a2)

    # backward
    dy = (y - t) / batch_num
    grads['W2'] = np.dot(z1.T, dy)
    grads['b2'] = np.sum(dy, axis=0)

    da1 = np.dot(dy, W2.T)
    dz1 = sigmoid_grad(a1) * da1
    grads['W1'] = np.dot(x.T, dz1)
    grads['b1'] = np.sum(dz1, axis=0)

    return grads

```

## 2層ニューラルネットワークを使った学習

In [18]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from two_layer_net import TwoLayerNet

# データの読み込み
(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True, one_hot_label=True)

network = TwoLayerNet(input_size=784, hidden_size=50, output_size=10)

iters_num = 10000 # 繰り返しの回数を適宜設定する
train_size = x_train.shape[0]
batch_size = 100
learning_rate = 0.1

train_loss_list = []
train_acc_list = []
test_acc_list = []

iter_per_epoch = max(train_size / batch_size, 1)

for i in range(iters_num):
    batch_mask = np.random.choice(train_size, batch_size)
    x_batch = x_train[batch_mask]
    t_batch = t_train[batch_mask]

    # 勾配の計算
    #grad = network.numerical_gradient(x_batch, t_batch)
    grad = network.gradient(x_batch, t_batch)

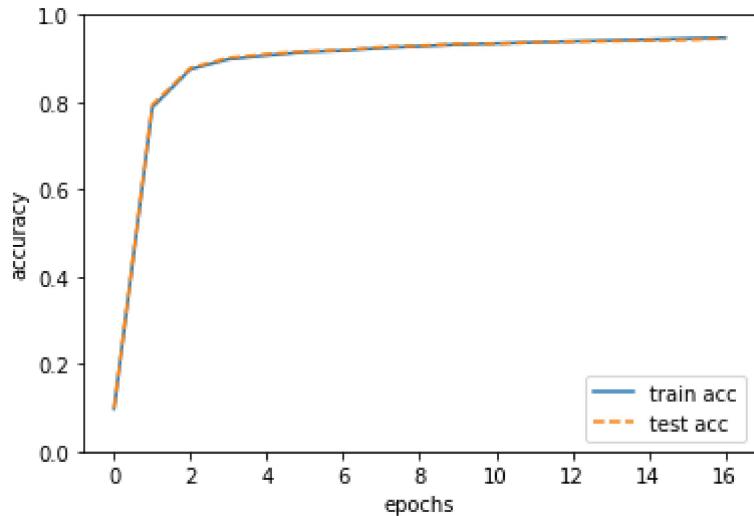
    # パラメータの更新
    for key in ('W1', 'b1', 'W2', 'b2'):
        network.params[key] -= learning_rate * grad[key]

    loss = network.loss(x_batch, t_batch)
    train_loss_list.append(loss)

    if i % iter_per_epoch == 0:
        train_acc = network.accuracy(x_train, t_train)
        test_acc = network.accuracy(x_test, t_test)
        train_acc_list.append(train_acc)
        test_acc_list.append(test_acc)
        print("train acc, test acc | " + str(train_acc) + ", " + str(test_acc))

# グラフの描画
markers = {'train': 'o', 'test': 's'}
x = np.arange(len(train_acc_list))
plt.plot(x, train_acc_list, label='train acc')
plt.plot(x, test_acc_list, label='test acc', linestyle='--')
plt.xlabel("epochs")
plt.ylabel("accuracy")
plt.ylim(0, 1.0)
plt.legend(loc='lower right')
plt.show()
```

train acc, test acc	0.09736666666666667, 0.0982
train acc, test acc	0.7876666666666666, 0.7933
train acc, test acc	0.8752166666666666, 0.8781
train acc, test acc	0.89835, 0.9014
train acc, test acc	0.906933333333334, 0.9097
train acc, test acc	0.91465, 0.916
train acc, test acc	0.91805, 0.919
train acc, test acc	0.92405, 0.926
train acc, test acc	0.927983333333334, 0.9289
train acc, test acc	0.9319166666666666, 0.9331
train acc, test acc	0.93435, 0.9334
train acc, test acc	0.936883333333333, 0.9367
train acc, test acc	0.939383333333333, 0.9385
train acc, test acc	0.9413, 0.9398
train acc, test acc	0.9433666666666667, 0.9411
train acc, test acc	0.945683333333333, 0.9425
train acc, test acc	0.9476, 0.9463



学習データにおける正確さとテストデータにおける正確さが概ね合致しているので、「過学習」は起きていないと思われる！

# 誤差逆伝播法

バックプロパゲーション, Backpropagation

(<https://ja.wikipedia.org/wiki/%E3%83%90%E3%83%83%E3%82%AF%E3%83%97%E3%83%AD%E3%83%C9>)のこと。ニューロン単位で損失関数計算し「局所誤差」を求め、ニューロンに対する入力の内、より大きな重みで接続された前段のニューロンに対して、局所誤差の責任があると判定する。連鎖律により、層全体のニューロンに対する入力を集積させてその入力を呼び起こしたニューロンを特定し、重みの傾斜を再計算することで責任を逆伝播させる。



## 連鎖律

連鎖律 (<https://ja.wikipedia.org/wiki/%E9%80%A3%E9%8E%96%E5%BE%8B>)とは微分法において以下の性質が成り立つ式のこと。合成関数の導関数の積が元の構成関数の導関数と等しくなる。

$$\frac{dz}{dx} = \frac{dz}{dt} \frac{dt}{dx}$$

## 計算グラフに置ける誤差逆伝播

誤差逆伝播法のための計算グラフまとめ

(<http://marumaru.tonkotsu.jp/%E8%AA%A4%E5%B7%AE%E9%80%86%E4%BC%9D%E6%92%AD%E6%B3%8B>)  
より

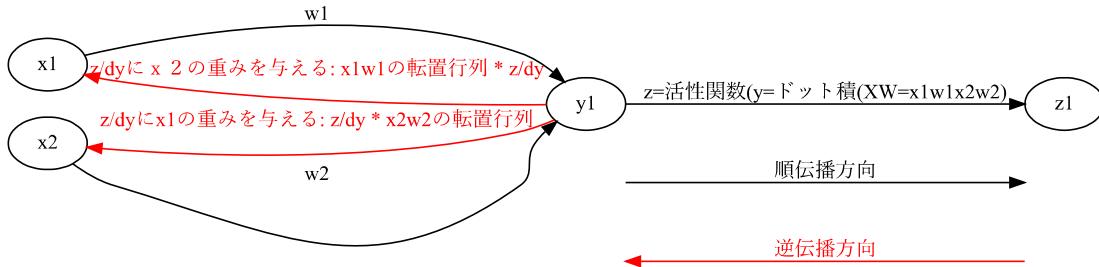


## ドット積の逆伝播

In [1]:

```
from graphviz import Digraph
dot = Digraph(comment="ドット積の逆伝播")
dot.attr(rankdir="LR")
#dot.attr(splines="line") #line or curved or ortho or polyline:
dot.attr(fixedsize="true")
dot.attr(label="ドット積の逆伝播（単純に転置行列をしかるべき方向から掛け合わせて元の行列に戻すだけ）")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "x1")
        x.node("x2", "x2")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y0", "y0", color="white", fontcolor="white")
        y.node("y1", "y1")
        y.node("y2", "y2", color="white", fontcolor="white")
    dot.edge("x1", "y1", label="w1")
    dot.edge("x2", "y1", label="w2")
    with main.subgraph(name="cluster_z") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z0", "z0", color="white", fontcolor="white")
        z.node("z1", "z1")
        z.node("z2", "z2", color="white", fontcolor="white")
    main.edge("y0", "z0", label="順伝播方向")
    main.edge("z2", "y2", label="逆伝播方向", color="red", fontcolor="red")
    main.edge("y1", "z1", label="z=活性関数(y=ドット積(XW=x1w1x2w2))")
    main.edge("y1", "x1", label="z/dyにx2の重みを与える: x1w1の転置行列 * z/dy", color="red", fontcolor="red")
    main.edge("y1", "x2", label="z/dyにx1の重みを与える: z/dy * x2w2の転置行列", color="red", fontcolor="red")
    #print(dot)
dot
```

Out[1]:



ドット積の逆伝播（単純に転置行列をしかるべき方向から掛け合わせて元の行列に戻すだけ）

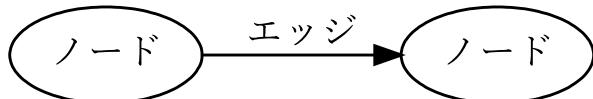
## 計算グラフの復習

以下のようなグラフで表されたもの

In [2]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="line") #line or curved or ortho or polyline:
dot.attr(fixedsize="true")
dot.attr(label="計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "ノード")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "ノード")
    dot.edge("x1", "y1", label="エッジ")
#print(dot)
dot
```

Out[2]:



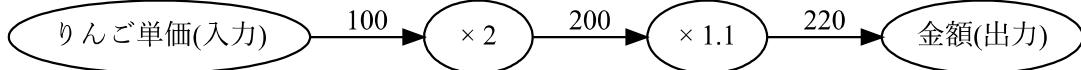
計算グラフ

問1. 太郎くんはスーパーで一個100円のりんごを2個買いました。支払う金額を求めなさい。ただし、消費税が10%適用されるものとします。

In [3]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="line") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="エッジを計算結果、ノードを計算式とした計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "りんご単価(入力)")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "\times 2")
    with main.subgraph(name="cluster_y") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z1", "\times 1.1")
    with main.subgraph(name="cluster_y") as out:
        out.attr(label="")
        out.attr(color="white")
        out.node("out1", "金額(出力)")
    dot.edge("x1", "y1", label="100")
    dot.edge("y1", "z1", label="200")
    dot.edge("z1", "out1", label="220")
#print(dot)
dot
```

Out[3]:



エッジを計算結果、ノードを計算式とした計算グラフ

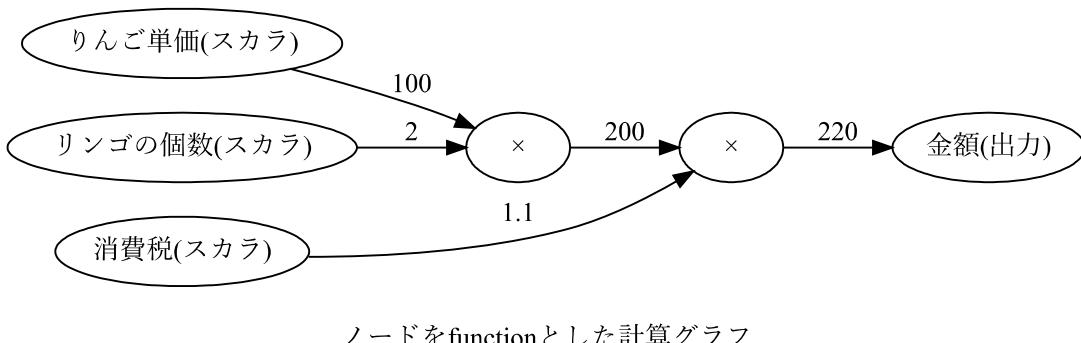
In [4]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="")
dot.attr(fixedsize="true")
dot.attr(label="ノードをfunctionとした計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "りんご単価(スカラ)")
        x.node("x2", "リンゴの個数(スカラ)")
        x.node("x3", "消費税(スカラ)")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "×")
    with main.subgraph(name="cluster_z") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z1", "×")
    with main.subgraph(name="cluster_out") as out:
        out.attr(label="")
        out.attr(color="white")
        out.node("out1", "金額(出力)")

    dot.edge("x1", "y1", label="100")
    dot.edge("x2", "y1", label="2")
    dot.edge("x3", "z1", label="1.1")
    dot.edge("y1", "z1", label="200")
    dot.edge("z1", "out1", label="220")

#print(dot)
dot
```

Out[4]:

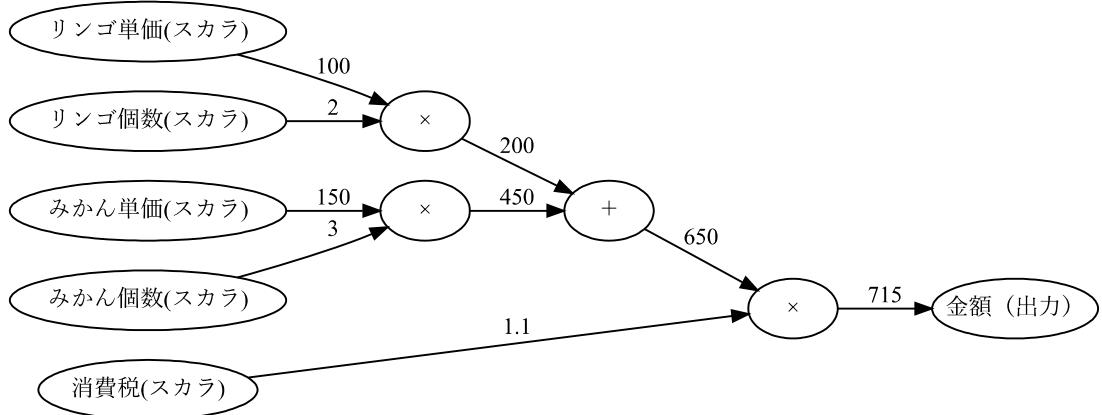


問2. 太郎くんはスーパーで一個100円のりんごを2個、1個150円のみかんを3個買いました。支払う金額を求めなさい。ただし、消費税が10%適用されるものとします。

In [5]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="積算ノードと加算ノードをあわせた計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "りんご単価(スカラ)")
        x.node("x2", "りんご個数(スカラ)")
        x.node("x3", "みかん単価(スカラ)")
        x.node("x4", "みかん個数(スカラ)")
        x.node("x5", "消費税(スカラ)")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "×")
        y.node("y2", "×")
    with main.subgraph(name="cluster_z") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z1", "+")
    with main.subgraph(name="cluster_a") as a:
        a.attr(label="")
        a.attr(color="white")
        a.node("a1", "×")
    with main.subgraph(name="cluster_out") as out:
        out.attr(label="")
        out.attr(color="white")
        out.node("out1", "金額(出力) ")
    dot.edge("x1", "y1", label="100")
    dot.edge("x2", "y1", label="2")
    dot.edge("x3", "y2", label="150")
    dot.edge("x4", "y2", label="3")
    dot.edge("y1", "z1", label="200")
    dot.edge("y2", "z1", label="450")
    dot.edge("z1", "a1", label="650")
    dot.edge("x5", "a1", label="1.1")
    dot.edge("a1", "out1", label="715")
#print(dot)
dot
```

Out[5]:



積算ノードと加算ノードをあわせた計算グラフ

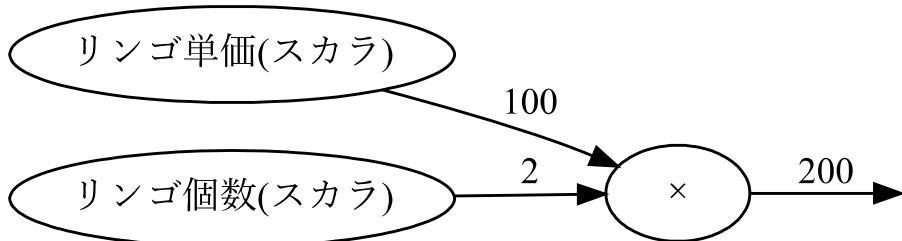
## 局所的な計算

一部のみを抜粋しても計算が可能であるということが、一つの計算ノードの再利用可能性を示している。

In [6]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="積算ノードと加算ノードをあわせた計算グラフ（局地的な計算）")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "リンゴ単価(スカラ)")
        x.node("x2", "リンゴ個数(スカラ)")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "×")
    with main.subgraph(name="cluster_z") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z1", "", color="white")
    dot.edge("x1", "y1", label="100")
    dot.edge("x2", "y1", label="2")
    dot.edge("y1", "z1", label="200")
#print(dot)
dot
```

Out[6]:



積算ノードと加算ノードをあわせた計算グラフ（局地的な計算）

## 逆伝搬の例

In [7]:

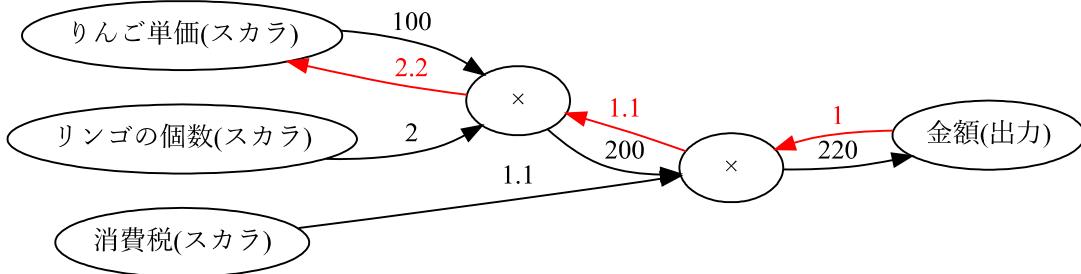
```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="")
dot.attr(fixedsize="true")
dot.attr(label="ノードをfunctionとした計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "りんご単価(スカラ)")
        x.node("x2", "リンゴの個数(スカラ)")
        x.node("x3", "消費税(スカラ)")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "×")
    with main.subgraph(name="cluster_z") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z1", "×")
    with main.subgraph(name="cluster_out") as out:
        out.attr(label="")
        out.attr(color="white")
        out.node("out1", "金額(出力)")

    #Forward propagation
    dot.edge("x1", "y1", label="100")
    dot.edge("x2", "y1", label="2")
    dot.edge("x3", "z1", label="1.1")
    dot.edge("y1", "z1", label="200")
    dot.edge("z1", "out1", label="220")

    #Back propagation
    dot.edge("out1", "z1", label="1", color="red", fontcolor="red")
    dot.edge("z1", "y1", label="1.1", color="red", fontcolor="red")
    dot.edge("y1", "x1", label="2.2", color="red", fontcolor="red")

# print(dot)
dot
```

Out[7]:



ノードをfunctionとした計算グラフ

りんごが「1」微動した場合の価格の微動は「2.2」であることが示されている。

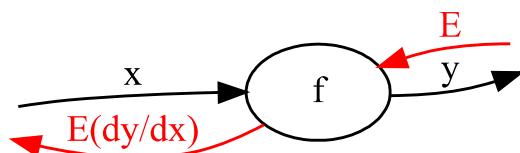
# 連鎖律

## 計算グラフの逆伝搬

In [8]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="line") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="計算グラフの逆伝搬")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_x") as x:
        x.attr(label="")
        x.attr(color="white")
        x.node("x1", "", color="white")
    with main.subgraph(name="cluster_y") as y:
        y.attr(label="")
        y.attr(color="white")
        y.node("y1", "f")
    with main.subgraph(name="cluster_y") as z:
        z.attr(label="")
        z.attr(color="white")
        z.node("z1", "", color="white")
    dot.edge("x1", "y1", label="x")
    dot.edge("y1", "z1", label="y")
    dot.edge("z1", "y1", label="E", color="red", fontcolor="red")
    dot.edge("y1", "x1", label="E(dy/dx)", color="red", fontcolor="red")
#print(dot)
dot
```

Out[8]:



計算グラフの逆伝搬

- $x$ : 下流から得たスカラ値
- $y$ :  $f(x)$
- $E$ : 上流から得たスカラ値
- $dy/dx$ : 関数 $f$ の導関数

## 連鎖律とは

ある関数が合成関数で表すことができる場合、その合成関数の微分は、合成関数を構成するそれぞれの関数の微分の積によって表すことができる。これを連鎖律の原理と呼ぶ。各ノードの微分式が逆伝搬の際に元の式の有効性を保ちつつそのまま伝達できることを示している。

## $y = (x + y)^2$ の微分の例

$y = (x + y)^2$  は以下のような変数  $z$  と  $t$  によって表せる。

式1.  $z = t^2$

式2.  $t = x + y$

式1,式2を合成関数と呼ぶ。

$y = (x + y)^2$  の導関数は  $\frac{\partial y}{\partial x}$

$z = t^2$  の導関数は  $\frac{\partial z}{\partial t}$

であるので、連鎖律によりこの合成関数の導関数は

$$\frac{\partial z}{\partial x} = \frac{\partial z}{\partial t} \frac{\partial t}{\partial x} \text{ となる。}$$

$\partial t$  は積算で互いに打ち消し合い、最終的に元の式の導関数に戻ることを確認する。

## 合成関数の微分の計算

$\frac{\partial z}{\partial x} = \frac{\partial z}{\partial t} \frac{\partial t}{\partial x}$  を計算する。

- $\frac{\partial z}{\partial t} = 2t$  (通常の解析微分)
- $\frac{\partial t}{\partial x} = 1$

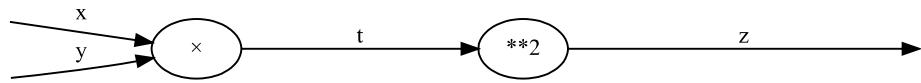
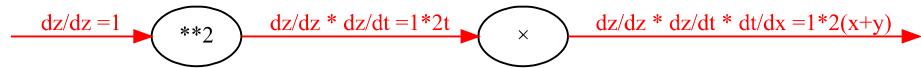
$t$  を展開すると  $2(x + y)$ 。この結果は  $y = (x + y)^2$  の導関数:  $\frac{\partial y}{\partial x}$  と一致することを確認する。

## $y = (x + y)^2$ を計算グラフで示す

In [9]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(ranksep="1.2")
dot.attr(nodesep=".05")
#dot.attr(margin="1")
#dot.attr(splines="polyline") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="y = x^2の計算グラフと逆伝搬計算グラフ（赤字）")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("main.L1N1", "", color="white")
        L1.node("main.L1N2", "", color="white")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("main.L2N1", "x")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("main.L3N1", "**2")
    with main.subgraph(name="cluster_a") as L4:
        L4.attr(label="")
        L4.attr(color="white")
        L4.node("main.L4N1", "", color="white")
    #Forward Propagation
    dot.edge("main.L1N1", "main.L2N1", label="x")
    dot.edge("main.L1N2", "main.L2N1", label="y")
    dot.edge("main.L2N1", "main.L3N1", label="t")
    dot.edge("main.L3N1", "main.L4N1", label="z")
with dot.subgraph(name="sub") as sub:
    with sub.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("sub.L1N1", "", color="white")
        L1.node("sub.L1N2", "", color="white")
    with sub.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("sub.L2N1", "x")
    with sub.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("sub.L3N1", "**2")
    with sub.subgraph(name="cluster_a") as L4:
        L4.attr(label="")
        L4.attr(color="white")
        L4.node("sub.L4N1", "", color="white")
    #Back Propagation
    dot.edge("sub.L4N1", "sub.L3N1", label="dz/dz =1", color="red", fontcolor="red")
    dot.edge("sub.L3N1", "sub.L2N1", label="dz/dz * dz/dt =1*2t", color="red", fontcolor="red")
    dot.edge("sub.L2N1", "sub.L1N1", label="dz/dz * dz/dt * dt/dx =1*2(x+y)", color="red", fontcolor="red")
    #dot.edge("L2N1", "L1N2", label="", color="red", fontcolor="red")
#print(dot)
dot
```

Out[9]:



$y = x^2$  の計算グラフと逆伝搬計算グラフ（赤字）

あらゆる式は2入力1出力の計算グラフに直すことが出来る

例

$$f(x, y, z) = 2x + 3y * 4z$$

In [10]:

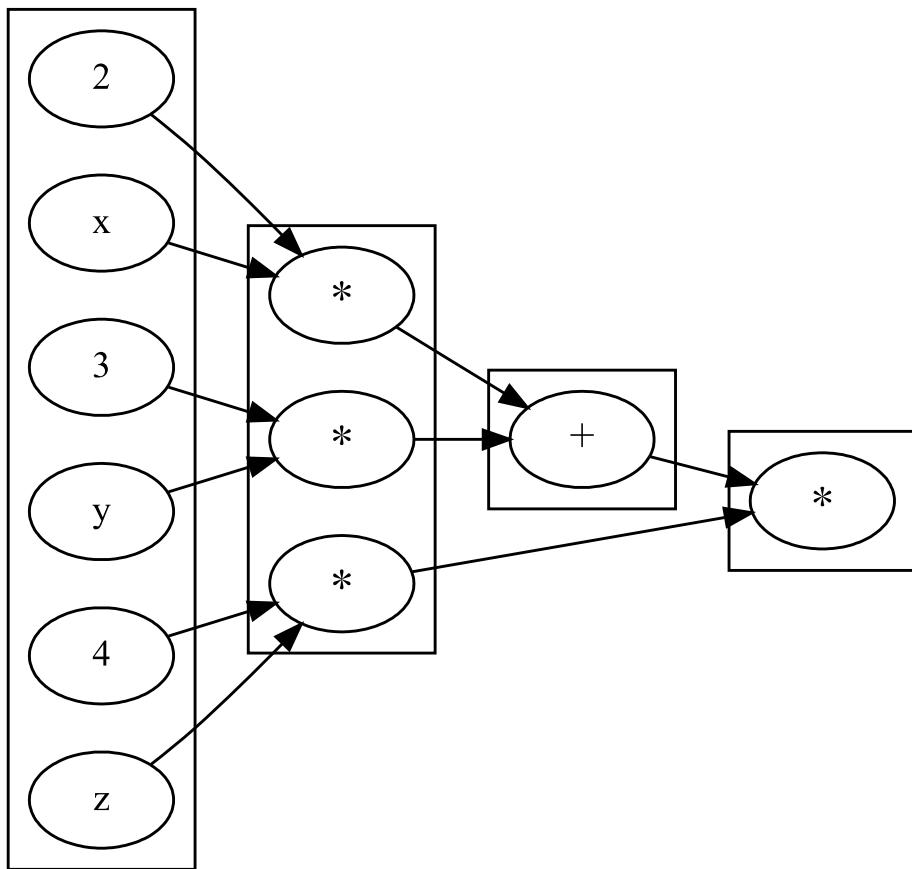
```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="f(x, y, z) = 2x + 3y * 4zの計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.node("L1N1", "2")
        L1.node("L1N2", "x")
        L1.node("L1N3", "3")
        L1.node("L1N4", "y")
        L1.node("L1N5", "4")
        L1.node("L1N6", "z")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.node("L2N1", "*")
        L2.node("L2N2", "*")
        L2.node("L2N3", "*")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.node("L3N1", "+")
    with main.subgraph(name="cluster_L4") as L4:
        L4.attr(label="")
        L4.node("L4N1", "*")
    dot.edge("L1N1", "L2N1", label="")
    dot.edge("L1N2", "L2N1", label="")
    dot.edge("L1N3", "L2N2", label="")
    dot.edge("L1N4", "L2N2", label="")
    dot.edge("L1N5", "L2N3", label="")
    dot.edge("L1N6", "L2N3", label="")

    dot.edge("L2N1", "L3N1", label="")
    dot.edge("L2N2", "L3N1", label="")

    dot.edge("L3N1", "L4N1", label="")
    dot.edge("L2N3", "L4N1", label="")

#print(dot)
dot
```

Out[10]:



$$f(x,y,z) = 2x + 3y * 4z \text{ の計算グラフ}$$

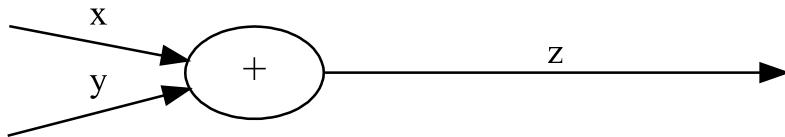
片方の成分での微分を（双方に対する誤差として）逆伝搬させることで、**より誤差を大きく出した片方に責任を負わせることが可能となる**ことが分かる。これが計算グラフによって示されている。

## 加算ノードの逆伝搬

In [11]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="加算ノード計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("main.L1N1", "", color="white")
        L1.node("main.L1N2", "", color="white")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("main.L2N1", "+")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("main.L3N1", "", color="white")
    #Forward Propagation
    dot.edge("main.L1N1", "main.L2N1", label="x")
    dot.edge("main.L1N2", "main.L2N1", label="y")
    dot.edge("main.L2N1", "main.L3N1", label="z")
with dot.subgraph(name="sub") as sub:
    with sub.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("sub.L1N1", "", color="white")
        L1.node("sub.L1N2", "", color="white")
    with sub.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("sub.L2N1", "+")
    with sub.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("sub.L3N1", "", color="white")
    #Back Propagation
    dot.edge("sub.L3N1", "sub.L2N1", label="dL/dz", color="red", fontcolor="red")
    dot.edge("sub.L2N1", "sub.L1N1", label="dL/dz * dz/dx = dL/dz * 1", color="red", fontcolor="red")
#dot
dot
```

Out[11]:



加算ノード計算グラフ

In [12]:

```
class AddLayer:  
    """  
    加算ノード  
    """  
    def __init__(self):  
        pass  
  
    def forward(self, x, y):  
        """  
        順伝播  
        """  
        out = x + y  
        return out  
  
    def backward(self, dout):  
        """  
        逆伝播：微分  
        """  
        dx = dout * 1  
        dy = dout * 1  
        return dx, dy
```

- $z = x + y$

- $\frac{\partial z}{\partial x} = 1$

- $\frac{\partial z}{\partial y} = 1$

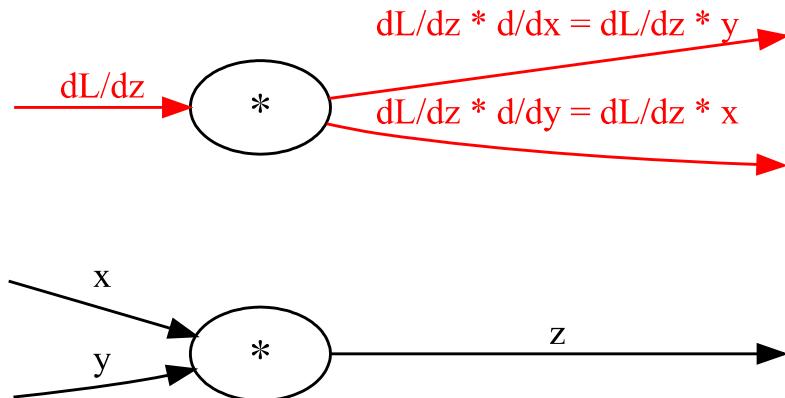
よって、加算ノードの微分逆伝搬は上流からの伝搬 $L$ をそのまま下流に伝達させるのみ。

## 乗算ノードの逆伝搬

In [13]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="乗算ノード計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("main.L1N1", "", color="white")
        L1.node("main.L1N2", "", color="white")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("main.L2N1", "*")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("main.L3N1", "", color="white")
    #Forward Propagation
    dot.edge("main.L1N1", "main.L2N1", label="x")
    dot.edge("main.L1N2", "main.L2N1", label="y")
    dot.edge("main.L2N1", "main.L3N1", label="z")
with dot.subgraph(name="sub") as sub:
    with sub.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("sub.L1N1", "", color="white")
        L1.node("sub.L1N2", "", color="white")
    with sub.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("sub.L2N1", "*")
    with sub.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("sub.L3N1", "", color="white")
    #Back Propagation
    dot.edge("sub.L3N1", "sub.L2N1", label="dL/dz", color="red", fontcolor="red")
    dot.edge("sub.L2N1", "sub.L1N1", label="dL/dz * d/dx = dL/dz * y", color="red", fontcolor="red")
    dot.edge("sub.L2N1", "sub.L1N2", label="dL/dz * d/dy = dL/dz * x", color="red", fontcolor="red")
#print(dot)
dot
```

Out[13]:



乗算ノード計算グラフ

In [14]:

```
class MulLayer:  
    """  
    乗算ノード  
    """  
  
    def __init__(self):  
        self.x = None  
        self.y = None  
  
    def forward(self, x, y):  
        """  
        順伝播  
        """  
  
        self.x = x  
        self.y = y  
        out = x * y  
        return out  
  
    def backward(self, dout):  
        """  
        逆伝播：微分  
        """  
  
        dx = dout * self.y  
        dy = dout * self.x  
        return dx, dy
```

- $z = xy$ 
  - $\frac{\partial z}{\partial x} = y$
  - $\frac{\partial z}{\partial y} = x$

よって、乗算ノードの微分逆伝搬は上流からの伝搬 $L$ を入力変数で微分して下流に伝達させる。（伝搬方向がひっくり返る）

## ReLUノード（ReLUレイヤ）

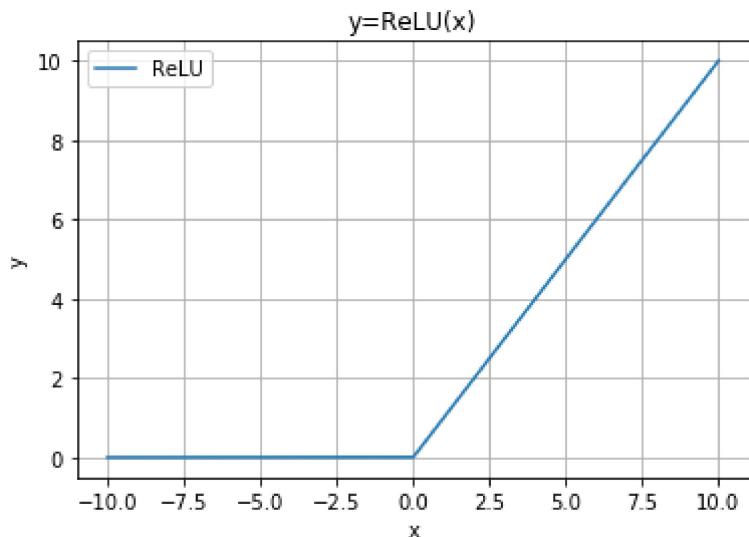
$$\begin{aligned} \text{Forwarding } f(x) &= \begin{cases} x & (x > 0) \\ 0 & (x \leq 0) \end{cases} \\ \text{BackProp } f'(x) &= \begin{cases} 1 & (x > 0) \\ 0 & (x \leq 0) \end{cases} \end{aligned}$$

In [15]:

```
%matplotlib inline
import matplotlib.pyplot as plt
import numpy as np
x = np.arange(-10, 10, 0.001) # -10 to 10 by 0.001
y = x * (x > 0)
plt.plot(x, y, label="ReLU", linestyle="-")
plt.xlabel("x")
plt.ylabel("y")
plt.title("y=ReLU(x)")
plt.legend()
plt.grid()
plt.show()
plt.close()
```

/home/nbuser/anaconda3\_420/lib/python3.5/site-packages/matplotlib/font\_manager.py:281: UserWarning: Matplotlib is building the font cache using fc-list. This may take a moment.

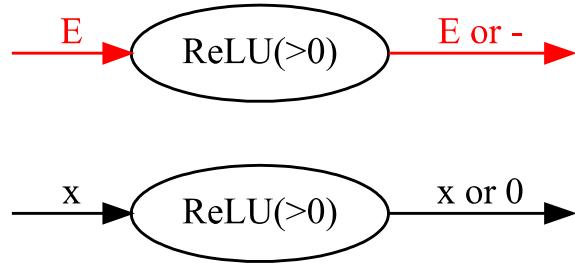
'Matplotlib is building the font cache using fc-list.'



In [16]:

```
from graphviz import Digraph
dot = Digraph(comment="ReLUノード計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="")
dot.attr(fixedsize="true")
dot.attr(label="ReLUノード計算グラフ")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("main.L1N1", "", color="white")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("main.L2N1", "ReLU(>0)")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("main.L3N1", "", color="white")
    #Forward Propagation
    dot.edge("main.L1N1", "main.L2N1", label="x")
    dot.edge("main.L2N1", "main.L3N1", label="x or 0")
with dot.subgraph(name="sub") as sub:
    with sub.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("sub.L1N1", "", color="white")
    with sub.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("sub.L2N1", "ReLU(>0)")
    with sub.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("sub.L3N1", "", color="white")
    #Back Propagation
    dot.edge("sub.L3N1", "sub.L2N1", label="E", color="red", fontcolor="red")
    dot.edge("sub.L2N1", "sub.L1N1", label="E or -", color="red", fontcolor="red")
dot
```

Out[16]:



ReLUノード計算グラフ

ReLUノードにおける逆伝搬をすることで「発火しなかった細胞はそこで伝搬をストップする」という作用を与えることが可能

In [17]:

```
class Relu:  
    """  
    ReLUの実装  
    """  
  
    def __init__(self):  
        self.mask = None  
  
    def forward(self, x):  
        """  
        type x: numpy.array  
        """  
        self.mask = (x <= 0)  
        out = x.copy()  
        out[self.mask] = 0  
        return out  
  
    def backward(self, dout):  
        """  
        type dout: numpy.array  
        """  
        dout[self.mask] = 0  
        dx = dout  
        return dx
```

## Sigmoidノード (Sigmoidレイヤ)

$$\text{順伝播 } f(x) = \frac{1}{1+e^{-x}}$$

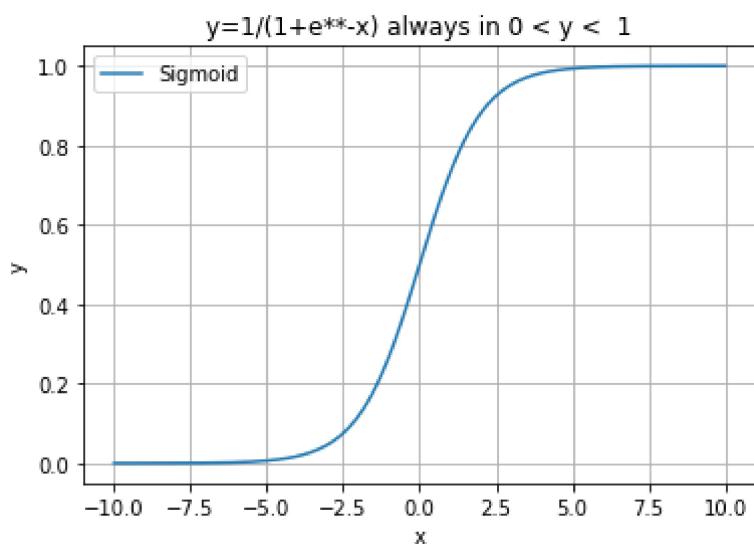
$$1 \geq f(x), f'(x) \geq 0$$

$$\text{逆伝播 } f'(x) = f(x)(1 - f(x))$$

→

In [18]:

```
%matplotlib inline
import matplotlib.pyplot as plt
import numpy as np
x = np.arange(-10, 10, 0.001) # -10 to 10 by 0.001
y = 1.0/(1.0 + np.e ** (-1.0*x))
plt.plot(x, y, label="Sigmoid", linestyle="-")
plt.xlabel("x")
plt.ylabel("y")
plt.title("y=1/(1+e**-x) always in 0 < y < 1")
plt.legend() #show label box
plt.grid()
plt.show()
plt.close()
```



In [19]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir)

from common.functions import sigmoid

class Sigmoid:
    """
    シグモイド関数の実装
    """
    def __init__(self):
        self.out = None

    def forward(self, x):
        out = sigmoid(x)
        self.out = out
        return out

    def backward(self, dout):
        dx = dout * (1.0 - self.out) * self.out

        return dx
```

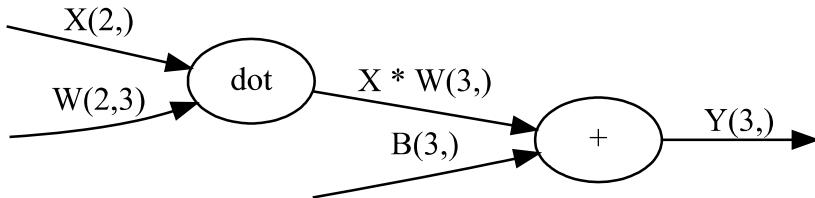
## Affineノード (Affineレイヤ)

行列の内積を求めるなどを幾何学の分野でアフィン変換と呼ぶ。  
スカラが複数同時に行列として計算できるということが以下に示される。  
ただし、行列の次元数は合わせる必要がある。

In [20]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="")
dot.attr(fixedsize="true")
dot.attr(label="Affine変換とバイアス加算の計算グラフ※括弧内は(行数, 列数) ")
with dot.subgraph(name="main") as main:
    main.attr(color="white")
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.node("L1N1", "", color="white")
        L1.node("L1N2", "", color="white")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.node("L2N1", "dot")
        L2.node("L2N2", "", color="white")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.node("L3N1", "+")
    with main.subgraph(name="cluster_L4") as L4:
        L4.attr(label="")
        L4.node("L4N1", "", color="white")
dot.edge("L1N1", "L2N1", label="X(2,)")
dot.edge("L1N2", "L2N1", label="W(2,3)")
dot.edge("L2N1", "L3N1", label="X * W(3,)")
dot.edge("L2N2", "L3N1", label="B(3,)")
dot.edge("L3N1", "L4N1", label="Y(3,)")
dot
```

Out[20]:



Affine変換とバイアス加算の計算グラフ※括弧内は(行数, 列数)

Affine変換は単純にこれまでの算術ノードの計算を一つ一つの行列の要素毎に実行しているにすぎない

In [21]:

