

## 3D Transformation

### 3D Translation



$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & T_x \\ 0 & 1 & 0 & T_y \\ 0 & 0 & 1 & T_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

3D Translation Matrix

Given a 3D object with coordinate points A(0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0). Apply the translation with the distance 1 towards X axis, 1 towards Y axis and 2 towards Z axis and obtain the new coordinates of the object.

- Given-
- Old coordinates of the object = A (0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0)
- Translation vector =  $(T_x, T_y, T_z) = (1, 1, 2)$
- For Coordinates A(0, 3, 1)**
- Let the new coordinates of A =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the translation equations, we have-
  - $X_{new} = X_{old} + T_x = 0 + 1 = 1$
  - $Y_{new} = Y_{old} + T_y = 3 + 1 = 4$
  - $Z_{new} = Z_{old} + T_z = 1 + 2 = 3$
- Thus, New coordinates of A = (1, 4, 3).

Given a 3D object with coordinate points A(0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0). Apply the translation with the distance 1 towards X axis, 1 towards Y axis and 2 towards Z axis and obtain the new coordinates of the object.

- For Coordinates B(3, 3, 2)**
- Let the new coordinates of B =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the translation equations, we have-
  - $X_{new} = X_{old} + T_x = 3 + 1 = 4$
  - $Y_{new} = Y_{old} + T_y = 3 + 1 = 4$
  - $Z_{new} = Z_{old} + T_z = 2 + 2 = 4$
- Thus, New coordinates of B = (4, 4, 4).

Given a 3D object with coordinate points A(0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0). Apply the translation with the distance 1 towards X axis, 1 towards Y axis and 2 towards Z axis and obtain the new coordinates of the object.

- For Coordinates C(3, 0, 0)**
- Let the new coordinates of C =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the translation equations, we have-
  - $X_{new} = X_{old} + T_x = 3 + 1 = 4$
  - $Y_{new} = Y_{old} + T_y = 0 + 1 = 1$
  - $Z_{new} = Z_{old} + T_z = 0 + 2 = 2$
- Thus, New coordinates of C = (4, 1, 2).

Given a 3D object with coordinate points A(0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0). Apply the translation with the distance 1 towards X axis, 1 towards Y axis and 2 towards Z axis and obtain the new coordinates of the object.

- For Coordinates D(0, 0, 0)**
- Let the new coordinates of D =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the translation equations, we have-
  - $X_{new} = X_{old} + T_x = 0 + 1 = 1$
  - $Y_{new} = Y_{old} + T_y = 0 + 1 = 1$
  - $Z_{new} = Z_{old} + T_z = 0 + 2 = 2$
- Thus, New coordinates of D = (1, 1, 2).

Thus, New coordinates of the object = A (1, 4, 3), B(4, 4, 4), C(4, 1, 2), D(1, 1, 2).

### 3D Rotation

For X-Axis Rotation-

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta & 0 \\ 0 & \sin\theta & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

3D Rotation Matrix  
(For X-Axis Rotation)

### 3D Rotation

For Y-Axis Rotation-

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & 0 & \sin\theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

3D Rotation Matrix  
(For Y-Axis Rotation)

### 3D Rotation

For Z-Axis Rotation-

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 & 0 \\ \sin\theta & \cos\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

3D Rotation Matrix  
(For Z-Axis Rotation)

Given a homogeneous point (1, 2, 3). Apply rotation 90 degree towards X, Y and Z axis and find out the new coordinate points.

- Given-
- Old coordinates =  $(X_{\text{old}}, Y_{\text{old}}, Z_{\text{old}}) = (1, 2, 3)$
- Rotation angle =  $\theta = 90^\circ$
- **For X-Axis Rotation-**
- Let the new coordinates after rotation =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .
- Applying the rotation equations, we have-
- $X_{\text{new}} = X_{\text{old}} = 1$
- $Y_{\text{new}} = Y_{\text{old}} \times \cos\theta - Z_{\text{old}} \times \sin\theta = 2 \times \cos 90^\circ - 3 \times \sin 90^\circ = 2 \times 0 - 3 \times 1 = -3$
- $Z_{\text{new}} = Y_{\text{old}} \times \sin\theta + Z_{\text{old}} \times \cos\theta = 2 \times \sin 90^\circ + 3 \times \cos 90^\circ = 2 \times 1 + 3 \times 0 = 2$
- Thus, New coordinates after rotation = (1, -3, 2).

Given a homogeneous point (1, 2, 3). Apply rotation 90 degree towards X, Y and Z axis and find out the new coordinate points.

