

Profitability of a Two-Product Biorefinery

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Conversion of biomass to energy products is not new

- By 1900, a fully operational biodiesel engine was on display at the World's Fair.
- During WW2, biodiesel served as a gap motor fuel and even as engine fuel for combat airplanes and tanks.
- Distilled alcohol as ethanol was developed in the 12th century.
- Some biofuels such as corn, soybeans, and sugarcane do support substantial scale economies for ethanol or Dimethyl ether (not but at scales of fossil fuels).
- Can cotton support biopower sustainably and profitably?

Why cotton?

- Cotton gin waste (CGW) is the byproduct of ginning cotton and contains a significant amount of cellulose.
- LePori et al. (1982): CGW collected at the gin could supply the entire amount of energy needed for the gin in stripper harvesting areas.
- Lacewell et al. (1982): one ton of CGW potentially contains 14 million Btus of energy, which is the same amount of energy contained in 120 gallons of gasoline.
- Multer et al. (2010): carbon dioxide released during the process of converting CGW into viable energy does not contribute to greenhouse gas emissions.

Why biopower?

- The feedstock (cotton -> cotton gin waste) is already shipped to the gin.
- Peaking power electricity is very high during the winter ginning season, so any excess biopower adds value streams to gin cooperatives.
- Biopower production is partly counter-cyclical to weather risks:
 - During bumper crops all excess gin trash can be used to avoid beetle infestation
 - During droughts, the entirety of the reduced gin trash is applied to the highest valued products - peak electric prices, and if prices eventually allow ammonia fertilizer.

Delivery-scale dilemma

- Can we sustainably and profitably produce electricity (and if price allows, ammonia) from cotton gin waste?
- Successful conversion of biomass to energy requires the right size plant, and the right transportation process — the so-called “delivery-scale” dilemma.

Too few data points

- Annual cotton gin waste data
- Monthly ammonia price data
- Hourly electricity price data
- How can we run an optimization model with (i) too few data points (cotton gin waste) and (ii) inconsistent data frequency/granularity

Bayesian simulation

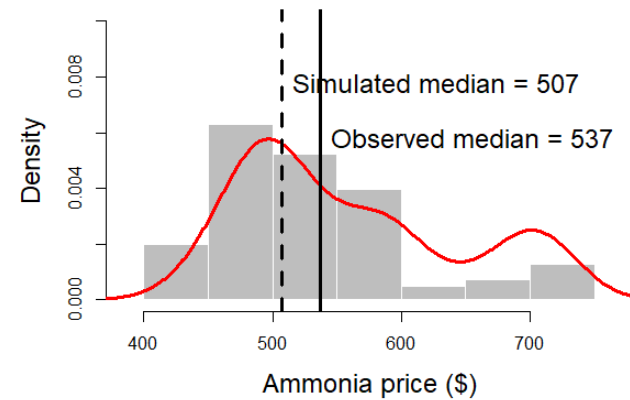
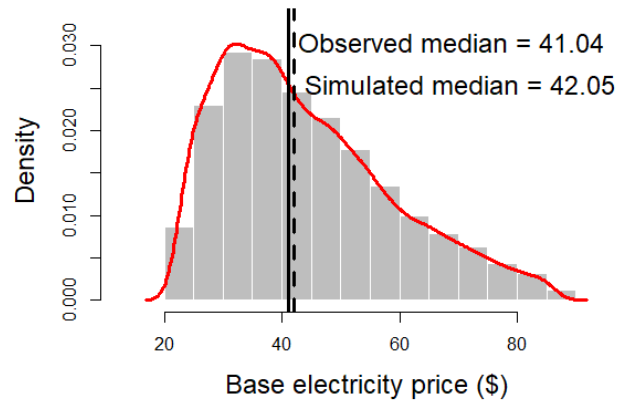
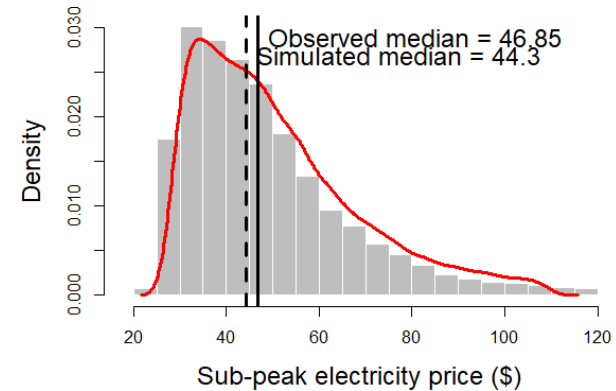
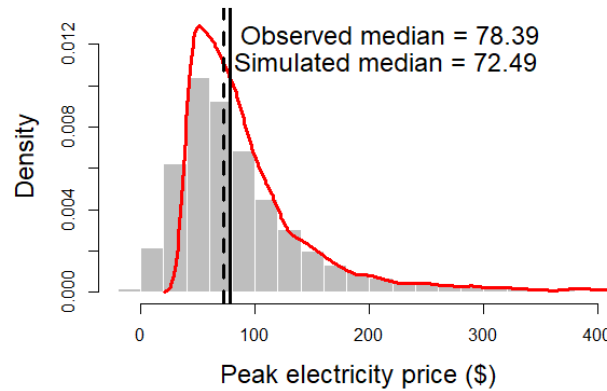
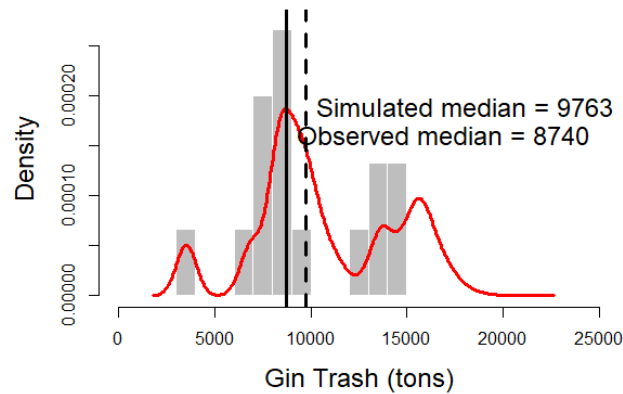
$$Y = \beta X + \epsilon$$