```
class Affine:  
    def __init__(self, W, b):  
        self.W = W  
        self.b = b  
  
        self.x = None  
        self.original_x_shape = None  
        # 重み・バイアスパラメータの微分  
        self.dW = None  
        self.db = None  
  
    def forward(self, x):  
        # テンソル対応  
        self.original_x_shape = x.shape  
        x = x.reshape(x.shape[0], -1)  
        self.x = x  
  
        out = np.dot(self.x, self.W) + self.b  
  
        return out  
  
    def backward(self, dout):  
        dx = np.dot(dout, self.W.T)  
        self.dW = np.dot(self.x.T, dout)  
        self.db = np.sum(dout, axis=0)  
  
        dx = dx.reshape(*self.original_x_shape) # 入力データの形状に戻す (テンソル対応)  
        return dx
```

## SoftMax-WithLossノード (Softmaxレイヤ)

複数のスコアが適用された出力を正規化し、後のレイヤにおいてそのデータを正規的に使用する際に必要なノード。損失関数として、クロスエントロピー誤差計算関数を使っているので-WithLossというサフィックスが付いている。正規化が必要ない（スコアのたった一つの最頻値や最大値・最小値・平均値を使うような機械学習）の場合はこのノードは必要なし。ディープラーニングの際はスコアをそのまま入力として使うことをせず、一度確率的な数値( $1 > p_n (\sum p_n == 1) > 0$ )に直してから使用するためこのノードが必要となるケースがある。出力層で使われる際、もし分類問題の場合は入力データの数==出力データの数==分類数となっている必要がある。

In [22]:

```
def softmax(x):
    if x.ndim == 2:
        x = x.T
        x = x - np.max(x, axis=0)
        y = np.exp(x) / np.sum(np.exp(x), axis=0)
        return y.T

    x = x - np.max(x) # オーバーフロー対策
    return np.exp(x) / np.sum(np.exp(x))

def cross_entropy_error(y, t):
    if y.ndim == 1:
        t = t.reshape(1, t.size)
        y = y.reshape(1, y.size)

    # 教師データがone-hot-vectorの場合、正解ラベルのインデックスに変換
    if t.size == y.size:
        t = t.argmax(axis=1)

    batch_size = y.shape[0]
    return -np.sum(np.log(y[np.arange(batch_size), t] + 1e-7)) / batch_size

def softmax_loss(X, t):
    y = softmax(X)
    return cross_entropy_error(y, t)
```

In [23]:

```
softmax(np.array([[0, 1], [2, 3]]))
```

Out[23]:

```
array([[0.26894142, 0.73105858],
       [0.26894142, 0.73105858]])
```

In [24]:

```
class SoftmaxWithLoss:  
    def __init__(self):  
        self.loss = None  
        self.y = None # softmaxの出力  
        self.t = None # 教師データ  
  
    def forward(self, x, t):  
        self.t = t  
        self.y = softmax(x)  
        self.loss = cross_entropy_error(self.y, self.t)  
  
        return self.loss  
  
    def backward(self, dout=1):  
        batch_size = self.t.shape[0]  
        if self.t.size == self.y.size: # 教師データがone-hot-vectorの場合  
            dx = (self.y - self.t) / batch_size  
        else:  
            dx = self.y.copy()  
            dx[np.arange(batch_size), self.t] -= 1  
            dx = dx / batch_size  
  
        return dx
```

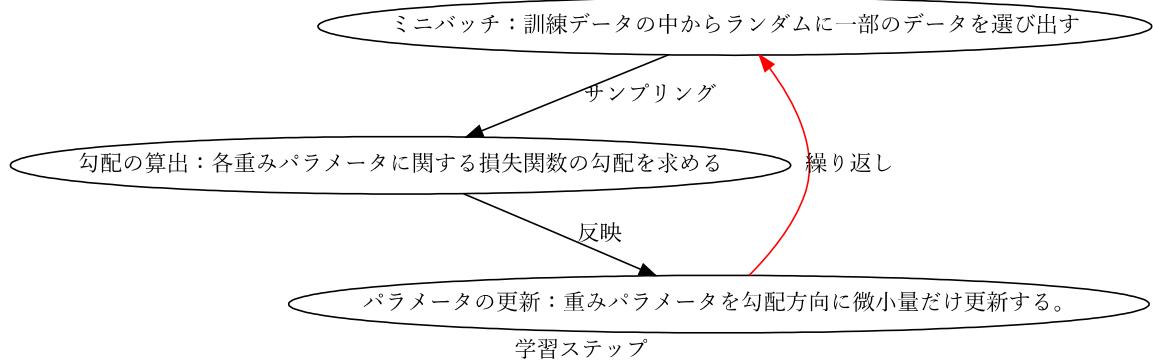
## 誤差逆伝搬法

### ニューラルネットワークの学習ステップ<sup>°</sup>

In [25]:

```
from graphviz import Digraph
dot = Digraph(comment="学習ステップ")
dot.attr(rankdir="UD")
#dot.attr(splines="")
dot.attr(fixedsize="true")
dot.attr(label="学習ステップ")
with dot.subgraph(name="main") as main:
    dot.node("MiniBatch", "ミニバッチ：訓練データの中からランダムに一部のデータを選び出す")
    dot.node("CalcGrad", "勾配の算出：各重みパラメータに関する損失関数の勾配を求める")
    dot.node("ReParam", "パラメータの更新：重みパラメータを勾配方向に微小量だけ更新する。")
    dot.edge("MiniBatch", "CalcGrad", label="サンプリング")
    dot.edge("CalcGrad", "ReParam", label="反映")
    dot.edge("ReParam", "MiniBatch", label="繰り返し", color="red")
dot
```

Out [25] :



## TwoLayerNet（誤差逆伝搬法（非：数値微分法）を追加バージョン）の実装

In [26]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
from common.layers import *
from common.gradient import numerical_gradient
from collections import OrderedDict

class TwoLayerNet:
    """
    このクラス自身は特に処理をしません。
    """

    def __init__(self, input_size, hidden_size, output_size, weight_init_std = 0.01):
        """
        各種レイヤを作成し、レイヤのハイパーパラメータを初期化します。
        ガウス分布などの分布の適合線に関する情報: https://support.minitab.com/ja-jp/minitab/18/help-and-how-to/graphs/supporting-topics/exploring-data-and-revising-graphs/distributions-for-fitted-lines/
        分布のスケールパラメータに関する情報: https://en.wikipedia.org/wiki/Scale\_parameter
        Args:
            input_size (int): 入力層のニューロン数 (入力データ要素数)
            hidden_size (int): 隠れ層のニューロン数
            output_size (int): 出力層のニューロン数 (出力データ要素数)
            weight_init_std (int): 重み初期化時のガウス分布 (正規分布) のスケールパラメタ=分布の幅
        Returns:
            None
        """
        self.params = {}
        #randnで"正規分布"でランダムな行列 (input_size列、hidden_size行) を生成し
        #それをweight_init_stdのスケールに狭めて重みデータの初期値を決める
        #バイアスはhidden_size行数だけ必要になるのでゼロで初期化
        self.params['W1'] = weight_init_std * np.random.randn(input_size, hidden_size)
        self.params['b1'] = np.zeros(hidden_size)
        #隠れ層についても同様に実施
        self.params['W2'] = weight_init_std * np.random.randn(hidden_size, output_size)
        self.params['b2'] = np.zeros(output_size)
        #それらの重み・バイアスの変数を持った各々の各レイヤを作成。
        self.layers = OrderedDict()
        #Affine1→Relu1→Affine2
        self.layers['Affine1'] = Affine(self.params['W1'], self.params['b1'])
        self.layers['Relu1'] = Relu()
        self.layers['Affine2'] = Affine(self.params['W2'], self.params['b2'])

        #出力層（誤差計算層）を初期化
        self.lastLayer = SoftmaxWithLoss()

    def predict(self, x):
        """
        OrderedDictを取り出し順伝搬させる
        各レイヤの持っている重みとバイアスが使われる。
        Args:
            x (int): 計算対象の行列 (入力行列)
        Returns:
            x (int): 計算結果 (出力行列)
        """
        for layer in self.layers.values():
            x = layer.forward(x)

        return x
```

```

    return x

# x:入力データ, t:教師データ
def loss(self, x, t):
    """
    OrderedDictを取り出し順伝搬させた後
    学習データと教師データを
    Args:
        x (int): 入力データ
        t (int): 教師データ
    Returns:
        x (int): 出力データ
    """
    y = self.predict(x)
    return self.lastLayer.forward(y, t)

def accuracy(self, x, t):
    """
    Args:
        x (int): 入力データ
        t (int): 教師データ
    Returns:
        accuracy (float): 認識精度
    """
    y = self.predict(x)
    y = np.argmax(y, axis=1)
    if t.ndim != 1: t = np.argmax(t, axis=1)

    accuracy = np.sum(y == t) / float(x.shape[0])
    return accuracy

# x:入力データ, t:教師データ
def numerical_gradient(self, x, t):
    """
    Args:
        x (int): 入力データ
        t (int): 教師データ
    Returns:
        grads (dict): 数理的微分法を用いて計算された傾き及びバイアス
    """
    loss_W = lambda W: self.loss(x, t)

    grads = {}
    grads['W1'] = numerical_gradient(loss_W, self.params['W1'])
    grads['b1'] = numerical_gradient(loss_W, self.params['b1'])
    grads['W2'] = numerical_gradient(loss_W, self.params['W2'])
    grads['b2'] = numerical_gradient(loss_W, self.params['b2'])

    return grads

def gradient(self, x, t):
    """
    Args:
        x (int): 入力データ
        t (int): 教師データ
    Returns:
        grads (dict): 解析的微分法を用いて計算された傾き及びバイアス
    """
    # forward
    self.loss(x, t)

```

```
# backward
dout = 1
dout = self.lastLayer.backward(dout)

layers = list(self.layers.values())
layers.reverse()
for layer in layers:
    dout = layer.backward(dout)

# 設定
grads = {}
grads['W1'], grads['b1'] = self.layers['Affine1'].dW, self.layers['Affine1'].db
grads['W2'], grads['b2'] = self.layers['Affine2'].dW, self.layers['Affine2'].db

return grads
```

誤差逆伝播法の微分方式の内、解析的微分法の勾配が正しく計算されていることを確認するには数値的微分法の計算結果と照らし合わせると良い。

## 誤差逆伝播法の学習

In [27]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir)

import numpy as np
from dataset.mnist import load_mnist
from two_layer_net import TwoLayerNet

# データの読み込み ★学習データとテストデータは同じものを使ってはならない
(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True, one_hot_label=True)
#784個の入力データ : 縦28画素*横28画素
#50個の想定される構成因子数
#10個の出力データ : 0~9の数字
network = TwoLayerNet(input_size=784, hidden_size=50, output_size=10)

iters_num = 10000 #学習回数
train_size = x_train.shape[0] #学習データ数
batch_size = 100 #バッチサイズ (100個サンプリングして学習)
learning_rate = 0.1 #学習率

train_loss_list = [] #途中経過保存用
train_acc_list = [] #途中経過保存用
test_acc_list = [] #途中経過保存用

iter_per_epoch = max(train_size / batch_size, 1) #バッチ回数

print("学習回数 : ", iters_num, "学習データ数 : ", train_size, "バッチサイズ : ", batch_size, "学習率 : ", learning_rate)

for i in range(iters_num):
    #学習データからバッチ用のデータをランダムに抽出 (一様分布)
    batch_mask = np.random.choice(train_size, batch_size)
    x_batch = x_train[batch_mask]
    t_batch = t_train[batch_mask]
    # 勾配
    #grad = network.numerical_gradient(x_batch, t_batch)
    grad = network.gradient(x_batch, t_batch)
    # 更新
    for key in ('W1', 'b1', 'W2', 'b2'):
        network.params[key] -= learning_rate * grad[key]
    # 差分 * 学習率 を減算し、ニューラルネットワークの重みとバイアスの値を更新
    loss = network.loss(x_batch, t_batch)
    train_loss_list.append(loss)

    #以下、経過出力用コード
    if i % iter_per_epoch == 0:
        train_acc = network.accuracy(x_train, t_train)
        test_acc = network.accuracy(x_test, t_test)
        train_acc_list.append(train_acc)
        test_acc_list.append(test_acc)
        print("★%d個サンプル学習データを%d回学習★" % (batch_size, i), "学習率 : ", train_acc,
              "認識率 : ", test_acc, "勾配差分 : ", loss)
```

学習回数 : 10000 学習データ数 : 60000 バッチサイズ : 100 学習率 : 0.1  
★100個サンプル学習データを0回学習★ 学習率 : 0.05986666666666666666 認識率 : 0.0604  
勾配差分 : 2.3029724580090503  
★100個サンプル学習データを600回学習★ 学習率 : 0.9049333333333334 認識率 : 0.9079  
勾配差分 : 0.25196564925931403  
★100個サンプル学習データを1200回学習★ 学習率 : 0.9239333333333334 認識率 : 0.924  
3 勾配差分 : 0.33200771267981016  
★100個サンプル学習データを1800回学習★ 学習率 : 0.93385 認識率 : 0.9338 勾配差分 : 0.2631430208924852  
★100個サンプル学習データを2400回学習★ 学習率 : 0.9451666666666667 認識率 : 0.943  
7 勾配差分 : 0.27544850688906797  
★100個サンプル学習データを3000回学習★ 学習率 : 0.9511833333333334 認識率 : 0.946  
8 勾配差分 : 0.20889939210592628  
★100個サンプル学習データを3600回学習★ 学習率 : 0.9557 認識率 : 0.9522 勾配差分 : 0.12284927627356054  
★100個サンプル学習データを4200回学習★ 学習率 : 0.9613 認識率 : 0.9563 勾配差分 : 0.0860223050467403  
★100個サンプル学習データを4800回学習★ 学習率 : 0.9644166666666667 認識率 : 0.960  
6 勾配差分 : 0.18300004043458046  
★100個サンプル学習データを5400回学習★ 学習率 : 0.96675 認識率 : 0.9634 勾配差分 : 0.05001404369577504  
★100個サンプル学習データを6000回学習★ 学習率 : 0.96875 認識率 : 0.9627 勾配差分 : 0.08052315605516638  
★100個サンプル学習データを6600回学習★ 学習率 : 0.970183333333333 認識率 : 0.965  
5 勾配差分 : 0.07549477934736186  
★100個サンプル学習データを7200回学習★ 学習率 : 0.9729 認識率 : 0.9664 勾配差分 : 0.05086949475875577  
★100個サンプル学習データを7800回学習★ 学習率 : 0.974233333333333 認識率 : 0.967  
6 勾配差分 : 0.05080182316512686  
★100個サンプル学習データを8400回学習★ 学習率 : 0.9753333333333334 認識率 : 0.968  
9 勾配差分 : 0.08594969223927429  
★100個サンプル学習データを9000回学習★ 学習率 : 0.9769666666666666 認識率 : 0.970  
4 勾配差分 : 0.03641650867545596  
★100個サンプル学習データを9600回学習★ 学習率 : 0.9769666666666666 認識率 : 0.968  
2 勾配差分 : 0.04800738457481304

# 学習に関するテクニック

最適化 (optimization) ([http://www.orsj.or.jp/archive2/or60-4/or60\\_4\\_191.pdf](http://www.orsj.or.jp/archive2/or60-4/or60_4_191.pdf))はニューラルネットワークの課題。損失関数 (loss function) の値を小さくするようにパラメータを調整すること。過学習・勾配消失・爆発 (発散) を防ぐ手法を学ぶことが学習に関するテクニックである。一般的には以下のよな手法が知られている。

- パラメータの更新方法を変更する
- 活性化関数を変更する
- ネットワークの重みの初期値を調整する
- 学習係数を下げる
- ネットワークの自由度を制約する (Dropoutなど)

しかし、近年においては

- Batch Normalizationを挿入する
- ハイパーパラメータを探索する

という手法が主流になっている。

## 勾配更新アルゴリズムの選定による最適化

基本的には、勾配消失・爆発を防ぐための手法であり、これまで

活性化関数を変更する (ReLUなど) ネットワークの重みの初期値を事前学習する 学習係数を下げる ネットワークの自由度を制約する (Dropoutなど)

## 勾配降下法

微分の傾きを収束させることを目指す方法。

### バッチ勾配降下法

ミニバッチ処理により、全てのデータ／テストを一括で順番に計算し勾配を求める。確実だが、リソースの問題がある。

### 確率的勾配降下法

全てのデータを一括で処理せず、データがある確率分布に基づいて無作為全抽出し勾配を求める。優良なデータを先に処理することが出来る可能性がある。

### ミニバッチ勾配降下法

全てのデータを一括で処理せず、データがある確率分布に基づいて無作為標本抽出し勾配を求める。サンプリングレート（バッチサイズ）とサンプリング分布（基本的にランダムサンプリングとなる）により優良な標本データを先に処理し目的関数に近づける事ができる。現在の機械学習においては基本的にこの手法が推奨される。

## 勾配更新アルゴリズムによる収束までの違い

<http://ruder.io/optimizing-gradient-descent/> (<http://ruder.io/optimizing-gradient-descent/>)  
<https://keras.io/optimizers/> (<https://keras.io/optimizers/>)

## 様々な勾配降下法の最適化アルゴリズム

### SGD(Stochastic Gradient Descent, 確率的勾配降下法)

$$W \leftarrow W - \eta \frac{\partial L}{\partial W}$$

$$0 < \eta < 1$$

$W$  :: Weight  $\eta$  :: Learning Rate  $L$  :: Loss Function  $\partial$  :: Partial Differentiation

単純な勾配降下法全てのベース(Vanilla)となる。全集合（学習データ集合、テストデータ集合）の中の一部(batch\_size分)の集合をepoch回だけ無作為サンプリング（サンプリング分布に注意）し、勾配降下法の計算に反映する手法。大規模なデータを処理する際、少ない計算量で実装可能であり、非常にシンプルなのでMLアルゴリズムのデバッグが容易。目的関数と一致しない集合で学習してしまうと急激に勾配が上下し目的関数もそれにつられて大きく変動する可能性がある。

In [1]:

```
class SGD:  
    """確率的勾配降下法 (Stochastic Gradient Descent) """  
    def __init__(self, lr=0.01):  
        self.lr = lr  
    def update(self, params, grads):  
        for key in params.keys():  
            params[key] -= self.lr * grads[key]
```

### Momentum (Momentum SGD)

$$v \leftarrow \alpha v - \eta \frac{\partial L}{\partial W}$$

$$W \leftarrow W + v$$

$$0 < \alpha < 1$$

$v$  :: velocity  $\alpha$  :: Air Resistance (aka. Friction)

SGDにおいて勾配更新の際に勾配を直接計算に反映するのではなく「直前の勾配の加速度」変数を掛け算し続けることでSGDの勾配更新を滑らかにする方法。複雑な関数でなければSGDよりも早く収束する可能性がある。勾配と正方向の加速度が「勢い」であり、逆方向の加速度が物理学でいう「摩擦」や「空気抵抗」に近い。**加速度に定数 $\alpha$ を毎回掛け算しているのは、静止摩擦を付加し収束を期待する為である。**

In [8]:

```
class Momentum:
    """惯性SGD (Momentum SGD)"""
    def __init__(self, lr=0.01, momentum=0.9):
        self.lr = lr
        self.momentum = momentum
        self.v = None
    def update(self, params, grads):
        if self.v is None:
            self.v = {}
        for key, val in params.items():
            self.v[key] = np.zeros_like(val)
        for key in params.keys():
            self.v[key] = self.momentum * self.v[key] - self.lr * grads[key]
            params[key] += self.v[key]
```

## NAG (Nesterov's Accelerated Gradient)

Momentumでは加速度を計算する際に勾配計算前の値を使用していたが、NAGでは勾配計算後の値を使用することで、勾配の変化に関してMomentumよりも一步先で気づくことが出来るようになる。それ以外は特に変わらない。同盟で複数のアルゴリズムが存在する。

## Adagrad

$$h \leftarrow h + \frac{\partial L}{\partial W} \odot \frac{\partial L}{\partial W}$$

$$W \leftarrow W - \eta \frac{1}{\sqrt{h}} \frac{\partial L}{\partial W}$$

$h$  :: Rate of Learning Rate  $\odot$  :: Hadamard Product (アダマール積::行列の要素ごとの単純乗算。内積でない。)

勾配更新の際に「学習率」自体を勾配で自乗したもので割る。これにより学習率そのものの指數関数的な減衰をもたらす。最初の勾配が大きいものが強く学習され、収束に従って緩やかに学習されるようになるので最初に大きく学習を進めることが出来る。最初に学習したデータが良好なデータであればあるほど効果的に働くが学習が進むに連れて学習率が0に近づく為、**オンライン学習（継続的学习）の場合は新鮮なデータを受け入れるのが難しくなる欠点がある**。アダマール積を使用しているのは、各種パラメータ（行・列）毎のデータ変動を一個ずつ対応して反映できるようにするためにある。※ $h$ は最初は非常に小さな数値に設定し、ゼロ除算を回避すること。

In [4]:

```
class AdaGrad:  
    """AdaGrad (Adaptive subgradient methods for online learning and stochastic optimization)"""  
    def __init__(self, lr=0.01):  
        self.lr = lr  
        self.h = None  
    def update(self, params, grads):  
        if self.h is None:  
            self.h = {}  
        for key, val in params.items():  
            self.h[key] = np.zeros_like(val)  
    for key in params.keys():  
        self.h[key] += grads[key] * grads[key]  
        params[key] -= self.lr * grads[key] / (np.sqrt(self.h[key]) + 1e-7)  
        #1e-7はゼロ除算を防ぐため
```

## RMSprop

$$h \leftarrow \alpha h + (1 - \alpha) \frac{\partial L}{\partial W}$$

$$W \leftarrow W - \eta \frac{1}{\sqrt{h}} \frac{\partial L}{\partial W}$$

$$0 \leq \alpha \leq 1$$

$\alpha$  :: Rate of exponential moving average; EMA; 指数移動平均

Adagradにおいて学習が進むにつれて新鮮なデータを受入し難くなる欠点を克服するため、**一つ前の学習率に定数 $\alpha$ を掛けて減衰させ、受け入れる新鮮なデータの学習率の影響を強める**手法。hに関して指数移動平均を適用したものである。過去のデータの影響力の加重が指数関数的に減衰するので、 $\alpha$ の数値が低すぎた場合は過去のデータの影響力が直ちに低下してしまい、新鮮すぎる結果が発生し、数値が高すぎた場合は腐った結果が発生するリスクがある。

In [5]:

```
class RMSprop:  
    """RMSprop"""  
    def __init__(self, lr=0.01, decay_rate = 0.99):  
        self.lr = lr  
        self.decay_rate = decay_rate  
        self.h = None  
    def update(self, params, grads):  
        if self.h is None:  
            self.h = {}  
        for key, val in params.items():  
            self.h[key] = np.zeros_like(val)  
    for key in params.keys():  
        self.h[key] *= self.decay_rate  
        self.h[key] += (1 - self.decay_rate) * grads[key] * grads[key]  
        params[key] -= self.lr * grads[key] / (np.sqrt(self.h[key]) + 1e-7)
```

## AdaDelta

AdagradとRMSpropをあわせたもの。学習率が存在せず移動平均がそのまま学習率に反映される。

## Adam

AdaGrad、RMSprop、AdaDeltaを合わせスケールを追加したもの

In [6]:

```
class Adam:  
    """Adam (Adaptive moment estimation)"""  
    def __init__(self, lr=0.001, beta1=0.9, beta2=0.999):  
        self.lr = lr  
        self.beta1 = beta1  
        self.beta2 = beta2  
        self.iter = 0  
        self.m = None  
        self.v = None  
    def update(self, params, grads):  
        if self.m is None:  
            self.m, self.v = {}, {}  
            for key, val in params.items():  
                self.m[key] = np.zeros_like(val)  
                self.v[key] = np.zeros_like(val)  
        self.iter += 1  
        lr_t = self.lr * np.sqrt(1.0 - self.beta2**self.iter) / (1.0 - self.beta1**self.iter)  
  
        for key in params.keys():  
            #self.m[key] = self.beta1*self.m[key] + (1-self.beta1)*grads[key]  
            #self.v[key] = self.beta2*self.v[key] + (1-self.beta2)*(grads[key]**2)  
            self.m[key] += (1 - self.beta1) * (grads[key] - self.m[key])  
            self.v[key] += (1 - self.beta2) * (grads[key]**2 - self.v[key])  
  
            params[key] -= lr_t * self.m[key] / (np.sqrt(self.v[key]) + 1e-7)  
  
            #unbias_m += (1 - self.beta1) * (grads[key] - self.m[key]) # correct bias  
            #unbias_b += (1 - self.beta2) * (grads[key]*grads[key] - self.v[key]) # correct bias  
            #params[key] += self.lr * unbiased_m / (np.sqrt(unbiased_b) + 1e-7)
```

MNISTデータセットによる更新手法の比較

In [2]:

```
# coding: utf-8
import os
import sys
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.util import smooth_curve
from common.multi_layer_net import MultiLayerNet
from common.optimizer import *

# 0:MNISTデータの読み込み=====
(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

train_size = x_train.shape[0]
batch_size = 128
max_iterations = 2000

# 1:実験の設定=====
optimizers = {}
optimizers['SGD'] = SGD()
optimizers['Momentum'] = Momentum()
optimizers['AdaGrad'] = AdaGrad()
optimizers['Adam'] = Adam()
#optimizers['RMSprop'] = RMSprop()

networks = {}
train_loss = {}
for key in optimizers.keys():
    networks[key] = MultiLayerNet(
        input_size=784, hidden_size_list=[100, 100, 100, 100],
        output_size=10)
    train_loss[key] = []

# 2:訓練の開始=====
for i in range(max_iterations):
    batch_mask = np.random.choice(train_size, batch_size)
    x_batch = x_train[batch_mask]
    t_batch = t_train[batch_mask]

    for key in optimizers.keys():
        grads = networks[key].gradient(x_batch, t_batch)
        optimizers[key].update(networks[key].params, grads)

        loss = networks[key].loss(x_batch, t_batch)
        train_loss[key].append(loss)

    if i % 100 == 0:
        print("===== " + "iteration:" + str(i) + " =====")
        for key in optimizers.keys():
            loss = networks[key].loss(x_batch, t_batch)
            print(key + ":" + str(loss))

# 3. グラフの描画=====
markers = {"SGD": "o", "Momentum": "x", "AdaGrad": "s", "Adam": "D"}
x = np.arange(max_iterations)
```

```
for key in optimizers.keys():
    plt.plot(x, smooth_curve(train_loss[key]), marker=markers[key], markevery=100, label=key)
plt.xlabel("iterations")
plt.ylabel("loss")
plt.ylim(0, 1)
plt.legend()
plt.show()
```

=====iteration:0=====

AdaGrad:2.073306458903855  
SGD:2.523300165662966  
Adam:2.121038352570406  
Momentum:2.38792091140304

=====iteration:100=====

AdaGrad:0.2131088105273944  
SGD:1.6044179080128664  
Adam:0.3808571137285117  
Momentum:0.3969831247395848

=====iteration:200=====

AdaGrad:0.13124025086807267  
SGD:0.7830985515944628  
Adam:0.22064014047211133  
Momentum:0.3216731484452754

=====iteration:300=====

AdaGrad:0.06808923098744606  
SGD:0.6325237467606476  
Adam:0.16051907326110734  
Momentum:0.23042036201574118

=====iteration:400=====

AdaGrad:0.06313508623562003  
SGD:0.45209547106182657  
Adam:0.13090639195898196  
Momentum:0.16881274795022827

=====iteration:500=====

AdaGrad:0.0746353204854379  
SGD:0.33067102745064325  
Adam:0.12430283308476585  
Momentum:0.17795406996349522

=====iteration:600=====

AdaGrad:0.041437727939144256  
SGD:0.36918525431898697  
Adam:0.127014809423026  
Momentum:0.16947254478379217

=====iteration:700=====

AdaGrad:0.07854171706682012  
SGD:0.3318232246950431  
Adam:0.1209986514495654  
Momentum:0.14913166839228031

=====iteration:800=====

AdaGrad:0.05195006133127446  
SGD:0.3025152503875316  
Adam:0.10859296970221899  
Momentum:0.1732654572600429

=====iteration:900=====

AdaGrad:0.07781836733265007  
SGD:0.26347814560455185  
Adam:0.08727690727995363  
Momentum:0.15707644843134425

=====iteration:1000=====

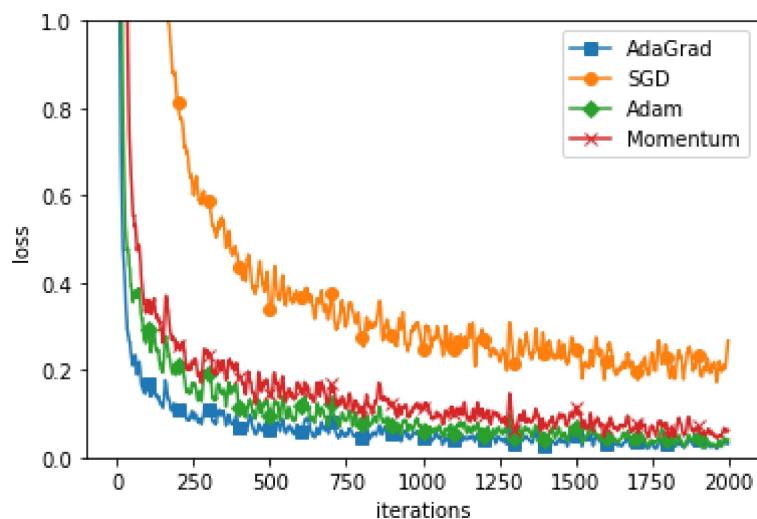
AdaGrad:0.03065622516498518  
SGD:0.20389467073413406  
Adam:0.027024578641755104  
Momentum:0.07996497290843516

=====iteration:1100=====

AdaGrad:0.09872289321572919  
SGD:0.23547226998879367  
Adam:0.0934946021846558  
Momentum:0.14254957758981768

=====iteration:1200=====

```
AdaGrad:0. 055191379811268274
SGD:0. 3109738353784294
Adam:0. 06514229213904917
Momentum:0. 1379175719410351
=====iteration:1300=====
AdaGrad:0. 04387204579920525
SGD:0. 26196650572611313
Adam:0. 0625853256957209
Momentum:0. 09036903564636829
=====iteration:1400=====
AdaGrad:0. 02219086430991235
SGD:0. 1877208319403718
Adam:0. 029426675946386555
Momentum:0. 0845638241078313
=====iteration:1500=====
AdaGrad:0. 11608670588608397
SGD:0. 33773967606904787
Adam:0. 08622036049471533
Momentum:0. 21650175829174115
=====iteration:1600=====
AdaGrad:0. 046115608649423
SGD:0. 25291991636150213
Adam:0. 09449451108675003
Momentum:0. 09031445958452815
=====iteration:1700=====
AdaGrad:0. 03207546608854157
SGD:0. 16174878427926614
Adam:0. 019466190695012753
Momentum:0. 03876243380325855
=====iteration:1800=====
AdaGrad:0. 014310622225061862
SGD:0. 17121837372399037
Adam:0. 0194596575829714
Momentum:0. 0393406117694879
=====iteration:1900=====
AdaGrad:0. 020184199816534614
SGD:0. 20354824799564297
Adam:0. 021922311598918012
Momentum:0. 040479245423072255
```



## 留意

- SGDは最初から最後まで学習に行き詰まっている
- Momentumは振れ幅が大きい
- Adamは最初の収束が早く振れ幅が少ない
- AdaGradが最初の方で効率よく学習しそのままキープできている

## 重みの初期値の調整による最適化

### 重みの初期値を0にするのはNG

これまでではガウス分布（正規分布,np.random.randn）により生成される平均0標準偏差1のランダム分布から得られる重みを0.01倍して重みに割り当てていた。それを例えば $W = np.zeros\_like(W)$ してしまうというのはバッドプラクティスである。

**ニューラルネットワークにおいて重みの初期値を各要素毎に均一に設定してしまうと誤差逆伝搬方で各層が均一の値で更新されてしまい、層と層の間の計算に意味が無くなってしまうためである。**

### 隠れ層のアクティベーション分布から重みの初期値の最適な標準偏差を探る

隠れ層のアクティベーション（活性化関数適用後の出力データ）の分布を観察することで、ニューラルネットワークのパラメータの調整に関して有効な手立てを考えることができる。重みの初期値を調整しアクティベーション分布に偏りなくさせてニューラルネットワークの「表現の制限」と「勾配消失（Gradient Vanishing）」を避けることが目標。

### 重みの初期値（Sigmoid関数をアクティベーション関数にした場合）

In [14]:

```
# coding: utf-8
import numpy as np
import matplotlib.pyplot as plt

def sigmoid(x):
    return 1 / (1 + np.exp(-x))

def ReLU(x):
    return np.maximum(0, x)

def tanh(x):
    return np.tanh(x)

input_data = np.random.randn(1000, 100) # 1000個のデータ
node_num = 100 # 各隠れ層のノード（ニューロン）の数
hidden_layer_size = 5 # 隠れ層が5層
activations = {} # ここにアクティベーションの結果を格納する

x = input_data
print("標準偏差1の正規分布 : w = np.random.randn(node_num, node_num) * 1")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    w = np.random.randn(node_num, node_num) * 1
    # w = np.random.randn(node_num, node_num) * 0.01
    # w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    # w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    z = sigmoid(a)
    # z = ReLU(a)
    # z = tanh(a)

    activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()

x = input_data

print("標準偏差0.01の正規分布 : w = np.random.randn(node_num, node_num) * 0.01")
for i in range(hidden_layer_size):
    if i != 0:
```

```

x = activations[i-1]

# 初期値の値をいろいろ変えて実験しよう !
# w = np.random.randn(node_num, node_num) * 1
w = np.random.randn(node_num, node_num) * 0.01
# w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
# w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

a = np.dot(x, w)

# 活性化関数の種類も変えて実験しよう !
z = sigmoid(a)
# z = ReLU(a)
# z = tanh(a)

activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0.1, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()

x = input_data

print("Xavierの初期値 : w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    # w = np.random.randn(node_num, node_num) * 1
    # w = np.random.randn(node_num, node_num) * 0.01
    w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    # w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    z = sigmoid(a)
    # z = ReLU(a)
    # z = tanh(a)

    activations[i] = z

    # ヒストグラムを描画
    for i, a in activations.items():
        plt.subplot(1, len(activations), i+1)
        plt.title(str(i+1) + "-layer")
        if i != 0: plt.yticks([], [])
        # plt.xlim(0.1, 1)
        # plt.ylim(0, 7000)
        plt.hist(a.flatten(), 30, range=(0, 1))

```

```
plt.show()

x = input_data

print("Heの初期値 : w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    #w = np.random.randn(node_num, node_num) * 1
    #w = np.random.randn(node_num, node_num) * 0.01
    #w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

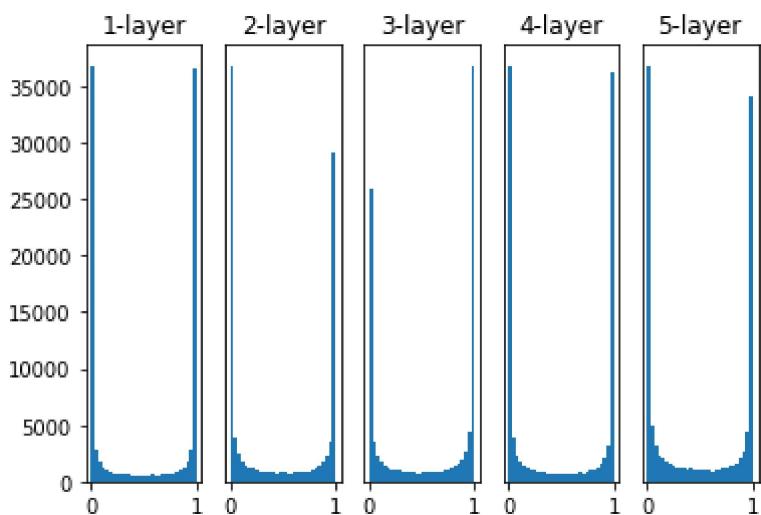
    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    z = sigmoid(a)
    # z = ReLU(a)
    # z = tanh(a)

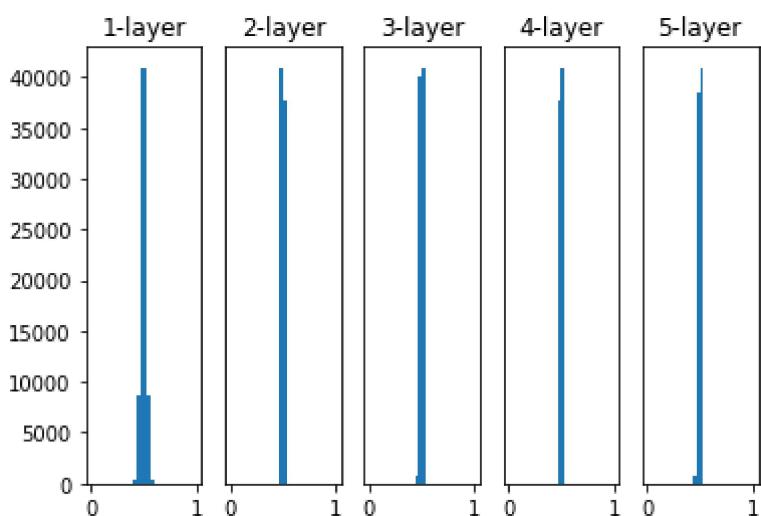
    activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()
```

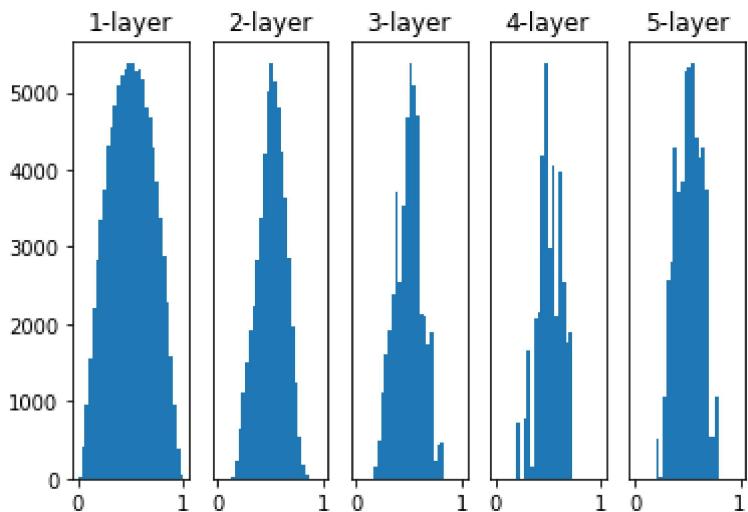
標準偏差1の正規分布 :  $w = np.random.randn(node\_num, node\_num) * 1$



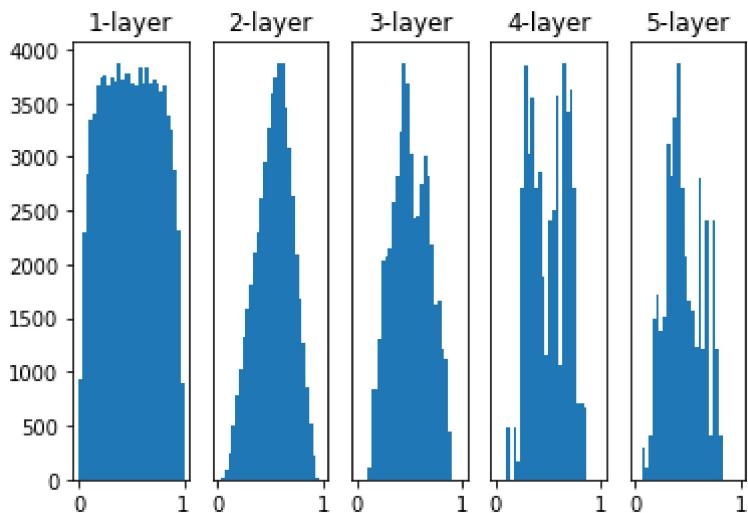
標準偏差0.01の正規分布 :  $w = np.random.randn(node\_num, node\_num) * 0.01$



Xavierの初期値 :  $w = np.random.randn(node\_num, node\_num) * np.sqrt(1.0 / node\_num)$



Heの初期値 : `w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)`



**重みの初期値 (ReLU関数をアクティベーション関数にした場合)**

In [15]:

```
# coding: utf-8
import numpy as np
import matplotlib.pyplot as plt

def sigmoid(x):
    return 1 / (1 + np.exp(-x))

def ReLU(x):
    return np.maximum(0, x)

def tanh(x):
    return np.tanh(x)

input_data = np.random.randn(1000, 100) # 1000個のデータ
node_num = 100 # 各隠れ層のノード（ニューロン）の数
hidden_layer_size = 5 # 隠れ層が5層
activations = {} # ここにアクティベーションの結果を格納する

x = input_data
print("標準偏差1の正規分布 : w = np.random.randn(node_num, node_num) * 1")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    w = np.random.randn(node_num, node_num) * 1
    # w = np.random.randn(node_num, node_num) * 0.01
    # w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    # w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    # z = sigmoid(a)
    z = ReLU(a)
    # z = tanh(a)

    activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0.1, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()

x = input_data

print("標準偏差0.01の正規分布 : w = np.random.randn(node_num, node_num) * 0.01")
for i in range(hidden_layer_size):
    if i != 0:
```

