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CSC400-802 Loop

Assignment HW#5-1

Section 6.1

1d. Neither  $A \subseteq B$ , nor  $B \subseteq A$ .

3c. Yes. Let  $z \in T$ , there exists an integer  $k$  that  $z = 6k$ . By algebra,  $z = 6k = 3 \cdot (2k)$ . Hence  $z$  can also be divisible by 3. Therefore,  $z \in S$ . Every element in  $T$  is also in  $S$ . Therefore,  $T \subseteq S$ .

4a. No. For example,  $5 \in A$  but  $5 \notin B$ . In set  $B$ ,  $s$  should be some integers.

b. Yes. Let  $m \in B$ , there exists an integer  $s$  that  $m = 20s$ . By algebra,  $m = 5 \cdot (4s)$ . Hence  $m \in A$ . Every element of  $B$  is also an element of  $A$ . Therefore,  $B \subseteq A$ .  
Let  $r = 4s$ , then  $m = 5r$ .

10f.  $B - A = \{6\}$

g.  $B \cup C = \{2, 3, 4, 6, 8, 9\}$

h.  $B \cap C = \{6\}$

16b.  $A \cap (B \cup C) = \{b, c\}$

$(A \cap B) \cup C = \{b, c, e\}$

$(A \cap B) \cup (A \cap C) = \{b, c\}$

$\therefore A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

35c.  ~~$A \times (B \cap C) = \{(a, 2), (b, 2)\}$~~   $A \times (B \cap C) = \{(a, 2), (b, 2)\}$

d.  $(A \times B) \cap (A \times C) = \{(a, 2), (b, 2)\}$