- Given-
- Old coordinates =  $(X_{\text{old}}, Y_{\text{old}}, Z_{\text{old}}) = (1, 2, 3)$
- Rotation angle =  $\theta = 90^\circ$
- **For Y-Axis Rotation-**
- Let the new coordinates after rotation =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .
- Applying the rotation equations, we have-
- $X_{\text{new}} = Z_{\text{old}} \times \sin\theta + X_{\text{old}} \times \cos\theta = 3 \times \sin 90^\circ + 1 \times \cos 90^\circ = 3 \times 1 + 1 \times 0 = 3$
- $Y_{\text{new}} = Y_{\text{old}} = 2$
- $Z_{\text{new}} = Y_{\text{old}} \times \cos\theta - X_{\text{old}} \times \sin\theta = 2 \times \cos 90^\circ - 1 \times \sin 90^\circ = 2 \times 0 - 1 \times 1 = -1$
- Thus, New coordinates after rotation = (3, 2, -1).

Given a homogeneous point (1, 2, 3). Apply rotation 90 degree towards X, Y and Z axis and find out the new coordinate points.

- Given-
- Old coordinates =  $(X_{\text{old}}, Y_{\text{old}}, Z_{\text{old}}) = (1, 2, 3)$
- Rotation angle =  $\theta = 90^\circ$
- **For Z-Axis Rotation-**
- Let the new coordinates after rotation =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .
- Applying the rotation equations, we have-
- $X_{\text{new}} = X_{\text{old}} \times \cos\theta - Y_{\text{old}} \times \sin\theta = 1 \times \cos 90^\circ - 2 \times \sin 90^\circ = 1 \times 0 - 2 \times 1 = -2$
- $Y_{\text{new}} = X_{\text{old}} \times \sin\theta + Y_{\text{old}} \times \cos\theta = 1 \times \sin 90^\circ + 2 \times \cos 90^\circ = 1 \times 1 + 2 \times 0 = 1$
- $Z_{\text{new}} = Z_{\text{old}} = 3$
- Thus, New coordinates after rotation = (-2, 1, 3).

### 3D Scaling

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

**3D Scaling Matrix**

Given a 3D object with coordinate points A(0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0). Apply the scaling parameter 2 towards X axis, 3 towards Y axis and 3 towards Z axis and obtain the new coordinates of the object.

- Given-
- Old coordinates of the object = A (0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0)
- Scaling factor along X axis = 2
- Scaling factor along Y axis = 3
- Scaling factor along Z axis = 3
- **For Coordinates A(0, 3, 3)**
- Let the new coordinates of A after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the scaling equations, we have-
- $X_{new} = X_{old} \times S_x = 0 \times 2 = 0$
- $Y_{new} = Y_{old} \times S_y = 3 \times 3 = 9$
- $Z_{new} = Z_{old} \times S_z = 3 \times 3 = 9$
- Thus, New coordinates of corner A after scaling = (0, 9, 9).

Given a 3D object with coordinate points A(0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0). Apply the scaling parameter 2 towards X axis, 3 towards Y axis and 3 towards Z axis and obtain the new coordinates of the object.

- **For Coordinates B(3, 3, 6)**
- Let the new coordinates of B after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the scaling equations, we have-
- $X_{new} = X_{old} \times S_x = 3 \times 2 = 6$
- $Y_{new} = Y_{old} \times S_y = 3 \times 3 = 9$
- $Z_{new} = Z_{old} \times S_z = 6 \times 3 = 18$
- Thus, New coordinates of corner B after scaling = (6, 9, 18).

Given a 3D object with coordinate points A(0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0). Apply the scaling parameter 2 towards X axis, 3 towards Y axis and 3 towards Z axis and obtain the new coordinates of the object.

- **For Coordinates C(3, 0, 1)**
- Let the new coordinates of C after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the scaling equations, we have-
- $X_{new} = X_{old} \times S_x = 3 \times 2 = 6$
- $Y_{new} = Y_{old} \times S_y = 0 \times 3 = 0$
- $Z_{new} = Z_{old} \times S_z = 1 \times 3 = 3$
- Thus, New coordinates of corner C after scaling = (6, 0, 3).

Given a 3D object with coordinate points A(0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0). Apply the scaling parameter 2 towards X axis, 3 towards Y axis and 3 towards Z axis and obtain the new coordinates of the object.

- **For Coordinates D(0, 0, 0)**
- Let the new coordinates of D after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the scaling equations, we have-
- $X_{new} = X_{old} \times S_x = 0 \times 2 = 0$
- $Y_{new} = Y_{old} \times S_y = 0 \times 3 = 0$
- $Z_{new} = Z_{old} \times S_z = 0 \times 3 = 0$
- Thus, New coordinates of corner D after scaling = (0, 0, 0).
- A (0, 9, 9), B (6, 9, 18), C(6, 0, 3), D(0, 0, 0).