```

x = activations[i-1]

# 初期値の値をいろいろ変えて実験しよう !
#w = np.random.randn(node_num, node_num) * 1
w = np.random.randn(node_num, node_num) * 0.01
# w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
# w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

a = np.dot(x, w)

# 活性化関数の種類も変えて実験しよう !
#z = sigmoid(a)
z = ReLU(a)
# z = tanh(a)

activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    #plt.xlim(0.1, 1)
    #plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()

x = input_data

print("Xavierの初期値 : w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    #w = np.random.randn(node_num, node_num) * 1
    #w = np.random.randn(node_num, node_num) * 0.01
    w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    # w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    #z = sigmoid(a)
    z = ReLU(a)
    # z = tanh(a)

    activations[i] = z

    # ヒストグラムを描画
    for i, a in activations.items():
        plt.subplot(1, len(activations), i+1)
        plt.title(str(i+1) + "-layer")
        if i != 0: plt.yticks([], [])
        #plt.xlim(0.1, 1)
        #plt.ylim(0, 7000)
        plt.hist(a.flatten(), 30, range=(0, 1))

```

```
plt.show()

x = input_data

print("Heの初期値 : w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    #w = np.random.randn(node_num, node_num) * 1
    #w = np.random.randn(node_num, node_num) * 0.01
    #w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

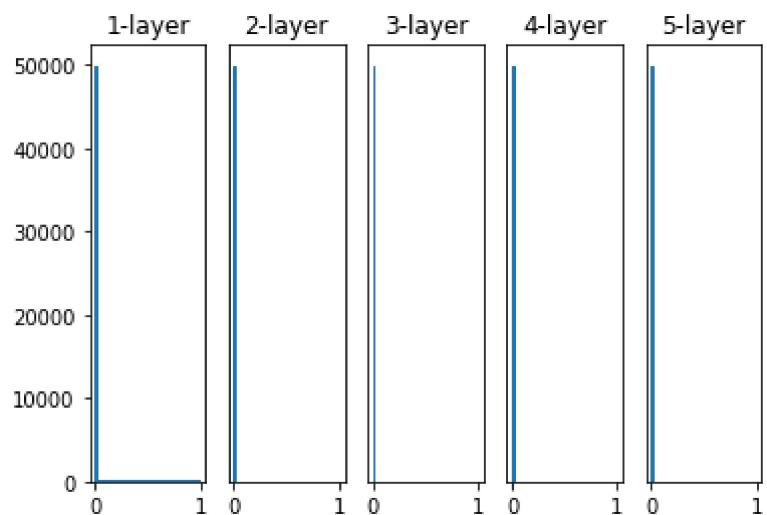
    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    #z = sigmoid(a)
    z = ReLU(a)
    # z = tanh(a)

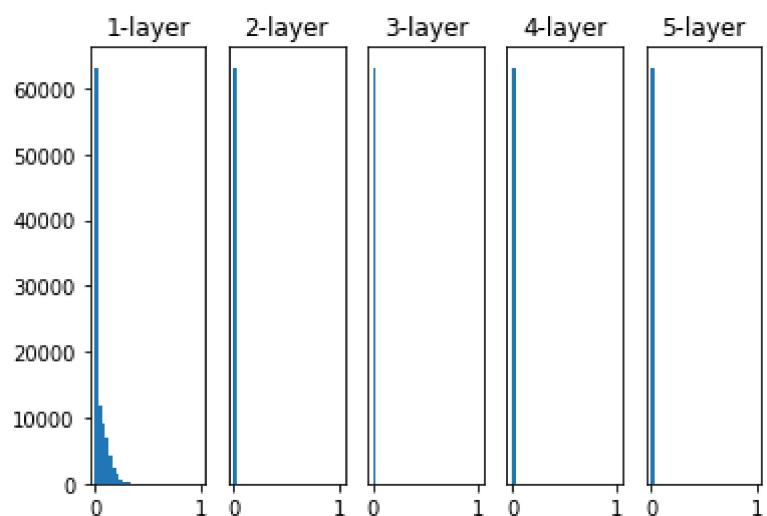
    activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()
```

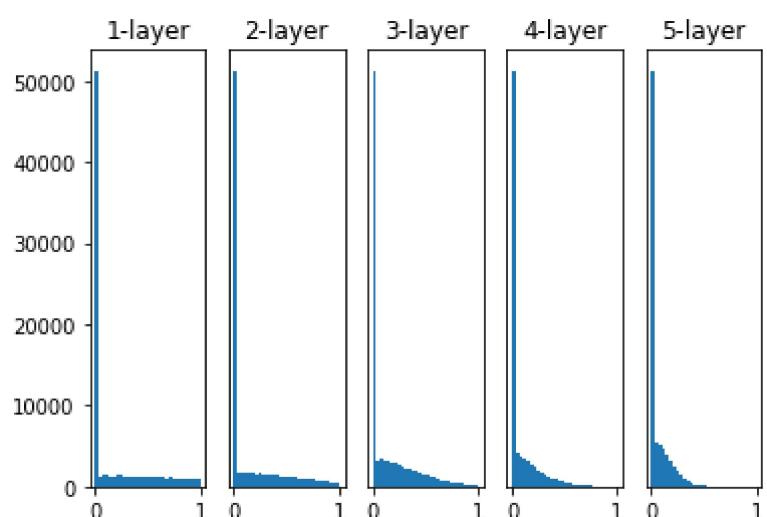
標準偏差1の正規分布 :  $w = np.random.randn(node\_num, node\_num) * 1$



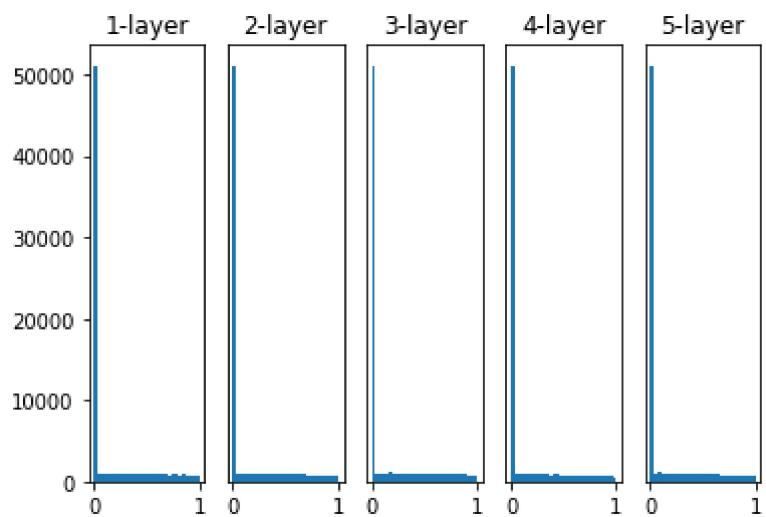
標準偏差0.01の正規分布 :  $w = np.random.randn(node\_num, node\_num) * 0.01$



Xavierの初期値 :  $w = np.random.randn(node\_num, node\_num) * np.sqrt(1.0 / node\_num)$



Heの初期値 :  $w = np.random.randn(node\_num, node\_num) * np.sqrt(2.0 / node\_num)$



重みの初期値 (tanh関数をアクティベーション関数にした場合)

In [16]:

```
# coding: utf-8
import numpy as np
import matplotlib.pyplot as plt

def sigmoid(x):
    return 1 / (1 + np.exp(-x))

def ReLU(x):
    return np.maximum(0, x)

def tanh(x):
    return np.tanh(x)

input_data = np.random.randn(1000, 100) # 1000個のデータ
node_num = 100 # 各隠れ層のノード（ニューロン）の数
hidden_layer_size = 5 # 隠れ層が5層
activations = {} # ここにアクティベーションの結果を格納する

x = input_data
print("標準偏差1の正規分布 : w = np.random.randn(node_num, node_num) * 1")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    w = np.random.randn(node_num, node_num) * 1
    # w = np.random.randn(node_num, node_num) * 0.01
    # w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    # w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    z = sigmoid(a)
    #z = ReLU(a)
    #z = tanh(a)

    activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()

x = input_data

print("標準偏差0.01の正規分布 : w = np.random.randn(node_num, node_num) * 0.01")
for i in range(hidden_layer_size):
    if i != 0:
```

```

x = activations[i-1]

# 初期値の値をいろいろ変えて実験しよう !
#w = np.random.randn(node_num, node_num) * 1
w = np.random.randn(node_num, node_num) * 0.01
# w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
# w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

a = np.dot(x, w)

# 活性化関数の種類も変えて実験しよう !
#z = sigmoid(a)
#z = ReLU(a)
z = tanh(a)

activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    #plt.xlim(0.1, 1)
    #plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()

x = input_data

print("Xavierの初期値 : w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    #w = np.random.randn(node_num, node_num) * 1
    #w = np.random.randn(node_num, node_num) * 0.01
    w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    # w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    #z = sigmoid(a)
    #z = ReLU(a)
    z = tanh(a)

    activations[i] = z

    # ヒストグラムを描画
    for i, a in activations.items():
        plt.subplot(1, len(activations), i+1)
        plt.title(str(i+1) + "-layer")
        if i != 0: plt.yticks([], [])
        #plt.xlim(0.1, 1)
        #plt.ylim(0, 7000)
        plt.hist(a.flatten(), 30, range=(0, 1))

```

```
plt.show()

x = input_data

print("Heの初期値 : w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)")
for i in range(hidden_layer_size):
    if i != 0:
        x = activations[i-1]

    # 初期値の値をいろいろ変えて実験しよう !
    #w = np.random.randn(node_num, node_num) * 1
    #w = np.random.randn(node_num, node_num) * 0.01
    #w = np.random.randn(node_num, node_num) * np.sqrt(1.0 / node_num)
    w = np.random.randn(node_num, node_num) * np.sqrt(2.0 / node_num)

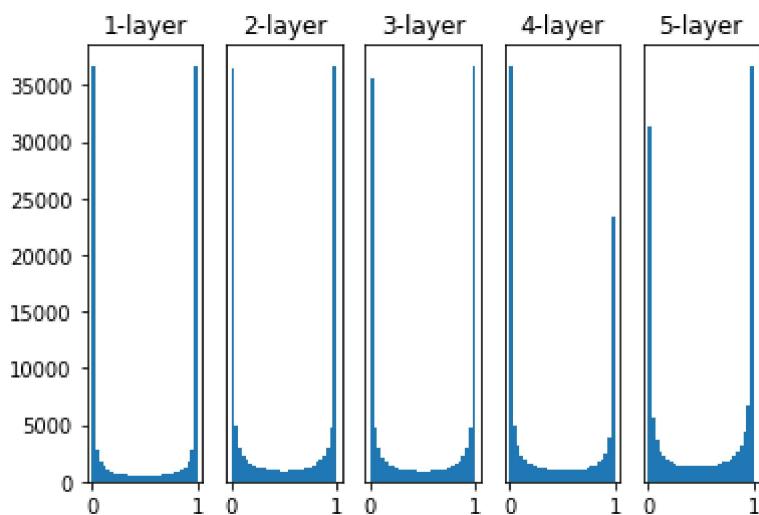
    a = np.dot(x, w)

    # 活性化関数の種類も変えて実験しよう !
    #z = sigmoid(a)
    #z = ReLU(a)
    z = tanh(a)

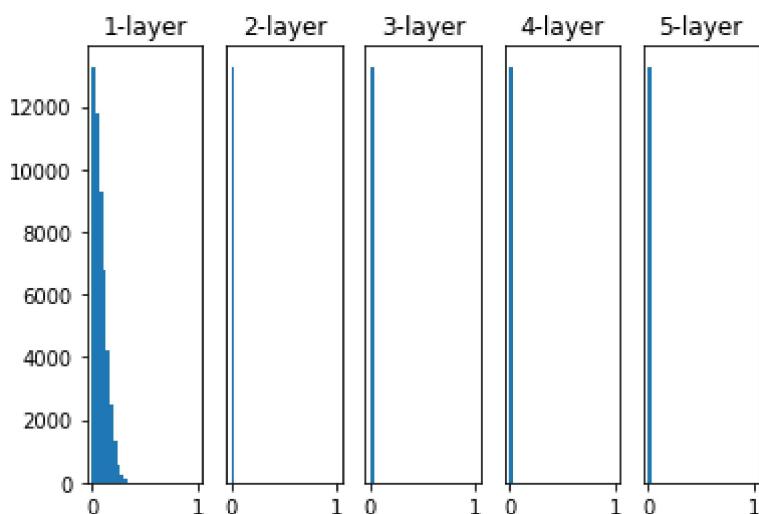
    activations[i] = z

# ヒストグラムを描画
for i, a in activations.items():
    plt.subplot(1, len(activations), i+1)
    plt.title(str(i+1) + "-layer")
    if i != 0: plt.yticks([], [])
    # plt.xlim(0, 1)
    # plt.ylim(0, 7000)
    plt.hist(a.flatten(), 30, range=(0, 1))
plt.show()
```

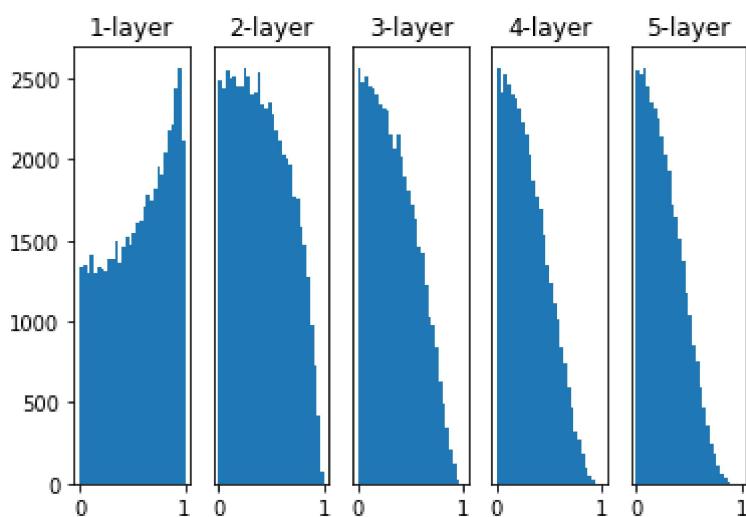
標準偏差1の正規分布 :  $w = np.random.randn(node\_num, node\_num) * 1$



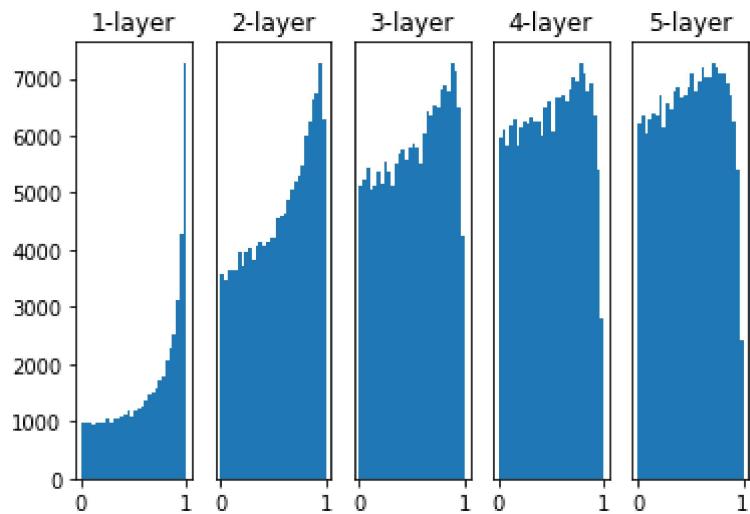
標準偏差0.01の正規分布 :  $w = np.random.randn(node\_num, node\_num) * 0.01$



Xavierの初期値 :  $w = np.random.randn(node\_num, node\_num) * np.sqrt(1.0 / node\_num)$



Heの初期値 :  $w = np.random.randn(node\_num, node\_num) * np.sqrt(2.0 / node\_num)$



ベストプラクティス：アクティベーション関数がReLU関数ならHeの初期値を、アクティベーション関数がSigmoid関数ならXavierの初期値を、アクティベーション関数がtanh関数なら・・・？

ReLU関数をアクティベーション関数として持ったMNISTニューラルネットワークに対するの重み初期値分布による誤差比較

In [28]:

```
# coding: utf-8
import os
import sys

sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.util import smooth_curve
from common.multi_layer_net import MultiLayerNet
from common.optimizer import SGD

# 0:MNISTデータの読み込み=====
(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

train_size = x_train.shape[0]
batch_size = 128
max_iterations = 2000

# 1:実験の設定=====
weight_init_types = {'std=0.01': 0.01, 'Xavier': 'sigmoid', 'He': 'relu'}
optimizer = SGD(lr=0.01)

networks = {}
train_loss = {}
for key, weight_type in weight_init_types.items():
    networks[key] = MultiLayerNet(input_size=784, hidden_size_list=[100, 100, 100, 100],
                                    output_size=10, weight_init_std=weight_type)
    train_loss[key] = []

# 2:訓練の開始=====
for i in range(max_iterations):
    batch_mask = np.random.choice(train_size, batch_size)
    x_batch = x_train[batch_mask]
    t_batch = t_train[batch_mask]

    for key in weight_init_types.keys():
        grads = networks[key].gradient(x_batch, t_batch)
        optimizer.update(networks[key].params, grads)

        loss = networks[key].loss(x_batch, t_batch)
        train_loss[key].append(loss)

    if i % 100 == 0:
        print("===== iteration:" + str(i) + "=====")
        for key in weight_init_types.keys():
            loss = networks[key].loss(x_batch, t_batch)
            print(key + ":" + str(loss))

# 3. グラフの描画=====
markers = {'std=0.01': 'o', 'Xavier': 's', 'He': 'D'}
x = np.arange(max_iterations)
for key in weight_init_types.keys():
    plt.plot(x, smooth_curve(train_loss[key]), marker=markers[key], markevery=100, label=key)
plt.xlabel("iterations")
```

```
plt.ylabel("loss")
plt.ylim(0, 2.5)
plt.legend()
plt.show()
```

=====iteration:0=====

std=0.01: 2.3025047128640304  
Xavier: 2.313383374896556  
He: 2.352801464350353

=====iteration:100=====

std=0.01: 2.30188197530518  
Xavier: 2.2583643765094026  
He: 1.6330238543552074

=====iteration:200=====

std=0.01: 2.30225644165031  
Xavier: 2.127229207938062  
He: 0.8634702094812619

=====iteration:300=====

std=0.01: 2.301582259289641  
Xavier: 1.8551789364382827  
He: 0.5666139899888614

=====iteration:400=====

std=0.01: 2.301262224991351  
Xavier: 1.448088413431125  
He: 0.5453957233261428

=====iteration:500=====

std=0.01: 2.304384023598031  
Xavier: 0.9737266777861089  
He: 0.45937795981259955

=====iteration:600=====

std=0.01: 2.301924097038047  
Xavier: 0.6974414715127122  
He: 0.40279157119477155

=====iteration:700=====

std=0.01: 2.3049056291970613  
Xavier: 0.6206533838797386  
He: 0.3511152901133047

=====iteration:800=====

std=0.01: 2.3021688467700567  
Xavier: 0.5277811176619274  
He: 0.31619016329750155

=====iteration:900=====

std=0.01: 2.305490581934902  
Xavier: 0.5316058519119236  
He: 0.3863825629734081

=====iteration:1000=====

std=0.01: 2.3019716689938097  
Xavier: 0.33345604396308015  
He: 0.19290576757400066

=====iteration:1100=====

std=0.01: 2.3047431769893496  
Xavier: 0.32166373878701876  
He: 0.19660967913562705

=====iteration:1200=====

std=0.01: 2.3065100112564387  
Xavier: 0.3919677636547596  
He: 0.2811031060728417

=====iteration:1300=====

std=0.01: 2.298382991120612  
Xavier: 0.3256385951040112  
He: 0.23813610990007453

=====iteration:1400=====

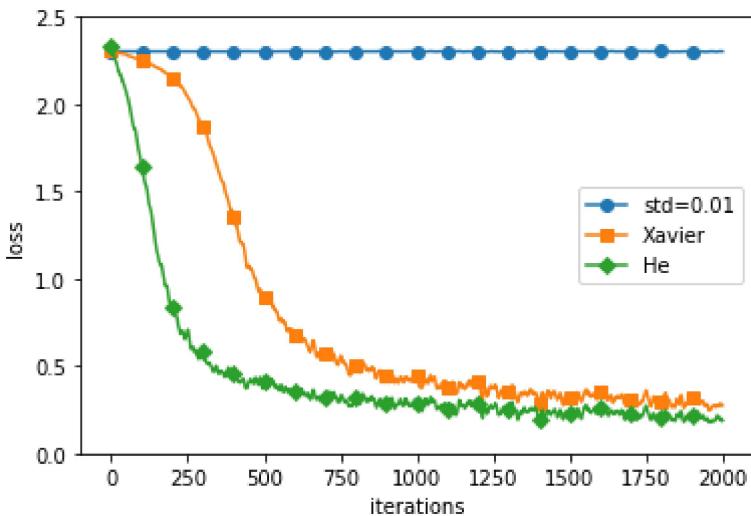
std=0.01: 2.3002620821553146  
Xavier: 0.19148429374938503  
He: 0.1170751590197682

=====iteration:1500=====

```

std=0.01: 2.3102575567578034
Xavier: 0.2768294280683701
He: 0.17432819226626506
=====iteration:1600=====
std=0.01: 2.296022719092897
Xavier: 0.3269595160743929
He: 0.2578675253280397
=====iteration:1700=====
std=0.01: 2.2974744452575573
Xavier: 0.2851566039208631
He: 0.21482860725066988
=====iteration:1800=====
std=0.01: 2.305259722415504
Xavier: 0.3747880669248833
He: 0.28387139627777247
=====iteration:1900=====
std=0.01: 2.2960603606317145
Xavier: 0.30538080507020426
He: 0.21328616728326982

```



先述の通り、Heの初期値で学習が上手くいっている（誤差が減衰していっている）ことを確認する。これは

```

networks[key] = MultiLayerNet(input_size=784, hidden_size_list=[100, 100, 100, 100],
                                output_size=10, weight_init_std=weight_type)

```

がReLU関数をアクティベーション関数としてもっているからである。今回は5層 × 100個のニューロンのニューラルネットワークでMNISTの手書き文字を学習する際のケースである。

アクティベーション関数によって発火されるニューロンの分布が偏った場合は学習以前の問題であり、もし偏りにより発火しなかった／発火の度合いが極端に低いニューロンにより引き起こされる学習が滞ってしまう。（学習の結果ニューロンの発火が起らぬのではなく、学習パラメータの設定が偏った結果発火が起らぬというのは正当なアクティベーションとは呼ばない）

## Batch Normalization

先述では各層での「発火分布の正規化」をすることで学習の偏りを無くすということでしたがBatch Normalizationでは「各層の中の、ミニバッチ処理の中での発火分布の正規化」をすることで学習の方よりも無くす。以下のメリットがある。

- 学習を速く進行させることができる（学習係数を大きくすることが出来る）
- 初期値にそれほど依存しない
- 過学習を抑制する（Dropoutなどの必要性を減らす）

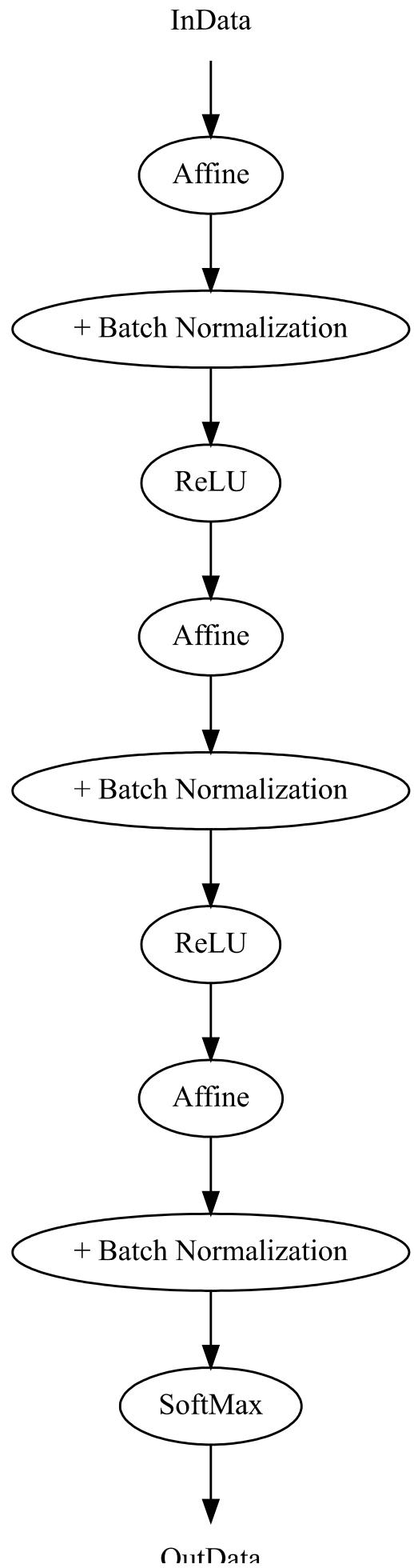
## Batch Normalization とは

In [25]:

```
from graphviz import Digraph
dot = Digraph(comment="Batch Normalization: バッチ毎に正規化処理を行う")
dot.attr(rankdir="UD")
#dot.attr(ranksep="1.2")
dot.attr(nodesep=".05")
#dot.attr(margin="1")
#dot.attr(splines="polyline") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="Batch Normalization: バッチ毎に正規化処理を行う")
with dot.subgraph(name="main") as main:
    with main.subgraph(name="cluster_L1") as L1:
        L1.attr(label="")
        L1.attr(color="white")
        L1.node("main.L1N1", "InData", color="white")
    with main.subgraph(name="cluster_L2") as L2:
        L2.attr(label="")
        L2.attr(color="white")
        L2.node("main.L2N1", "Affine")
    with main.subgraph(name="cluster_L3") as L3:
        L3.attr(label="")
        L3.attr(color="white")
        L3.node("main.L3N1", "+ Batch Normalization")
    with main.subgraph(name="cluster_L4") as L4:
        L4.attr(label="")
        L4.attr(color="white")
        L4.node("main.L4N1", "ReLU")
    with main.subgraph(name="cluster_L5") as L5:
        L5.attr(label="")
        L5.attr(color="white")
        L5.node("main.L5N1", "Affine")
    with main.subgraph(name="cluster_L6") as L6:
        L6.attr(label="")
        L6.attr(color="white")
        L6.node("main.L6N1", "+ Batch Normalization")
    with main.subgraph(name="cluster_L7") as L7:
        L7.attr(label="")
        L7.attr(color="white")
        L7.node("main.L7N1", "ReLU")
    with main.subgraph(name="cluster_L8") as L8:
        L8.attr(label="")
        L8.attr(color="white")
        L8.node("main.L8N1", "Affine")
    with main.subgraph(name="cluster_L9") as L9:
        L9.attr(label="")
        L9.attr(color="white")
        L9.node("main.L9N1", "+ Batch Normalization")
    with main.subgraph(name="cluster_L10") as L10:
        L10.attr(label="")
        L10.attr(color="white")
        L10.node("main.L10N1", "SoftMax")
    with main.subgraph(name="cluster_L11") as L11:
        L11.attr(label="")
        L11.attr(color="white")
        L11.node("main.L11N1", "OutData", color="white")
dot.edge("main.L1N1", "main.L2N1", label="")
dot.edge("main.L2N1", "main.L3N1", label="")
dot.edge("main.L3N1", "main.L4N1", label="")
dot.edge("main.L4N1", "main.L5N1", label="")
dot.edge("main.L5N1", "main.L6N1", label="")
```

```
dot.edge("main.L6N1", "main.L7N1", label="")
dot.edge("main.L7N1", "main.L8N1", label="")
dot.edge("main.L8N1", "main.L9N1", label="")
dot.edge("main.L9N1", "main.L10N1", label="")
dot.edge("main.L10N1", "main.L11N1", label="")
dot
```

Out[25] :



## Batch Normalization: バッチ毎に正規化処理を行う

Batch Normalizationはその名の通り学習の際のミニバッチを基本単位としてミニバッチ毎に正規化を行います。具体的には、データの平均が0で分散が1になるように正規化をその都度行う。正規化を行うタイミングは活性化関数の前（または後）にすることで、データ分布の偏りを減らすことが出来る。

### BatchNormalizationによる正規化処理

<https://qiita.com/t-tkd3a/items/14950dbf55f7a3095600> (<https://qiita.com/t-tkd3a/items/14950dbf55f7a3095600>)

#### ミニバッチ配列を平均0 分散1に計算し直す処理（一般的な正規化処理）

- ミニバッチ平均:  $\mu_x \leftarrow \frac{1}{N} \sum_{i=1}^N x_i$
- ミニバッチ分散:  $\sigma_x^2 \leftarrow \frac{1}{N} \sum_{i=1}^N (x_i - \mu_x)^2$
- ミニバッチの正規化計算式:  $\hat{x}_i \leftarrow \frac{x_i - \mu_x}{\sqrt{\sigma_x^2 + \epsilon}}$

$x_i$ : ミニバッチ配列  $(x_1, x_2, x_3, x_4, \dots, x_i)$

$\epsilon$ : 非常に小さな値(0.0000001等)※0除算回避の為

$\hat{x}_i$ : 正規化後ミニバッチ配列  $(\hat{x}_1, \hat{x}_2, \hat{x}_3, \hat{x}_4, \dots, \hat{x}_i)$

#### 正規化したデータに対するスケールとシフト変換が可能になる

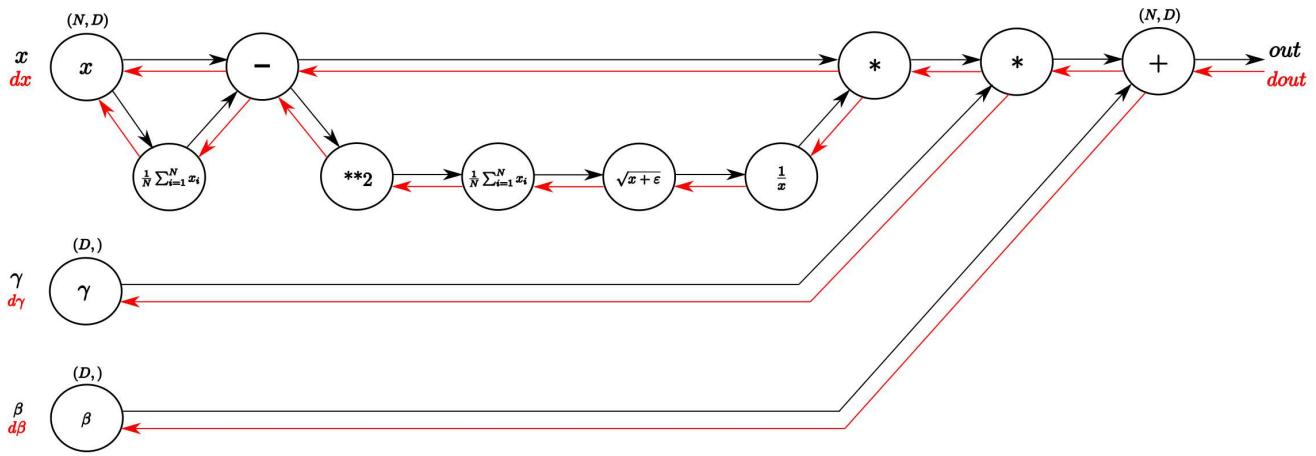
- ミニバッチ配列のスケール・シフト:  $y_i \leftarrow \gamma \hat{x}_i + \beta$

$\gamma$ : 変倍調整パラメタ。 $\gamma = 1$ を初期値とする。

$\beta$ : 移動調整パラメタ。 $\beta = 0$ を初期値とする。

### Batch Normalizationの計算グラフ

<https://kratzert.github.io/2016/02/12/understanding-the-gradient-flow-through-the-batch-normalization-layer.html> (<https://kratzert.github.io/2016/02/12/understanding-the-gradient-flow-through-the-batch-normalization-layer.html>)



## Batch Normalizationの評価

In [27]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.multi_layer_net_extend import MultiLayerNetExtend
from common.optimizer import SGD, Adam

(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

# 学習データを削減
x_train = x_train[:1000]
t_train = t_train[:1000]

max_epochs = 20
train_size = x_train.shape[0]
batch_size = 100
learning_rate = 0.01

def __train(weight_init_std):
    bn_network = MultiLayerNetExtend(input_size=784, hidden_size_list=[100, 100, 100, 100, 100], output_size=10,
                                      weight_init_std=weight_init_std, use_batchnorm=True)
    network = MultiLayerNetExtend(input_size=784, hidden_size_list=[100, 100, 100, 100, 100], output_size=10,
                                   weight_init_std=weight_init_std)
    optimizer = SGD(lr=learning_rate)

    train_acc_list = []
    bn_train_acc_list = []

    iter_per_epoch = max(train_size / batch_size, 1)
    epoch_cnt = 0

    for i in range(1000000000):
        batch_mask = np.random.choice(train_size, batch_size)
        x_batch = x_train[batch_mask]
        t_batch = t_train[batch_mask]

        for _network in (bn_network, network):
            grads = _network.gradient(x_batch, t_batch)
            optimizer.update(_network.params, grads)

        if i % iter_per_epoch == 0:
            train_acc = network.accuracy(x_train, t_train)
            bn_train_acc = bn_network.accuracy(x_train, t_train)
            train_acc_list.append(train_acc)
            bn_train_acc_list.append(bn_train_acc)

            print("epoch:" + str(epoch_cnt) + " | " + str(train_acc) + " - " + str(bn_train_acc))
        epoch_cnt += 1
        if epoch_cnt >= max_epochs:
            break

    return train_acc_list, bn_train_acc_list
```

```
# 3. グラフの描画=====
weight_scale_list = np.logspace(0, -4, num=16)
x = np.arange(max_epochs)

for i, w in enumerate(weight_scale_list):
    print("===== " + str(i+1) + "/16 =====")
    train_acc_list, bn_train_acc_list = __train(w)

    plt.subplot(4, 4, i+1)
    plt.title("W:" + str(w))
    if i == 15:
        plt.plot(x, bn_train_acc_list, label='Batch Normalization', markevery=2)
        plt.plot(x, train_acc_list, linestyle="--", label='Normal (without BatchNorm)', markevery=2)
    else:
        plt.plot(x, bn_train_acc_list, markevery=2)
        plt.plot(x, train_acc_list, linestyle="--", markevery=2)

    plt.ylim(0, 1.0)
    if i % 4:
        plt.yticks([])
    else:
        plt.ylabel("accuracy")
    if i < 12:
        plt.xticks([])
    else:
        plt.xlabel("epochs")
    plt.legend(loc='lower right')

plt.show()
```

===== 1/16 =====

```
epoch:0 | 0.093 - 0.113
epoch:1 | 0.117 - 0.128
epoch:2 | 0.116 - 0.134
epoch:3 | 0.116 - 0.15
epoch:4 | 0.116 - 0.172
epoch:5 | 0.117 - 0.188
epoch:6 | 0.116 - 0.217
epoch:7 | 0.116 - 0.23
epoch:8 | 0.116 - 0.25
epoch:9 | 0.116 - 0.266
epoch:10 | 0.116 - 0.286
epoch:11 | 0.116 - 0.304
epoch:12 | 0.116 - 0.325
epoch:13 | 0.116 - 0.331
epoch:14 | 0.116 - 0.339
epoch:15 | 0.116 - 0.354
epoch:16 | 0.116 - 0.371
epoch:17 | 0.116 - 0.386
epoch:18 | 0.116 - 0.407
```

No handles with labels found to put in legend.

```
epoch:19 | 0.116 - 0.416
```

===== 2/16 =====

```
epoch:0 | 0.097 - 0.068
```

```
/home/nbuser/library/common/multi_layer_net_extend.py:101: RuntimeWarning: overflow encountered in square
```

```
    weight_decay += 0.5 * self.weight_decay_lambda * np.sum(W**2)
```

```
/home/nbuser/library/common/multi_layer_net_extend.py:101: RuntimeWarning: invalid value encountered in double_scalars
```

```
    weight_decay += 0.5 * self.weight_decay_lambda * np.sum(W**2)
```

```
/home/nbuser/anaconda3_420/lib/python3.5/site-packages/numpy/core/_methods.py:26:
```

```
RuntimeWarning: invalid value encountered in reduce
```

```
    return umr_maximum(a, axis, None, out, keepdims)
```

```
/home/nbuser/library/common/layers.py:12: RuntimeWarning: invalid value encountered in less_equal
```

```
    self.mask = (x <= 0)
```

```
epoch:1 | 0.097 - 0.079
```

```
epoch:2 | 0.097 - 0.104
```

```
epoch:3 | 0.097 - 0.113
```

```
epoch:4 | 0.097 - 0.133
```

```
epoch:5 | 0.097 - 0.165
```

```
epoch:6 | 0.097 - 0.185
```

```
epoch:7 | 0.097 - 0.203
```

```
epoch:8 | 0.097 - 0.245
```

```
epoch:9 | 0.097 - 0.284
```

```
epoch:10 | 0.097 - 0.295
```

```
epoch:11 | 0.097 - 0.332
```

```
epoch:12 | 0.097 - 0.347
```

```
epoch:13 | 0.097 - 0.373
```

```
epoch:14 | 0.097 - 0.385
```

```
epoch:15 | 0.097 - 0.407
```

```
epoch:16 | 0.097 - 0.42
```

```
epoch:17 | 0.097 - 0.441
```

```
epoch:18 | 0.097 - 0.454
```

No handles with labels found to put in legend.

```
epoch:19 | 0.097 - 0.464
===== 3/16 =====
epoch:0 | 0.087 - 0.072
epoch:1 | 0.268 - 0.087
epoch:2 | 0.373 - 0.109
epoch:3 | 0.502 - 0.13
epoch:4 | 0.58 - 0.179
epoch:5 | 0.636 - 0.202
epoch:6 | 0.694 - 0.241
epoch:7 | 0.715 - 0.279
epoch:8 | 0.765 - 0.318
epoch:9 | 0.794 - 0.353
epoch:10 | 0.809 - 0.373
epoch:11 | 0.84 - 0.413
epoch:12 | 0.864 - 0.446
epoch:13 | 0.885 - 0.478
epoch:14 | 0.894 - 0.507
epoch:15 | 0.916 - 0.529
epoch:16 | 0.925 - 0.541
epoch:17 | 0.93 - 0.57
epoch:18 | 0.944 - 0.599
```

No handles with labels found to put in legend.

```
epoch:19 | 0.95 - 0.62
===== 4/16 =====
epoch:0 | 0.11 - 0.079
epoch:1 | 0.202 - 0.104
epoch:2 | 0.33 - 0.16
epoch:3 | 0.455 - 0.225
epoch:4 | 0.517 - 0.291
epoch:5 | 0.602 - 0.362
epoch:6 | 0.643 - 0.421
epoch:7 | 0.67 - 0.482
epoch:8 | 0.695 - 0.518
epoch:9 | 0.714 - 0.559
epoch:10 | 0.74 - 0.594
epoch:11 | 0.752 - 0.616
epoch:12 | 0.77 - 0.646
epoch:13 | 0.78 - 0.668
epoch:14 | 0.789 - 0.682
epoch:15 | 0.801 - 0.698
epoch:16 | 0.815 - 0.722
epoch:17 | 0.825 - 0.737
epoch:18 | 0.831 - 0.755
```

No handles with labels found to put in legend.

```
epoch:19 | 0.839 - 0.764
===== 5/16 =====
epoch:0 | 0.095 - 0.105
epoch:1 | 0.099 - 0.164
epoch:2 | 0.107 - 0.222
epoch:3 | 0.115 - 0.333
epoch:4 | 0.131 - 0.421
epoch:5 | 0.156 - 0.516
epoch:6 | 0.169 - 0.585
epoch:7 | 0.199 - 0.646
epoch:8 | 0.227 - 0.694
epoch:9 | 0.239 - 0.719
epoch:10 | 0.257 - 0.742
epoch:11 | 0.247 - 0.76
epoch:12 | 0.247 - 0.78
epoch:13 | 0.261 - 0.807
epoch:14 | 0.264 - 0.82
epoch:15 | 0.275 - 0.833
epoch:16 | 0.26 - 0.846
epoch:17 | 0.27 - 0.852
epoch:18 | 0.264 - 0.861
```