- Uses Gibbs sampling to estimate the posterior distribution of the model coefficients (β) and error variance (σ^2). (Preserves data quirks without resampling.)
- How does it work? Iteratively draw samples from conditional distributions of both parameters:
 1. Set a specified number of iterations for the Gibbs sample (11,000) and a burn-in sample (1,000).
 2. Enter a loop where in each iteration, β and σ^2 parameters are alternately updated.
 3. For β , a sample is drawn from a multivariate normal distribution based on the covariance matrix and mean values parameters.
 4. The mean and covariance matrix for this distribution are calculated based on the current values of the data and a σ starting value of 0.50.
 5. The σ is subsequently updated by drawing a sample (inverse transformation sampling) from an inverse gamma distribution, and the updated σ is used in the next iteration of drawing β
 6. The loop continues until 10,000 samples are drawn after discarding the burn-in samples.
 7. Finally, new values of the dependent variable are simulated using the sampled β coefficients.

Data – 10,000 data points simulated from real data

- Annual cotton gin waste data over 15 years collected from Ropes Farmer Co-op Gin
 - Simulated from precipitation data (includes two of top five 2-yr records for drought and one of the three highest 2 years rainfall events since 1908)
- Monthly anhydrous ammonia price from DTN Progressive Farmer database
 - Simulated from price of major crops and oil (corn, cotton, oats prices and lagged oil price)
- Hourly electricity price from ERCOT over 12 years
 - Simulated from temperature

Simulated data very close to observed data



Optimization

$$\text{Revenue: } P_p E_p + P_{SP} E_{SP} + P_B E_B + P_M M + 10 * GW_f$$

$$\text{Marginal cost: } 5.5(E_p + E_{SP} + E_B + E_M) + 130.34 * M$$

$$\text{Fixed cost: } 37645 * ME + 0.100385 * \left[640000 + \frac{4000000}{1.2 * C + 5} \right] * C$$

$$\begin{aligned} &\text{MAX Revenue } [P_p E_p + P_{SP} E_{SP} + P_B E_B + P_M \frac{E_M}{11} + 10 * GW_f] - \text{Marginal Costs} \\ &[5.5(E_p + E_{SP} + E_B + E_M) + 130.34 * \frac{E_M}{11}] - \text{Fixed Costs } [0.100385 * \left[640000 + \right. \\ &\left. \frac{4000000}{1.2 * C + 5} \right] * C - 37645 * ME] \end{aligned}$$

