

Fourier Transform

$$F\{f(x)\} = \int_{-\infty}^{\infty} f(x) e^{isx} dx$$

or

$$F\{f(x)\} = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{isx} f(x) dx$$

or

$$F\{f(x)\} = \int_{-\infty}^{\infty} f(x) e^{-isx} dx$$

or

$$F\{f(x)\} = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(x) e^{-isx} dx$$

Fourier Sine Transform

$$F_s\{f(x)\} = \int_0^{\infty} f(x) \sin sx \, dx = F_s(s)$$

or

$$F_s\{f(x)\} = \sqrt{\frac{2}{\pi}} \int_0^{\infty} f(x) \sin sx \, dx = F_s(s)$$

Fourier Cosine Transform

$$F_c\{f(x)\} = \int_0^{\infty} f(x) \cos sx \, dx = F_c(s)$$

or

$$F_c\{f(x)\} = \sqrt{\frac{2}{\pi}} \int_0^{\infty} f(x) \cos sx \, dx = F_c(s)$$

* Remember the difference of $-s \rightarrow s$ $\xleftrightarrow{-t \rightarrow t}$ in inverse & further topics.