No handles with labels found to put in legend.

```
epoch:19 | 0.279 - 0.872
===== 6/16 =====
epoch:0 | 0.087 - 0.092
epoch:1 | 0.125 - 0.268
epoch:2 | 0.137 - 0.511
epoch:3 | 0.129 - 0.637
epoch:4 | 0.132 - 0.709
epoch:5 | 0.113 - 0.749
epoch:6 | 0.113 - 0.788
epoch:7 | 0.121 - 0.824
epoch:8 | 0.139 - 0.848
epoch:9 | 0.113 - 0.863
epoch:10 | 0.143 - 0.878
epoch:11 | 0.122 - 0.897
epoch:12 | 0.123 - 0.908
epoch:13 | 0.116 - 0.916
epoch:14 | 0.116 - 0.932
epoch:15 | 0.116 - 0.938
epoch:16 | 0.116 - 0.947
epoch:17 | 0.129 - 0.955
epoch:18 | 0.157 - 0.958
```

No handles with labels found to put in legend.

```
epoch:19 | 0.146 - 0.963
===== 7/16 =====
epoch:0 | 0.094 - 0.102
epoch:1 | 0.118 - 0.34
epoch:2 | 0.117 - 0.635
epoch:3 | 0.117 - 0.731
epoch:4 | 0.117 - 0.768
epoch:5 | 0.117 - 0.808
epoch:6 | 0.116 - 0.831
epoch:7 | 0.116 - 0.849
epoch:8 | 0.116 - 0.871
epoch:9 | 0.116 - 0.889
epoch:10 | 0.116 - 0.91
epoch:11 | 0.116 - 0.919
epoch:12 | 0.116 - 0.93
epoch:13 | 0.116 - 0.952
epoch:14 | 0.116 - 0.962
epoch:15 | 0.116 - 0.969
epoch:16 | 0.116 - 0.98
epoch:17 | 0.116 - 0.985
epoch:18 | 0.116 - 0.985
```

No handles with labels found to put in legend.

```
epoch:19 | 0.116 - 0.988
===== 8/16 =====
epoch:0 | 0.105 - 0.092
epoch:1 | 0.117 - 0.299
epoch:2 | 0.117 - 0.553
epoch:3 | 0.105 - 0.677
epoch:4 | 0.105 - 0.757
epoch:5 | 0.116 - 0.83
epoch:6 | 0.116 - 0.879
epoch:7 | 0.117 - 0.919
epoch:8 | 0.116 - 0.944
epoch:9 | 0.116 - 0.967
epoch:10 | 0.116 - 0.975
epoch:11 | 0.116 - 0.978
epoch:12 | 0.116 - 0.987
epoch:13 | 0.116 - 0.989
epoch:14 | 0.117 - 0.993
epoch:15 | 0.117 - 0.995
epoch:16 | 0.117 - 0.998
epoch:17 | 0.116 - 0.997
epoch:18 | 0.117 - 0.997
```

No handles with labels found to put in legend.

```
epoch:19 | 0.116 - 0.997
===== 9/16 =====
epoch:0 | 0.105 - 0.134
epoch:1 | 0.116 - 0.532
epoch:2 | 0.116 - 0.736
epoch:3 | 0.116 - 0.811
epoch:4 | 0.116 - 0.846
epoch:5 | 0.116 - 0.889
epoch:6 | 0.116 - 0.907
epoch:7 | 0.116 - 0.913
epoch:8 | 0.117 - 0.948
epoch:9 | 0.116 - 0.98
epoch:10 | 0.116 - 0.986
epoch:11 | 0.116 - 0.989
epoch:12 | 0.116 - 0.996
epoch:13 | 0.116 - 0.996
epoch:14 | 0.116 - 0.999
epoch:15 | 0.116 - 0.999
epoch:16 | 0.116 - 1.0
epoch:17 | 0.116 - 1.0
epoch:18 | 0.116 - 1.0
```

No handles with labels found to put in legend.

```
epoch:19 | 0.116 - 1.0
===== 10/16 =====
epoch:0 | 0.105 - 0.137
epoch:1 | 0.116 - 0.499
epoch:2 | 0.117 - 0.75
epoch:3 | 0.117 - 0.807
epoch:4 | 0.117 - 0.912
epoch:5 | 0.117 - 0.862
epoch:6 | 0.116 - 0.979
epoch:7 | 0.116 - 0.979
epoch:8 | 0.116 - 0.968
epoch:9 | 0.116 - 0.987
epoch:10 | 0.116 - 0.993
epoch:11 | 0.116 - 0.992
epoch:12 | 0.116 - 0.992
epoch:13 | 0.116 - 0.994
epoch:14 | 0.117 - 0.996
epoch:15 | 0.117 - 0.997
epoch:16 | 0.117 - 0.997
epoch:17 | 0.117 - 0.997
epoch:18 | 0.117 - 0.998
```

No handles with labels found to put in legend.

```
epoch:19 | 0.117 - 0.998
===== 11/16 =====
epoch:0 | 0.092 - 0.212
epoch:1 | 0.117 - 0.73
epoch:2 | 0.117 - 0.777
epoch:3 | 0.117 - 0.823
epoch:4 | 0.116 - 0.923
epoch:5 | 0.116 - 0.936
epoch:6 | 0.116 - 0.884
epoch:7 | 0.116 - 0.968
epoch:8 | 0.116 - 0.98
epoch:9 | 0.116 - 0.982
epoch:10 | 0.116 - 0.991
epoch:11 | 0.116 - 0.991
epoch:12 | 0.116 - 0.985
epoch:13 | 0.116 - 0.987
epoch:14 | 0.116 - 0.968
epoch:15 | 0.116 - 0.992
epoch:16 | 0.116 - 0.995
epoch:17 | 0.116 - 0.955
epoch:18 | 0.116 - 0.995
```

No handles with labels found to put in legend.

```
epoch:19 | 0.116 - 0.992
===== 12/16 =====
epoch:0 | 0.105 - 0.112
epoch:1 | 0.116 - 0.517
epoch:2 | 0.117 - 0.647
epoch:3 | 0.116 - 0.674
epoch:4 | 0.117 - 0.642
epoch:5 | 0.117 - 0.687
epoch:6 | 0.117 - 0.689
epoch:7 | 0.117 - 0.698
epoch:8 | 0.117 - 0.696
epoch:9 | 0.117 - 0.701
epoch:10 | 0.117 - 0.782
epoch:11 | 0.117 - 0.786
epoch:12 | 0.117 - 0.875
epoch:13 | 0.116 - 0.89
epoch:14 | 0.117 - 0.963
epoch:15 | 0.117 - 0.884
epoch:16 | 0.117 - 0.891
epoch:17 | 0.117 - 0.896
epoch:18 | 0.117 - 0.985
```

No handles with labels found to put in legend.

```
epoch:19 | 0.117 - 0.935
===== 13/16 =====
epoch:0 | 0.099 - 0.16
epoch:1 | 0.117 - 0.39
epoch:2 | 0.117 - 0.472
epoch:3 | 0.117 - 0.585
epoch:4 | 0.117 - 0.6
epoch:5 | 0.117 - 0.653
epoch:6 | 0.117 - 0.662
epoch:7 | 0.117 - 0.663
epoch:8 | 0.117 - 0.671
epoch:9 | 0.117 - 0.678
epoch:10 | 0.117 - 0.692
epoch:11 | 0.117 - 0.692
epoch:12 | 0.117 - 0.695
epoch:13 | 0.117 - 0.702
epoch:14 | 0.117 - 0.776
epoch:15 | 0.117 - 0.791
epoch:16 | 0.117 - 0.736
epoch:17 | 0.117 - 0.748
epoch:18 | 0.116 - 0.781
```

No handles with labels found to put in legend.

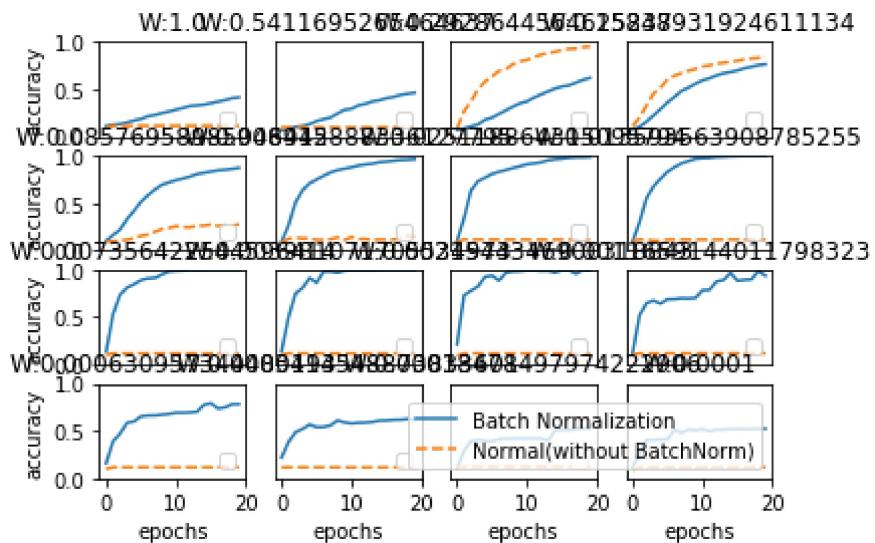
```
epoch:19 | 0.116 - 0.782
===== 14/16 =====
epoch:0 | 0.116 - 0.22
epoch:1 | 0.117 - 0.383
epoch:2 | 0.117 - 0.486
epoch:3 | 0.117 - 0.52
epoch:4 | 0.117 - 0.567
epoch:5 | 0.117 - 0.539
epoch:6 | 0.117 - 0.541
epoch:7 | 0.117 - 0.558
epoch:8 | 0.117 - 0.61
epoch:9 | 0.116 - 0.589
epoch:10 | 0.116 - 0.578
epoch:11 | 0.116 - 0.585
epoch:12 | 0.116 - 0.587
epoch:13 | 0.116 - 0.594
epoch:14 | 0.116 - 0.609
epoch:15 | 0.116 - 0.61
epoch:16 | 0.116 - 0.617
epoch:17 | 0.116 - 0.618
epoch:18 | 0.116 - 0.625
```

No handles with labels found to put in legend.

```
epoch:19 | 0.116 - 0.618
===== 15/16 =====
epoch:0 | 0.117 - 0.103
epoch:1 | 0.117 - 0.289
epoch:2 | 0.117 - 0.39
epoch:3 | 0.117 - 0.405
epoch:4 | 0.117 - 0.393
epoch:5 | 0.117 - 0.391
epoch:6 | 0.117 - 0.413
epoch:7 | 0.117 - 0.418
epoch:8 | 0.117 - 0.419
epoch:9 | 0.117 - 0.419
epoch:10 | 0.117 - 0.418
epoch:11 | 0.117 - 0.419
epoch:12 | 0.117 - 0.419
epoch:13 | 0.117 - 0.396
epoch:14 | 0.117 - 0.503
epoch:15 | 0.117 - 0.508
epoch:16 | 0.117 - 0.508
epoch:17 | 0.117 - 0.526
epoch:18 | 0.117 - 0.526
```

No handles with labels found to put in legend.

```
epoch:19 | 0.117 - 0.525
===== 16/16 =====
epoch:0 | 0.087 - 0.116
epoch:1 | 0.117 - 0.258
epoch:2 | 0.116 - 0.402
epoch:3 | 0.116 - 0.404
epoch:4 | 0.117 - 0.409
epoch:5 | 0.117 - 0.409
epoch:6 | 0.117 - 0.512
epoch:7 | 0.117 - 0.479
epoch:8 | 0.117 - 0.515
epoch:9 | 0.117 - 0.502
epoch:10 | 0.117 - 0.52
epoch:11 | 0.117 - 0.494
epoch:12 | 0.117 - 0.513
epoch:13 | 0.117 - 0.512
epoch:14 | 0.117 - 0.522
epoch:15 | 0.117 - 0.518
epoch:16 | 0.117 - 0.521
epoch:17 | 0.117 - 0.521
epoch:18 | 0.117 - 0.522
epoch:19 | 0.117 - 0.523
```



## 正則化

正則化とは特定のデータに囚われない学習モデルを作ること。

## 過学習

過学習とは、訓練データだけに適応しすぎてしまい、訓練データに含まれない他のデータにはうまく対応できない状態を言う。

過学習が起きる原因としては以下のような原因が挙げられる。

- パラメータを大量に持ち、表現力の高いモデルであること
- 訓練データが少ないとこと

## わざと過学習させる

In [29]:

```
# coding: utf-8
import os
import sys

sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.multi_layer_net import MultiLayerNet
from common.optimizer import SGD

(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

# 過学習を再現するために、学習データを削減
x_train = x_train[:300]
t_train = t_train[:300]

# weight decay (荷重減衰) の設定 =====
#weight_decay_lambda = 0 # weight decayを使用しない場合
weight_decay_lambda = 0.1
# =====

network = MultiLayerNet(input_size=784, hidden_size_list=[100, 100, 100, 100, 100, 100], output_size=10,
                        weight_decay_lambda=weight_decay_lambda)
optimizer = SGD(lr=0.01)

max_epochs = 201
train_size = x_train.shape[0]
batch_size = 100

train_loss_list = []
train_acc_list = []
test_acc_list = []

iter_per_epoch = max(train_size / batch_size, 1)
epoch_cnt = 0

for i in range(1000000000):
    batch_mask = np.random.choice(train_size, batch_size)
    x_batch = x_train[batch_mask]
    t_batch = t_train[batch_mask]

    grads = network.gradient(x_batch, t_batch)
    optimizer.update(network.params, grads)

    if i % iter_per_epoch == 0:
        train_acc = network.accuracy(x_train, t_train)
        test_acc = network.accuracy(x_test, t_test)
        train_acc_list.append(train_acc)
        test_acc_list.append(test_acc)

        print("epoch:" + str(epoch_cnt) + ", train acc:" + str(train_acc) + ", test acc:" + str(test_acc))

    epoch_cnt += 1
    if epoch_cnt >= max_epochs:
        break
```

```
# 3. グラフの描画=====
markers = {'train': 'o', 'test': 's'}
x = np.arange(max_epochs)
plt.plot(x, train_acc_list, marker='o', label='train', markevery=10)
plt.plot(x, test_acc_list, marker='s', label='test', markevery=10)
plt.xlabel("epochs")
plt.ylabel("accuracy")
plt.ylim(0, 1.0)
plt.legend(loc='lower right')
plt.show()
```

epoch:0, train acc:0.14666666666666667, test acc:0.1087  
epoch:1, train acc:0.1733333333333334, test acc:0.127  
epoch:2, train acc:0.21666666666666667, test acc:0.1475  
epoch:3, train acc:0.2433333333333335, test acc:0.1669  
epoch:4, train acc:0.26, test acc:0.1875  
epoch:5, train acc:0.283333333333333, test acc:0.2045  
epoch:6, train acc:0.30666666666666664, test acc:0.2249  
epoch:7, train acc:0.34, test acc:0.2411  
epoch:8, train acc:0.3466666666666667, test acc:0.2496  
epoch:9, train acc:0.36666666666666664, test acc:0.2624  
epoch:10, train acc:0.3633333333333334, test acc:0.2681  
epoch:11, train acc:0.41, test acc:0.2916  
epoch:12, train acc:0.4233333333333334, test acc:0.3005  
epoch:13, train acc:0.4133333333333333, test acc:0.3031  
epoch:14, train acc:0.4433333333333336, test acc:0.3216  
epoch:15, train acc:0.4633333333333333, test acc:0.3298  
epoch:16, train acc:0.4933333333333335, test acc:0.3542  
epoch:17, train acc:0.49, test acc:0.3539  
epoch:18, train acc:0.5466666666666666, test acc:0.3776  
epoch:19, train acc:0.5366666666666666, test acc:0.3813  
epoch:20, train acc:0.55, test acc:0.392  
epoch:21, train acc:0.58, test acc:0.409  
epoch:22, train acc:0.56, test acc:0.4  
epoch:23, train acc:0.5866666666666667, test acc:0.4197  
epoch:24, train acc:0.613333333333333, test acc:0.4506  
epoch:25, train acc:0.6266666666666667, test acc:0.4604  
epoch:26, train acc:0.6533333333333333, test acc:0.4668  
epoch:27, train acc:0.6466666666666666, test acc:0.4606  
epoch:28, train acc:0.6533333333333333, test acc:0.4579  
epoch:29, train acc:0.63, test acc:0.4444  
epoch:30, train acc:0.673333333333333, test acc:0.4795  
epoch:31, train acc:0.67, test acc:0.4755  
epoch:32, train acc:0.66, test acc:0.4763  
epoch:33, train acc:0.67, test acc:0.4813  
epoch:34, train acc:0.673333333333333, test acc:0.4952  
epoch:35, train acc:0.69, test acc:0.5024  
epoch:36, train acc:0.683333333333333, test acc:0.4992  
epoch:37, train acc:0.683333333333333, test acc:0.5056  
epoch:38, train acc:0.703333333333334, test acc:0.5105  
epoch:39, train acc:0.72, test acc:0.5236  
epoch:40, train acc:0.7266666666666667, test acc:0.5294  
epoch:41, train acc:0.713333333333334, test acc:0.5265  
epoch:42, train acc:0.7366666666666667, test acc:0.5455  
epoch:43, train acc:0.7266666666666667, test acc:0.5378  
epoch:44, train acc:0.733333333333333, test acc:0.547  
epoch:45, train acc:0.73, test acc:0.5428  
epoch:46, train acc:0.733333333333333, test acc:0.549  
epoch:47, train acc:0.743333333333333, test acc:0.5504  
epoch:48, train acc:0.743333333333333, test acc:0.5557  
epoch:49, train acc:0.76, test acc:0.5782  
epoch:50, train acc:0.7566666666666667, test acc:0.5692  
epoch:51, train acc:0.75, test acc:0.5744  
epoch:52, train acc:0.76, test acc:0.5832  
epoch:53, train acc:0.7566666666666667, test acc:0.5899  
epoch:54, train acc:0.7566666666666667, test acc:0.582  
epoch:55, train acc:0.7566666666666667, test acc:0.595  
epoch:56, train acc:0.7666666666666667, test acc:0.6031  
epoch:57, train acc:0.7566666666666667, test acc:0.5873  
epoch:58, train acc:0.7766666666666666, test acc:0.6036  
epoch:59, train acc:0.7733333333333333, test acc:0.6112  
epoch:60, train acc:0.78, test acc:0.6178

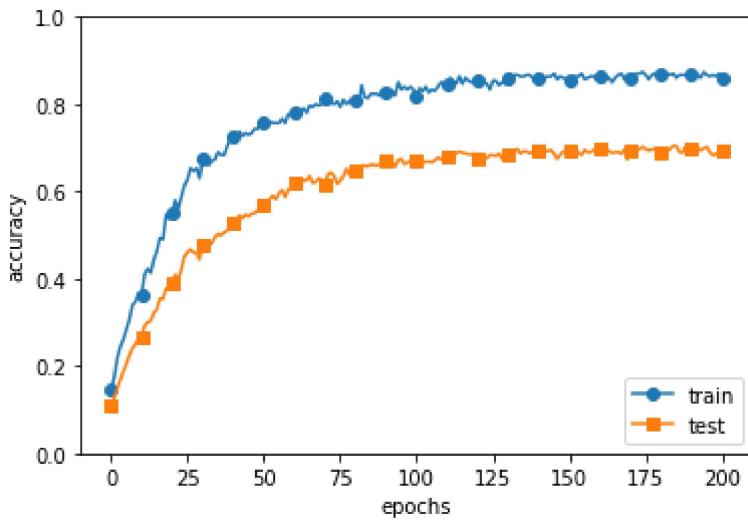
epoch:61, train acc:0.7866666666666666, test acc:0.6215  
epoch:62, train acc:0.7833333333333333, test acc:0.6201  
epoch:63, train acc:0.79, test acc:0.6258  
epoch:64, train acc:0.78, test acc:0.6258  
epoch:65, train acc:0.7966666666666666, test acc:0.6354  
epoch:66, train acc:0.7933333333333333, test acc:0.6198  
epoch:67, train acc:0.8, test acc:0.6219  
epoch:68, train acc:0.7966666666666666, test acc:0.6297  
epoch:69, train acc:0.8, test acc:0.625  
epoch:70, train acc:0.8133333333333334, test acc:0.6176  
epoch:71, train acc:0.8, test acc:0.6394  
epoch:72, train acc:0.8033333333333333, test acc:0.6428  
epoch:73, train acc:0.8, test acc:0.6353  
epoch:74, train acc:0.8066666666666666, test acc:0.6169  
epoch:75, train acc:0.7933333333333333, test acc:0.6248  
epoch:76, train acc:0.81, test acc:0.6346  
epoch:77, train acc:0.8, test acc:0.6519  
epoch:78, train acc:0.8066666666666666, test acc:0.6388  
epoch:79, train acc:0.8066666666666666, test acc:0.6458  
epoch:80, train acc:0.81, test acc:0.6473  
epoch:81, train acc:0.8, test acc:0.6401  
epoch:82, train acc:0.8433333333333334, test acc:0.6587  
epoch:83, train acc:0.8166666666666667, test acc:0.659  
epoch:84, train acc:0.8133333333333334, test acc:0.6574  
epoch:85, train acc:0.8233333333333334, test acc:0.6614  
epoch:86, train acc:0.8233333333333334, test acc:0.6604  
epoch:87, train acc:0.8233333333333334, test acc:0.6593  
epoch:88, train acc:0.82, test acc:0.6623  
epoch:89, train acc:0.8333333333333334, test acc:0.66  
epoch:90, train acc:0.8266666666666667, test acc:0.6722  
epoch:91, train acc:0.8333333333333334, test acc:0.6602  
epoch:92, train acc:0.83, test acc:0.668  
epoch:93, train acc:0.82, test acc:0.6559  
epoch:94, train acc:0.85, test acc:0.6719  
epoch:95, train acc:0.8333333333333334, test acc:0.6745  
epoch:96, train acc:0.84, test acc:0.6625  
epoch:97, train acc:0.8333333333333334, test acc:0.6657  
epoch:98, train acc:0.84, test acc:0.6708  
epoch:99, train acc:0.8333333333333334, test acc:0.656  
epoch:100, train acc:0.8166666666666667, test acc:0.6687  
epoch:101, train acc:0.8366666666666667, test acc:0.6751  
epoch:102, train acc:0.83, test acc:0.6647  
epoch:103, train acc:0.84, test acc:0.6682  
epoch:104, train acc:0.8266666666666667, test acc:0.6682  
epoch:105, train acc:0.8333333333333334, test acc:0.6666  
epoch:106, train acc:0.83, test acc:0.671  
epoch:107, train acc:0.84, test acc:0.6772  
epoch:108, train acc:0.85, test acc:0.6735  
epoch:109, train acc:0.8466666666666667, test acc:0.6762  
epoch:110, train acc:0.8433333333333334, test acc:0.6779  
epoch:111, train acc:0.86, test acc:0.6819  
epoch:112, train acc:0.8533333333333334, test acc:0.6779  
epoch:113, train acc:0.8466666666666667, test acc:0.6881  
epoch:114, train acc:0.8633333333333333, test acc:0.6912  
epoch:115, train acc:0.8466666666666667, test acc:0.6884  
epoch:116, train acc:0.86, test acc:0.6872  
epoch:117, train acc:0.8533333333333334, test acc:0.6851  
epoch:118, train acc:0.85, test acc:0.6842  
epoch:119, train acc:0.8533333333333334, test acc:0.6871  
epoch:120, train acc:0.8566666666666667, test acc:0.6741  
epoch:121, train acc:0.8533333333333334, test acc:0.6797

epoch:122, train acc:0.85, test acc:0.6805  
epoch:123, train acc:0.8466666666666667, test acc:0.6762  
epoch:124, train acc:0.8333333333333334, test acc:0.683  
epoch:125, train acc:0.8533333333333334, test acc:0.6827  
epoch:126, train acc:0.8533333333333334, test acc:0.6809  
epoch:127, train acc:0.8433333333333334, test acc:0.6866  
epoch:128, train acc:0.85, test acc:0.6748  
epoch:129, train acc:0.8466666666666667, test acc:0.6789  
epoch:130, train acc:0.86, test acc:0.6842  
epoch:131, train acc:0.8533333333333334, test acc:0.691  
epoch:132, train acc:0.8666666666666667, test acc:0.6924  
epoch:133, train acc:0.8666666666666667, test acc:0.6966  
epoch:134, train acc:0.863333333333333, test acc:0.6866  
epoch:135, train acc:0.863333333333333, test acc:0.6918  
epoch:136, train acc:0.8666666666666667, test acc:0.6916  
epoch:137, train acc:0.8666666666666667, test acc:0.6869  
epoch:138, train acc:0.86, test acc:0.6909  
epoch:139, train acc:0.8533333333333334, test acc:0.6889  
epoch:140, train acc:0.86, test acc:0.6936  
epoch:141, train acc:0.86, test acc:0.6987  
epoch:142, train acc:0.86, test acc:0.6918  
epoch:143, train acc:0.863333333333333, test acc:0.6921  
epoch:144, train acc:0.863333333333333, test acc:0.6945  
epoch:145, train acc:0.87, test acc:0.6864  
epoch:146, train acc:0.8566666666666667, test acc:0.6747  
epoch:147, train acc:0.863333333333333, test acc:0.6838  
epoch:148, train acc:0.86, test acc:0.6914  
epoch:149, train acc:0.8566666666666667, test acc:0.6888  
epoch:150, train acc:0.8533333333333334, test acc:0.6922  
epoch:151, train acc:0.8566666666666667, test acc:0.6854  
epoch:152, train acc:0.863333333333333, test acc:0.6877  
epoch:153, train acc:0.863333333333333, test acc:0.6891  
epoch:154, train acc:0.87, test acc:0.6831  
epoch:155, train acc:0.8566666666666667, test acc:0.695  
epoch:156, train acc:0.86, test acc:0.6894  
epoch:157, train acc:0.863333333333333, test acc:0.6901  
epoch:158, train acc:0.863333333333333, test acc:0.6948  
epoch:159, train acc:0.8566666666666667, test acc:0.6952  
epoch:160, train acc:0.863333333333333, test acc:0.6997  
epoch:161, train acc:0.863333333333333, test acc:0.6964  
epoch:162, train acc:0.86, test acc:0.6969  
epoch:163, train acc:0.86, test acc:0.6923  
epoch:164, train acc:0.85, test acc:0.6878  
epoch:165, train acc:0.86, test acc:0.6896  
epoch:166, train acc:0.8666666666666667, test acc:0.6905  
epoch:167, train acc:0.87, test acc:0.686  
epoch:168, train acc:0.8566666666666667, test acc:0.6954  
epoch:169, train acc:0.8666666666666667, test acc:0.6733  
epoch:170, train acc:0.86, test acc:0.6944  
epoch:171, train acc:0.863333333333333, test acc:0.7021  
epoch:172, train acc:0.87, test acc:0.6985  
epoch:173, train acc:0.87, test acc:0.6966  
epoch:174, train acc:0.873333333333333, test acc:0.7019  
epoch:175, train acc:0.8666666666666667, test acc:0.6967  
epoch:176, train acc:0.8566666666666667, test acc:0.6941  
epoch:177, train acc:0.8666666666666667, test acc:0.6958  
epoch:178, train acc:0.87, test acc:0.6978  
epoch:179, train acc:0.87, test acc:0.6945  
epoch:180, train acc:0.8666666666666667, test acc:0.6881  
epoch:181, train acc:0.8666666666666667, test acc:0.6954  
epoch:182, train acc:0.87, test acc:0.6921

```

epoch:183, train acc:0.8666666666666667, test acc:0.6971
epoch:184, train acc:0.87, test acc:0.7043
epoch:185, train acc:0.86, test acc:0.7043
epoch:186, train acc:0.8666666666666667, test acc:0.6904
epoch:187, train acc:0.8666666666666667, test acc:0.6886
epoch:188, train acc:0.8666666666666667, test acc:0.7035
epoch:189, train acc:0.87, test acc:0.6978
epoch:190, train acc:0.87, test acc:0.6995
epoch:191, train acc:0.863333333333333, test acc:0.6968
epoch:192, train acc:0.8666666666666667, test acc:0.6996
epoch:193, train acc:0.86, test acc:0.6943
epoch:194, train acc:0.873333333333333, test acc:0.6986
epoch:195, train acc:0.8666666666666667, test acc:0.7018
epoch:196, train acc:0.863333333333333, test acc:0.6899
epoch:197, train acc:0.8666666666666667, test acc:0.6829
epoch:198, train acc:0.863333333333333, test acc:0.6856
epoch:199, train acc:0.87, test acc:0.6921
epoch:200, train acc:0.86, test acc:0.693

```



訓練データに関する認識精度は100%なのに、テストデータに関する認識精度は60%～80%で高止まりしている→過学習状態

## Weight Decay (荷重減衰)

学習途中で大きな重みを持ったニューロンに対してペナルティを付与（損失関数への加算）すること。過学習により大きな重みを持つてしまったニューロンの発火を抑制できる。

- $w \leftarrow w - \eta \frac{\partial C(w)}{\partial w} - WeightDecay$ 
  - $WeightDecay \leftarrow \frac{1}{2} \lambda W^2$ 
    - $W(L2realm) \leftarrow \sqrt{w_1^2 + w_2^2 + \dots + w_n^2}$
    - $W(L1realm) \leftarrow |w_1^2| + |w_2^2| + \dots + |w_n^2|$

※Weight Decayのイメージ的には $-(\frac{\partial C(w)}{\partial w} + WeightDecay)$ であり、Cost関数+WeightDecayで重みの大きさに比例してと言った感じになる

## Weight Decay対応版NN

In [2]:

```
# coding: utf-8
import os
import sys

sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.multi_layer_net import MultiLayerNet
from common.optimizer import SGD

(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

# 過学習を再現するために、学習データを削減
x_train = x_train[:300]
t_train = t_train[:300]

# weight decay (荷重減衰) の設定 =====
#weight_decay_lambda = 0 # weight decayを使用しない場合
weight_decay_lambda = 0.1
# =====

network = MultiLayerNet(input_size=784, hidden_size_list=[100, 100, 100, 100, 100], output_size=10,
                        weight_decay_lambda=weight_decay_lambda)
optimizer = SGD(lr=0.01)

max_epochs = 201
train_size = x_train.shape[0]
batch_size = 100

train_loss_list = []
train_acc_list = []
test_acc_list = []

iter_per_epoch = max(train_size / batch_size, 1)
epoch_cnt = 0

for i in range(1000000000):
    batch_mask = np.random.choice(train_size, batch_size)
    x_batch = x_train[batch_mask]
    t_batch = t_train[batch_mask]

    grads = network.gradient(x_batch, t_batch)
    optimizer.update(network.params, grads)

    if i % iter_per_epoch == 0:
        train_acc = network.accuracy(x_train, t_train)
        test_acc = network.accuracy(x_test, t_test)
        train_acc_list.append(train_acc)
        test_acc_list.append(test_acc)

        print("epoch:" + str(epoch_cnt) + ", train acc:" + str(train_acc) + ", test acc:" + str(test_acc))

    epoch_cnt += 1
    if epoch_cnt >= max_epochs:
        break
```

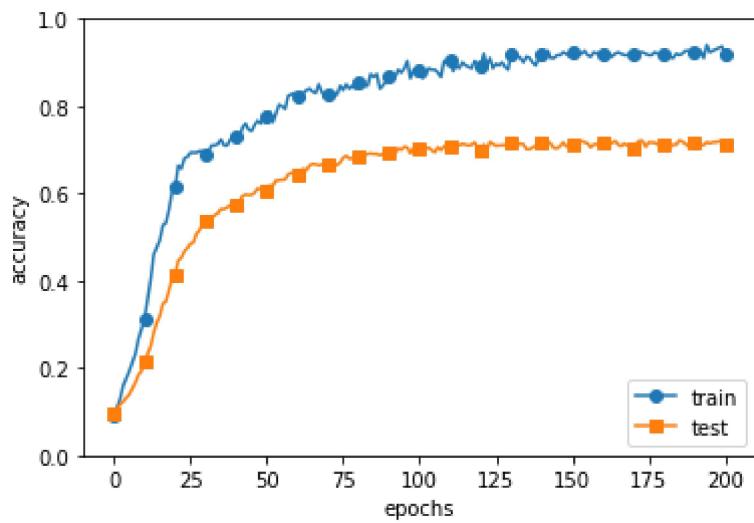
```
# 3. グラフの描画=====
markers = ['train': 'o', 'test': 's'}
x = np.arange(max_epochs)
plt.plot(x, train_acc_list, marker='o', label='train', markevery=10)
plt.plot(x, test_acc_list, marker='s', label='test', markevery=10)
plt.xlabel("epochs")
plt.ylabel("accuracy")
plt.ylim(0, 1.0)
plt.legend(loc='lower right')
plt.show()
```

epoch:0, train acc:0.0933333333333334, test acc:0.0978  
epoch:1, train acc:0.11, test acc:0.1078  
epoch:2, train acc:0.13, test acc:0.1171  
epoch:3, train acc:0.16, test acc:0.1228  
epoch:4, train acc:0.1766666666666667, test acc:0.1323  
epoch:5, train acc:0.1933333333333333, test acc:0.1394  
epoch:6, train acc:0.2133333333333335, test acc:0.1529  
epoch:7, train acc:0.2333333333333334, test acc:0.1672  
epoch:8, train acc:0.2666666666666666, test acc:0.1844  
epoch:9, train acc:0.29, test acc:0.1938  
epoch:10, train acc:0.3133333333333335, test acc:0.2147  
epoch:11, train acc:0.36, test acc:0.2329  
epoch:12, train acc:0.4033333333333333, test acc:0.2501  
epoch:13, train acc:0.46, test acc:0.2811  
epoch:14, train acc:0.4766666666666667, test acc:0.3041  
epoch:15, train acc:0.4933333333333335, test acc:0.3196  
epoch:16, train acc:0.5266666666666666, test acc:0.3472  
epoch:17, train acc:0.5333333333333333, test acc:0.3533  
epoch:18, train acc:0.5633333333333334, test acc:0.3796  
epoch:19, train acc:0.6033333333333334, test acc:0.4042  
epoch:20, train acc:0.6133333333333333, test acc:0.4144  
epoch:21, train acc:0.6633333333333333, test acc:0.4455  
epoch:22, train acc:0.6566666666666666, test acc:0.4527  
epoch:23, train acc:0.68, test acc:0.4668  
epoch:24, train acc:0.6833333333333333, test acc:0.4745  
epoch:25, train acc:0.6933333333333334, test acc:0.4847  
epoch:26, train acc:0.6933333333333334, test acc:0.4874  
epoch:27, train acc:0.6933333333333334, test acc:0.5076  
epoch:28, train acc:0.6966666666666667, test acc:0.5159  
epoch:29, train acc:0.6966666666666667, test acc:0.5329  
epoch:30, train acc:0.69, test acc:0.5351  
epoch:31, train acc:0.6966666666666667, test acc:0.5316  
epoch:32, train acc:0.71, test acc:0.5443  
epoch:33, train acc:0.71, test acc:0.5501  
epoch:34, train acc:0.7133333333333334, test acc:0.555  
epoch:35, train acc:0.7233333333333334, test acc:0.5645  
epoch:36, train acc:0.71, test acc:0.5637  
epoch:37, train acc:0.71, test acc:0.5683  
epoch:38, train acc:0.7233333333333334, test acc:0.5725  
epoch:39, train acc:0.7233333333333334, test acc:0.5785  
epoch:40, train acc:0.73, test acc:0.5759  
epoch:41, train acc:0.7266666666666667, test acc:0.582  
epoch:42, train acc:0.75, test acc:0.5937  
epoch:43, train acc:0.76, test acc:0.5974  
epoch:44, train acc:0.7466666666666667, test acc:0.5962  
epoch:45, train acc:0.7433333333333333, test acc:0.5969  
epoch:46, train acc:0.7566666666666667, test acc:0.6018  
epoch:47, train acc:0.7666666666666667, test acc:0.6109  
epoch:48, train acc:0.76, test acc:0.6097  
epoch:49, train acc:0.7733333333333333, test acc:0.6061  
epoch:50, train acc:0.7766666666666666, test acc:0.6075  
epoch:51, train acc:0.7866666666666666, test acc:0.6187  
epoch:52, train acc:0.7633333333333333, test acc:0.618  
epoch:53, train acc:0.7833333333333333, test acc:0.6295  
epoch:54, train acc:0.8033333333333333, test acc:0.6302  
epoch:55, train acc:0.8, test acc:0.6311  
epoch:56, train acc:0.7933333333333333, test acc:0.6321  
epoch:57, train acc:0.8233333333333334, test acc:0.6435  
epoch:58, train acc:0.8266666666666667, test acc:0.6464  
epoch:59, train acc:0.83, test acc:0.6491  
epoch:60, train acc:0.8233333333333334, test acc:0.6407

epoch:61, train acc:0.8266666666666667, test acc:0.6528  
epoch:62, train acc:0.83, test acc:0.6561  
epoch:63, train acc:0.8366666666666667, test acc:0.6535  
epoch:64, train acc:0.84, test acc:0.6641  
epoch:65, train acc:0.8333333333333334, test acc:0.6673  
epoch:66, train acc:0.83, test acc:0.6664  
epoch:67, train acc:0.85, test acc:0.6641  
epoch:68, train acc:0.8333333333333334, test acc:0.6661  
epoch:69, train acc:0.82, test acc:0.6627  
epoch:70, train acc:0.8266666666666667, test acc:0.6657  
epoch:71, train acc:0.83, test acc:0.6624  
epoch:72, train acc:0.83, test acc:0.6688  
epoch:73, train acc:0.8266666666666667, test acc:0.665  
epoch:74, train acc:0.8466666666666667, test acc:0.6707  
epoch:75, train acc:0.8366666666666667, test acc:0.6816  
epoch:76, train acc:0.85, test acc:0.6861  
epoch:77, train acc:0.84, test acc:0.6792  
epoch:78, train acc:0.8466666666666667, test acc:0.6811  
epoch:79, train acc:0.84, test acc:0.6822  
epoch:80, train acc:0.8566666666666667, test acc:0.6849  
epoch:81, train acc:0.86, test acc:0.6881  
epoch:82, train acc:0.8466666666666667, test acc:0.6873  
epoch:83, train acc:0.8466666666666667, test acc:0.6904  
epoch:84, train acc:0.8733333333333333, test acc:0.6917  
epoch:85, train acc:0.8666666666666667, test acc:0.6902  
epoch:86, train acc:0.8733333333333333, test acc:0.6906  
epoch:87, train acc:0.84, test acc:0.6871  
epoch:88, train acc:0.8466666666666667, test acc:0.6911  
epoch:89, train acc:0.8566666666666667, test acc:0.6964  
epoch:90, train acc:0.8666666666666667, test acc:0.6943  
epoch:91, train acc:0.8733333333333333, test acc:0.6938  
epoch:92, train acc:0.8666666666666667, test acc:0.6913  
epoch:93, train acc:0.8833333333333333, test acc:0.7031  
epoch:94, train acc:0.8766666666666667, test acc:0.6998  
epoch:95, train acc:0.8866666666666667, test acc:0.707  
epoch:96, train acc:0.9033333333333333, test acc:0.7051  
epoch:97, train acc:0.8633333333333333, test acc:0.6918  
epoch:98, train acc:0.8833333333333333, test acc:0.7044  
epoch:99, train acc:0.87, test acc:0.6986  
epoch:100, train acc:0.88, test acc:0.7018  
epoch:101, train acc:0.8633333333333333, test acc:0.6954  
epoch:102, train acc:0.87, test acc:0.7016  
epoch:103, train acc:0.8866666666666667, test acc:0.705  
epoch:104, train acc:0.8833333333333333, test acc:0.6991  
epoch:105, train acc:0.8833333333333333, test acc:0.6942  
epoch:106, train acc:0.8766666666666667, test acc:0.7057  
epoch:107, train acc:0.8666666666666667, test acc:0.699  
epoch:108, train acc:0.9033333333333333, test acc:0.7076  
epoch:109, train acc:0.9, test acc:0.7124  
epoch:110, train acc:0.9033333333333333, test acc:0.7089  
epoch:111, train acc:0.88, test acc:0.6996  
epoch:112, train acc:0.8933333333333333, test acc:0.7129  
epoch:113, train acc:0.8866666666666667, test acc:0.7104  
epoch:114, train acc:0.9, test acc:0.7134  
epoch:115, train acc:0.8933333333333333, test acc:0.7115  
epoch:116, train acc:0.89, test acc:0.7099  
epoch:117, train acc:0.8866666666666667, test acc:0.7113  
epoch:118, train acc:0.9033333333333333, test acc:0.7166  
epoch:119, train acc:0.8966666666666666, test acc:0.7059  
epoch:120, train acc:0.8933333333333333, test acc:0.6997  
epoch:121, train acc:0.92, test acc:0.712

epoch:122, train acc:0.8933333333333333, test acc:0.7  
epoch:123, train acc:0.91, test acc:0.7175  
epoch:124, train acc:0.8866666666666667, test acc:0.7131  
epoch:125, train acc:0.8966666666666666, test acc:0.7092  
epoch:126, train acc:0.8933333333333333, test acc:0.7099  
epoch:127, train acc:0.9, test acc:0.7104  
epoch:128, train acc:0.89, test acc:0.7107  
epoch:129, train acc:0.8833333333333333, test acc:0.7036  
epoch:130, train acc:0.92, test acc:0.7185  
epoch:131, train acc:0.9133333333333333, test acc:0.7157  
epoch:132, train acc:0.9166666666666666, test acc:0.7161  
epoch:133, train acc:0.91, test acc:0.7129  
epoch:134, train acc:0.9, test acc:0.7127  
epoch:135, train acc:0.9133333333333333, test acc:0.7014  
epoch:136, train acc:0.91, test acc:0.7011  
epoch:137, train acc:0.9, test acc:0.7051  
epoch:138, train acc:0.8933333333333333, test acc:0.7085  
epoch:139, train acc:0.91, test acc:0.7144  
epoch:140, train acc:0.9166666666666666, test acc:0.7168  
epoch:141, train acc:0.9166666666666666, test acc:0.7163  
epoch:142, train acc:0.9266666666666666, test acc:0.7193  
epoch:143, train acc:0.91, test acc:0.713  
epoch:144, train acc:0.91, test acc:0.7039  
epoch:145, train acc:0.9166666666666666, test acc:0.7028  
epoch:146, train acc:0.9166666666666666, test acc:0.7088  
epoch:147, train acc:0.9233333333333333, test acc:0.7165  
epoch:148, train acc:0.92, test acc:0.7081  
epoch:149, train acc:0.9133333333333333, test acc:0.7121  
epoch:150, train acc:0.9233333333333333, test acc:0.7113  
epoch:151, train acc:0.9166666666666666, test acc:0.7211  
epoch:152, train acc:0.92, test acc:0.7175  
epoch:153, train acc:0.92, test acc:0.7201  
epoch:154, train acc:0.9266666666666666, test acc:0.7168  
epoch:155, train acc:0.9166666666666666, test acc:0.7146  
epoch:156, train acc:0.9133333333333333, test acc:0.7056  
epoch:157, train acc:0.9233333333333333, test acc:0.7123  
epoch:158, train acc:0.92, test acc:0.7121  
epoch:159, train acc:0.9233333333333333, test acc:0.7161  
epoch:160, train acc:0.9166666666666666, test acc:0.7169  
epoch:161, train acc:0.92, test acc:0.7155  
epoch:162, train acc:0.92, test acc:0.7148  
epoch:163, train acc:0.9133333333333333, test acc:0.715  
epoch:164, train acc:0.92, test acc:0.7201  
epoch:165, train acc:0.9233333333333333, test acc:0.7117  
epoch:166, train acc:0.92, test acc:0.7084  
epoch:167, train acc:0.9166666666666666, test acc:0.714  
epoch:168, train acc:0.9166666666666666, test acc:0.7098  
epoch:169, train acc:0.92, test acc:0.7088  
epoch:170, train acc:0.92, test acc:0.7044  
epoch:171, train acc:0.9233333333333333, test acc:0.7139  
epoch:172, train acc:0.9233333333333333, test acc:0.7207  
epoch:173, train acc:0.9233333333333333, test acc:0.7202  
epoch:174, train acc:0.92, test acc:0.7069  
epoch:175, train acc:0.9166666666666666, test acc:0.7169  
epoch:176, train acc:0.9166666666666666, test acc:0.7166  
epoch:177, train acc:0.9233333333333333, test acc:0.7161  
epoch:178, train acc:0.92, test acc:0.712  
epoch:179, train acc:0.9166666666666666, test acc:0.7081  
epoch:180, train acc:0.9166666666666666, test acc:0.713  
epoch:181, train acc:0.92, test acc:0.7135  
epoch:182, train acc:0.9133333333333333, test acc:0.706

```
epoch:183, train acc:0.91, test acc:0.7115
epoch:184, train acc:0.92, test acc:0.7119
epoch:185, train acc:0.9166666666666666, test acc:0.7214
epoch:186, train acc:0.92, test acc:0.7187
epoch:187, train acc:0.9266666666666666, test acc:0.7135
epoch:188, train acc:0.9266666666666666, test acc:0.7074
epoch:189, train acc:0.92, test acc:0.7173
epoch:190, train acc:0.9233333333333333, test acc:0.7184
epoch:191, train acc:0.9266666666666666, test acc:0.7122
epoch:192, train acc:0.9266666666666666, test acc:0.711
epoch:193, train acc:0.91, test acc:0.7109
epoch:194, train acc:0.94, test acc:0.7173
epoch:195, train acc:0.9233333333333333, test acc:0.7149
epoch:196, train acc:0.9266666666666666, test acc:0.7172
epoch:197, train acc:0.93, test acc:0.7172
epoch:198, train acc:0.9333333333333333, test acc:0.7196
epoch:199, train acc:0.9366666666666666, test acc:0.7162
epoch:200, train acc:0.92, test acc:0.7141
```