Optimization

$$\begin{aligned} \text{MAX } & P_p E_p + P_{UB} E_{UB} + P_{LB} E_{LB} + P_M \frac{E_M}{11} + 10 * GW_f - 5.5(E_p + E_{UB} + E_{LB} + E_M) - 130.34 * \\ & \frac{E_M}{11} - 0.100385 * \left[640000 + \frac{4000000}{1.2 * C + 5} \right] * C - 37645 * ME \end{aligned}$$

Subject to:

$$[1] (E_p + E_{UB} + E_{LB} + E_M + GW_f) \leq CGW$$

$$[2] (E_p + E_{UB} + E_{LB} + E_M) \leq 5403 * C$$

$$[3] 0 \leq E_p \leq 1071$$

$$[4] 0 \leq E_{UB} \leq 2432$$

$$[5] 0 \leq E_{LB} \leq 1900$$

$$[6] 0 \leq M \leq 550$$

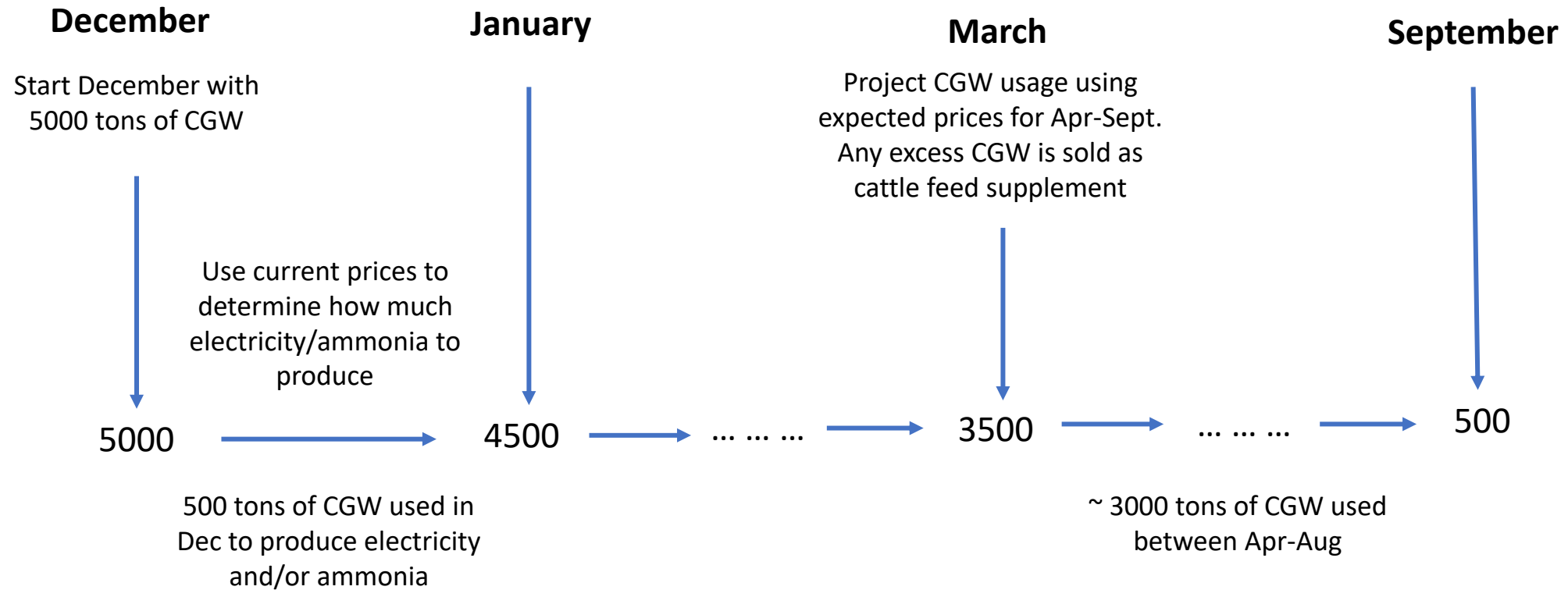
$$[7] 0 \leq E_M \leq 6050$$

Optimization

$$\begin{aligned} &MAX P_p E_p + P_{UB} E_{UB} + P_{LB} E_{LB} + P_M M - 5.5(E_p + E_{UB} + E_{LB} + E_M) - 130.34 * M - 37645 * \\ &ME - 0.100385 * \left[640000 + \frac{4000000}{1.2 * C + 5} \right] * C + 10 * GW_f \end{aligned}$$

