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#### LAB 1: Programme to compact gravity

#### 1.1 Objectives:

Use python

- 1. to evaluate double integration.
- 2. to compute area and volume.
- 3. to calculate center of gravity of 2D object.

Syntax for the commands used:

- Data pretty printer in Python: pprint ()
- integrate: integrate (function, (variable, min\_limit, max\_limit))

## 1.2 Double and triple integration

#### Example 1:

Evaluate the integral  $\int_0^1 \int_0^x (x^2 + y^2) dy dx$ 

```
from sympy import *
x ,y , z= symbols ('x y z')
w1= integrate ( x ** 2+y ** 2 ,( y ,0 , x ) ,(x ,0 ,1 ) )
print ( w1 )
```

#### Example 2:

Evaluate the integral  $\int_0^3 \int_0^{3-z} \int_0^{3-z-y} (xyz) dxdydz$ 

```
from sympy import *

x= Symbol ('x')

y= Symbol ('y')

z= Symbol ('z')

w2= integrate (( x*y*z ) ,(z ,0 , 3-x-y ) ,(y ,0 , 3-x ) ,(x ,0 , 3 ))

print ( w2 )
```

Example 3:

```
Prove that \int \int (x^2 + y^2) dy dx = \int \int (x^2 + y^2) dx dy
       from sympy import *
       x = Symbol ('x')
       y= Symbol ('y')
       z= Symbol ('z')
       w3 = integrate (x ** 2+y ** 2, y, x)
       pprint (w3)
       w4= integrate ( x ** 2+y ** 2, x, y )
       pprint (w4)
```

#### Area and Volume 1.3

Area of the region R in the cartesian form is  $\iint_R dxdy$ 

Example 4:

Find the area of an ellipse by double integration.  $A = 4 \int_0^a \int_0^{\frac{b}{a}\sqrt{a^2-x^2}} dy dx$ .

```
from sympy import *
x = Symbol ('x')
y= Symbol ('y')
#a= Symbol ('a')
#b= Symbol ('b')
a=4
b=6
w3=4* integrate (1, (y, 0, (b/a)* sqrt (a ** 2-x ** 2)),(x, 0, a))
print (w3)
```

## Area of the region R in the polar form is $\iint_R r dr d\theta$

Example 5:

Find the area of the cardioid  $r = a(1 + \cos\theta)$  by double integration

from sympy import \*

```
r= Symbol ('r')
t= Symbol ('t')
a= Symbol ('a')
#a=4
w3=2* integrate (r,(r,0,a*(1+cos(t))),(t,0,pi))
pprint (w3)
```

## Volume of a solid is given by $\iiint_{v} dxdydz$

Find the volume of the tetrahedron bounded by the planes x=0, y=0 and

$$z=0, \frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$$

```
from sympy import *
x = Symbol ('x')
y= Symbol ('y')
z= Symbol ('z')
a= Symbol ('a')
b= Symbol ('b')
c= Symbol ('c')
w2= integrate (1,(z,0,c*(1-x/a-y/b)),(y,0,b*(1-x/a)),(x,0,a))
print (w2)
```

#### Center of Gravity 1.6

#### Example 7:

Find the center of gravity of cardioid . Plot the graph of cardioid and mark the center of gravity.

import numpy as np import matplotlib . pyplot as plt import math from sympy import \* r= Symbol ('r') t= Symbol ('t') a= Symbol ('a')

```
II= integrate (cos (t)*r ** 2, (r,0, a*(1+cos (t))), (t,-pi,pi))

I2= integrate (r, (r,0, a*(1+cos (t))), (t,-pi,pi))

I=I1/I2

print (I)

I=I. subs (a,5)

plt. axes (projection = 'polar')

a=5

rad = np. arange (0, (2*np.pi), 0.01)

# plotting the cardioid

for i in rad:

r = a + (a*np.cos(i))

plt. polar (i,r,'g.')

plt. show ()
```

## LAB 2: Evaluation of improper integrals, Beta and Gamma functions

#### 2.1 Objectives:

Use python

- 1. to evaluate improper integrals using Beta function.
- 2. to evaluate improper integrals using Gamma function.

#### Syntax for the commands used:

```
    gamma
        math . gamma ( x )
        Parameters :
        x : The number whose gamma value needs to be computed.
    beta
        math . beta (x , y )
        Parameters :
        x ,y: The numbers whose beta value needs to be computed.
```

#### Example 1:

Evaluate  $\int_0^\infty e^{-x} dx$ 

```
from sympy import *

x= symbols ('x')

wl = integrate (exp (-x),(x,0, float ('inf')))

print (simplify (wl))
```

#### Gamma function:

Gamma function is  $\Gamma(n) = \int_0^\infty e^{-x} x^{n-1} dx$ 

#### Example 2:

Evaluate  $\Gamma(5)$  by using definition

```
from sympy import *

x= symbols ('x')

w1= integrate (exp (-x )*x ** 4 ,( x ,0 , float ('inf') ))

print ( simplify ( w1 ) )
```