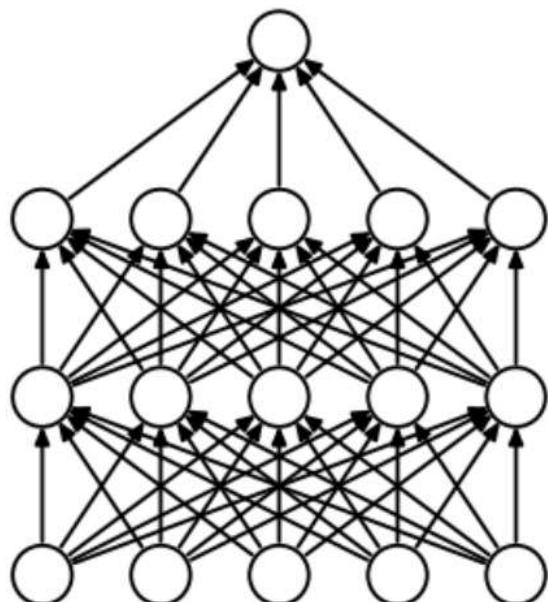
## Dropout (忘却)

[Dropout \(<https://medium.com/@amarbudhiraja/https-medium-com-amarbudhiraja-learning-less-to-learn-better-dropout-in-deep-machine-learning-74334da4bf5>\)](https://medium.com/@amarbudhiraja/https-medium-com-amarbudhiraja-learning-less-to-learn-better-dropout-in-deep-machine-learning-74334da4bf5)は一つの学習モデルの中でニューロンをランダムに選び出し、データが流れるたびに消去する手法。

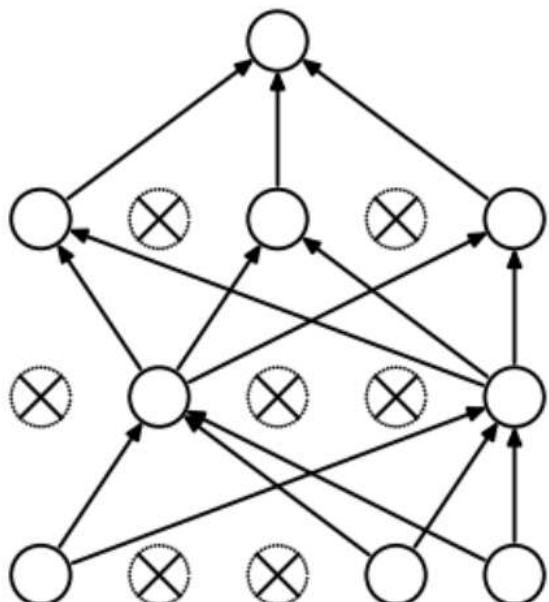
「1 - 消去する割合」を最後の伝達の際に乗算することにより消去分の平均化を実施し 一つの学習モデルの中で多種のニューロンが発火するように強制させることができる。

複数の学習モデルによる出力を平均したものをアンサンブル学習と呼ぶが、それに近いことを一つの学習モデルで実施することができる。

DropoutされたニューロンはReLUによるスイッチオフ作用と同様、逆伝搬の対象とならない。



(a) Standard Neural Net



(b) After applying dropout.

In [3]:

```
class Dropout:  
    """  
    http://arxiv.org/abs/1207.0580  
    """  
  
    def __init__(self, dropout_ratio=0.5):  
        self.dropout_ratio = dropout_ratio  
        self.mask = None  
  
    def forward(self, x, train_flg=True):  
        if train_flg:  
            self.mask = np.random.rand(*x.shape) > self.dropout_ratio  
            return x * self.mask  
        else:  
            return x * (1.0 - self.dropout_ratio)  
  
    def backward(self, dout):  
        return dout * self.mask
```

In [1]:

```
# coding: utf-8
import os
import sys
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.multi_layer_net_extend import MultiLayerNetExtend
from common.trainer import Trainer

(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

# 過学習を再現するために、学習データを削減
x_train = x_train[:300]
t_train = t_train[:300]

# Dropoutの有無、割り合いの設定 =====
use_dropout = True # DropoutなしのときはFalseに
dropout_ratio = 0.2
# =====

network = MultiLayerNetExtend(input_size=784, hidden_size_list=[100, 100, 100, 100, 100, 100], output_size=10, use_dropout=use_dropout, dropout_ratio=dropout_ratio)
trainer = Trainer(network, x_train, t_train, x_test, t_test,
                  epochs=301, mini_batch_size=100,
                  optimizer='sgd', optimizer_param={'lr': 0.01}, verbose=True)
trainer.train()

train_acc_list, test_acc_list = trainer.train_acc_list, trainer.test_acc_list

# グラフの描画=====
markers = {'train': 'o', 'test': 's'}
x = np.arange(len(train_acc_list))
plt.plot(x, train_acc_list, marker='o', label='train', markevery=10)
plt.plot(x, test_acc_list, marker='s', label='test', markevery=10)
plt.xlabel("epochs")
plt.ylabel("accuracy")
plt.ylim(0, 1.0)
plt.legend(loc='lower right')
plt.show()
```

train loss:2.29832839634101  
==== epoch:1, train acc:0.1133333333333333, test acc:0.0791 ===  
train loss:2.297517209178537  
train loss:2.2955034213216354  
train loss:2.2935054357429094  
==== epoch:2, train acc:0.13, test acc:0.0836 ===  
train loss:2.2915445943865134  
train loss:2.2932091073647025  
train loss:2.2944382333283424  
==== epoch:3, train acc:0.13, test acc:0.0884 ===  
train loss:2.2996963623609634  
train loss:2.2962057345642095  
train loss:2.2918471366115747  
==== epoch:4, train acc:0.1366666666666666, test acc:0.0943 ===  
train loss:2.2985209683004317  
train loss:2.2938675797102275  
train loss:2.2881600803373585  
==== epoch:5, train acc:0.14, test acc:0.0969 ===  
train loss:2.286785688408503  
train loss:2.290505963341967  
train loss:2.288732557618638  
==== epoch:6, train acc:0.15, test acc:0.1036 ===  
train loss:2.2949984009511666  
train loss:2.3009488920719052  
train loss:2.2973663366129697  
==== epoch:7, train acc:0.1566666666666666, test acc:0.1083 ===  
train loss:2.2903975188256704  
train loss:2.280853564123864  
train loss:2.2913004521441804  
==== epoch:8, train acc:0.17, test acc:0.1129 ===  
train loss:2.2952920620965487  
train loss:2.2960547856730296  
train loss:2.2800716735007676  
==== epoch:9, train acc:0.1733333333333334, test acc:0.1171 ===  
train loss:2.294858623863755  
train loss:2.2792948736124417  
train loss:2.2903521925650683  
==== epoch:10, train acc:0.1733333333333334, test acc:0.1226 ===  
train loss:2.2645030804239754  
train loss:2.2889437386336073  
train loss:2.2927251088557297  
==== epoch:11, train acc:0.17, test acc:0.1247 ===  
train loss:2.2782813904556933  
train loss:2.282887423615841  
train loss:2.2805177549452167  
==== epoch:12, train acc:0.17, test acc:0.1281 ===  
train loss:2.2848701947712713  
train loss:2.2819798640644207  
train loss:2.286856187291836  
==== epoch:13, train acc:0.16, test acc:0.1279 ===  
train loss:2.285458398812042  
train loss:2.2770987651166217  
train loss:2.2772608904251035  
==== epoch:14, train acc:0.16, test acc:0.1331 ===  
train loss:2.2935405977943186  
train loss:2.2791208944756076  
train loss:2.2778281293311857  
==== epoch:15, train acc:0.1633333333333333, test acc:0.1349 ===  
train loss:2.285538189129508  
train loss:2.2754843954083115  
train loss:2.2701752627414917

```
==== epoch:16, train acc:0.1633333333333333, test acc:0.1386 ===
train loss:2.2852088432172555
train loss:2.2754783810332886
train loss:2.2730095540020803
==== epoch:17, train acc:0.17, test acc:0.1413 ===
train loss:2.2816786124792845
train loss:2.2824435716401066
train loss:2.2791824233244147
==== epoch:18, train acc:0.1766666666666667, test acc:0.1447 ===
train loss:2.2720210030438444
train loss:2.2822256442993925
train loss:2.2853501795346336
==== epoch:19, train acc:0.18, test acc:0.1464 ===
train loss:2.273037078676334
train loss:2.2849280809849803
train loss:2.2748931142712046
==== epoch:20, train acc:0.1766666666666667, test acc:0.1477 ===
train loss:2.263865080045291
train loss:2.2809122986443597
train loss:2.2719997473502436
==== epoch:21, train acc:0.1733333333333334, test acc:0.1498 ===
train loss:2.281826646616146
train loss:2.2660933022643768
train loss:2.2789564214731346
==== epoch:22, train acc:0.1666666666666666, test acc:0.1514 ===
train loss:2.2664560433149394
train loss:2.2754734824715137
train loss:2.277203339121532
==== epoch:23, train acc:0.18, test acc:0.1553 ===
train loss:2.2745572712969695
train loss:2.2762141676849468
train loss:2.279957844025212
==== epoch:24, train acc:0.18, test acc:0.1562 ===
train loss:2.2711526413276
train loss:2.274253252730152
train loss:2.2728695900838893
==== epoch:25, train acc:0.19, test acc:0.1587 ===
train loss:2.2678753501058897
train loss:2.2747538936780183
train loss:2.2671982243905777
==== epoch:26, train acc:0.1966666666666666, test acc:0.1628 ===
train loss:2.2649169297714966
train loss:2.268527663570704
train loss:2.2733035468560443
==== epoch:27, train acc:0.1966666666666666, test acc:0.1648 ===
train loss:2.2716226906046946
train loss:2.272909988214367
train loss:2.2709899108399307
==== epoch:28, train acc:0.1966666666666666, test acc:0.1669 ===
train loss:2.252917218814546
train loss:2.2671874530759535
train loss:2.266114683658497
==== epoch:29, train acc:0.2, test acc:0.1679 ===
train loss:2.26612574419879
train loss:2.272834810620966
train loss:2.255908925152327
==== epoch:30, train acc:0.2166666666666667, test acc:0.1721 ===
train loss:2.259900863748509
train loss:2.2662396817914527
train loss:2.255211388382625
==== epoch:31, train acc:0.2166666666666667, test acc:0.1736 ===
```

train loss:2.2716823833007114  
train loss:2.2551021577626686  
train loss:2.25756456628241  
== epoch:32, train acc:0.2266666666666666, test acc:0.1756 ==  
train loss:2.2615404238871077  
train loss:2.2629584035190997  
train loss:2.260159467130955  
== epoch:33, train acc:0.2233333333333333, test acc:0.1774 ==  
train loss:2.2588688962947128  
train loss:2.2497292944907725  
train loss:2.2642899289856375  
== epoch:34, train acc:0.2333333333333334, test acc:0.1784 ==  
train loss:2.2574746148859335  
train loss:2.283248975395685  
train loss:2.2529112240595106  
== epoch:35, train acc:0.2366666666666666, test acc:0.1837 ==  
train loss:2.2622975417300513  
train loss:2.2624054267357185  
train loss:2.249895615444449  
== epoch:36, train acc:0.24, test acc:0.1849 ==  
train loss:2.2670328726038598  
train loss:2.2621533687290696  
train loss:2.2588617512240075  
== epoch:37, train acc:0.2433333333333335, test acc:0.1867 ==  
train loss:2.259179399059643  
train loss:2.253242469348756  
train loss:2.247486517750717  
== epoch:38, train acc:0.25, test acc:0.1879 ==  
train loss:2.2533742735867084  
train loss:2.254941007058005  
train loss:2.2407765820346395  
== epoch:39, train acc:0.2533333333333335, test acc:0.1916 ==  
train loss:2.258613534954242  
train loss:2.247623559283962  
train loss:2.268959664046296  
== epoch:40, train acc:0.26, test acc:0.1933 ==  
train loss:2.249891330378538  
train loss:2.256890796810187  
train loss:2.247667066989199  
== epoch:41, train acc:0.26, test acc:0.1953 ==  
train loss:2.2704824088637743  
train loss:2.2488045143502355  
train loss:2.2437003127282664  
== epoch:42, train acc:0.2666666666666666, test acc:0.1973 ==  
train loss:2.2523807950539116  
train loss:2.2397836718422135  
train loss:2.24990683008903  
== epoch:43, train acc:0.27, test acc:0.2005 ==  
train loss:2.2578519128744285  
train loss:2.245957259608089  
train loss:2.2455337022932746  
== epoch:44, train acc:0.2833333333333333, test acc:0.2022 ==  
train loss:2.2368133046152505  
train loss:2.262788080324759  
train loss:2.2458886315206934  
== epoch:45, train acc:0.2733333333333333, test acc:0.2061 ==  
train loss:2.2591430991965438  
train loss:2.234241043993578  
train loss:2.2586311029223025  
== epoch:46, train acc:0.28, test acc:0.2053 ==  
train loss:2.222956956758696

train loss:2.228936803838681  
train loss:2.249675717408843  
== epoch:47, train acc:0.283333333333333, test acc:0.2077 ==  
train loss:2.2629887629670034  
train loss:2.245758133203707  
train loss:2.2467057453249604  
== epoch:48, train acc:0.29, test acc:0.2129 ==  
train loss:2.2543647819232944  
train loss:2.2453637517095584  
train loss:2.240164806992922  
== epoch:49, train acc:0.286666666666667, test acc:0.2129 ==  
train loss:2.254486378612578  
train loss:2.2201123098316953  
train loss:2.2358391483161792  
== epoch:50, train acc:0.29, test acc:0.217 ==  
train loss:2.2306948543954297  
train loss:2.2387434363935004  
train loss:2.2473820654757386  
== epoch:51, train acc:0.3, test acc:0.2189 ==  
train loss:2.236813776616849  
train loss:2.2327346416822356  
train loss:2.2313009134611725  
== epoch:52, train acc:0.3, test acc:0.2214 ==  
train loss:2.2327784127447683  
train loss:2.2466330516219633  
train loss:2.2349343107036757  
== epoch:53, train acc:0.3066666666666664, test acc:0.22 ==  
train loss:2.2120717657043683  
train loss:2.214069398395574  
train loss:2.2449798731115522  
== epoch:54, train acc:0.31, test acc:0.2226 ==  
train loss:2.231670010271403  
train loss:2.208174297828759  
train loss:2.2310706224590025  
== epoch:55, train acc:0.3066666666666664, test acc:0.2245 ==  
train loss:2.248968844804475  
train loss:2.2379922462270883  
train loss:2.2311563585547827  
== epoch:56, train acc:0.31, test acc:0.2277 ==  
train loss:2.2365131425041938  
train loss:2.2320453124203565  
train loss:2.2284694205679587  
== epoch:57, train acc:0.3133333333333335, test acc:0.2303 ==  
train loss:2.240106986259587  
train loss:2.2072662986245453  
train loss:2.240476220852277  
== epoch:58, train acc:0.32, test acc:0.2331 ==  
train loss:2.2022581701275707  
train loss:2.2305626728040977  
train loss:2.232550576319791  
== epoch:59, train acc:0.3133333333333335, test acc:0.2355 ==  
train loss:2.2164690108743788  
train loss:2.2384948349091247  
train loss:2.2174577187363536  
== epoch:60, train acc:0.3166666666666665, test acc:0.2377 ==  
train loss:2.203436636070427  
train loss:2.2404318985893332  
train loss:2.231574927495129  
== epoch:61, train acc:0.3166666666666665, test acc:0.2385 ==  
train loss:2.247779013772617  
train loss:2.2123116139375227

train loss:2.2117629419841047  
==== epoch:62, train acc:0.32, test acc:0.2404 ===  
train loss:2.231018472985949  
train loss:2.2134659140320823  
train loss:2.2011576165551014  
==== epoch:63, train acc:0.3166666666666666, test acc:0.2398 ===  
train loss:2.2251669704074115  
train loss:2.2128283050378745  
train loss:2.228705887045967  
==== epoch:64, train acc:0.3233333333333333, test acc:0.2403 ===  
train loss:2.2266405273524708  
train loss:2.2283060698461337  
train loss:2.220345354242907  
==== epoch:65, train acc:0.3266666666666666, test acc:0.241 ===  
train loss:2.237107954598329  
train loss:2.22430519050207  
train loss:2.22021881929206  
==== epoch:66, train acc:0.3333333333333333, test acc:0.244 ===  
train loss:2.2156404558751897  
train loss:2.208203764009914  
train loss:2.231787058600594  
==== epoch:67, train acc:0.3366666666666667, test acc:0.2443 ===  
train loss:2.1945454470826498  
train loss:2.2150530940962994  
train loss:2.225977097337029  
==== epoch:68, train acc:0.34, test acc:0.2475 ===  
train loss:2.1945139231452306  
train loss:2.2097811970283523  
train loss:2.23011405625922  
==== epoch:69, train acc:0.34, test acc:0.2485 ===  
train loss:2.189245972540314  
train loss:2.2321913926930774  
train loss:2.2128769501911303  
==== epoch:70, train acc:0.34, test acc:0.2505 ===  
train loss:2.209266847309963  
train loss:2.176589871637686  
train loss:2.229902944427294  
==== epoch:71, train acc:0.34, test acc:0.2521 ===  
train loss:2.1982242913214107  
train loss:2.1840348027463548  
train loss:2.214237344426824  
==== epoch:72, train acc:0.3466666666666667, test acc:0.2539 ===  
train loss:2.191702721981008  
train loss:2.2241854594834023  
train loss:2.2197084818423574  
==== epoch:73, train acc:0.35, test acc:0.254 ===  
train loss:2.181630354147048  
train loss:2.2046671667545423  
train loss:2.201394397955632  
==== epoch:74, train acc:0.35, test acc:0.2575 ===  
train loss:2.178275874617148  
train loss:2.2006772537541943  
train loss:2.2064814714724084  
==== epoch:75, train acc:0.3566666666666667, test acc:0.2595 ===  
train loss:2.2012985610647666  
train loss:2.193641728229958  
train loss:2.216273029760619  
==== epoch:76, train acc:0.35, test acc:0.2603 ===  
train loss:2.2092634712797166  
train loss:2.2058755765889906  
train loss:2.197699747531764

```
==== epoch:77, train acc:0.3533333333333333, test acc:0.2615 ===
train loss:2.180238675074255
train loss:2.1814282623429757
train loss:2.205994926510995
==== epoch:78, train acc:0.36, test acc:0.2652 ===
train loss:2.167356653829178
train loss:2.187012304756953
train loss:2.1963325293936076
==== epoch:79, train acc:0.3633333333333334, test acc:0.2672 ===
train loss:2.1863307494982736
train loss:2.1746856847859486
train loss:2.213334870217395
==== epoch:80, train acc:0.36, test acc:0.2689 ===
train loss:2.165857739306088
train loss:2.20828948841151
train loss:2.1832698268212463
==== epoch:81, train acc:0.37, test acc:0.2684 ===
train loss:2.133199185867035
train loss:2.2134738164785737
train loss:2.185963233861319
==== epoch:82, train acc:0.3633333333333334, test acc:0.2672 ===
train loss:2.1610250867454335
train loss:2.184446294636514
train loss:2.1626425763014865
==== epoch:83, train acc:0.3666666666666664, test acc:0.2665 ===
train loss:2.2136047062933715
train loss:2.191795617877527
train loss:2.1528031667063643
==== epoch:84, train acc:0.3666666666666664, test acc:0.2703 ===
train loss:2.173837084499662
train loss:2.170769218481603
train loss:2.1540714331212274
==== epoch:85, train acc:0.3666666666666664, test acc:0.2706 ===
train loss:2.1780299712930584
train loss:2.1609687650636777
train loss:2.1486965443000785
==== epoch:86, train acc:0.3733333333333335, test acc:0.2709 ===
train loss:2.135846031839616
train loss:2.1395748147344746
train loss:2.1635213850066024
==== epoch:87, train acc:0.3633333333333334, test acc:0.2699 ===
train loss:2.2219853369711395
train loss:2.155097212159508
train loss:2.1438370538022844
==== epoch:88, train acc:0.3633333333333334, test acc:0.27 ===
train loss:2.1513360814796774
train loss:2.169221200481271
train loss:2.1676650716010823
==== epoch:89, train acc:0.36, test acc:0.2701 ===
train loss:2.1210169377858117
train loss:2.136203346860075
train loss:2.13054361059659
==== epoch:90, train acc:0.3633333333333334, test acc:0.2706 ===
train loss:2.1293628025675355
train loss:2.1323041786814345
train loss:2.186175816479871
==== epoch:91, train acc:0.36, test acc:0.2707 ===
train loss:2.1869058183399033
train loss:2.1414327108739117
train loss:2.1403571933673127
==== epoch:92, train acc:0.36, test acc:0.2686 ===
```

train loss:2.1896068773217405  
train loss:2.1565571282789757  
train loss:2.1745130760527744  
== epoch:93, train acc:0.3733333333333335, test acc:0.2726 ==  
train loss:2.1266097907382098  
train loss:2.118985398484502  
train loss:2.1429953747649866  
== epoch:94, train acc:0.3666666666666664, test acc:0.2709 ==  
train loss:2.1162481521891277  
train loss:2.152306315688107  
train loss:2.1388200459142026  
== epoch:95, train acc:0.37, test acc:0.2708 ==  
train loss:2.1571580145616904  
train loss:2.1357840464698232  
train loss:2.1495652115848416  
== epoch:96, train acc:0.37, test acc:0.272 ==  
train loss:2.1843436786685766  
train loss:2.1716691123020815  
train loss:2.1373181165144626  
== epoch:97, train acc:0.3733333333333335, test acc:0.2738 ==  
train loss:2.136421507622148  
train loss:2.107752786400467  
train loss:2.1437163283578053  
== epoch:98, train acc:0.3733333333333335, test acc:0.2736 ==  
train loss:2.145714789986651  
train loss:2.167947929353382  
train loss:2.115169835949725  
== epoch:99, train acc:0.3766666666666665, test acc:0.2773 ==  
train loss:2.1780990883264986  
train loss:2.141827623419385  
train loss:2.1459647961940895  
== epoch:100, train acc:0.3766666666666665, test acc:0.278 ==  
train loss:2.10069193433242  
train loss:2.10529606890214  
train loss:2.145674583179772  
== epoch:101, train acc:0.3766666666666665, test acc:0.2764 ==  
train loss:2.124901235300126  
train loss:2.1137755339491924  
train loss:2.139267445137226  
== epoch:102, train acc:0.3766666666666665, test acc:0.2775 ==  
train loss:2.123183688794261  
train loss:2.1779798602167104  
train loss:2.104651215866207  
== epoch:103, train acc:0.3766666666666665, test acc:0.2791 ==  
train loss:2.134380708915295  
train loss:2.1272637413473707  
train loss:2.1287629504726184  
== epoch:104, train acc:0.3766666666666665, test acc:0.2792 ==  
train loss:2.1030514390000783  
train loss:2.118164627057271  
train loss:2.124158595675108  
== epoch:105, train acc:0.3766666666666665, test acc:0.2805 ==  
train loss:2.127945843099574  
train loss:2.116919386437551  
train loss:2.15211923327773  
== epoch:106, train acc:0.3766666666666665, test acc:0.2816 ==  
train loss:2.1228520004854214  
train loss:2.1531099601497408  
train loss:2.088836316377165  
== epoch:107, train acc:0.3766666666666665, test acc:0.2827 ==  
train loss:2.0739639840115016

train loss:2.0809786881902865  
train loss:2.1089833193726673  
==== epoch:108, train acc:0.3766666666666666, test acc:0.2818 ===  
train loss:2.100121154569872  
train loss:2.08434224585347  
train loss:2.076249154592536  
==== epoch:109, train acc:0.3766666666666666, test acc:0.2846 ===  
train loss:2.138235022532617  
train loss:2.082355661666623  
train loss:2.074983908103446  
==== epoch:110, train acc:0.3766666666666666, test acc:0.2876 ===  
train loss:2.140514280938427  
train loss:2.121031602410614  
train loss:2.07049448551188  
==== epoch:111, train acc:0.3766666666666666, test acc:0.2883 ===  
train loss:2.1330693282454107  
train loss:2.103974284301976  
train loss:2.094920490977927  
==== epoch:112, train acc:0.3766666666666666, test acc:0.2909 ===  
train loss:2.085128522963577  
train loss:2.084155008658898  
train loss:2.0782318962152893  
==== epoch:113, train acc:0.3766666666666666, test acc:0.2913 ===  
train loss:2.0905232147244113  
train loss:2.105097377926383  
train loss:2.132134530449913  
==== epoch:114, train acc:0.3766666666666666, test acc:0.2912 ===  
train loss:2.0893305480304396  
train loss:2.033906427703011  
train loss:2.132713222368998  
==== epoch:115, train acc:0.3866666666666666, test acc:0.2915 ===  
train loss:2.0307767395986485  
train loss:2.055616347132545  
train loss:2.0932661508024997  
==== epoch:116, train acc:0.38, test acc:0.2905 ===  
train loss:2.083538747634126  
train loss:2.0871128866573034  
train loss:2.061687430765731  
==== epoch:117, train acc:0.3833333333333336, test acc:0.2907 ===  
train loss:2.017599563151018  
train loss:2.1271040201485767  
train loss:2.0730842231670046  
==== epoch:118, train acc:0.3833333333333336, test acc:0.2921 ===  
train loss:2.049924315176204  
train loss:2.084346847922379  
train loss:2.093901064020835  
==== epoch:119, train acc:0.3833333333333336, test acc:0.2918 ===  
train loss:2.1075371846210027  
train loss:2.0153969150476057  
train loss:2.0694832123918414  
==== epoch:120, train acc:0.3866666666666666, test acc:0.2932 ===  
train loss:2.0497482057127763  
train loss:2.0253302107827755  
train loss:2.171133021647678  
==== epoch:121, train acc:0.3866666666666666, test acc:0.2946 ===  
train loss:2.0408664269443157  
train loss:2.0458376541495227  
train loss:2.0666756494108065  
==== epoch:122, train acc:0.4, test acc:0.296 ===  
train loss:2.0388988286452703  
train loss:2.0195411534736447

train loss:2.0870410633720438  
==== epoch:123, train acc:0.3966666666666667, test acc:0.297 ===  
train loss:2.1065908292712763  
train loss:2.0643881965477306  
train loss:2.0390656631892603  
==== epoch:124, train acc:0.3966666666666667, test acc:0.2973 ===  
train loss:2.0182127632009874  
train loss:2.0594335311104355  
train loss:2.023359138726855  
==== epoch:125, train acc:0.3966666666666667, test acc:0.297 ===  
train loss:1.9826138918041791  
train loss:2.024198173161602  
train loss:2.05024663599046  
==== epoch:126, train acc:0.4, test acc:0.2972 ===  
train loss:2.076031377941603  
train loss:2.044183425208949  
train loss:2.101608317062335  
==== epoch:127, train acc:0.41, test acc:0.2982 ===  
train loss:1.9969917179597758  
train loss:2.0089532894489794  
train loss:2.0945686001829666  
==== epoch:128, train acc:0.41, test acc:0.2988 ===  
train loss:2.0915268886694216  
train loss:2.072352134576801  
train loss:2.003426824021395  
==== epoch:129, train acc:0.4166666666666667, test acc:0.3059 ===  
train loss:2.0860832349315923  
train loss:2.0211463704620636  
train loss:1.9820403094489263  
==== epoch:130, train acc:0.42, test acc:0.3091 ===  
train loss:1.9682435400603964  
train loss:1.994428807291368  
train loss:2.017806930743705  
==== epoch:131, train acc:0.4133333333333333, test acc:0.3063 ===  
train loss:2.080331827784879  
train loss:2.0010969828290186  
train loss:2.022092749768271  
==== epoch:132, train acc:0.4233333333333334, test acc:0.312 ===  
train loss:2.1052754756390804  
train loss:1.9965313104307567  
train loss:2.0040488177322864  
==== epoch:133, train acc:0.4266666666666667, test acc:0.3136 ===  
train loss:1.9224892914674312  
train loss:2.0029194506628865  
train loss:2.0332973609258724  
==== epoch:134, train acc:0.43, test acc:0.3149 ===  
train loss:1.9895067359495997  
train loss:1.9722918128832712  
train loss:2.0218221744310663  
==== epoch:135, train acc:0.4333333333333335, test acc:0.3168 ===  
train loss:2.0375256793239553  
train loss:1.9624881024770664  
train loss:1.9970082526912902  
==== epoch:136, train acc:0.43, test acc:0.3161 ===  
train loss:1.9071749533118196  
train loss:1.9495676773131563  
train loss:1.9427318714183024  
==== epoch:137, train acc:0.4266666666666667, test acc:0.3145 ===  
train loss:2.0485491676073573  
train loss:2.0190723516321505  
train loss:2.0503322083770446

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==== epoch:138, train acc:0.4266666666666667, test acc:0.3183 ===
train loss:1.9068774972522449
train loss:2.043070759262321
train loss:2.030819737086666
==== epoch:139, train acc:0.43, test acc:0.3213 ===
train loss:2.0082380224687655
train loss:1.9048421564007365
train loss:1.9868865322809819
==== epoch:140, train acc:0.43, test acc:0.3228 ===
train loss:1.9606151841970219
train loss:1.9788873153994126
train loss:1.9312944817914774
==== epoch:141, train acc:0.43, test acc:0.3238 ===
train loss:1.970039851077012
train loss:1.9395630459199487
train loss:1.919286404122869
==== epoch:142, train acc:0.4266666666666667, test acc:0.3209 ===
train loss:1.9953231799925815
train loss:1.9718620451478757
train loss:1.9412270293649376
==== epoch:143, train acc:0.4266666666666667, test acc:0.3235 ===
train loss:1.8853875304722099
train loss:1.9565685151596304
train loss:1.964097177434063
==== epoch:144, train acc:0.4266666666666667, test acc:0.3235 ===
train loss:1.9461219277274047
train loss:1.8821691461400427
train loss:1.944036506499269
==== epoch:145, train acc:0.4266666666666667, test acc:0.3241 ===
train loss:1.8971360697462227
train loss:1.951830379679794
train loss:1.9410498156636375
==== epoch:146, train acc:0.43, test acc:0.3244 ===
train loss:1.9956665230819508
train loss:1.8957443558418903
train loss:1.9156289575768006
==== epoch:147, train acc:0.4333333333333335, test acc:0.3245 ===
train loss:1.938402577170696
train loss:1.923679607694646
train loss:1.9509386453225905
==== epoch:148, train acc:0.4433333333333336, test acc:0.3276 ===
train loss:1.8648072358117036
train loss:1.9385239006006083
train loss:1.829007137174299
==== epoch:149, train acc:0.44, test acc:0.3306 ===
train loss:1.9731857988750088
train loss:1.8787589139139103
train loss:1.9085524346504612
==== epoch:150, train acc:0.4366666666666665, test acc:0.329 ===
train loss:1.9149361944903753
train loss:1.8555522782054275
train loss:1.9670544389159899
==== epoch:151, train acc:0.4333333333333335, test acc:0.3302 ===
train loss:1.8991626522408578
train loss:1.9671371426890878
train loss:1.8746604677484127
==== epoch:152, train acc:0.4333333333333335, test acc:0.3316 ===
train loss:1.8848841537745509
train loss:1.9855028399121337
train loss:1.86251804223826
==== epoch:153, train acc:0.44, test acc:0.3364 ===
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train loss:1.8612438011658048  
train loss:1.900514756634074  
train loss:1.9497803755275087  
==== epoch:154, train acc:0.44, test acc:0.3372 ===  
train loss:1.874318510006663  
train loss:1.8487472555081157  
train loss:1.845850742639374  
==== epoch:155, train acc:0.4433333333333336, test acc:0.3426 ===  
train loss:1.9110121298349783  
train loss:1.91263465196669  
train loss:1.8779332626107177  
==== epoch:156, train acc:0.4433333333333336, test acc:0.3414 ===  
train loss:1.8577232727713189  
train loss:1.8792238124361003  
train loss:1.9033427951892596  
==== epoch:157, train acc:0.4433333333333336, test acc:0.3443 ===  
train loss:1.8495938400176988  
train loss:1.8928944255262952  
train loss:1.8219448713943533  
==== epoch:158, train acc:0.4433333333333336, test acc:0.3446 ===  
train loss:1.943519381447387  
train loss:1.9239985898629937  
train loss:1.8780054171818992  
==== epoch:159, train acc:0.4466666666666666, test acc:0.3528 ===  
train loss:1.7509194833599897  
train loss:1.9589477275353504  
train loss:1.8267850775070427  
==== epoch:160, train acc:0.4433333333333336, test acc:0.3535 ===  
train loss:1.8161705320654375  
train loss:1.8077639298505188  
train loss:1.8321940452913277  
==== epoch:161, train acc:0.4433333333333336, test acc:0.3569 ===  
train loss:1.7990097556738938  
train loss:1.863737606074631  
train loss:1.8678210851851935  
==== epoch:162, train acc:0.44, test acc:0.3578 ===  
train loss:1.834643614935043  
train loss:1.7643975943197094  
train loss:1.909453328725977  
==== epoch:163, train acc:0.4366666666666665, test acc:0.3602 ===  
train loss:1.8336880743171877  
train loss:1.8258596219442842  
train loss:1.7631824680290018  
==== epoch:164, train acc:0.4366666666666665, test acc:0.3595 ===  
train loss:1.7519686727794674  
train loss:1.781297722754459  
train loss:1.8058772550522648  
==== epoch:165, train acc:0.4366666666666665, test acc:0.3593 ===  
train loss:1.8647998704501247  
train loss:1.793448828088624  
train loss:1.9186107178532381  
==== epoch:166, train acc:0.46, test acc:0.3655 ===  
train loss:1.7449722008676714  
train loss:1.8143708673840642  
train loss:1.8262517277483812  
==== epoch:167, train acc:0.4666666666666667, test acc:0.3685 ===  
train loss:1.8673199752894405  
train loss:1.7164652124555246  
train loss:1.771392244628406  
==== epoch:168, train acc:0.4733333333333333, test acc:0.3693 ===  
train loss:1.8239060602134114