### 3D Shearing

**Shearing in X Axis-**

$$\begin{aligned} X_{new} &= X_{old} \\ Y_{new} &= Y_{old} + Sh_y \times X_{old} \\ Z_{new} &= Z_{old} + Sh_z \times X_{old} \end{aligned}$$

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ Sh_y & 1 & 0 & 0 \\ Sh_z & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

**3D Shearing Matrix (in X axis)**

### 3D Shearing

#### Shearing in Y Axis:-

$$\begin{aligned} X_{\text{new}} &= X_{\text{old}} + Sh_y \times Y_{\text{old}} \\ Y_{\text{new}} &= Y_{\text{old}} \\ Z_{\text{new}} &= Z_{\text{old}} + Sh_z \times Y_{\text{old}} \end{aligned}$$

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & Sh_y & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

3D Shearing Matrix  
(in Y axis)

### 3D Shearing

#### Shearing in Z Axis:-

$$\begin{aligned} X_{\text{new}} &= X_{\text{old}} + Sh_x \times Z_{\text{old}} \\ Y_{\text{new}} &= Y_{\text{old}} + Sh_y \times Z_{\text{old}} \\ Z_{\text{new}} &= Z_{\text{old}} \end{aligned}$$

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & Sh_x & 0 \\ 0 & 1 & Sh_y & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

3D Shearing Matrix  
(in Z axis)

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

- Given-
  - Old corner coordinates of the triangle = A (0, 0, 0), B(1, 1, 2), C(1, 1, 3)
  - Shearing parameter towards X direction ( $Sh_x$ ) = 2
  - Shearing parameter towards Y direction ( $Sh_y$ ) = 2
  - Shearing parameter towards Z direction ( $Sh_z$ ) = 3
- Shearing in X Axis:-**
- For Coordinates A(0, 0, 0)**
  - Applying the shearing equations, we have-
    - $X_{\text{new}} = X_{\text{old}} = 0$
    - $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times X_{\text{old}} = 0 + 2 \times 0 = 0$
    - $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times X_{\text{old}} = 0 + 3 \times 0 = 0$
  - Thus, New coordinates of corner A after shearing = (0, 0, 0).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

- For Coordinates B(1, 1, 2)**
  - Let the new coordinates of corner B after shearing = ( $X_{\text{new}}$ ,  $Y_{\text{new}}$ ,  $Z_{\text{new}}$ ).
  - Applying the shearing equations, we have-
    - $X_{\text{new}} = X_{\text{old}} = 1$
    - $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times X_{\text{old}} = 1 + 2 \times 1 = 3$
    - $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times X_{\text{old}} = 2 + 3 \times 1 = 5$
  - Thus, New coordinates of corner B after shearing = (1, 3, 5).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

- For Coordinates C(1, 1, 3)**
  - Let the new coordinates of corner C after shearing = ( $X_{\text{new}}$ ,  $Y_{\text{new}}$ ,  $Z_{\text{new}}$ ).
  - Applying the shearing equations, we have-
    - $X_{\text{new}} = X_{\text{old}} = 1$
    - $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times X_{\text{old}} = 1 + 2 \times 1 = 3$
    - $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times X_{\text{old}} = 3 + 3 \times 1 = 6$
  - Thus, New coordinates of corner C after shearing = (1, 3, 6).
- Thus, New coordinates of the triangle after shearing in X axis = A (0, 0, 0), B(1, 3, 5), C(1, 3, 6).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

- Shearing in Y Axis:-**
- For Coordinates A(0, 0, 0)**
  - Let the new coordinates of corner A after shearing = ( $X_{\text{new}}$ ,  $Y_{\text{new}}$ ,  $Z_{\text{new}}$ ).
  - Applying the shearing equations, we have-
    - $X_{\text{new}} = X_{\text{old}} + Sh_x \times Y_{\text{old}} = 0 + 2 \times 0 = 0$
    - $Y_{\text{new}} = Y_{\text{old}} = 0$
    - $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times Y_{\text{old}} = 0 + 3 \times 0 = 0$
  - Thus, New coordinates of corner A after shearing = (0, 0, 0).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

• Shearing in Y Axis-

• For Coordinates B(1, 1, 2)

- Let the new coordinates of corner B after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the shearing equations, we have-
  - $X_{new} = X_{old} + Sh_x \times Y_{old} = 1 + 2 \times 1 = 3$
  - $Y_{new} = Y_{old} = 1$
  - $Z_{new} = Z_{old} + Sh_z \times Y_{old} = 2 + 3 \times 1 = 5$
- Thus, New coordinates of corner B after shearing = (3, 1, 5).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

• Shearing in Y Axis-

• For Coordinates C(1, 1, 3)