- P_p is peak electricity price; E_p is the MWe of electricity sold each month at peak prices;
- P_{UB} is sub peak electricity price; E_{UB} is the MWe of electricity sold each month at subpeak prices;
- P_{LB} is the price of base electricity; E_{LB} is the MWe of electricity each month at base prices;
- P_M is the price of ammonia, M; E_M is electricity in MWe required to produce M (11 is needed to produce every ton of ammonia, M);
- ME is the number of ammonia processors, which ranges from 0 to 2;
- C is installed power capacity, which ranges from 1-5 MWe for the small gin and 1-9 MWe for medium gins;
- GW_f is gin waste sold as feed

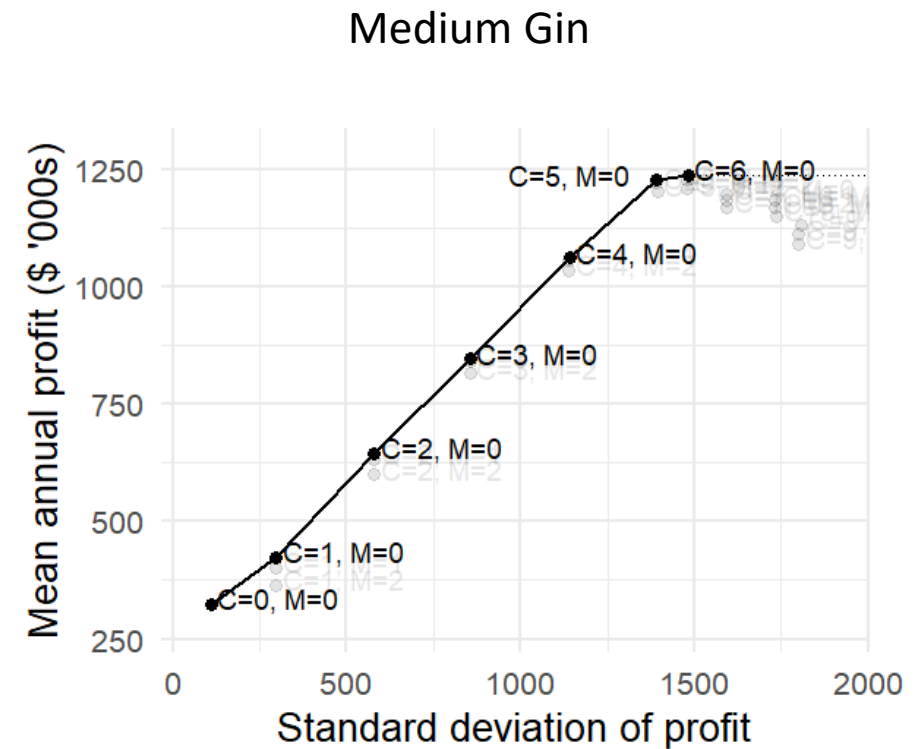
Illustration: Solving Profit Maximization and Investor Choices



Model is flexible: Key trade-off to optimize

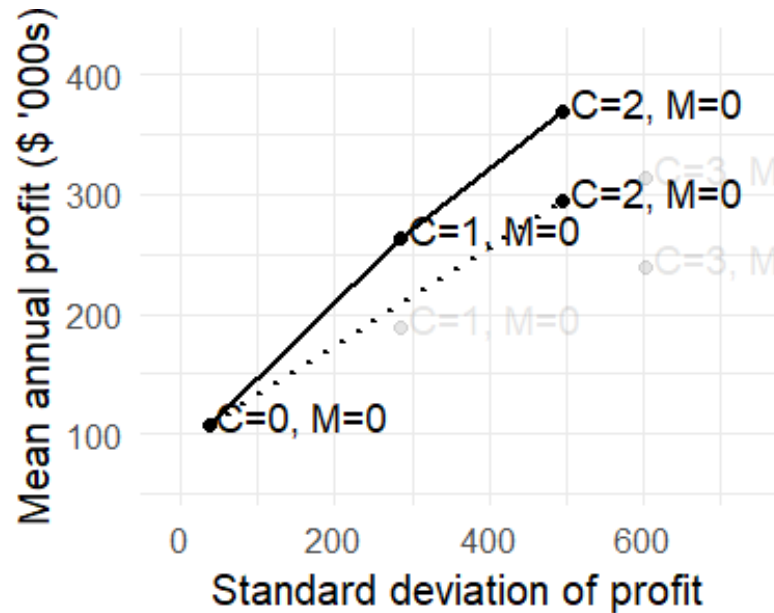
- Trade-off: Do we use all the gin during winter to produce electricity or store some for the summer?
 - Average electricity prices highest in winter
 - Yet, peaking prices are higher in the summer
- Model is flexible and allows for month-to-month individualized operational decision-making
 - Once gin trash volume for the season is known, operator will have precise expectations of electric prices for immediate month and reasonable expectations of future month.
 - Also know the schedule of their own electric power demands over the ginning season, then to allocate power to ginning operations and the grid.
 - Has the option to sell gin waste as animal feed supplement in March or hold gin waste to sell peak electricity during summer months. (But risk beetle emergence).