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train loss:1.8360233175430178
train loss:1.7571416293211461
== epoch:169, train acc:0.48, test acc:0.3712 ===
train loss:1.8692933149925448
train loss:1.8353859184089691
train loss:1.731120863526684
== epoch:170, train acc:0.48, test acc:0.3758 ===
train loss:1.686311558843458
train loss:1.8247101090737474
train loss:1.663157837890984
== epoch:171, train acc:0.4733333333333333, test acc:0.3738 ===
train loss:1.7968381127197637
train loss:1.7830320348760953
train loss:1.826336163556094
== epoch:172, train acc:0.4766666666666667, test acc:0.3785 ===
train loss:1.722506314653719
train loss:1.8032776022220742
train loss:1.801556646146871
== epoch:173, train acc:0.4833333333333334, test acc:0.3828 ===
train loss:1.7675268241339992
train loss:1.75140722564387
train loss:1.851109060838458
== epoch:174, train acc:0.49, test acc:0.3886 ===
train loss:1.651648527361461
train loss:1.7654359574530505
train loss:1.7976802452518859
== epoch:175, train acc:0.4833333333333334, test acc:0.3848 ===
train loss:1.7381087519080578
train loss:1.8074650752076007
train loss:1.8354123492170251
== epoch:176, train acc:0.4833333333333334, test acc:0.3875 ===
train loss:1.6816927869415803
train loss:1.837948925265058
train loss:1.8197879679307127
== epoch:177, train acc:0.49, test acc:0.3889 ===
train loss:1.7782287870758864
train loss:1.7288460980407194
train loss:1.7850543229044087
== epoch:178, train acc:0.5, test acc:0.3917 ===
train loss:1.7012075538122622
train loss:1.5073768183658487
train loss:1.8349949568985655
== epoch:179, train acc:0.5033333333333333, test acc:0.3939 ===
train loss:1.6878720387221633
train loss:1.7798215761972835
train loss:1.7164386645425032
== epoch:180, train acc:0.5, test acc:0.3921 ===
train loss:1.7041270358153202
train loss:1.7435848443107984
train loss:1.7295246508551927
== epoch:181, train acc:0.5033333333333333, test acc:0.3958 ===
train loss:1.8613056970774684
train loss:1.7881524370579793
train loss:1.720722457707567
== epoch:182, train acc:0.5066666666666667, test acc:0.399 ===
train loss:1.6778067015990303
train loss:1.7829789161424916
train loss:1.670981518907206
== epoch:183, train acc:0.5033333333333333, test acc:0.4017 ===
train loss:1.8029589435022608
train loss:1.639963239755873
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train loss:1.7716996574614574  
==== epoch:184, train acc:0.51, test acc:0.4061 ===  
train loss:1.6827613393514034  
train loss:1.6462675926409096  
train loss:1.7897547738801836  
==== epoch:185, train acc:0.51, test acc:0.4054 ===  
train loss:1.7244268988466305  
train loss:1.6794946556009864  
train loss:1.6786125330311241  
==== epoch:186, train acc:0.51, test acc:0.4047 ===  
train loss:1.709813926916945  
train loss:1.6749336540043331  
train loss:1.6444440493716395  
==== epoch:187, train acc:0.51, test acc:0.4095 ===  
train loss:1.6901316489177902  
train loss:1.6258524558864627  
train loss:1.6650110792321604  
==== epoch:188, train acc:0.5133333333333333, test acc:0.4104 ===  
train loss:1.7723278387054133  
train loss:1.7831826974900822  
train loss:1.736583402227726  
==== epoch:189, train acc:0.52, test acc:0.4153 ===  
train loss:1.7243797052821792  
train loss:1.8635439556015725  
train loss:1.5796871948070126  
==== epoch:190, train acc:0.5333333333333333, test acc:0.418 ===  
train loss:1.6623420039244914  
train loss:1.7016542422708738  
train loss:1.73565115666519728  
==== epoch:191, train acc:0.5266666666666666, test acc:0.422 ===  
train loss:1.7062698202666835  
train loss:1.7086935022678282  
train loss:1.7291357208964806  
==== epoch:192, train acc:0.5266666666666666, test acc:0.4254 ===  
train loss:1.6711756315186972  
train loss:1.6327873968630104  
train loss:1.6959206067651207  
==== epoch:193, train acc:0.5266666666666666, test acc:0.4244 ===  
train loss:1.6778762980027775  
train loss:1.6157384178400802  
train loss:1.7085513106943815  
==== epoch:194, train acc:0.5333333333333333, test acc:0.4237 ===  
train loss:1.7482967343734137  
train loss:1.5849192855503094  
train loss:1.6936581362689833  
==== epoch:195, train acc:0.5366666666666666, test acc:0.4274 ===  
train loss:1.7152920076647091  
train loss:1.632362777120693  
train loss:1.7358648375317285  
==== epoch:196, train acc:0.54, test acc:0.4283 ===  
train loss:1.6243867995951407  
train loss:1.6442338912547658  
train loss:1.7240110002874953  
==== epoch:197, train acc:0.5333333333333333, test acc:0.4267 ===  
train loss:1.5428374199380996  
train loss:1.6229867062375798  
train loss:1.6876764398303175  
==== epoch:198, train acc:0.5366666666666666, test acc:0.4259 ===  
train loss:1.6755693108077745  
train loss:1.595730123876183  
train loss:1.5046518303420018

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==== epoch:199, train acc:0.5333333333333333, test acc:0.4242 ===
train loss:1.5918511749789364
train loss:1.6262421887689382
train loss:1.6485144067161983
==== epoch:200, train acc:0.5466666666666666, test acc:0.428 ===
train loss:1.4631485979498877
train loss:1.6164756557992563
train loss:1.6090414535523672
==== epoch:201, train acc:0.5466666666666666, test acc:0.4316 ===
train loss:1.657305072285242
train loss:1.7097605787473968
train loss:1.657547343599202
==== epoch:202, train acc:0.5466666666666666, test acc:0.4346 ===
train loss:1.6319034680268916
train loss:1.555679045560186
train loss:1.6494659826349138
==== epoch:203, train acc:0.5533333333333333, test acc:0.4378 ===
train loss:1.6735395811806495
train loss:1.694376670203009
train loss:1.5707392516307224
==== epoch:204, train acc:0.5566666666666666, test acc:0.4419 ===
train loss:1.5844265380416158
train loss:1.5096792868405107
train loss:1.511955675525893
==== epoch:205, train acc:0.5533333333333333, test acc:0.442 ===
train loss:1.52480319412095
train loss:1.6696999601967875
train loss:1.5078975029309973
==== epoch:206, train acc:0.55, test acc:0.4416 ===
train loss:1.6611845668964893
train loss:1.5781575892832607
train loss:1.523912235210865
==== epoch:207, train acc:0.5566666666666666, test acc:0.4451 ===
train loss:1.6679421386258966
train loss:1.5103637389578644
train loss:1.6755019970965461
==== epoch:208, train acc:0.5533333333333333, test acc:0.4495 ===
train loss:1.5014021658940664
train loss:1.607813314928856
train loss:1.519853310533234
==== epoch:209, train acc:0.56, test acc:0.4519 ===
train loss:1.4581950031945268
train loss:1.6363156742218559
train loss:1.6303501907431077
==== epoch:210, train acc:0.5666666666666667, test acc:0.4541 ===
train loss:1.6162799641572403
train loss:1.528322036811921
train loss:1.5645230114314734
==== epoch:211, train acc:0.57, test acc:0.4568 ===
train loss:1.7125762356035483
train loss:1.627258160405607
train loss:1.6805479655254294
==== epoch:212, train acc:0.5766666666666667, test acc:0.461 ===
train loss:1.5614200679860089
train loss:1.5296029921545875
train loss:1.4217465198513872
==== epoch:213, train acc:0.58, test acc:0.4614 ===
train loss:1.4584725067734732
train loss:1.6451437385362297
train loss:1.6127904239492634
==== epoch:214, train acc:0.58, test acc:0.4612 ===
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train loss:1.6029260321451482  
train loss:1.456196597131088  
train loss:1.4649867329843869  
== epoch:215, train acc:0.573333333333334, test acc:0.4604 ==  
train loss:1.4121363841886676  
train loss:1.6190467931317907  
train loss:1.635359114473035  
== epoch:216, train acc:0.573333333333334, test acc:0.4606 ==  
train loss:1.4881906514793826  
train loss:1.6429552288502278  
train loss:1.4965347403190339  
== epoch:217, train acc:0.5766666666666667, test acc:0.4663 ==  
train loss:1.5356503816877036  
train loss:1.5878253144653645  
train loss:1.616513269394687  
== epoch:218, train acc:0.583333333333334, test acc:0.4669 ==  
train loss:1.4094760811294063  
train loss:1.5315387913965524  
train loss:1.481291292498078  
== epoch:219, train acc:0.583333333333334, test acc:0.4646 ==  
train loss:1.486132431102844  
train loss:1.4674464909984388  
train loss:1.6648192319535362  
== epoch:220, train acc:0.5866666666666667, test acc:0.4667 ==  
train loss:1.5917942811035775  
train loss:1.623724956044348  
train loss:1.5543725346573984  
== epoch:221, train acc:0.583333333333334, test acc:0.4718 ==  
train loss:1.4376415627728811  
train loss:1.5345723234131932  
train loss:1.5733983683798918  
== epoch:222, train acc:0.58, test acc:0.4733 ==  
train loss:1.5420796925223448  
train loss:1.5055808609756978  
train loss:1.5681149346639112  
== epoch:223, train acc:0.58, test acc:0.4744 ==  
train loss:1.479872747579446  
train loss:1.499778138714185  
train loss:1.5580150920162652  
== epoch:224, train acc:0.583333333333334, test acc:0.478 ==  
train loss:1.409883549923255  
train loss:1.6102658543388984  
train loss:1.4423528169845437  
== epoch:225, train acc:0.583333333333334, test acc:0.4779 ==  
train loss:1.5432657342490623  
train loss:1.4188541842418911  
train loss:1.6059647502549075  
== epoch:226, train acc:0.583333333333334, test acc:0.477 ==  
train loss:1.3912771628841318  
train loss:1.4300122878777788  
train loss:1.4978587086395252  
== epoch:227, train acc:0.583333333333334, test acc:0.4786 ==  
train loss:1.563694544653839  
train loss:1.4388622479232598  
train loss:1.4868839848961728  
== epoch:228, train acc:0.593333333333334, test acc:0.4804 ==  
train loss:1.5698933091175302  
train loss:1.4362801209692089  
train loss:1.3117389931019547  
== epoch:229, train acc:0.59, test acc:0.4798 ==  
train loss:1.627591315774281

train loss:1.529241359834925  
train loss:1.4640083750668547  
== epoch:230, train acc:0.5966666666666667, test acc:0.4833 ==  
train loss:1.5760679420887795  
train loss:1.4324450471545518  
train loss:1.592123079945782  
== epoch:231, train acc:0.5966666666666667, test acc:0.4853 ==  
train loss:1.4755663746793073  
train loss:1.4294715958895123  
train loss:1.5980396752970858  
== epoch:232, train acc:0.5966666666666667, test acc:0.4878 ==  
train loss:1.5161016155632114  
train loss:1.4606502110460784  
train loss:1.4397633695346976  
== epoch:233, train acc:0.5966666666666667, test acc:0.4902 ==  
train loss:1.5385670642162006  
train loss:1.4751708550607012  
train loss:1.3954419195585437  
== epoch:234, train acc:0.6066666666666667, test acc:0.4914 ==  
train loss:1.5096913203268238  
train loss:1.3558539418999072  
train loss:1.4157901308278897  
== epoch:235, train acc:0.603333333333334, test acc:0.496 ==  
train loss:1.3590444496603125  
train loss:1.2694058142685294  
train loss:1.6003143439721208  
== epoch:236, train acc:0.61, test acc:0.4925 ==  
train loss:1.477281168593999  
train loss:1.4341444792812883  
train loss:1.5669903065580955  
== epoch:237, train acc:0.6133333333333333, test acc:0.4941 ==  
train loss:1.4357021126740548  
train loss:1.4381279642245344  
train loss:1.5137010668470254  
== epoch:238, train acc:0.6166666666666667, test acc:0.4959 ==  
train loss:1.4628133361381066  
train loss:1.4625908812206754  
train loss:1.4410826582255643  
== epoch:239, train acc:0.6166666666666667, test acc:0.4939 ==  
train loss:1.493846985506153  
train loss:1.4885242497837783  
train loss:1.4600581548211284  
== epoch:240, train acc:0.6166666666666667, test acc:0.4928 ==  
train loss:1.4621277980082996  
train loss:1.3474370600416592  
train loss:1.5271540077345243  
== epoch:241, train acc:0.62, test acc:0.4932 ==  
train loss:1.6200439948547858  
train loss:1.5101871465151329  
train loss:1.4043282330559372  
== epoch:242, train acc:0.6133333333333333, test acc:0.4956 ==  
train loss:1.370642650589147  
train loss:1.3904241836040918  
train loss:1.3181735986293972  
== epoch:243, train acc:0.6133333333333333, test acc:0.4933 ==  
train loss:1.4427755412084915  
train loss:1.4176316211977416  
train loss:1.3596819475474171  
== epoch:244, train acc:0.62, test acc:0.4941 ==  
train loss:1.3856265601968079  
train loss:1.390152966041148

train loss:1.4587440527933424  
==== epoch:245, train acc:0.6233333333333333, test acc:0.4991 ===  
train loss:1.58952961586632  
train loss:1.4707709186179592  
train loss:1.4488052268931242  
==== epoch:246, train acc:0.62, test acc:0.499 ===  
train loss:1.4043825775051635  
train loss:1.4650628100392589  
train loss:1.3832041973843763  
==== epoch:247, train acc:0.6166666666666667, test acc:0.502 ===  
train loss:1.5534555306264237  
train loss:1.4786836695376708  
train loss:1.4781212997784823  
==== epoch:248, train acc:0.6233333333333333, test acc:0.5049 ===  
train loss:1.268035375025152  
train loss:1.4293120223174522  
train loss:1.3508572257983749  
==== epoch:249, train acc:0.63, test acc:0.507 ===  
train loss:1.4879923739950147  
train loss:1.3887185191889233  
train loss:1.5549914013002846  
==== epoch:250, train acc:0.63, test acc:0.5083 ===  
train loss:1.341191354517398  
train loss:1.1524690971788218  
train loss:1.341045043807285  
==== epoch:251, train acc:0.6233333333333333, test acc:0.5061 ===  
train loss:1.2709083535883685  
train loss:1.4276478180579886  
train loss:1.2357029133212898  
==== epoch:252, train acc:0.62, test acc:0.5089 ===  
train loss:1.3160007522305066  
train loss:1.1444118067356492  
train loss:1.5016176162485693  
==== epoch:253, train acc:0.62, test acc:0.5109 ===  
train loss:1.2805204306723152  
train loss:1.4594550438385319  
train loss:1.2760159384759342  
==== epoch:254, train acc:0.6233333333333333, test acc:0.513 ===  
train loss:1.2263614055350784  
train loss:1.315888889294026  
train loss:1.389463637558941  
==== epoch:255, train acc:0.6266666666666667, test acc:0.5118 ===  
train loss:1.4997616335511907  
train loss:1.4775674959075735  
train loss:1.394098991800057  
==== epoch:256, train acc:0.6233333333333333, test acc:0.5104 ===  
train loss:1.3744833120984907  
train loss:1.3118103222000892  
train loss:1.2380510276210484  
==== epoch:257, train acc:0.6266666666666667, test acc:0.5118 ===  
train loss:1.35066450456144  
train loss:1.4651622281039405  
train loss:1.4143904040087485  
==== epoch:258, train acc:0.6266666666666667, test acc:0.5131 ===  
train loss:1.3194570745500178  
train loss:1.1685561402886828  
train loss:1.4337578889872196  
==== epoch:259, train acc:0.63, test acc:0.514 ===  
train loss:1.3125739060889794  
train loss:1.3090392661851609  
train loss:1.4616375222484417

```
== epoch:260, train acc:0.6333333333333333, test acc:0.5142 ==
train loss:1.2792808150764539
train loss:1.4973884826240549
train loss:1.1570986656013584
== epoch:261, train acc:0.6333333333333333, test acc:0.5159 ==
train loss:1.2360936718833548
train loss:1.2673324028665487
train loss:1.3983416701983344
== epoch:262, train acc:0.6333333333333333, test acc:0.5161 ==
train loss:1.3568766983189124
train loss:1.51953208055084
train loss:1.3407403988367819
== epoch:263, train acc:0.6333333333333333, test acc:0.5209 ==
train loss:1.2892582469480223
train loss:1.1590885232308545
train loss:1.2105767417791444
== epoch:264, train acc:0.6333333333333333, test acc:0.52 ==
train loss:1.4112004281047839
train loss:1.249660674985193
train loss:1.3378797401348712
== epoch:265, train acc:0.6333333333333333, test acc:0.5193 ==
train loss:1.2434904702648655
train loss:1.1982376565698565
train loss:1.4409099394128027
== epoch:266, train acc:0.6366666666666667, test acc:0.5197 ==
train loss:1.1913454839312718
train loss:1.3330182874223282
train loss:1.2565606898504746
== epoch:267, train acc:0.66, test acc:0.5197 ==
train loss:1.281361344721476
train loss:1.147865640366727
train loss:1.163981259452073
== epoch:268, train acc:0.6566666666666666, test acc:0.5197 ==
train loss:1.3050407778158462
train loss:1.1619954966943815
train loss:1.3516389669760789
== epoch:269, train acc:0.6533333333333333, test acc:0.5199 ==
train loss:1.2279778768939327
train loss:1.2045699235228553
train loss:1.1854383839076568
== epoch:270, train acc:0.6566666666666666, test acc:0.521 ==
train loss:1.341665105501327
train loss:1.2692589962812761
train loss:1.2917721548176386
== epoch:271, train acc:0.6533333333333333, test acc:0.5222 ==
train loss:1.1781752965940457
train loss:1.298736468088618
train loss:1.390469090783325
== epoch:272, train acc:0.65, test acc:0.5245 ==
train loss:1.419372286320349
train loss:1.2626271986670716
train loss:1.4427941600920926
== epoch:273, train acc:0.66, test acc:0.5246 ==
train loss:1.2803669994551752
train loss:1.2157899788244215
train loss:1.254755257346305
== epoch:274, train acc:0.66, test acc:0.5261 ==
train loss:1.2735615889856557
train loss:1.2444637807621133
train loss:1.1768399185723328
== epoch:275, train acc:0.66, test acc:0.5264 ==
```

train loss:1.2619033611399286  
train loss:1.1686176424593873  
train loss:1.3758780429783155  
== epoch:276, train acc:0.6566666666666666, test acc:0.5303 ==  
train loss:1.297787282179929  
train loss:1.4100004998611348  
train loss:1.2754717405791272  
== epoch:277, train acc:0.66, test acc:0.5331 ==  
train loss:1.2135289260376156  
train loss:1.292731160987047  
train loss:1.2385992098865357  
== epoch:278, train acc:0.66, test acc:0.5343 ==  
train loss:1.3544960491638227  
train loss:1.2167287901148724  
train loss:1.0984436108384212  
== epoch:279, train acc:0.6666666666666666, test acc:0.535 ==  
train loss:1.2817858857115982  
train loss:1.10463088923796  
train loss:1.22116759022126  
== epoch:280, train acc:0.6633333333333333, test acc:0.5361 ==  
train loss:1.1159045173352622  
train loss:1.2087038199340692  
train loss:1.2346311030028962  
== epoch:281, train acc:0.6633333333333333, test acc:0.5371 ==  
train loss:1.3048945658090743  
train loss:1.1524022575034114  
train loss:1.208285521561405  
== epoch:282, train acc:0.66, test acc:0.5369 ==  
train loss:1.291017320996441  
train loss:1.1606354294634658  
train loss:1.2174675890227875  
== epoch:283, train acc:0.66, test acc:0.5366 ==  
train loss:1.2615897425843376  
train loss:1.363437385593665  
train loss:1.1208878630901955  
== epoch:284, train acc:0.6666666666666666, test acc:0.5398 ==  
train loss:1.123443615871755  
train loss:1.326286450720884  
train loss:1.317411938096556  
== epoch:285, train acc:0.66, test acc:0.5395 ==  
train loss:1.159788402428123  
train loss:1.00345292331444  
train loss:1.0294548312977447  
== epoch:286, train acc:0.6633333333333333, test acc:0.5397 ==  
train loss:1.1947424231617358  
train loss:1.1519514665515964  
train loss:1.1564194134903514  
== epoch:287, train acc:0.6733333333333333, test acc:0.5418 ==  
train loss:1.0998195639409252  
train loss:1.1124627273402778  
train loss:1.1093295600536204  
== epoch:288, train acc:0.6833333333333333, test acc:0.5438 ==  
train loss:1.2438564422312728  
train loss:1.0843781050699308  
train loss:1.2365612664081147  
== epoch:289, train acc:0.6833333333333333, test acc:0.5436 ==  
train loss:1.154932343200356  
train loss:1.2437153423373553  
train loss:1.2286979500859923  
== epoch:290, train acc:0.6933333333333334, test acc:0.5453 ==  
train loss:1.2582088674212202

```
train loss:1.2486933815430965
train loss:1.1661344088445074
== epoch:291, train acc:0.69, test acc:0.5468 ===
train loss:1.0637956121933334
train loss:1.1052771914603132
train loss:1.103153227178867
== epoch:292, train acc:0.6933333333333334, test acc:0.5455 ===
train loss:1.15177289063316
train loss:1.1265229393875222
train loss:1.0612983161066902
== epoch:293, train acc:0.6866666666666666, test acc:0.5475 ===
train loss:1.092782418198133
train loss:1.028531826528122
train loss:1.114657865537807
== epoch:294, train acc:0.7, test acc:0.5481 ===
train loss:1.048447756272369
train loss:1.1085499654859714
train loss:1.1358765118660985
== epoch:295, train acc:0.6933333333333334, test acc:0.5481 ===
train loss:1.1207715587884104
train loss:1.042577608945435
train loss:1.2942974538660619
== epoch:296, train acc:0.6966666666666667, test acc:0.5496 ===
train loss:1.075272148596963
train loss:1.0969113854657062
train loss:1.2738765853464067
== epoch:297, train acc:0.7033333333333334, test acc:0.5533 ===
train loss:1.1599976587630951
train loss:1.0945595856221981
train loss:1.0816429976751474
== epoch:298, train acc:0.7033333333333334, test acc:0.5498 ===
train loss:1.1731712515631025
train loss:1.0808633721308063
train loss:1.1718141165503868
== epoch:299, train acc:0.7066666666666667, test acc:0.5503 ===
train loss:1.1696123351320127
train loss:1.1458717185104812
train loss:1.0710112641225613
== epoch:300, train acc:0.7, test acc:0.55 ===
train loss:1.0482047864167503
train loss:1.1389192988301808
train loss:1.1782273781359587
== epoch:301, train acc:0.7033333333333334, test acc:0.5538 ===
train loss:1.0283817248874554
train loss:1.093119824364711
===== Final Test Accuracy =====
test acc:0.5542
<matplotlib.figure.Figure at 0x7f75ef73da20>
```

## ハイパーパラメータの検証

ハイパーパラメータとは、各層のニューロン数やバッチサイズ、パラメータ更新の際の学習係数など、今までてずつぽで設定していた数値。

ハイパーパラメータは適切な値に設定しなければ性能の悪い学習モデルになってしまう。

## 検証データ (Validation Data)

- ・検証データ: 学習モデルのハイパーパラメータを検証する際に使うデータ
- ・テストデータ（評価データ）: 学習モデルを検証する際に使うデータ
- ・学習データ（訓練データ）: 学習データ

ハイパーパラメータがテストデータ／学習データにのみ特化し汎化性能が失われる場合がある為

**テストデータ／学習データを検証データに使ってはならない。**

データの分け方としては以下のようなケースがある。

In [9]:

```
# coding: utf-8
import os
import sys
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.util import shuffle_dataset

(x_train, t_train), (x_test, t_test) = load_mnist()
#訓練データをシャッフル
x_train, t_train = shuffle_dataset(x_train, t_train)

#検証データの分割
validation_rate = 0.20
validation_num = int(x_train.shape[0] * validation_rate)

x_val = x_train[:validation_num] #検証データ
t_val = t_train[:validation_num] #検証データ
x_train = x_train[validation_num:] #学習データ
t_train = t_train[validation_num:] #テストデータ
```

一からデータを分けるなら

生データ → (検証データ → 学習用データ + 評価用データ) + (学習データ → 学習用データ + 評価用データ) となる。

け方については一様分布によるランダムサンプリングが好ましい。

サンプルコードでは一度データをシャッフルしてから一定の割合を抽出している。

## ハイパーパラメータの最適化

### ハイパーパラメータの最適化

- ・おおまかな範囲（10の階乗単位の対数スケール。例： $10^{-3} \sim 10^3$ ）を適当に決める。
- ・おおまかな範囲からランダムにハイパーパラメータを選出する。
- ・評価を行い学習モデルの認識精度を観察してから範囲を狭めていく。

ハイパーパラメータはおおまかにランダムにザクッと決めることが効果的

(<http://www.jmlr.org/papers/volume13/bergstra12a/bergstra12a.pdf>)であるがベイズ最適化を駆使

(<https://papers.nips.cc/paper/4522-practical-bayesian-optimization-of-machine-learning-algorithms.pdf>)して厳密に計算することも可能。

ただし、ハイパーパラメータは評価に至るまで時間がかかるため、時間削減のためepochを小さくして筋の悪そうなハイパーパラメータは早めに見切りをつけることが大切。

## ハイパー パラメータの最適化手順

1. ハイパー パラメータの範囲を設定する
2. 設定されたハイパー パラメータの範囲からランダムにサンプリングする
3. ステップ2でサンプリングされたハイパー パラメータの値を使用して学習を行い検証データでの認識精度を評価する（※epochは小さく設定する）
4. ステップ2とステップ3をある回数（100回など）繰り返しそれらの認識精度の結果から、ハイパー パラメータの範囲を狭める。
5. 1.から4.を気が済むまで繰り返す。

## ハイパー パラメータ最適化の実装

Pythonでは、 $10^{** \text{np.random.uniform}(-3, 3)}$ と書くことで $10^{-3} \sim 10^3$ の範囲でランダムサンプリング可能。

In [21]:

```
import numpy as np
print(10 ** np.random.uniform(-3, 3))
print(10 ** np.random.uniform(-3, 3))
print(10 ** np.random.uniform(-3, 3))
print(10 ** np.random.uniform(-3, 3))
```

2. 6031755993127823  
0. 6363440506605467  
429. 65687301578265  
349. 5372690293394

In [24]:

```
weight_decay = 10 ** np.random.uniform(-8, -4)
lr = 10 ** np.random.uniform(-6, -2)
print("weight_decay:", weight_decay)
print("learning rate:", lr)
```

weight\_decay: 4.289791449003003e-08  
learning rate: 5.510074094447752e-06

In [17]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from common.multi_layer_net import MultiLayerNet
from common.util import shuffle_dataset
from common.trainer import Trainer

(x_train, t_train), (x_test, t_test) = load_mnist(normalize=True)

# 高速化のため訓練データの削減
x_train = x_train[:500]
t_train = t_train[:500]

# 検証データの分離
validation_rate = 0.20
validation_num = int(x_train.shape[0] * validation_rate)
x_train, t_train = shuffle_dataset(x_train, t_train)
x_val = x_train[:validation_num]
t_val = t_train[:validation_num]
x_train = x_train[validation_num:]
t_train = t_train[validation_num:]

def __train(lr, weight_decay, epochs=50):
    network = MultiLayerNet(input_size=784, hidden_size_list=[100, 100, 100, 100, 100, 100], output_size=10, weight_decay_lambda=weight_decay)
    trainer = Trainer(network, x_train, t_train, x_val, t_val, epochs=epochs, mini_batch_size=100, optimizer='sgd', optimizer_param={'lr': lr}, verbose=False)
    trainer.train()

    return trainer.test_acc_list, trainer.train_acc_list

# ハイパーコンフィグレーションのランダム探索=====
optimization_trial = 100
results_val = {}
results_train = {}
for _ in range(optimization_trial):
    # 探索したハイパーコンフィグレーションを指定=====
    weight_decay = 10 ** np.random.uniform(-8, -4)
    lr = 10 ** np.random.uniform(-6, -2)
    # =====

    val_acc_list, train_acc_list = __train(lr, weight_decay)
    print("val acc:" + str(val_acc_list[-1]) + " | lr:" + str(lr) + ", weight decay:" + str(weight_decay))
    key = "lr:" + str(lr) + ", weight decay:" + str(weight_decay)
    results_val[key] = val_acc_list
    results_train[key] = train_acc_list

# グラフの描画=====
print("===== Hyper-Parameter Optimization Result =====")
graph_draw_num = 20
col_num = 5
row_num = int(np.ceil(graph_draw_num / col_num))
```

```
i = 0

for key, val_acc_list in sorted(results_val.items(), key=lambda x:x[1][-1], reverse=True):
    print("Best-" + str(i+1) + "(val acc:" + str(val_acc_list[-1]) + ") | " + key)

    plt.subplot(row_num, col_num, i+1)
    plt.title("Best-" + str(i+1))
    plt.ylim(0.0, 1.0)
    if i % 5: plt.yticks([])
    plt.xticks([])
    x = np.arange(len(val_acc_list))
    plt.plot(x, val_acc_list)
    plt.plot(x, results_train[key], "--")
    i += 1

    if i >= graph_draw_num:
        break

plt.show()
```

val acc:0.56 | lr:0.004566696120232825, weight decay:1.5969743292639288e-07  
val acc:0.67 | lr:0.006525974176274847, weight decay:1.2753302851950627e-07  
val acc:0.08 | lr:1.1516746032106855e-05, weight decay:3.7189747861876775e-05  
val acc:0.11 | lr:0.000260264068700295, weight decay:6.889341753981655e-07  
val acc:0.57 | lr:0.0040205140430813685, weight decay:7.366089464868839e-07  
val acc:0.11 | lr:5.0993701157740635e-06, weight decay:1.781310577020698e-08  
val acc:0.11 | lr:1.105994750024369e-05, weight decay:1.5707152987989059e-06  
val acc:0.12 | lr:6.0042844139806414e-05, weight decay:4.580200944918364e-06  
val acc:0.12 | lr:0.0005471894574985656, weight decay:1.2617970079911852e-07  
val acc:0.17 | lr:2.603729891157405e-05, weight decay:3.200377992803121e-06  
val acc:0.08 | lr:5.23834874861114e-05, weight decay:1.0251318508398392e-06  
val acc:0.1 | lr:1.094529307828141e-05, weight decay:9.453825835413832e-05  
val acc:0.08 | lr:3.879487392778149e-06, weight decay:1.0569174608096627e-08  
val acc:0.16 | lr:3.451373020909633e-06, weight decay:4.480359344197798e-07  
val acc:0.18 | lr:0.0010596414980648709, weight decay:9.283996502980033e-08  
val acc:0.13 | lr:3.0031329872430472e-06, weight decay:1.974049066745719e-08  
val acc:0.78 | lr:0.009779048474070934, weight decay:1.351682025547439e-06  
val acc:0.29 | lr:0.002309019930593434, weight decay:8.561708735450507e-06  
val acc:0.54 | lr:0.0038101215997068446, weight decay:1.7574178600691726e-05  
val acc:0.13 | lr:3.1107203795863696e-06, weight decay:3.323793465545872e-05  
val acc:0.13 | lr:0.0003450855004374945, weight decay:1.7646710648000065e-05  
val acc:0.12 | lr:0.00033261550485782257, weight decay:3.6912792427116194e-07  
val acc:0.08 | lr:4.843001704656871e-05, weight decay:2.557289613877472e-08  
val acc:0.15 | lr:1.4164040092490789e-06, weight decay:1.8824196286487735e-06  
val acc:0.29 | lr:0.0006761083432232099, weight decay:9.577261646331784e-05  
val acc:0.15 | lr:0.000360492404095738, weight decay:1.7750976479277526e-08  
val acc:0.21 | lr:0.0007978964376835612, weight decay:1.4428453765119217e-08  
val acc:0.13 | lr:6.848749908356776e-06, weight decay:7.989549207841927e-07  
val acc:0.69 | lr:0.004445971857514631, weight decay:5.8606897926086976e-08  
val acc:0.72 | lr:0.008220792113215686, weight decay:2.5325368104168772e-08  
val acc:0.17 | lr:0.000324726614354249, weight decay:2.9578190702854325e-06  
val acc:0.54 | lr:0.004029755255736933, weight decay:5.47933121162538e-07  
val acc:0.19 | lr:0.0006164121963136637, weight decay:1.4148327137096943e-05  
val acc:0.55 | lr:0.004359193185972747, weight decay:4.546379947243963e-07  
val acc:0.05 | lr:4.803128649485642e-05, weight decay:1.485951669384858e-06  
val acc:0.22 | lr:3.8581706337123985e-05, weight decay:5.579346796522656e-08  
val acc:0.08 | lr:2.0824451920771285e-05, weight decay:2.466493803362757e-05  
val acc:0.14 | lr:1.8943628853261206e-06, weight decay:3.851744658671523e-05  
val acc:0.78 | lr:0.008374908719779505, weight decay:8.349159115994573e-06  
val acc:0.09 | lr:1.4657645570309318e-06, weight decay:2.1448507872079716e-07  
val acc:0.13 | lr:0.0004472210326178419, weight decay:2.6097529292406664e-07  
val acc:0.07 | lr:1.679031562515611e-06, weight decay:5.358053813737613e-07  
val acc:0.09 | lr:7.047966422809452e-06, weight decay:9.2455192370086e-08  
val acc:0.74 | lr:0.006475159571652492, weight decay:7.2050817257212294e-06  
val acc:0.27 | lr:0.0018683199114762454, weight decay:2.879708798899426e-07  
val acc:0.16 | lr:1.033703624967391e-05, weight decay:1.4036926978716486e-08  
val acc:0.08 | lr:1.2119080600658149e-06, weight decay:1.1190364058808228e-06  
val acc:0.08 | lr:0.0010163825027416696, weight decay:9.138084636153747e-06  
val acc:0.46 | lr:0.003568102655626634, weight decay:3.1598815626968435e-05  
val acc:0.65 | lr:0.006789710392273347, weight decay:1.7478414439085595e-07  
val acc:0.15 | lr:3.494799891412799e-05, weight decay:4.38662124084519e-06  
val acc:0.77 | lr:0.009323085074401091, weight decay:4.625089765870598e-07  
val acc:0.33 | lr:0.0023201963637831044, weight decay:8.599198952080675e-05  
val acc:0.13 | lr:0.00022775845061572797, weight decay:7.011227793740556e-06  
val acc:0.24 | lr:0.0013307899272796172, weight decay:1.1559487537211119e-05  
val acc:0.68 | lr:0.004362195756987248, weight decay:2.8434760553946477e-08  
val acc:0.1 | lr:1.869330592751728e-05, weight decay:3.630681532090649e-06  
val acc:0.66 | lr:0.004391866605439157, weight decay:6.690754210451607e-08  
val acc:0.11 | lr:0.00012157840787319765, weight decay:3.019207683588879e-06  
val acc:0.07 | lr:5.73197619547558e-06, weight decay:2.1248114247065703e-08  
val acc:0.05 | lr:6.625590516575907e-05, weight decay:4.1668550057624566e-05

val acc:0.12 | lr:5.660096880946212e-06, weight decay:4.047970759554877e-06  
val acc:0.47 | lr:0.004094660684753804, weight decay:2.139026281739255e-05  
val acc:0.07 | lr:0.00014378353850230587, weight decay:3.501513239480806e-05  
val acc:0.07 | lr:2.7678348082938608e-06, weight decay:3.605875969270973e-05  
val acc:0.61 | lr:0.00501244747823184, weight decay:6.6061630974215995e-06  
val acc:0.08 | lr:1.4459656560560125e-06, weight decay:6.921478885518981e-08  
val acc:0.06 | lr:1.877902881369377e-06, weight decay:8.861234175020568e-06  
val acc:0.16 | lr:0.00027992860374476103, weight decay:8.136908635997955e-06  
val acc:0.64 | lr:0.005584996179822284, weight decay:2.090197431586645e-05  
val acc:0.09 | lr:3.7044851999906146e-05, weight decay:4.041497491549873e-06  
val acc:0.53 | lr:0.004741102906808209, weight decay:3.502481235924246e-07  
val acc:0.06 | lr:0.0001500538282592443, weight decay:8.710511069186092e-05  
val acc:0.05 | lr:0.0007201893628910685, weight decay:1.4141463050091068e-07  
val acc:0.1 | lr:0.0002495235789467229, weight decay:1.0247541807452934e-06  
val acc:0.33 | lr:0.003522635404612876, weight decay:5.607510911261655e-06  
val acc:0.54 | lr:0.00420288585593756, weight decay:2.9751099377293143e-08  
val acc:0.1 | lr:3.139872005608798e-05, weight decay:2.115085732690944e-08  
val acc:0.08 | lr:0.00017345508581192417, weight decay:1.572664068064797e-05  
val acc:0.09 | lr:4.8541455667862805e-05, weight decay:2.497774082582095e-06  
val acc:0.07 | lr:7.845278502551505e-05, weight decay:4.45901951288139e-07  
val acc:0.08 | lr:9.645301964391163e-05, weight decay:4.5264854697146816e-08  
val acc:0.1 | lr:0.00010109347952662167, weight decay:1.4972460411885978e-08  
val acc:0.2 | lr:8.355921001909981e-06, weight decay:2.7235869781658287e-08  
val acc:0.24 | lr:0.0014810412114846852, weight decay:5.607416368730088e-06  
val acc:0.16 | lr:6.507964953119368e-06, weight decay:1.3242922217095415e-05  
val acc:0.36 | lr:0.0025833134792508723, weight decay:2.6120485931760436e-06  
val acc:0.13 | lr:1.527643704818154e-06, weight decay:2.570591487346121e-07  
val acc:0.05 | lr:7.307140440620332e-06, weight decay:9.590537582632035e-05  
val acc:0.08 | lr:1.1744292411860575e-05, weight decay:3.821521013064728e-07  
val acc:0.08 | lr:1.4362586820432618e-05, weight decay:8.85781365016604e-08  
val acc:0.14 | lr:2.0988274915780365e-06, weight decay:1.9002015863970334e-06  
val acc:0.68 | lr:0.005762442868939066, weight decay:4.455212914034312e-05  
val acc:0.1 | lr:0.0004516820555058821, weight decay:8.336087557854645e-06  
val acc:0.42 | lr:0.003253784601778332, weight decay:1.9826434940886548e-07  
val acc:0.66 | lr:0.0063328970415446936, weight decay:2.3015817865279555e-05  
val acc:0.35 | lr:0.0020977436884009595, weight decay:1.8457007243634437e-05  
val acc:0.15 | lr:0.0004325436447926334, weight decay:1.5319094146776284e-07  
val acc:0.44 | lr:0.0023420582425195203, weight decay:6.1012606383627386e-06  
val acc:0.09 | lr:4.264418219877188e-06, weight decay:1.7105643403207038e-05

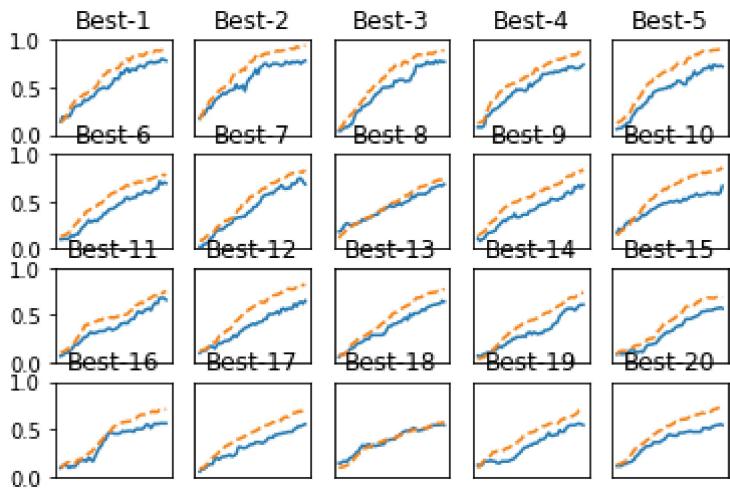
===== Hyper-Parameter Optimization Result =====

Best-1(val acc:0.78) | lr:0.008374908719779505, weight decay:8.349159115994573e-06  
Best-2(val acc:0.78) | lr:0.009779048474070934, weight decay:1.351682025547439e-06  
Best-3(val acc:0.77) | lr:0.009323085074401091, weight decay:4.625089765870598e-07  
Best-4(val acc:0.74) | lr:0.006475159571652492, weight decay:7.2050817257212294e-06  
Best-5(val acc:0.72) | lr:0.008220792113215686, weight decay:2.5325368104168772e-08  
Best-6(val acc:0.69) | lr:0.004445971857514631, weight decay:5.8606897926086976e-08  
Best-7(val acc:0.68) | lr:0.005762442868939066, weight decay:4.455212914034312e-05  
Best-8(val acc:0.68) | lr:0.004362195756987248, weight decay:2.8434760553946477e-08  
Best-9(val acc:0.67) | lr:0.006525974176274847, weight decay:1.2753302851950627e-07  
Best-10(val acc:0.66) | lr:0.004391866605439157, weight decay:6.690754210451607e-08  
Best-11(val acc:0.66) | lr:0.0063328970415446936, weight decay:2.3015817865279555e-05  
Best-12(val acc:0.65) | lr:0.006789710392273347, weight decay:1.7478414439085595e-07  
Best-13(val acc:0.64) | lr:0.005584996179822284, weight decay:2.090197431586645e-0