- Let the new coordinates of corner C after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the shearing equations, we have-
  - $X_{new} = X_{old} + Sh_x \times Y_{old} = 1 + 2 \times 1 = 3$
  - $Y_{new} = Y_{old} = 1$
  - $Z_{new} = Z_{old} + Sh_z \times Y_{old} = 3 + 3 \times 1 = 6$
- Thus, New coordinates of corner C after shearing = (3, 1, 6).
- Thus, New coordinates of the triangle after shearing in Y axis = A (0, 0, 0), B(3, 1, 5), C(3, 1, 6).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

• Shearing in Z Axis-

• For Coordinates A(0, 0, 0)

- Let the new coordinates of corner A after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the shearing equations, we have-
  - $X_{new} = X_{old} + Sh_x \times Z_{old} = 0 + 2 \times 0 = 0$
  - $Y_{new} = Y_{old} + Sh_y \times Z_{old} = 0 + 2 \times 0 = 0$
  - $Z_{new} = Z_{old} = 0$
- Thus, New coordinates of corner A after shearing = (0, 0, 0).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

• Shearing in Z Axis-

• For Coordinates B(1, 1, 2)

- Let the new coordinates of corner B after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the shearing equations, we have-
  - $X_{new} = X_{old} + Sh_x \times Z_{old} = 1 + 2 \times 2 = 5$
  - $Y_{new} = Y_{old} + Sh_y \times Z_{old} = 1 + 2 \times 2 = 5$
  - $Z_{new} = Z_{old} = 2$
- Thus, New coordinates of corner B after shearing = (5, 5, 2).

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

• Shearing in Z Axis-

• For Coordinates C(1, 1, 3)

- Let the new coordinates of corner C after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the shearing equations, we have-
  - $X_{new} = X_{old} + Sh_x \times Z_{old} = 1 + 2 \times 3 = 7$
  - $Y_{new} = Y_{old} + Sh_y \times Z_{old} = 1 + 2 \times 3 = 7$
  - $Z_{new} = Z_{old} = 3$
- Thus, New coordinates of corner C after shearing = (7, 7, 3).
- Thus, New coordinates of the triangle after shearing in Z axis = A (0, 0, 0), B(5, 5, 2), C(7, 7, 3).

## 3D Reflection

Reflection Relative to XY Plane:

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

3D Reflection Matrix  
(Reflection Relative to XY plane)

### 3D Reflection

Reflection Relative to YZ Plane:

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

**3D Reflection Matrix**  
(Reflection Relative to YZ plane)

### 3D Reflection

Reflection Relative to XZ Plane

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

**3D Reflection Matrix**  
(Reflection Relative to XZ plane)

Given a 3D triangle with coordinate points A(3, 4, 1), B(6, 4, 2), C(5, 6, 3). Apply the reflection on the XY plane and find out the new coordinates of the object.

- Given-
- Old corner coordinates of the triangle = A (3, 4, 1), B(6, 4, 2), C(5, 6, 3)
- Reflection has to be taken on the XY plane
- **For Coordinates A(3, 4, 1)**
- Let the new coordinates of corner A after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the reflection equations, we have-
- $X_{new} = X_{old} = 3$
- $Y_{new} = Y_{old} = 4$
- $Z_{new} = -Z_{old} = -1$
- Thus, New coordinates of corner A after reflection = (3, 4, -1).

Given a 3D triangle with coordinate points A(3, 4, 1), B(6, 4, 2), C(5, 6, 3). Apply the reflection on the XY plane and find out the new coordinates of the object.

- **For Coordinates B(6, 4, 2)**
- Let the new coordinates of corner B after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the reflection equations, we have-
- $X_{new} = X_{old} = 6$
- $Y_{new} = Y_{old} = 4$
- $Z_{new} = -Z_{old} = -2$
- Thus, New coordinates of corner B after reflection = (6, 4, -2).
- 

Given a 3D triangle with coordinate points A(3, 4, 1), B(6, 4, 2), C(5, 6, 3). Apply the reflection on the XY plane and find out the new coordinates of the object.

- **For Coordinates C(5, 6, 3)**
- Let the new coordinates of corner C after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .
- Applying the reflection equations, we have-
- $X_{new} = X_{old} = 5$
- $Y_{new} = Y_{old} = 6$
- $Z_{new} = -Z_{old} = -3$
- Thus, New coordinates of corner C after reflection = (5, 6, -3).
- Thus, New coordinates of the triangle after reflection = A (3, 4, -1), B(6, 4, -2), C(5, 6, -3).

Given a 3D triangle with coordinate points A(3, 4, 1), B(6, 4, 2), C(5, 6, 3). Apply the reflection on the XZ plane and find out the new coordinates of the object.