Profitable baseline analysis

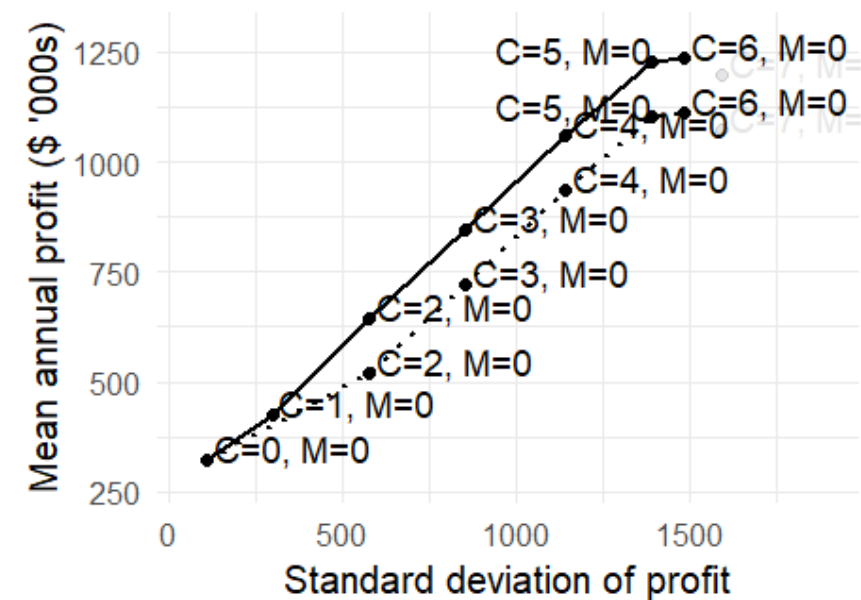


Profitable with added fixed cost for operator

Small Gin

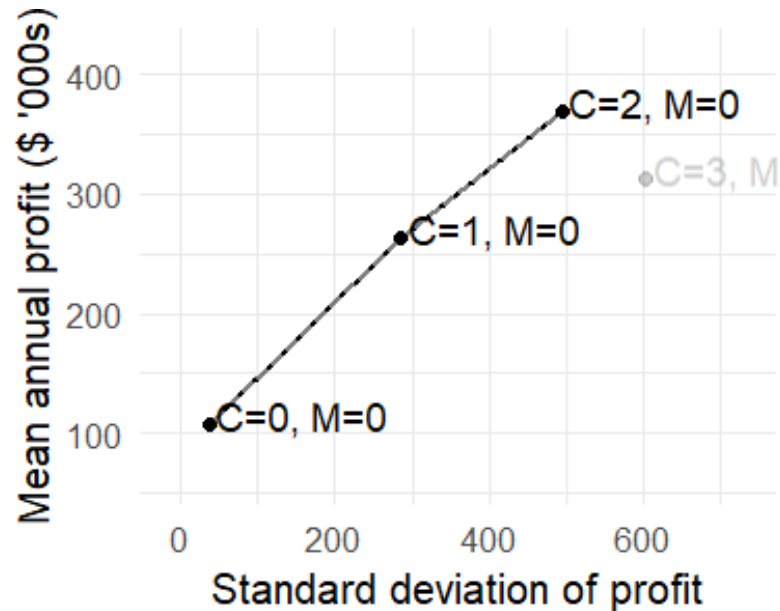


Medium Gin

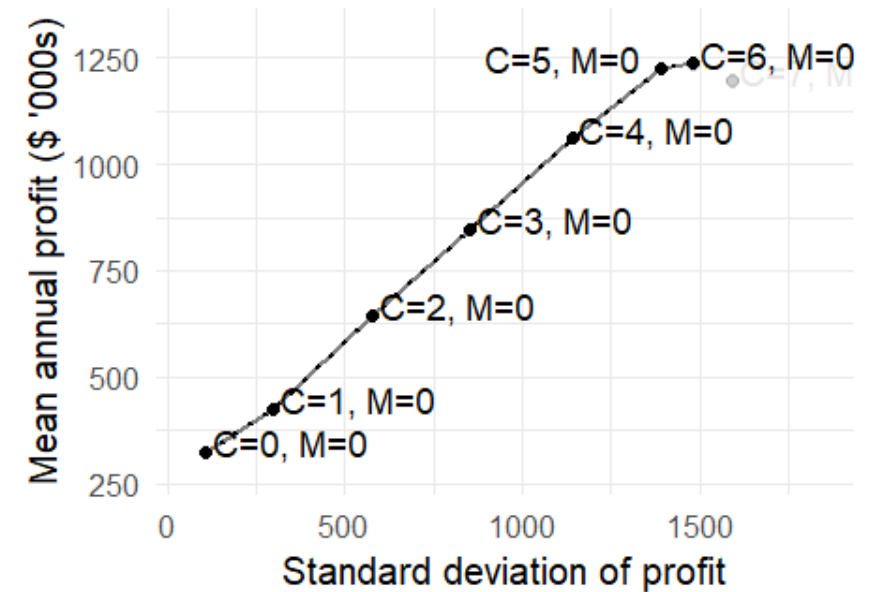