#### Example 3:

Find Beta(3,5), Gamma(5)

```
# beta and gamma functions
from sympy import beta, gamma
m= input ('m :');
n= input ('n :');
m= float ( m ); n
= float ( n );
s= beta (m, n );
t= gamma ( n )
print ('gamma (',n,') is %3.3f '%t )
print ('Beta (',m,n,') is %3.3f '%s )
```

#### Example 5:

Calculate Beta(5/2,7/2) and Gamma(5/2).

```
# beta and gamma functions
# If the number is a fraction give it in decimals . Eg 5/2=2.5
from sympy import beta, gamma
m= float (input ('m:'));
n=float (input ('n:'));
 s = beta(m, n);
 t= gamma (n)
 print ('gamma (',n,') is %3.3f '%t)
 print ('Beta (',m ,n ,') is %3.3f'%s)
```

Verify that Beta(m, n) = Gamma(m)Gamma(n)/Gamma(m + n) for m=5 and n=7

```
from sympy import beta, gamma
m=5;
n=7:
m=float(m);
n=float(n);
s = beta(m, n);
t=(gamma (m)*gamma (n))/gamma (m+n);
 print (s,t)
 if (abs (s-t)<=0.00001):
        print ('beta and gamma are related ')
 else:
        print ('given values are wrong ')
```

#### LAB 3: Finding gradient, divergent, curl and their geometrical interpretation and Verification of Green's theorem.

#### 3.1 Objectives:

Use python

1. to find the gradient of a given scalar function.

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- 2. to find find divergence and curl of a vector function.
- 3. to evaluate integrals using Green's theorem.

#### 1. To find gradient of $\emptyset = x^2y + 2xz - 4$ .

```
#To find gradient of scalar point function.
from sympy.vector import *
from sympy import symbols
                                               # Setting the coordinate system
N= CoordSys3D ('N')
x,y,z =  symbols ('x y z')
                                        # Variables x, y, z to be used with coordinate
A=N.x **2*N.y+2*N.x*N.z-4
system N
                                              #Del operator
delop = Del()
                                               #Del operator applied to A
display(delop (A))
                                              # Gradient function is used
gradA = gradient(A)
print (f"\n Gradient of {A} is \n")
display(gradA)
```

#### 2. To find divergence of $\vec{F} = x^2yz \hat{i} + y^2zx \hat{j} + z^2xy \hat{k}$ .

#To find divergence of a vector point function
from sympy.vector import \*
from sympy import symbols

N= CoordSys3D ('N')

x ,y , z= symbols ('x y z')

A=N . x \*\* 2\*N . y\*N . z\*N . i+N .y \*\* 2\*N . z\*N . x\*N . j+N .z \*\* 2\*N . x\*N . y\*N . k
delop = Del ()
divA = delop.dot (A)
display(divA)
print( f"\n Divergence of {A} is \n")
display(divergence(A))

#### 3. To find curl of $\vec{F} = x^2yz \hat{\imath} + y^2zx \hat{\jmath} + z^2xy \hat{k}$ .

#To find curl of a vector point function

```
from sympy . vector import * from sympy import symbols N= CoordSys3D \ ('N') \\ x \ ,y \ ,z= symbols \ ('x \ y \ z') \\ A=N \ .x \ *** \ 2*N \ .y \ *N \ .z \ *N \ .i \ +N \ .y \ *** \ 2*N \ .z \ *N \ .x \ *N \ .j \ +N \ .z \ *** \ 2*N \ .x \ *N \ .y \ *N \ .k \\ delop = Del \ () \\ curl A = delop.cross(A) \\ display(curl A) \\ print(f''\ n \ Curl \ of \ \{A\} \ is \ 'n'') \\ display(curl(A))
```

#### LAB 4: Verification of Green's theorem

#### 1.1 Objectives:

Use python

1. to evaluate integrals using Green's theorem.

#### 1.2 Green's theorem

#### Statement of Green's theorem in the plane:

If P(x, y) and Q(x, y) be two continuous functions having continuous partial derivatives in a region R of the xy-plane, bounded by a simple closed curve C, then

$$\oint (Pdx + Qdy) = \iint_R \left( \frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dx dy.$$

1. Using Green's theorem, evaluate  $\oint [(x+2y)dx + (x-2y)dy]$ , where c is the region bounded by coordinate axes and the line x = 1 and y = 1.