```

5
Best-14(val acc:0.61) | lr:0.00501244747823184, weight decay:6.6061630974215995e-0
6
Best-15(val acc:0.57) | lr:0.0040205140430813685, weight decay:7.366089464868839e-
07
Best-16(val acc:0.56) | lr:0.004566696120232825, weight decay:1.5969743292639288e-
07
Best-17(val acc:0.55) | lr:0.004359193185972747, weight decay:4.546379947243963e-0
7
Best-18(val acc:0.54) | lr:0.004029755255736933, weight decay:5.47933121162538e-07
Best-19(val acc:0.54) | lr:0.00420288585593756, weight decay:2.9751099377293143e-0
8
Best-20(val acc:0.54) | lr:0.0038101215997068446, weight decay:1.7574178600691726e
-05

```



認識精度が高い上位20のグラフを見る限りでは

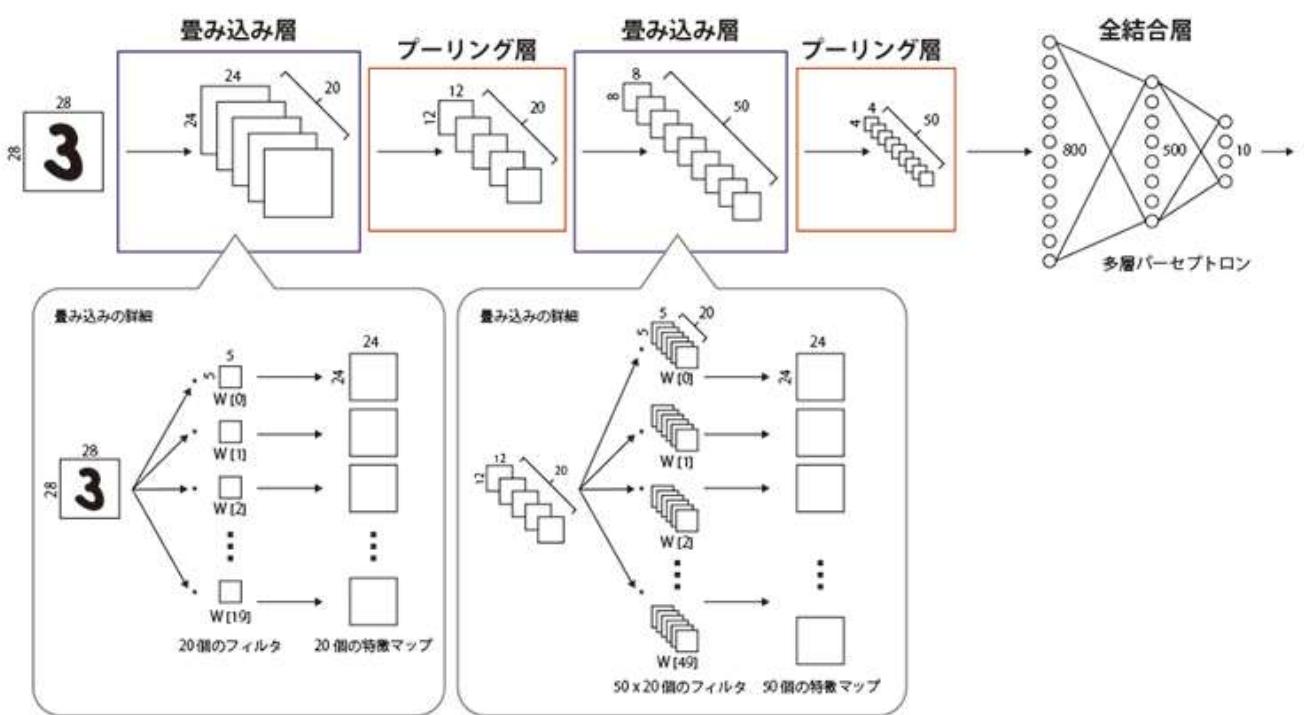
- lr(学習係数)が $0.001 \sim 0.01$
- weight\_decayが $10^{-8} \sim 10^{-6}$ くらいが良さそうである。

# 畳み込みニューラルネットワーク

## 畳み込み層

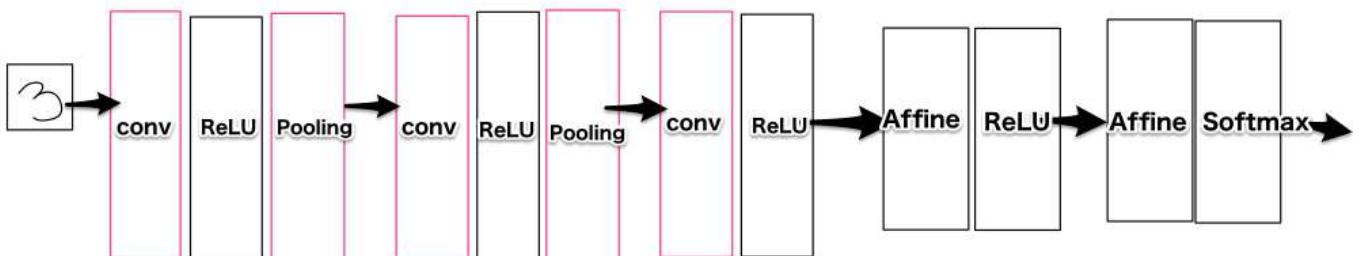
- ・ 畳み込み層: CNN (Convolutional Neural Network) で新たに取り入れられる層の一つ。
- ・ 特徴マップ(feature map): 畳み込み層における入出力データのこと
- ・ 入力特徴マップ(input feature map): 畳み込み層における入力データのこと
- ・ 出力特徴マップ(output feature map): 畳み込み層における出力データのこと

<http://www.hpc.co.jp/AboutDeepLearning.html> (<http://www.hpc.co.jp/AboutDeepLearning.html>)



<http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545>

(<http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545>).



## 全結合層の問題点

これまでのニューラルネットワークは隣接する層のすべてのニューロンとニューロンの間で結合がある  
(fully-connected; 全結合;) 状態だった。

我々はこれまでそれぞれの結合部をAffineレイヤ (行列の内積計算) で実装しReLUにて発火させた。これは何の考慮もせずに入力値をそのまま行列に変換してニューラルネットワークを構築したことになる。つまり今回のMNISTの手書き文字の場合、元々あった縦・横などの「データの形状情報」やRGB (ピクセルの色合いの順序情報; R要素・G要素・B要素の区別,) が失われてしまうことになる。

**データをそのまま全結合層の入力 (行列) として扱った場合3次元以上の情報は失われてしまう !**

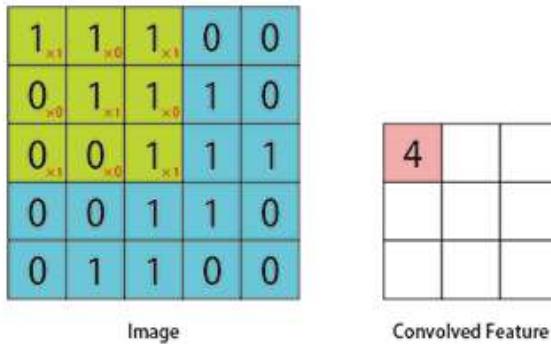
例えば、画像を行列として扱った場合に失われる情報としては以下が考えられる

- ピクセルのR,G,B,Aのそれぞれの濃度
- 縦・横のピクセル幅
- 上下左右で連続したピクセル間の値の推移

## 畳み込み演算

畳み込み演算は画像処理で言う「フィルター演算」にあたる。

<http://www.hpc.co.jp/AboutDeepLearning.html> (<http://www.hpc.co.jp/AboutDeepLearning.html>)



「フィルター」はカーネルとも呼ばれ、入力データに対してあるウインドウサイズの区画で積和演算を行う。全結合のニューラルネットワークでは行列が重みパラメータとなっていたが、CNNの場合はこのフィルターの乗算内容が「重み」に対応する。

積和演算の結果は各ウインドウの位置ごとに取得され、結果は新たな出力データとなる。

その出力データの行列にスカラをスカラ加算 (行列の要素全てに等しく加算) することでバイアスも実現する。

バイアスはスカラなので、 $1 \times 1$ の行列となる。

## パディング

入力データの大外にダミーの枠を用意することで、積和演算結果のサイズを調整できる。

畳み込み演算を繰り返すと段々出力サイズが小さくなるので、最終的な出力サイズが1になることを防ぐことができる。

畳み込み演算回数 (隠れ層の数) によっては不要の場合がある。

## ストライド

フィルターの適用する位置の間隔のこと。積和演算が一回終わった時点でウィンドウがスライドする幅。パディングとは逆に、ストライドは大きくすると積和演算結果の出力サイズは小さくなる。

## ストライドと出力サイズの関係

- 出力サイズ ( $OH = \frac{H+2P-FH}{S} + 1, OW = \frac{W+2P-FW}{S} + 1$ )
  - 入力サイズ ( $H, W$ )
  - フィルターサイズ ( $FH, FW$ )
  - パディング  $P$
  - ストライド  $S$

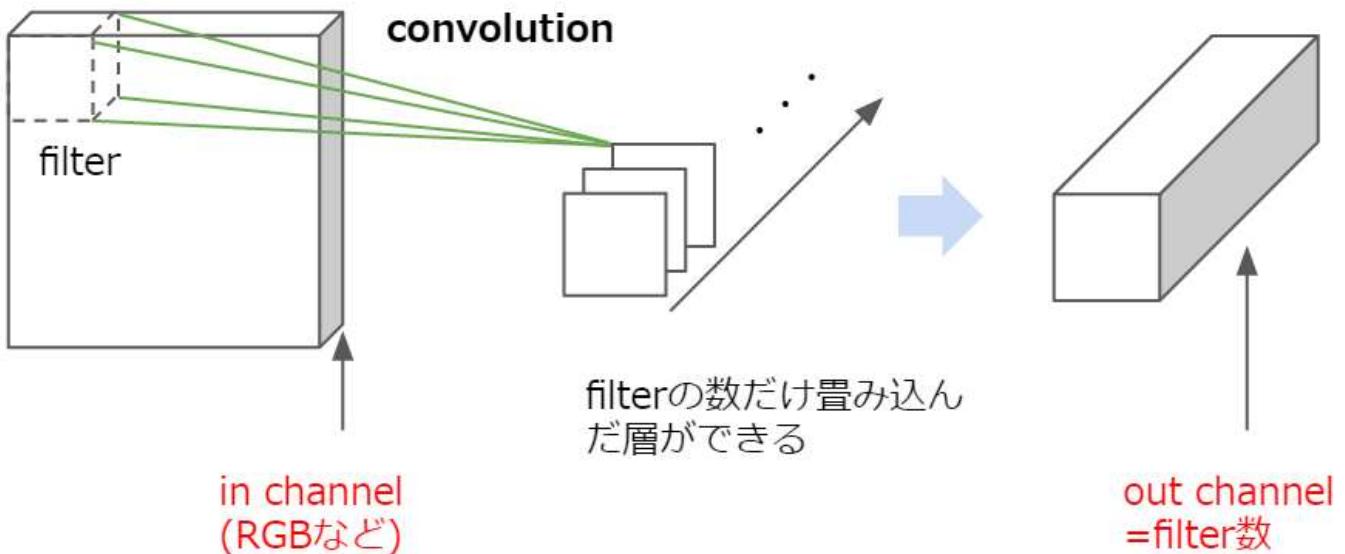
ただし、ストライドで割り切れない値の場合は長方形の形にならない（行列において欠損データが発生する）為割り切れない値を丸めるかダミー値を挿入すること。

## 3次元データの畳み込み演算

通常の畳み込み演算にチャンネル（奥行き）を加えたもの。

- 適用フィルターの枚数 (=重み)  $\times$  入力データ = 出力チャンネル数となる。
- バイアスは (フィルター数, 1, 1) という形でブロードキャスト演算により適用される。

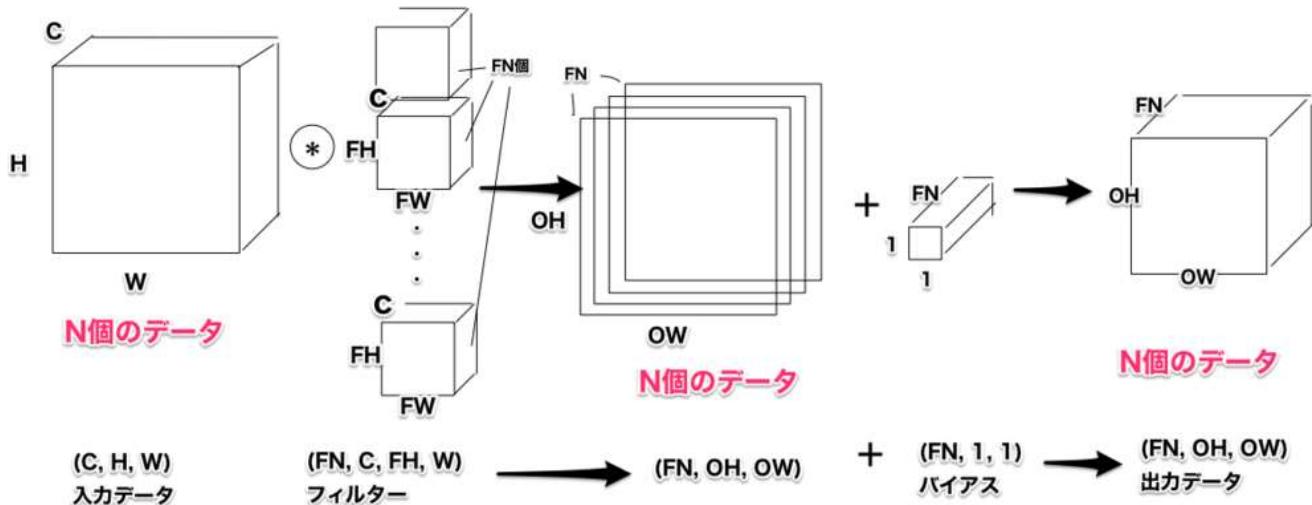
<http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545>  
(<http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545>).



## 畳み込み演算のバッチ演算

単にN個のデータを重ねただけ。（4次元データの演算）

<http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545>  
[\(<http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545>\).](http://pythonskywalker.hatenablog.com/entry/2016/12/26/164545)



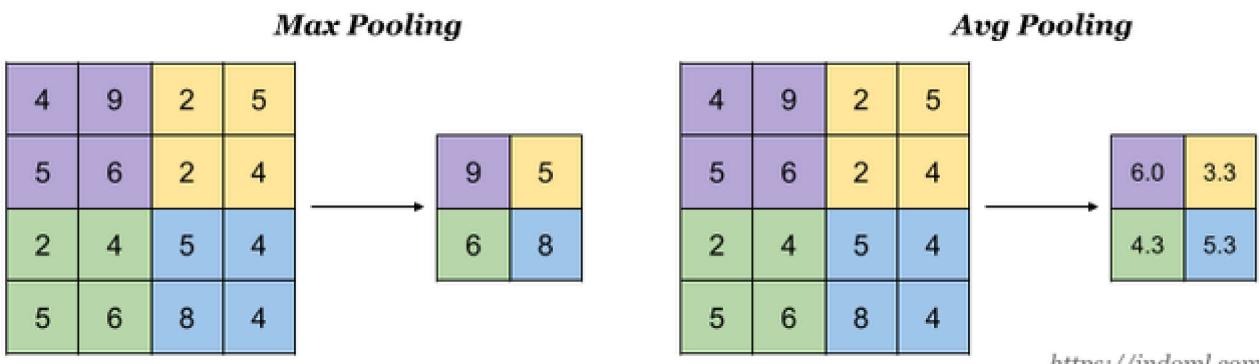
## プーリング層

プーリング層(Pooling)は引数フィルターなどを持たずに、関数のみで入力を縦・横の空間を狭くして出力する演算のこと。

一般的にはウインドウサイズ=ストライドとなるように設定する。

MAXプーリングは以下のような形で演算がなされる。他にも、Averageプーリングなどがある。

<https://indoml.com/2018/03/07/student-notes-convolutional-neural-networks-cnn-introduction/>  
[\(<https://indoml.com/2018/03/07/student-notes-convolutional-neural-networks-cnn-introduction/>\).](https://indoml.com/2018/03/07/student-notes-convolutional-neural-networks-cnn-introduction/)



## プーリング層の特徴

学習するパラメータがない

プーリング層は畳み込みそうと違い学習パラメータを持たない。(層自体が成長しない)

チャンネル層は変化しない

プーリング層を通過しても入力データと出力データのチャンネル数は変化しない。

### 微小な位置変化に対してロバスト（頑健）

入力データの小さなズレに対してもプーリング層は同じような結果を返す。

入力データが多少ズレっていてもウィンドウサイズに収まっている程度のズレであれば吸収できる。

## Convolution／Poolingレイヤの実装

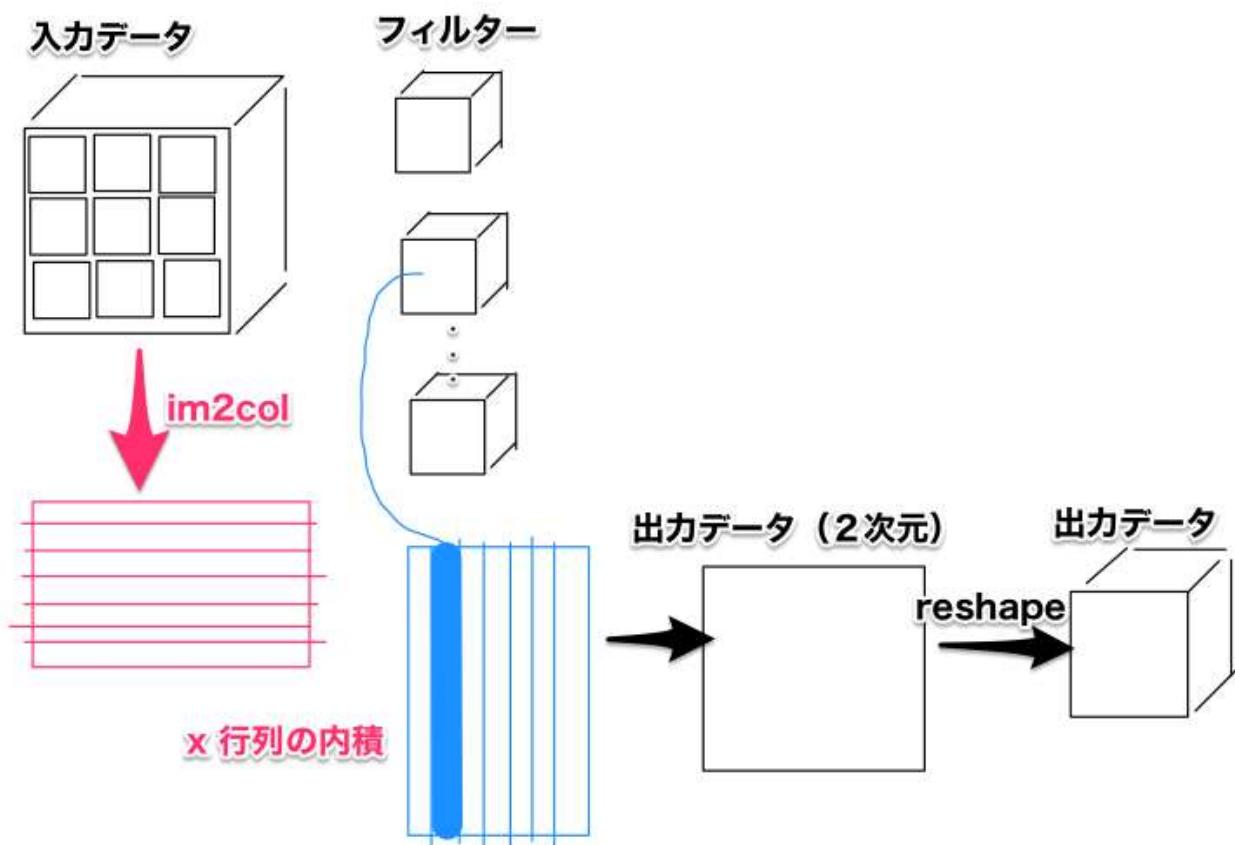
### 4次元配列

CNNは高さx横幅xチャネルxデータ数の四次元セットと言える。

### im2colによる展開

畳み込み演算はim2colを使用して入力データを単純な行列の計算に落とし込む方法を使うと線形代数ライブラリで高速処理できるようになる。

<http://narusawa-a-hiyoko.hatenablog.com/entry/2016/04/12/042039> (<http://narusawa-a-hiyoko.hatenablog.com/entry/2016/04/12/042039>)



## Convolutionレイヤの実装

## im2colの実装

In [14]:

```
def im2col(input_data, filter_h, filter_w, stride=1, pad=0):
    """
    Parameters
    -----
    input_data : (データ数, チャンネル, 高さ, 幅)の4次元配列からなる入力データ
    filter_h : フィルターの高さ
    filter_w : フィルターの幅
    stride : ストライド
    pad : パディング

    Returns
    -----
    col : 2次元配列
    """
    N, C, H, W = input_data.shape #データ数、チャンネル(奥行き)、高さ、幅
    out_h = (H + 2*pad - filter_h)//stride + 1#出力高さを計算
    out_w = (W + 2*pad - filter_w)//stride + 1#出力幅を計算

    img = np.pad(input_data, [(0, 0), (0, 0), (pad, pad), (pad, pad)], 'constant')#0埋めでパディング
    #no_pad(array, pad_width, mode=None, **kwargs)
    col = np.zeros((N, C, filter_h, filter_w, out_h, out_w))#出力用0埋め二次元データのハコを作成
    #np.zeros(shape, dtype=float, order='C')

    for y in range(filter_h):#ストライドを反映させる
        y_max = y + stride*out_h
        for x in range(filter_w):
            x_max = x + stride*out_w
            col[:, :, y, x, :, :] = img[:, :, y:y_max:stride, x:x_max:stride]

    col = col.transpose(0, 4, 5, 1, 2, 3).reshape(N*out_h*out_w, -1)
    #XXX: ここが分からん！！！
    return col
```

In [17]:

```
import sys, os
import numpy as np
sys.path.append(os.pardir)
from common.util import im2col

x1 = np.random.rand(1, 3, 7, 7)
print(x1.shape)
# 1: データ数(バッチ数)
# 3: チャンネル(奥行き)
# 7: 高さ
# 7: 幅
#4次元配列からなる入力データ

col1 = im2col(x1, 5, 5, stride=1, pad=0)
# x1 : (データ数(バッチ数), チャンネル(奥行き), 高さ, 幅)の4次元配列からなる入力データ
# 5 : フィルターの高さ
# 5 : フィルターの幅
# 1 : ストライド
# 0 : パディング
print(col1.shape)
# 9 = #XXX: ここが分からん !
# 75 = (チャンネル(奥行き) x フィルターの高さ x フィルターの高さ)

x2 = np.random.rand(10, 3, 7, 7)
print(x2.shape)

col2 = im2col(x2, 5, 5, stride=1, pad=0)
print(col2.shape)
# 90 = #XXX: ここが分からん !
# 75 = (チャンネル(奥行き) x フィルターの高さ x フィルターの高さ)
```

(1, 3, 7, 7)  
(9, 75)  
(10, 3, 7, 7)  
(90, 75)

畳み込み層をConvolutionという名前のクラスで実装する

In [19]:

```
class Convolution:  
    def __init__(self, W, b, stride=1, pad=0):  
        self.W = W # フィルターの「重み」  
        # FN, C, FH, FW = self.W.shape  
        self.b = b # フィルターの「バイアス」  
        self.stride = stride # フィルターのストライド  
        self.pad = pad # フィルター適用前のパディング  
  
        # 中間データ (backward時に使用)  
        self.x = None  
        self.col = None  
        self.col_W = None  
  
        # 重み・バイアスパラメータの勾配  
        self.dW = None  
        self.db = None  
  
    def forward(self, x):  
        FN, C, FH, FW = self.W.shape  
        # FN=Filterの数, C=チャンネル(奥行), FH=フィルターの高さ, FW=フィルターの幅  
        N, C, H, W = x.shape  
        out_h = 1 + int((H + 2 * self.pad - FH) / self.stride)  
        out_w = 1 + int((W + 2 * self.pad - FW) / self.stride)  
  
        col = im2col(x, FH, FW, self.stride, self.pad) # 入力データを行列式(二次元データ)に変換  
        col_W = self.W.reshape(FN, -1).T # フィルターデータを行列式(二次元データ)に変換  
  
        out = np.dot(col, col_W) + self.b # 二次元データとなり扱えるようになった。Affineレイヤと同じく、内積を取る  
        out = out.reshape(N, out_h, out_w, -1).transpose(0, 3, 1, 2) # 内積を取った後に元の出力データの形に戻す  
  
        self.x = x  
        self.col = col  
        self.col_W = col_W  
  
        return out  
  
    def backward(self, dout):  
        FN, C, FH, FW = self.W.shape  
        dout = dout.transpose(0, 2, 3, 1).reshape(-1, FN)  
  
        self.db = np.sum(dout, axis=0)  
        self.dW = np.dot(self.col.T, dout)  
        self.dW = self.dW.transpose(1, 0).reshape(FN, C, FH, FW)  
  
        dcol = np.dot(dout, self.col_W.T)  
        dx = col2im(dcol, self.x.shape, FH, FW, self.stride, self.pad)  
  
        return dx
```

Convolutionレイヤの順伝搬

- 入力データをim2colで2次元配列に展開
- フィルターもreshapeで二次元配列に展開
- Affine変換（内積の取得）

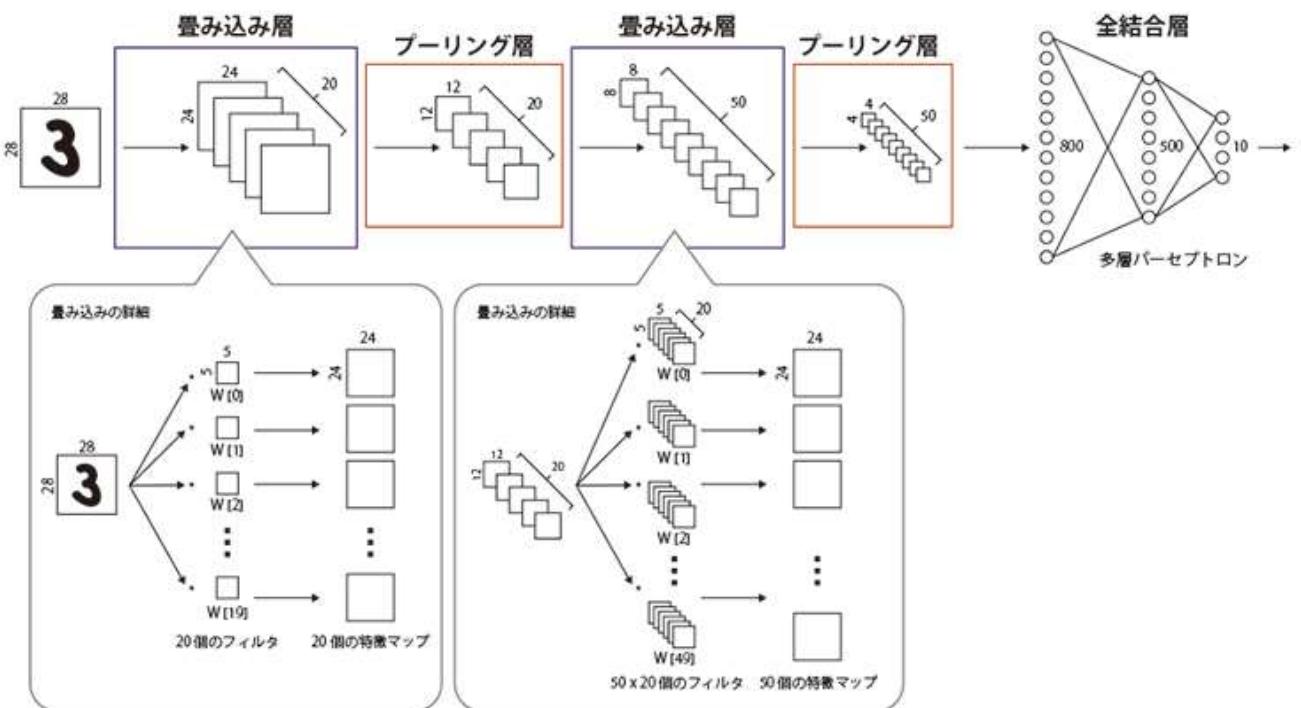
## Convolutionレイヤの逆伝搬

- col2imを使う

## Poolingレイヤの実装

PoolingレイヤもConvolutionレイヤと同様、im2colを使って入力データを展開する。但し、プーリングの適用領域チャンネル方向によって変わらない。展開した行列から最大値を求め、適切な計上に整形する。  
(MAX-Pooling)

<http://www.hpc.co.jp/AboutDeepLearning.html> (<http://www.hpc.co.jp/AboutDeepLearning.html>)



In [1]:

```
class Pooling:  
    def __init__(self, pool_h, pool_w, stride=1, pad=0):  
        self.pool_h = pool_h  
        self.pool_w = pool_w  
        self.stride = stride  
        self.pad = pad  
  
        self.x = None  
        self.arg_max = None  
  
    def forward(self, x):  
        N, C, H, W = x.shape  
        out_h = int(1 + (H - self.pool_h) / self.stride)  
        out_w = int(1 + (W - self.pool_w) / self.stride)  
  
        col = im2col(x, self.pool_h, self.pool_w, self.stride, self.pad)  
        col = col.reshape(-1, self.pool_h*self.pool_w)  
  
        arg_max = np.argmax(col, axis=1)  
        out = np.max(col, axis=1)  
        out = out.reshape(N, out_h, out_w, C).transpose(0, 3, 1, 2)  
  
        self.x = x  
        self.arg_max = arg_max  
  
        return out  
  
    def backward(self, dout):  
        dout = dout.transpose(0, 2, 3, 1)  
  
        pool_size = self.pool_h * self.pool_w  
        dmax = np.zeros((dout.size, pool_size))  
        dmax[np.arange(self.arg_max.size), self.arg_max.flatten()] = dout.flatten()  
        dmax = dmax.reshape(dout.shape + (pool_size,))  
  
        dcol = dmax.reshape(dmax.shape[0] * dmax.shape[1] * dmax.shape[2], -1)  
        dx = col2im(dcol, self.x.shape, self.pool_h, self.pool_w, self.stride, self.pad)  
  
        return dx
```

## CNNの実装

### SimpleConvNetクラスの実装

In [4]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="単純なCNNのネットワーク構成")
with dot.subgraph(name="main") as main:
    main.node("L1", "Conv")
    main.node("L2", "ReLU")
    main.node("L3", "Pooling")
    main.node("L4", "Affine")
    main.node("L5", "ReLU")
    main.node("L6", "Affine")
    main.node("L7", "Softmax")
    main.edge("L1", "L2", label="")
    main.edge("L2", "L3", label="")
    main.edge("L3", "L4", label="")
    main.edge("L4", "L5", label="")
    main.edge("L5", "L6", label="")
    main.edge("L6", "L7", label="")
#print(dot)
dot
```

Out[4]:



In [5]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import pickle
import numpy as np
from collections import OrderedDict
from common.layers import *
from common.gradient import numerical_gradient

class SimpleConvNet:
    """単純なConvNet

    conv - relu - pool - affine - relu - affine - softmax

    Parameters
    -----
    input_size : 入力サイズ (MNISTの場合は784)
    hidden_size_list : 隠れ層のニューロンの数のリスト (e.g. [100, 100, 100])
    output_size : 出力サイズ (MNISTの場合は10)
    activation : 'relu' or 'sigmoid'
    weight_init_std : 重みの標準偏差を指定 (e.g. 0.01)
        'relu'または'he'を指定した場合は「Heの初期値」を設定
        'sigmoid'または'xavier'を指定した場合は「Xavierの初期値」を設定
    """
    def __init__(self, input_dim=(1, 28, 28),
                 conv_param={'filter_num':30, 'filter_size':5, 'pad':0, 'stride':1},
                 hidden_size=100, output_size=10, weight_init_std=0.01):
        filter_num = conv_param['filter_num']
        filter_size = conv_param['filter_size']
        filter_pad = conv_param['pad']
        filter_stride = conv_param['stride']
        input_size = input_dim[1]
        conv_output_size = (input_size - filter_size + 2*filter_pad) / filter_stride + 1
        pool_output_size = int(filter_num * (conv_output_size/2) * (conv_output_size/2))

        # 重みの初期化
        self.params = {}
        # Convolution Weight
        self.params['W1'] = weight_init_std * \
            np.random.randn(filter_num, input_dim[0], filter_size, filter_size)
        self.params['b1'] = np.zeros(filter_num)
        # Affine Weight
        self.params['W2'] = weight_init_std * \
            np.random.randn(pool_output_size, hidden_size)
        self.params['b2'] = np.zeros(hidden_size)
        # Affine Weight
        self.params['W3'] = weight_init_std * \
            np.random.randn(hidden_size, output_size)
        self.params['b3'] = np.zeros(output_size)

        # レイヤの生成
        self.layers = OrderedDict()
        self.layers['Conv1'] = Convolution(self.params['W1'], self.params['b1'],
                                           conv_param['stride'], conv_param['pad'])
        self.layers['Relu1'] = ReLU()
        self.layers['Pool1'] = Pooling(pool_h=2, pool_w=2, stride=2)
        self.layers['Affine1'] = Affine(self.params['W2'], self.params['b2'])
        self.layers['Relu2'] = ReLU()
```

```

        self.layers['Affine2'] = Affine(self.params['W3'], self.params['b3'])

        self.last_layer = SoftmaxWithLoss()

    def predict(self, x):
        for layer in self.layers.values():
            x = layer.forward(x)

        return x

    def loss(self, x, t):
        """損失関数を求める
        引数のxは入力データ、tは教師ラベル
        """
        y = self.predict(x)
        return self.last_layer.forward(y, t)

    def accuracy(self, x, t, batch_size=100):
        if t.ndim != 1: t = np.argmax(t, axis=1)

        acc = 0.0

        for i in range(int(x.shape[0] / batch_size)):
            tx = x[i*batch_size:(i+1)*batch_size]
            tt = t[i*batch_size:(i+1)*batch_size]
            y = self.predict(tx)
            y = np.argmax(y, axis=1)
            acc += np.sum(y == tt)

        return acc / x.shape[0]

    def numerical_gradient(self, x, t):
        """勾配を求める(数値微分)

        Parameters
        -----
        x : 入力データ
        t : 教師ラベル

        Returns
        -----
        各層の勾配を持ったディクショナリ変数
        grads['W1'], grads['W2'], ... は各層の重み
        grads['b1'], grads['b2'], ... は各層のバイアス
        """
        loss_w = lambda w: self.loss(x, t)

        grads = {}
        for idx in (1, 2, 3):
            grads['W' + str(idx)] = numerical_gradient(loss_w, self.params['W' + str(idx)])
            grads['b' + str(idx)] = numerical_gradient(loss_w, self.params['b' + str(idx)])

        return grads

    def gradient(self, x, t):
        """勾配を求める(誤差逆伝搬法)

        Parameters
        -----
        x : 入力データ
        t : 教師ラベル

```

*Returns*

```
各層の勾配を持ったディクショナリ変数
grads['W1']、grads['W2']、... は各層の重み
grads['b1']、grads['b2']、... は各層のバイアス
"""
# forward
self.loss(x, t)

# backward
dout = 1
dout = self.last_layer.backward(dout)

layers = list(self.layers.values())
layers.reverse()
for layer in layers:
    dout = layer.backward(dout)

# 設定
grads = {}
grads['W1'], grads['b1'] = self.layers['Conv1'].dW, self.layers['Conv1'].db
grads['W2'], grads['b2'] = self.layers['Affine1'].dW, self.layers['Affine1'].db
grads['W3'], grads['b3'] = self.layers['Affine2'].dW, self.layers['Affine2'].db

return grads

def save_params(self, file_name="params.pkl"):
    params = {}
    for key, val in self.params.items():
        params[key] = val
    with open(file_name, 'wb') as f:
        pickle.dump(params, f)

def load_params(self, file_name="params.pkl"):
    with open(file_name, 'rb') as f:
        params = pickle.load(f)
    for key, val in params.items():
        self.params[key] = val

    for i, key in enumerate(['Conv1', 'Affine1', 'Affine2']):
        self.layers[key].W = self.params['W' + str(i+1)]
        self.layers[key].b = self.params['b' + str(i+1)]
```

## SimpleConvNetの引数

- 初期化の際の重みの標準偏差
- 入力データ ( $C, H, W$ ) の次元
- Convolution層
  - フィルターの数
  - フィルターのサイズ
  - フィルターのストライド
  - フィルターのパディング
- 隠れ層
  - 全結合ニューロン数
- 出力層
  - 全結合ニューロン数

### SimpleConvNetにおけるMNIST

In [ ]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import numpy as np
import matplotlib.pyplot as plt
from dataset.mnist import load_mnist
from simple_convnet import SimpleConvNet
from common.trainer import Trainer

# データの読み込み
(x_train, t_train), (x_test, t_test) = load_mnist(flatten=False)

# 処理に時間がかかる場合はデータを削減
#x_train, t_train = x_train[:5000], t_train[:5000]
#x_test, t_test = x_test[:1000], t_test[:1000]

max_epochs = 20

network = SimpleConvNet(input_dim=(1, 28, 28),
                        conv_param = {'filter_num': 30, 'filter_size': 5, 'pad': 0, 'stride': 1},
                        hidden_size=100, output_size=10, weight_init_std=0.01)

trainer = Trainer(network, x_train, t_train, x_test, t_test,
                  epochs=max_epochs, mini_batch_size=100,
                  optimizer='Adam', optimizer_param={'lr': 0.001},
                  evaluate_sample_num_per_epoch=1000)
trainer.train()

# パラメータの保存
network.save_params("params.pkl")
print("Saved Network Parameters!")

# グラフの描画
markers = {'train': 'o', 'test': 's'}
x = np.arange(max_epochs)
plt.plot(x, trainer.train_acc_list, marker='o', label='train', markevery=2)
plt.plot(x, trainer.test_acc_list, marker='s', label='test', markevery=2)
plt.xlabel("epochs")
plt.ylabel("accuracy")
plt.ylim(0, 1.0)
plt.legend(loc='lower right')
plt.show()
```

## CNNの可視化

### 一層目の重みの可視化

一層目は畳み込みフィルタである

In [2]:

```
from graphviz import Digraph
dot = Digraph(comment="計算グラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="単純なCNNのネットワーク構成")
with dot.subgraph(name="main") as main:
    main.node("L1", "Conv", color="red")
    main.node("L2", "ReLU")
    main.node("L3", "Pooling")
    main.node("L4", "Affine")
    main.node("L5", "ReLU")
    main.node("L6", "Affine")
    main.node("L7", "Softmax")
    main.edge("L1", "L2", label="")
    main.edge("L2", "L3", label="")
    main.edge("L3", "L4", label="")
    main.edge("L4", "L5", label="")
    main.edge("L5", "L6", label="")
    main.edge("L6", "L7", label="")
#print(dot)
dot
```

Out[2]:



- 畳み込み層の重みとなるフィルタはグレースケールの画像を表現する
  - サイズ(縦・横) :  $5 \times 5$
  - チャンネル(色彩): 1
  - フィルター(数) : 30

In [4]:

```
# coding: utf-8
import numpy as np
import matplotlib.pyplot as plt
from simple_convnet import SimpleConvNet

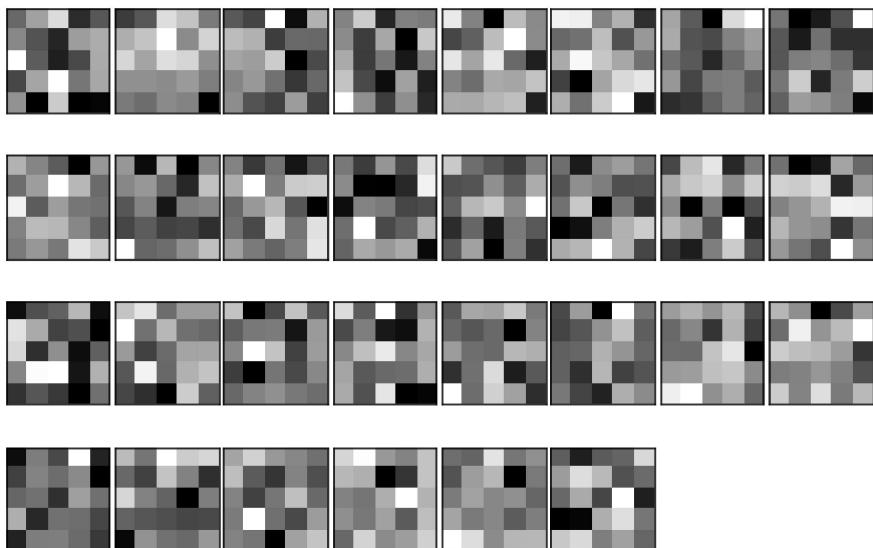
def filter_show(filters, nx=8, margin=3, scale=10):
    """
    c.f. https://gist.github.com/aidiary/07d530d5e08011832b12#file-draw_weight-py
    """
    FN, C, FH, FW = filters.shape
    ny = int(np.ceil(FN / nx))

    fig = plt.figure()
    fig.subplots_adjust(left=0, right=1, bottom=0, top=1, hspace=0.05, wspace=0.05)

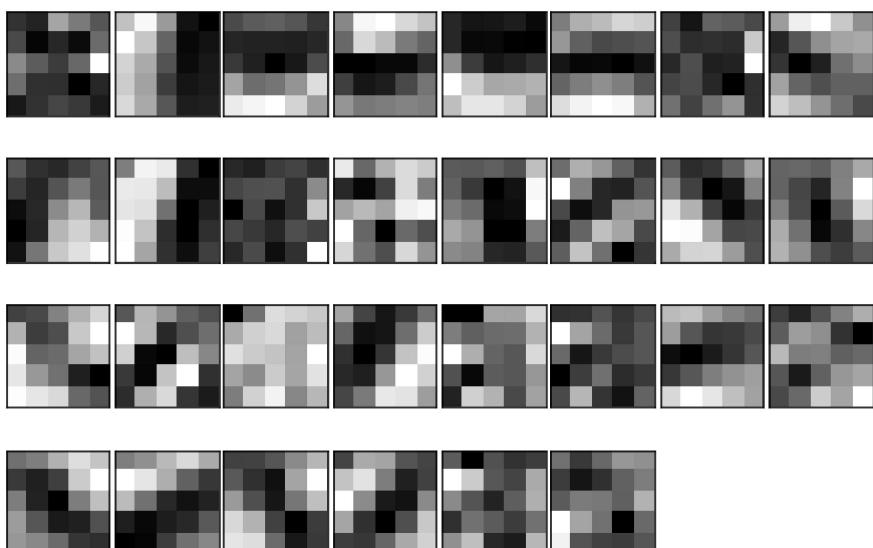
    for i in range(FN):
        ax = fig.add_subplot(ny, nx, i+1, xticks=[], yticks[])
        ax.imshow(filters[i, 0], cmap=plt.cm.gray_r, interpolation='nearest')
    plt.show()

network = SimpleConvNet()
# ランダム初期化後の重み
print("学習前")
filter_show(network.params['W1'])
print("学習後")
# 学習後の重み
network.load_params("params.pkl")
filter_show(network.params['W1'])
```