Profitable with lower base electricity price

Small Gin

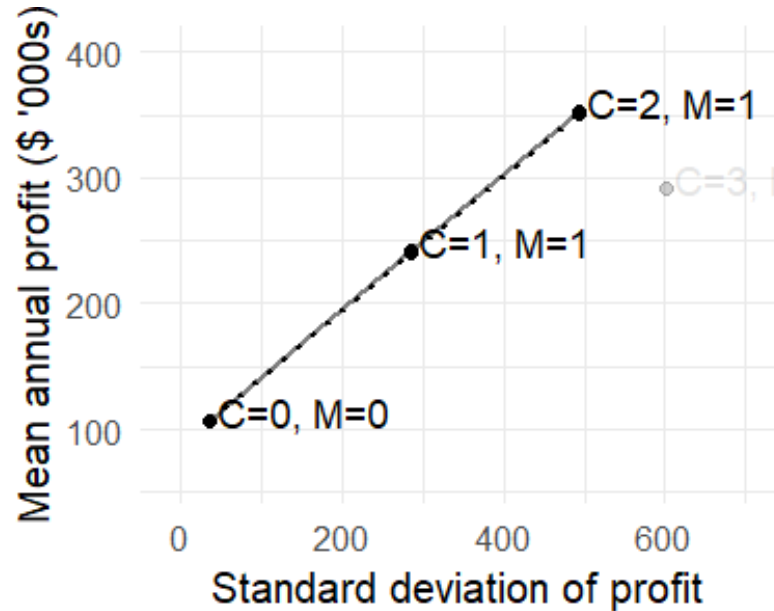


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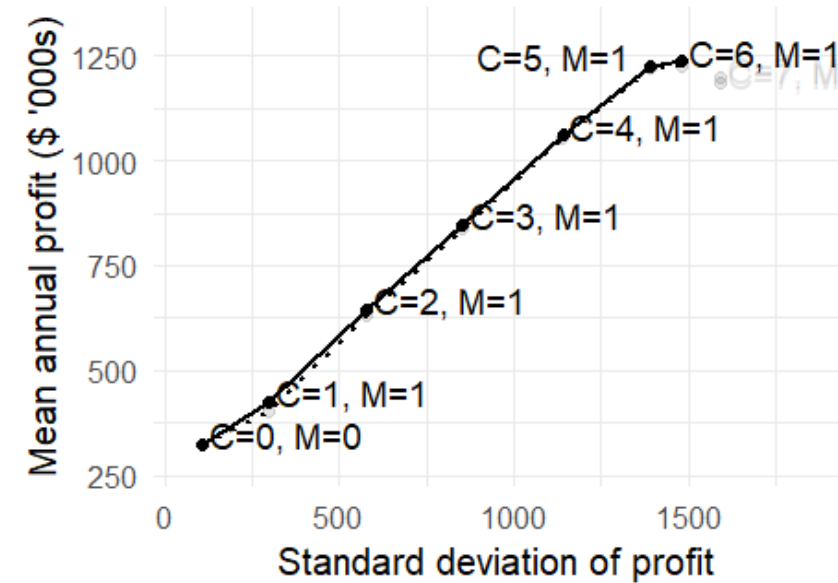