2. Using Green's theorem, evaluate  $\oint [(xy + y^2)dx + x^2dy]$ , where c is the closed curve bounded by y = x and  $y = x^2$ .

```
from sympy import *
var ('x,y')
p=x*y+y**2
q=x ** 2
f = diff(q,x) - diff(p,y)
soln = integrate (f,[y,x ** 2,x],[x,0,1])
print ("I=",soln)
```

#### LAB 5: Solution of Lagrange's linear partial differential equations

#### 1.1 Objectives:

Use python

1. to solve linear Partial Differential Equations of first order

```
1. Solve the PDE, xp + yq = z, where z = f(x, y)
   from sympy . solvers .pde import pdsolve
   from sympy import Function, Eq,cot, classify_pde, pprint
   from sympy .abc import x, y, a
   f = Function ('f')
  z = f(x, y)
  zx = z. diff (x)
  zy = z. diff (y)
  # Solve xp+yq=z
   eq = Eq(x*zx+y*zy, z)
   pprint (eq)
   print ("\n")
  soln = pdsolve(eq,z)
   pprint (soln)
```

2. Solve the PDE 2p + 3q = 1, where  $p = \frac{\partial z}{\partial x}$  and  $q = \frac{\partial z}{\partial y}$ 

from sympy . solvers .pde import pdsolve

from sympy import Function , Eq ,cot , classify\_pde , pprint

from sympy .abc import x, y, a

f = Function ('f')

z = f(x, y)

zx = z. diff (x)

zy = z. diff (y)

# Solve 2p+3q=1

eq = Eq(2\*zx+3\*zy , 1)

pprint (eq)

print ("\n")

soln = pdsolve (eq ,z)

pprint ( soln )

3. Solve the PDE  $x^2p + y^2q = (x + y)z$ , where  $p = \frac{\partial z}{\partial x}$  and  $q = \frac{\partial z}{\partial y}$  from sympy . solvers .pde import pdsolve

from sympy import Function, Eq,cot, classify\_pde, pprint from sympy .abc import x, y, a

f = Function ('f')

z = f(x, y)

zx = z. diff (x)

zy = z. diff (y)

# Solve  $x^2p+y^2q=(x+y)z$ 

eq=Eq(x \*\* 2\*zx+y \*\* 2\*zy,(x+y)\*z)

pprint (eq)

print ("\n")

soln = pdsolve(eq,z)

pprint (soln)

LAB 6: Solution of algebraic and transcendental equation by

Regula-Falsi and Newton-Raphson method

#### 6.1 Objectives:

Use python

- 1. to solve algebraic and transcendental equation by Regula-Falsi method.
- 2. to solve algebraic and transcendental equation by Newton-Raphson method.

#### 6.2 Regula-Falsi method to solve a transcendental equation.

1. Obtain a root of the equation  $x^3 - 2x - 5 = 0$  between 2 and 3 by regula-falsi method. Perform 5 iterations.

```
# Regula Falsi method
from sympy import *
x = Symbol ('x')
g = input ('Enter the function')
                                        #%x^3-2*x-5; % function
f = lambdify(x, g)
a= float (input ('Enter a value:'))
                                                       #2
b= float (input ('Enter b value:'))
                                                       #3
N=int (input ('Enter number of iterations:'))
                                                               #5
for i in range (1, N+1):
  c = (a*f(b)-b*f(a)) / (f(b)-f(a))
  if ((f(a)*f(c))<0):
         b=c
  else:
 print ('iteration %d \t the root %0.3f\t function value %0.3f\n'% (i, c, f(c)));
```

Using tolerance value, we can write the same program as follows:

1. Obtain a root of the equation  $x^3 - 2x - 5 = 0$  between 2 and 3 by regula-falsi method. Correct to 3 decimal places.

# Regula Falsi method

from sympy import \*

```
x = Symbol ('x')
                                                            #%x^3-2*x-5; % function
    g = input ('Enter the function')
    f= lambdify (x, g)
   a= float (input ('Enter a value:'))
                                                                    #2
   b= float (input ('Enter b value:'))
                                                                   #3
   N=float (input ('Enter tolerance:'))
                                                                           # 0.0001
  x=a:
  c=b:
  i=0
  while (abs(x-c)>=N):
    c = (a*f(b)-b*f(a)) / (f(b)-f(a))
    if ((f(a)*f(c))<0):
            b=c
    else:
           a=c
           i=i+1
    print ('iteration %d \t the root %0.3f\t function value \%0.3f\n'\% (i, c, f(c)));
print ('final value of the root is %0.5f' %c)
```

## 6.3 Newton-Raphson method to solve a transcendental equation.

1. Find a root of the equation  $3x = \cos x + 1$ , near 1, by Newton Raphson method. Perform 5 iterations.

```
from sympy import *
 x= Symbol ('x') g = input ('Enter the function ')
                                                        #%3x -cos(x)-1; % function
  f= lambdify (x, g)
dg = diff(g);
df= lambdify x, dg)
x0= float (input ('Enter the initial approximation '));
n= int (input ('Enter the number of iterations '));
                                                                        # x0=1
for i in range (1, n+1):
                                                                #n=5:
   x1 = (x0 - (f(x0)/df(x0)))
  print ('iteration %d \t the root %0.3f \t function value %0.3f \n'% (i, x1, f(x1)));
```

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