学習前



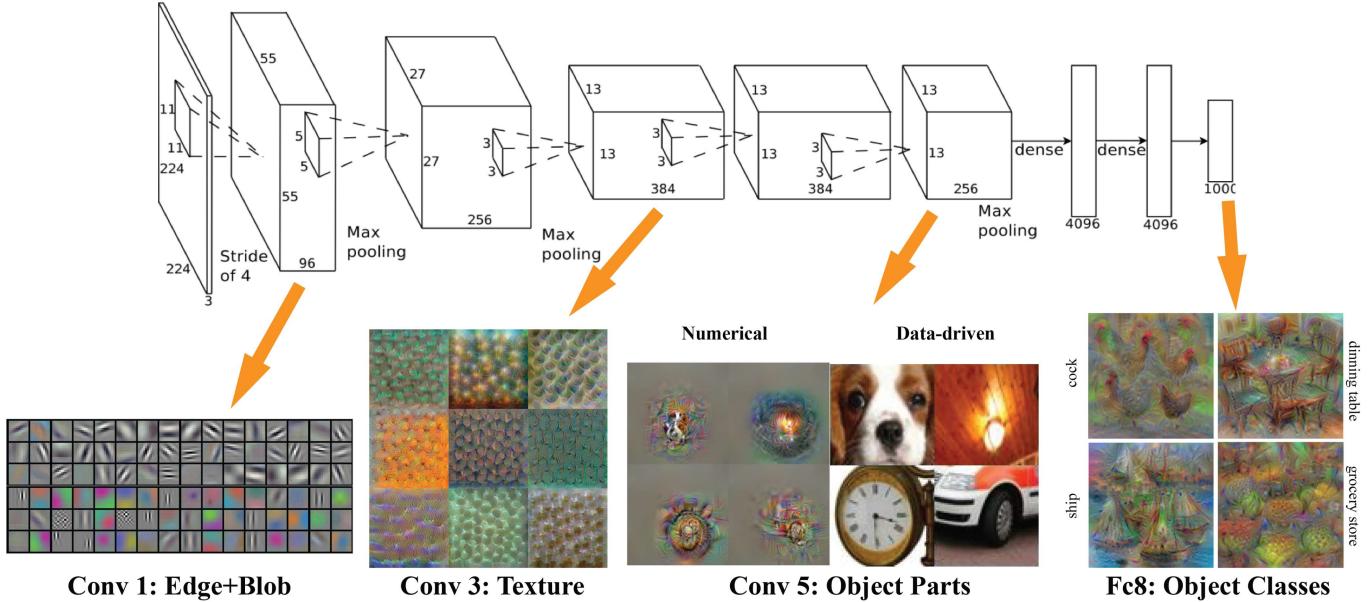
学習後



一様分布で生成されたフィルタが重みの学習後にある程度の偏りを見せていることが確認できる。  
これは画像におけるプリミティブな部分（色が大きく変わる部分や固まって同じ色が続く部分）をフィルタ  
が抽出していることを意味する。

## 階層構造による情報抽出

<https://www.kisspng.com/png-deep-learning-convolutional-neural-network-alexnet-3064759/>  
(<https://www.kisspng.com/png-deep-learning-convolutional-neural-network-alexnet-3064759/>)



上記はAlexNetによる例

- 1層目はEdge・Blob
- 3層目はTexture
- 5層目はObject Parts
- 全結合層はObject Class

## 代表的なCNN

### LeNet

CNNの元祖

### AlexNet

- ReLUを使用
- LRN(Local Response Normalization)を使う※正規化の走り
- Dropoutを使用

**アルゴリズムは既に存在していたが、ディープラーニング(ビッグデータ)の流行りは以下に支えられている**

- 大量のデータを個人でも保存できるディスク容量単価の底上げ
- 大量のデータを個人でもダウンロードできるネットワーク帯域容量単価の底上げ
- 大量のデータを個人でも並列処理できるGPU計算容量単価の底上げ

# ディープラーニング

## ディープな手書き数字認識

- 3x3の小さなフィルターによる畳込み層
- 活性化関数はReLU
- 全結合層の後にDropoutレイヤを使用
- Adamによる最適化
- 重みの初期値として「Heの初期値」を使用

In [1]:

```
# coding: utf-8
import sys, os
sys.path.append(os.pardir) # 親ディレクトリのファイルをインポートするための設定
import pickle
import numpy as np
from collections import OrderedDict
from common.layers import *

class DeepConvNet:
    """認識率99%以上の高精度なConvNet

    ネットワーク構成は下記の通り
    conv - relu - conv - relu - pool -
    conv - relu - conv - relu - pool -
    conv - relu - conv - relu - pool -
    affine - relu - dropout - affine - dropout - softmax
    """
    def __init__(self, input_dim=(1, 28, 28),
                 conv_param_1 = {'filter_num':16, 'filter_size':3, 'pad':1, 'stride':1},
                 conv_param_2 = {'filter_num':16, 'filter_size':3, 'pad':1, 'stride':1},
                 conv_param_3 = {'filter_num':32, 'filter_size':3, 'pad':1, 'stride':1},
                 conv_param_4 = {'filter_num':32, 'filter_size':3, 'pad':2, 'stride':1},
                 conv_param_5 = {'filter_num':64, 'filter_size':3, 'pad':1, 'stride':1},
                 conv_param_6 = {'filter_num':64, 'filter_size':3, 'pad':1, 'stride':1},
                 hidden_size=50, output_size=10):
        # 重みの初期化=====
        # 各層のニューロンひとつあたりが、前層のニューロンといくつのつながりがあるか (TODO:自動で計算する)
        pre_node_nums = np.array([1*3*3, 16*3*3, 16*3*3, 32*3*3, 32*3*3, 64*3*3, 64*4*4, hidden_size])
        wight_init_scales = np.sqrt(2.0 / pre_node_nums) # ReLUを使う場合に推奨される初期値

        self.params = {}
        pre_channel_num = input_dim[0]
        for idx, conv_param in enumerate([conv_param_1, conv_param_2, conv_param_3, conv_param_4,
                                         conv_param_5, conv_param_6]):
            self.params['W' + str(idx+1)] = wight_init_scales[idx] * np.random.randn(conv_param['filter_num'], pre_channel_num, conv_param['filter_size'], conv_param['filter_size'])
            self.params['b' + str(idx+1)] = np.zeros(conv_param['filter_num'])
            pre_channel_num = conv_param['filter_num']
        self.params['W7'] = wight_init_scales[6] * np.random.randn(64*4*4, hidden_size)
        self.params['b7'] = np.zeros(hidden_size)
        self.params['W8'] = wight_init_scales[7] * np.random.randn(hidden_size, output_size)
        self.params['b8'] = np.zeros(output_size)

        # レイヤの生成=====
        self.layers = []
        self.layers.append(Convolution(self.params['W1'], self.params['b1'],
                                      conv_param_1['stride'], conv_param_1['pad']))
        self.layers.append(ReLU())
        self.layers.append(Convolution(self.params['W2'], self.params['b2'],
                                      conv_param_2['stride'], conv_param_2['pad']))
        self.layers.append(ReLU())
        self.layers.append(Pooling(pool_h=2, pool_w=2, stride=2))
        self.layers.append(Convolution(self.params['W3'], self.params['b3'],
                                      conv_param_3['stride'], conv_param_3['pad']))
        self.layers.append(ReLU())
        self.layers.append(Convolution(self.params['W4'], self.params['b4'],
```

```

        conv_param_4['stride'], conv_param_4['pad']))
self.layers.append(ReLU())
self.layers.append(Pooling(pool_h=2, pool_w=2, stride=2))
self.layers.append(Convolution(self.params['W5'], self.params['b5'],
                               conv_param_5['stride'], conv_param_5['pad']))
self.layers.append(ReLU())
self.layers.append(Convolution(self.params['W6'], self.params['b6'],
                               conv_param_6['stride'], conv_param_6['pad']))
self.layers.append(ReLU())
self.layers.append(Pooling(pool_h=2, pool_w=2, stride=2))
self.layers.append(Affine(self.params['W7'], self.params['b7']))
self.layers.append(ReLU())
self.layers.append(Dropout(0.5))
self.layers.append(Affine(self.params['W8'], self.params['b8']))
self.layers.append(Dropout(0.5))

self.last_layer = SoftmaxWithLoss()

def predict(self, x, train_flg=False):
    for layer in self.layers:
        if isinstance(layer, Dropout):
            x = layer.forward(x, train_flg)
        else:
            x = layer.forward(x)
    return x

def loss(self, x, t):
    y = self.predict(x, train_flg=True)
    return self.last_layer.forward(y, t)

def accuracy(self, x, t, batch_size=100):
    if t.ndim != 1: t = np.argmax(t, axis=1)

    acc = 0.0

    for i in range(int(x.shape[0] / batch_size)):
        tx = x[i*batch_size:(i+1)*batch_size]
        tt = t[i*batch_size:(i+1)*batch_size]
        y = self.predict(tx, train_flg=False)
        y = np.argmax(y, axis=1)
        acc += np.sum(y == tt)

    return acc / x.shape[0]

def gradient(self, x, t):
    # forward
    self.loss(x, t)

    # backward
    dout = 1
    dout = self.last_layer.backward(dout)

    tmp_layers = self.layers.copy()
    tmp_layers.reverse()
    for layer in tmp_layers:
        dout = layer.backward(dout)

    # 設定
    grads = {}
    for i, layer_idx in enumerate((0, 2, 5, 7, 10, 12, 15, 18)):
        grads['W' + str(i+1)] = self.layers[layer_idx].dW

```

```
grads['b' + str(i+1)] = self.layers[layer_idx].db

return grads

def save_params(self, file_name="params.pkl"):
    params = {}
    for key, val in self.params.items():
        params[key] = val
    with open(file_name, 'wb') as f:
        pickle.dump(params, f)

def load_params(self, file_name="params.pkl"):
    with open(file_name, 'rb') as f:
        params = pickle.load(f)
    for key, val in params.items():
        self.params[key] = val

    for i, layer_idx in enumerate((0, 2, 5, 7, 10, 12, 15, 18)):
        self.layers[layer_idx].W = self.params['W' + str(i+1)]
        self.layers[layer_idx].b = self.params['b' + str(i+1)]
```

In [5]:

```
from graphviz import Digraph
dot = Digraph(comment="上記ディープラーニングのグラフ")
dot.attr(rankdir="LR")
#dot.attr(splines="") #line or curved or ortho or polyline;
dot.attr(fixedsize="true")
dot.attr(label="上記ディープラーニングのグラフ")
with dot.subgraph(name="main") as main:
    main.node("L1", "Conv")
    main.node("L2", "ReLU")
    main.node("L3", "Conv")
    main.node("L4", "ReLU")
    main.node("L5", "Pool")
    main.node("L6", "Conv")
    main.node("L7", "ReLU")
    main.node("L8", "Conv")
    main.node("L9", "ReLU")
    main.node("L10", "Pool")
    main.node("L11", "Conv")
    main.node("L12", "ReLU")
    main.node("L13", "Conv")
    main.node("L14", "ReLU")
    main.node("L15", "Pool")
    main.node("L16", "Affine")
    main.node("L17", "ReLU")
    main.node("L18", "Dropout")
    main.node("L19", "Affine")
    main.node("L20", "Dropout")
    main.node("L21", "Softmax")
    main.edge("L1", "L2", label="")
    main.edge("L2", "L3", label="")
    main.edge("L3", "L4", label="")
    main.edge("L4", "L5", label="")
    main.edge("L5", "L6", label="")
    main.edge("L6", "L7", label="")
    main.edge("L7", "L8", label="")
    main.edge("L8", "L9", label="")
    main.edge("L9", "L10", label="")
    main.edge("L10", "L11", label="")
    main.edge("L11", "L12", label="")
    main.edge("L12", "L13", label="")
    main.edge("L13", "L14", label="")
    main.edge("L14", "L15", label="")
    main.edge("L15", "L16", label="")
    main.edge("L16", "L17", label="")
    main.edge("L17", "L18", label="")
    main.edge("L18", "L19", label="")
    main.edge("L19", "L20", label="")
    main.edge("L20", "L21", label="")
    #print(dot)
dot
```

Out[5] :



このCNNの認識精度は概ね99%を超す

## さらに認識精度を高めるには

- アンサンブル学習(ensemble learning)
- 学習率の減衰(learning rate decay)
- データ拡張(data augmentation)

### Data Augmentation

入力画像を人工的なアルゴリズムによって微小変化させる

- Crop処理: データを切り出す
- flip処理: データを回線させる
- scale処理: データを拡大縮小させる

### 層を深くすることのモチベーション

層をいたずらに深くする事の重要性は証明されていないが、昨今の傾向としては層を深くする（認識性能の向上を見込んでいる）方向に向かっている。層を深くすることの利点

- 層を深くしない場合に比べより少ないパラメータで同レベル以上の表現をすることが出来る
- 特に小さなフィルターを重ねてネットワークを深くすることにより受容野（receptive field）を広くすることが出来る。
- 層を重ねることでReLU等の活性化関数が畳み込み層の間に挟まれることになり、非線形の力を強める事ができる。
- 各層が別の特徴を捉えることでCNN全体が一つの特徴以外に囚われなくなる
  - 各層が学習すべき課題がよりシンプルな問題へと分解される

### ディープラーニングの少歴史

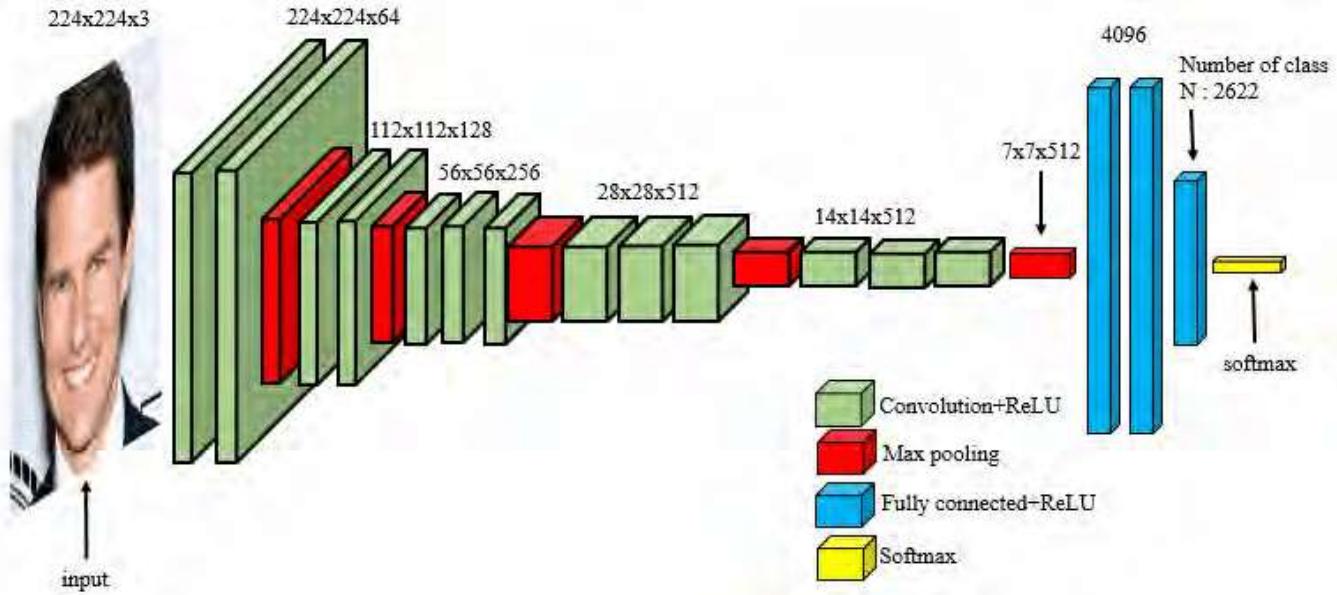
ILSVRC(ImageNet Large Scale Visual Recognition Challenge)でAlexNetが圧倒的成績で優勝したことがブームの始まり

### ImageNet

ILSVRC(ImageNet Large Scale Visual Recognition Challenge)(<http://www.image-net.org/challenges/LSVRC/>)は画像認識のコンペティション。  
その中でもVGG, GoogleLeNet, RasNetが有名。

### VGG

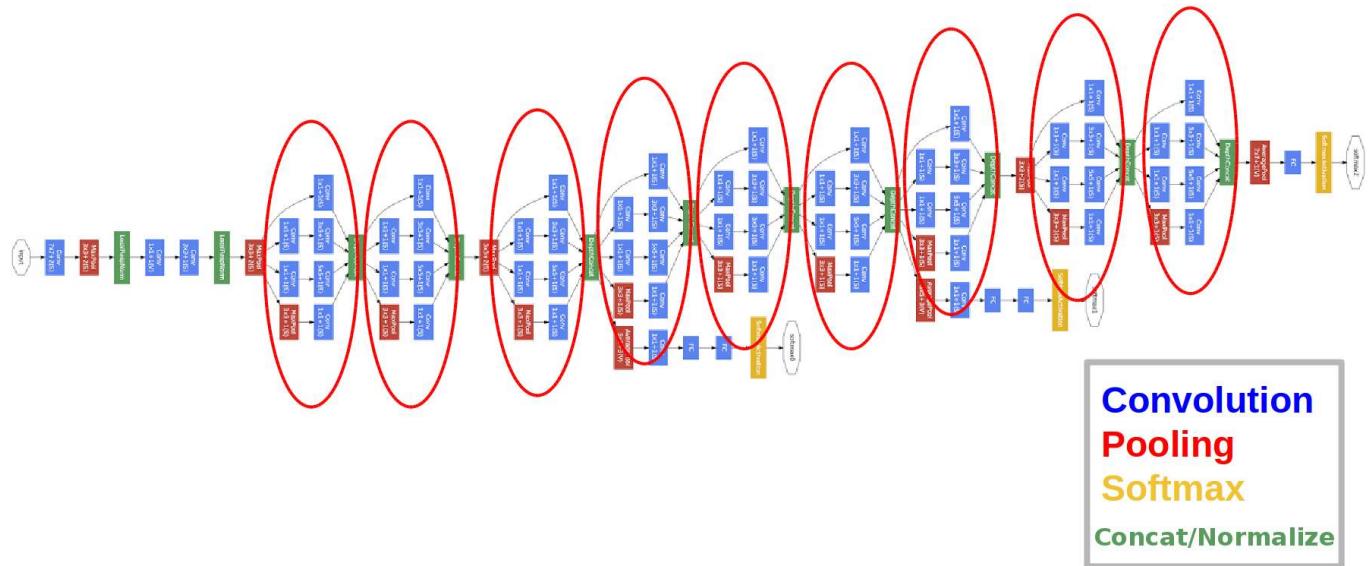
[https://www.researchgate.net/figure/A-visualization-of-the-VGG-architecture\\_fig2\\_318701491](https://www.researchgate.net/figure/A-visualization-of-the-VGG-architecture_fig2_318701491)  
([https://www.researchgate.net/figure/A-visualization-of-the-VGG-architecture\\_fig2\\_318701491](https://www.researchgate.net/figure/A-visualization-of-the-VGG-architecture_fig2_318701491))



VGGは非常にシンプル。3x3フィルタの畳み込み層を連続させ、プーリング層でサイズを半分にする。最後に全結合層を経由して出力。

## GoogLeNet

<https://leonardoaraujosantos.gitbooks.io/artificial-intelligence/content/googlenet.html>  
(<https://leonardoaraujosantos.gitbooks.io/artificial-intelligence/content/googlenet.html>)

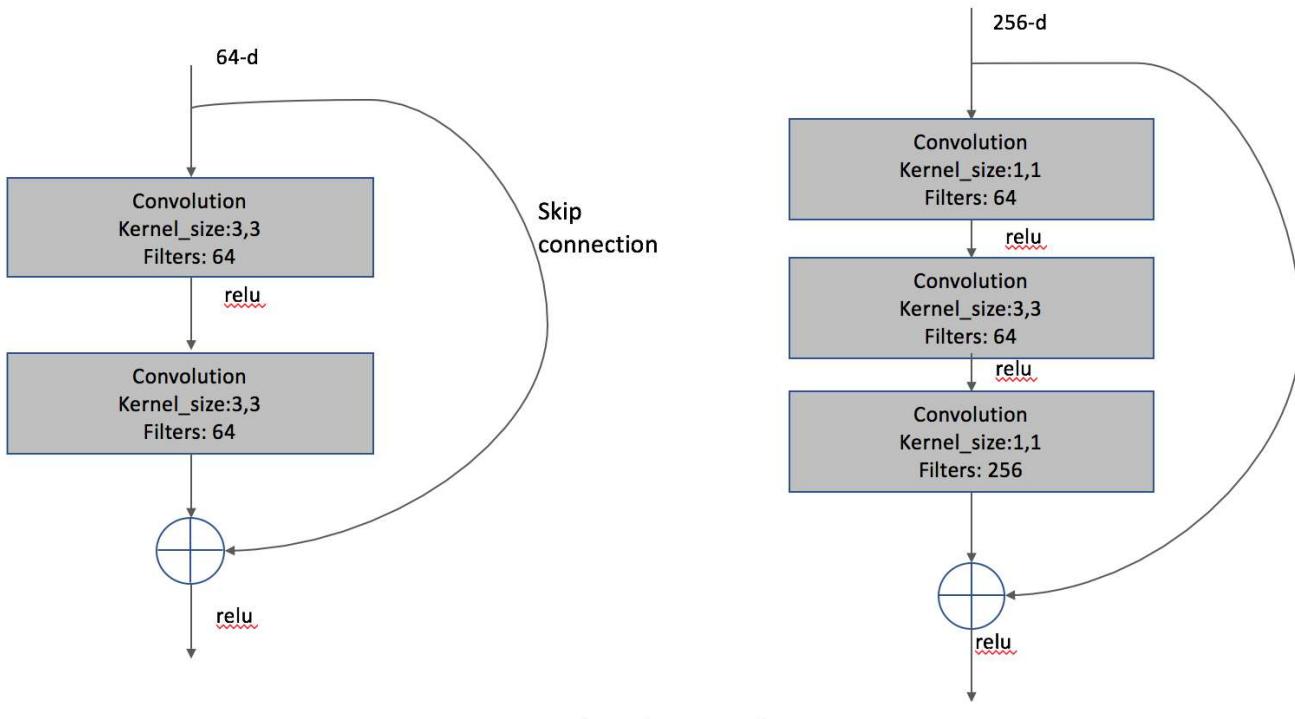


インセプション構造を1x1のフィルタによる畳み込み層で挟むことでパラメータの削減・処理の高速化をしている

## ResNet

層を深くしすぎると勾配減衰が発生し、最終的な性能が劣るという問題をクリアするために、「スキップ構造」を使っている。スキップ構造であつても伝搬時も逆伝搬時も入力データをそのまま流すので、勾配の変化がゆるやかになる。

<https://www.safaribooksonline.com/library/view/practical-computer-vision/9781788297684/12a933e6-e3c6-47d5-9064-512c8a0b4667.xhtml> (<https://www.safaribooksonline.com/library/view/practical-computer-vision/9781788297684/12a933e6-e3c6-47d5-9064-512c8a0b4667.xhtml>).

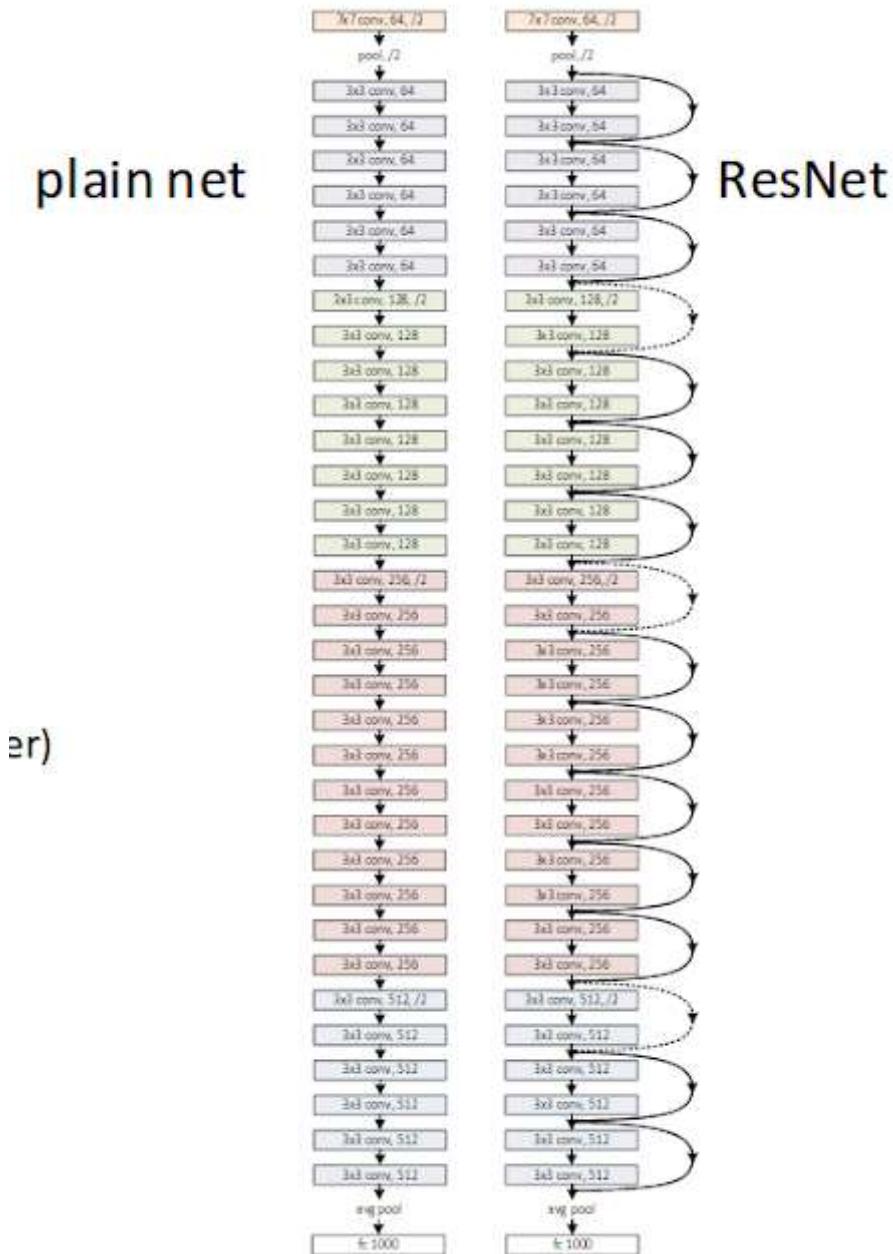


ResNet Block Designs

ResNetはVGGにスキップ構造を足したもの。

<http://alimurreza.blogspot.com/2017/04/deep-residual-network-resnet.html>

(<http://alimurreza.blogspot.com/2017/04/deep-residual-network-resnet.html>)



## **転移学習**

VGGなど既存のネットワーク構成をそのまま引き継ぐことで学習済みの重みを初期値として新しいデータセットを対象に再学習を行うことを「転移学習」と呼ぶ。手元にあるデータがスクアに場合において転移学習は有効な手法である。

## **ディープラーニングの高速化**

ディープラーニングフレームワークの多くはGPU処理をサポートしているが、最近では複数のGPUや複数の筐体での分散学習にも対応してきている。

### **取り組むべき課題**

<https://www2.eecs.berkeley.edu/Pubs/TechRpts/2014/EECS-2014-93.pdf>

(<https://www2.eecs.berkeley.edu/Pubs/TechRpts/2014/EECS-2014-93.pdf>)

畳み込み層の処理が最も計算容量が大きい為、学習時・推論時の両方の観点でいかに畳み込み層の計算量を減らすかがカギとなる。ここで言う畳み込み層の処理とは、元をたどれば大量の積和演算であり、最終的には積和演算をいかに拘束に効率的に処理するかということに行き着く。

### **GPUによる高速化**

NVIDIAが提供するCUDA開発環境を使ってGPUコンピューティングができる。特にim2colのように大きな塊を一気に計算できる形式に変換できる関数と相性が良い。

### **分散学習による高速化**

TensorFlowのような分散学習の機能が入ったライブラリを使用すること

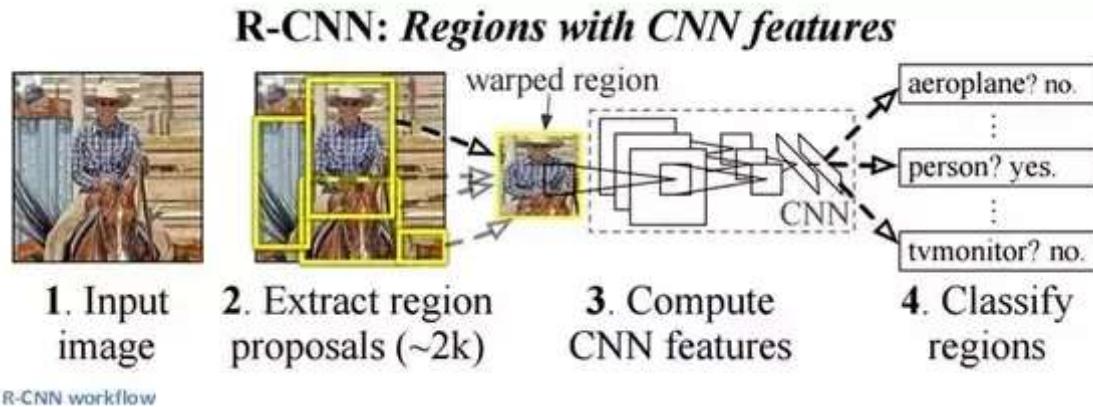
### **演算精度のビット削減**

演算精度のビットを削減しても、そこまで演算結果に影響が無いことが分かっている。一般的に16ビットの半精度浮動小数点数でディープラーニングを行うことができる事が分かっている。

## **ディープラーニングの実用例**

### **物体検出**

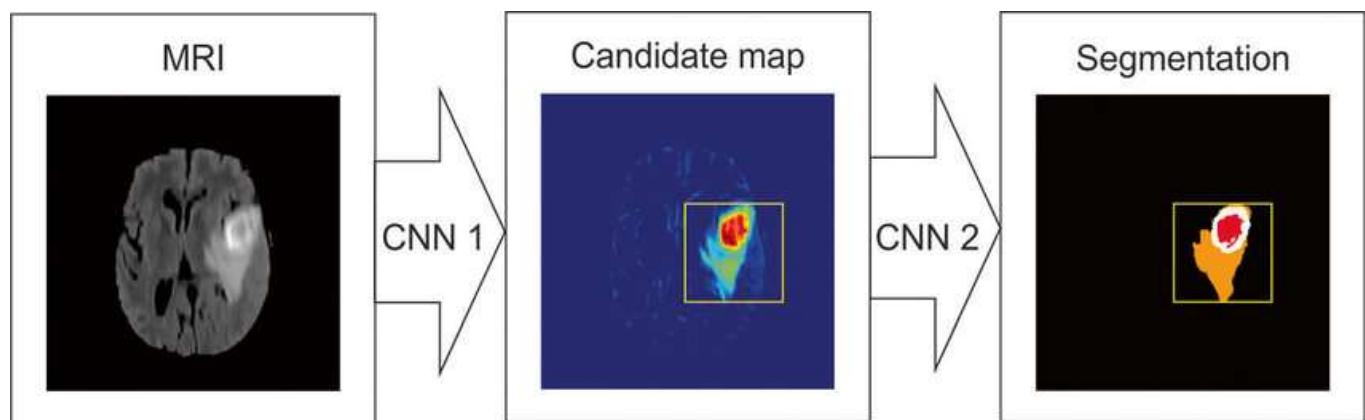
<https://www.quora.com/Where-can-I-find-a-nice-tutorial-for-Regional-based-Convolution-neural-Network>  
(<https://www.quora.com/Where-can-I-find-a-nice-tutorial-for-Regional-based-Convolution-neural-Network>)



物体検出では2.で物体らしき領域を抜き出し、3.で物体の内訳を処理するというフローとなる。  
2.についてはR-CNNではSelective Searchと呼ばれる手法で実装されているが、最近ではこれもCNNで行う手法が提案されている。

## セグメンテーション

[https://www.researchgate.net/figure/Schematic-illustration-of-a-cascaded-CNN-architecture-for-brain-tumor-segmentation-task\\_fig2\\_317341396](https://www.researchgate.net/figure/Schematic-illustration-of-a-cascaded-CNN-architecture-for-brain-tumor-segmentation-task_fig2_317341396) ([https://www.researchgate.net/figure/Schematic-illustration-of-a-cascaded-CNN-architecture-for-brain-tumor-segmentation-task\\_fig2\\_317341396](https://www.researchgate.net/figure/Schematic-illustration-of-a-cascaded-CNN-architecture-for-brain-tumor-segmentation-task_fig2_317341396))



画像のあるエリアを矩形抽出し、推論処理をすると縦x横のピクセル分も計算が必要なため、無駄である。  
そこで、計算する前に一度畳み込みによりエッジ抽出をし、全結合層でもCNNを使い逆畳み込みを実施しデータを抽象化する手法。

## 画像キャプション生成



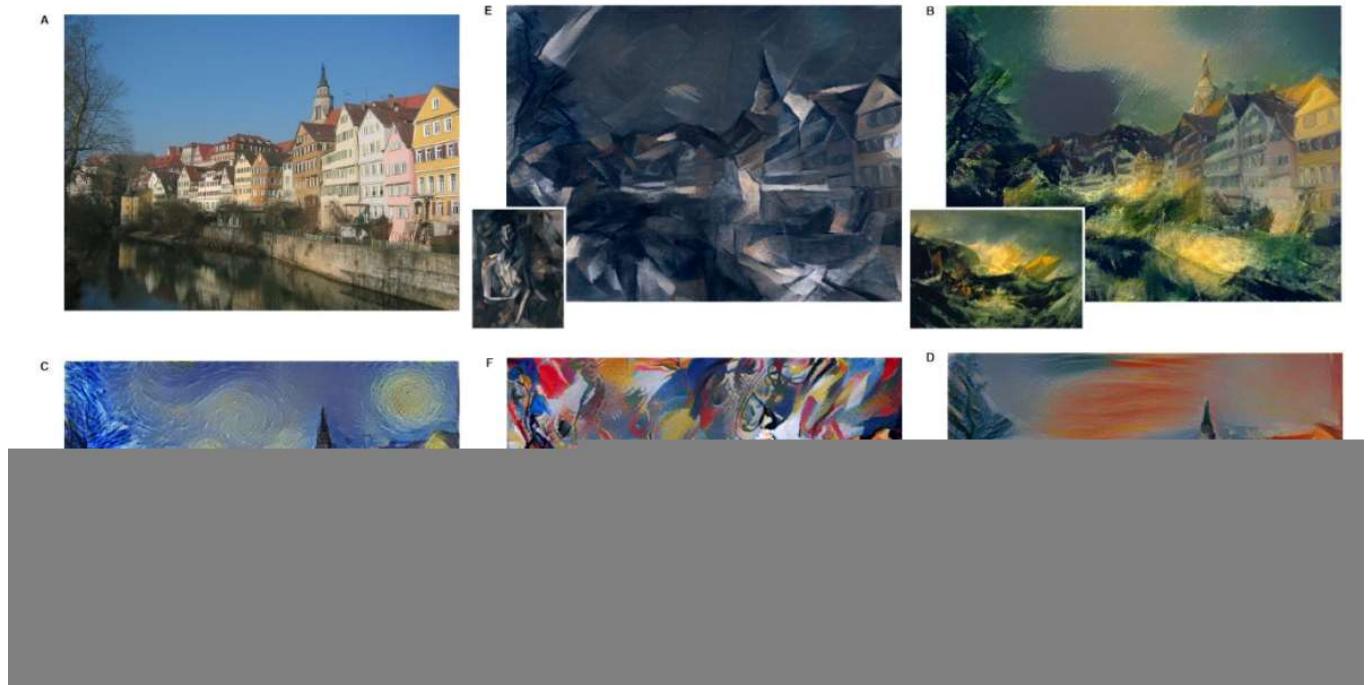
Figure 5. A selection of evaluation results, grouped by human rating.

CNNと自然言語処理を合わせたもの

## ディープラーニングの未来

### 画像スタイル変換

<https://japanese.engadget.com/2015/08/31/dnn/> (<https://japanese.engadget.com/2015/08/31/dnn/>)



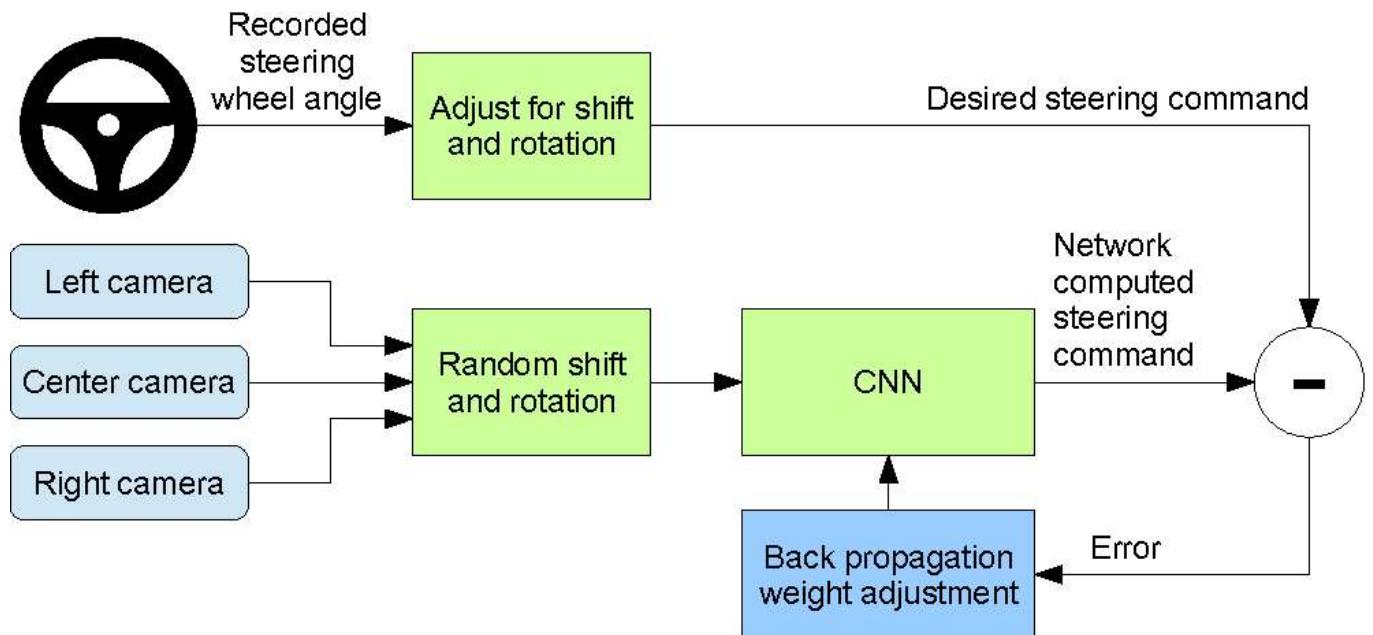
## 画像生成

<https://qiita.com/sergeant-wizard/items/0a57485bc90a35efcf26> (<https://qiita.com/sergeant-wizard/items/0a57485bc90a35efcf26>)



自動運転

<https://www.semanticscholar.org/paper/End-to-End-Learning-for-Self-Driving-Cars-Bojarski-Testa/0e3cc46583217ec81e87045a4f9ae3478a008227> (<https://www.semanticscholar.org/paper/End-to-End-Learning-for-Self-Driving-Cars-Bojarski-Testa/0e3cc46583217ec81e87045a4f9ae3478a008227>)



## Deep Q-Network (強化学習)

[https://www.toshiba-sol.co.jp/tech/sat/case/1804\\_1.htm](https://www.toshiba-sol.co.jp/tech/sat/case/1804_1.htm) ([https://www.toshiba-sol.co.jp/tech/sat/case/1804\\_1.htm](https://www.toshiba-sol.co.jp/tech/sat/case/1804_1.htm))

AlphaGoなど