Profitable with lower marginal cost of ammonia

Small Gin

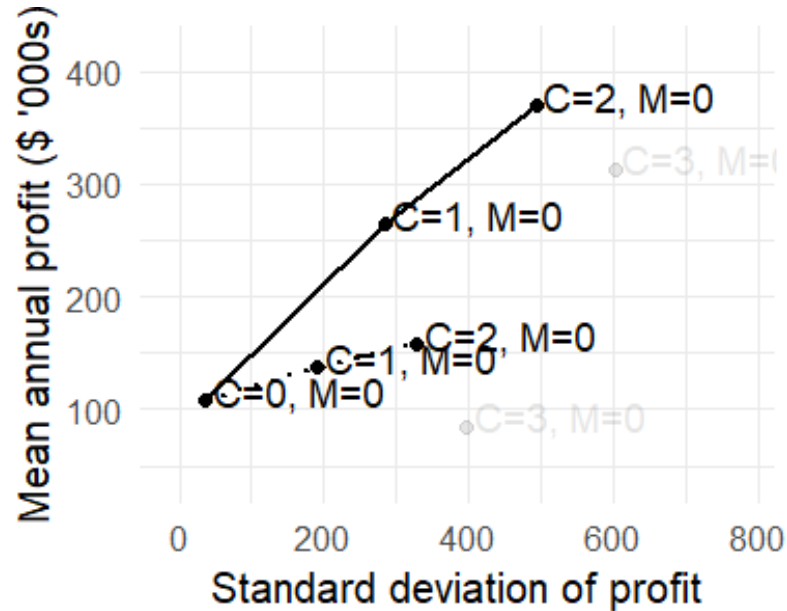


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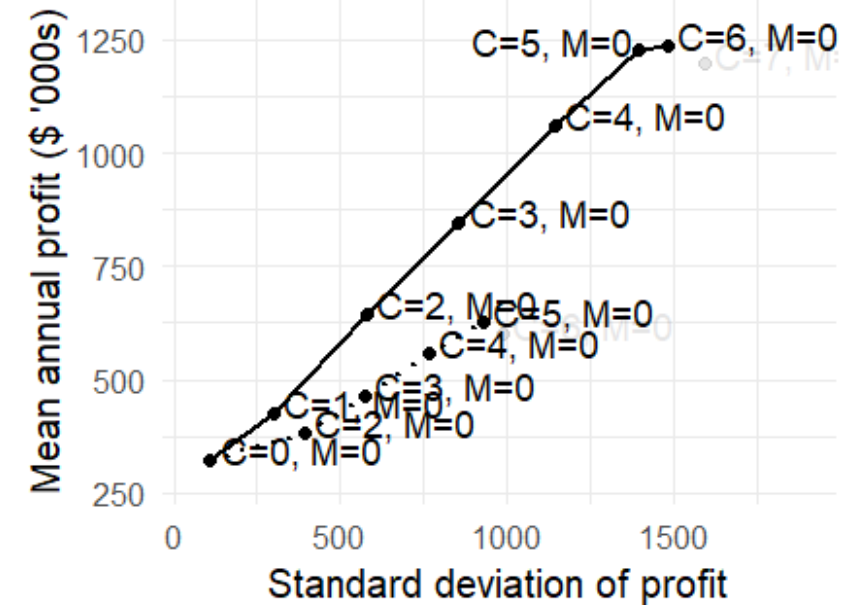


Profitable with lower gin-to-electricity conversion rate

Small Gin

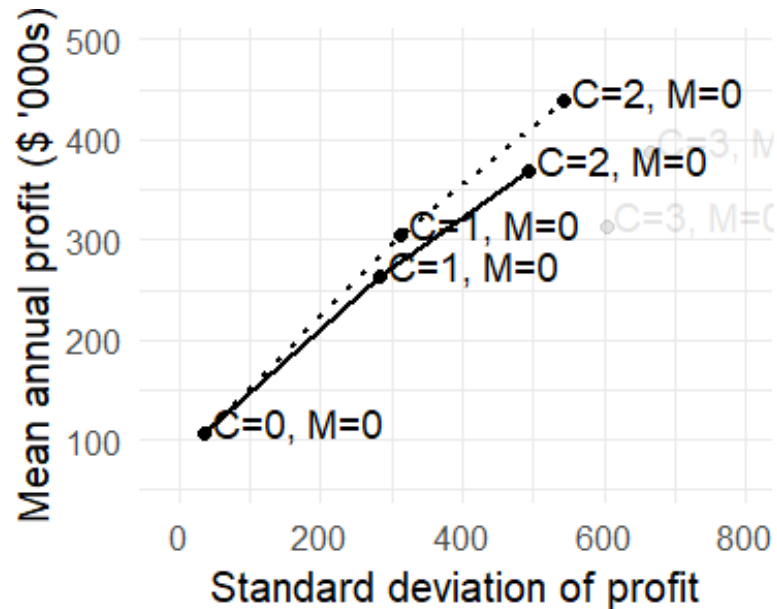


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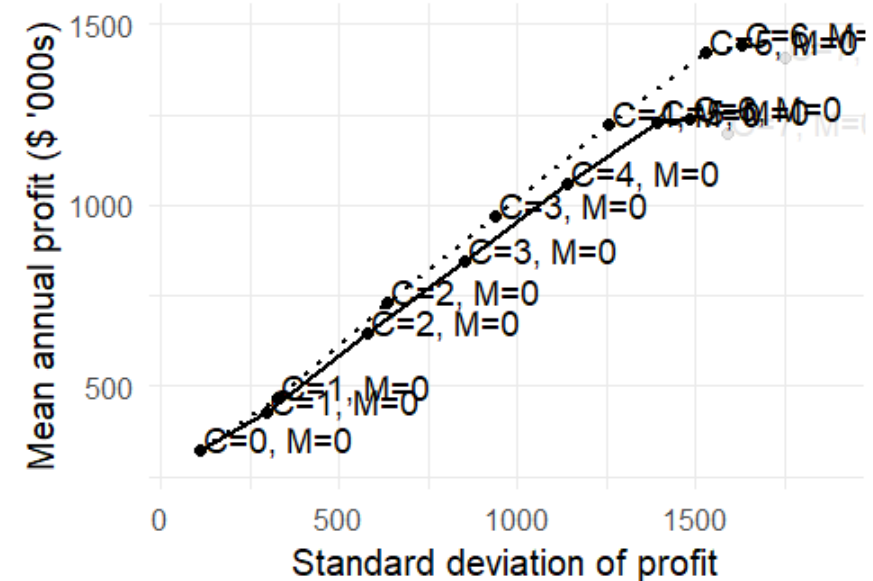


Profitable with higher electricity prices

Small Gin



Medium Gin



Profitability on the frontier

Profitability on the frontier - Small Gin

Models	Avg. ROIC	Prob. loss	Prob. ROIC > 100	Avg. profit	SD profit
C=0, M=0 ^{EV, *}	0.00	0.00	0.00	107,516	36,626
C=1, M=0 ^{EV}	82.17	0.29	17.26	264,011	284,846
C=2, M=0 ^{EV}	64.29	6.19	12.83	369,700	494,065

Profitability on the frontier - Medium Gin

Models	Avg. ROIC	Prob. loss	Prob. ROIC > 100	Avg. profit	SD profit
C=0, M=0 ^{EV, *}	0.00	0.00	0.00	322,549	109,878
C=1, M=0 ^{EV}	132.13	0.00	57.66	424,517	297,249
C=2, M=0 ^{EV}	112.01	0.00	31.23	644,104	577,942
C=3, M=0 ^{EV}	104.69	0.01	25.79	846,254	854,539
C=4, M=0 ^{EV}	103.31	1.04	25.02	1,061,195	1,140,497
C=5, M=0 ^{EV}	98.96	3.54	23.35	1,227,070	1,391,770
C=6, M=0 ^{EV}	85.76	5.10	19.02	1,237,195	1,482,193

12-yr cumulative profitability on the frontier

Cumulative profitability on the frontier - Small Gin

Models	Disc. Avg. profit 12 yrs.	SD disc. profit 12 yrs.	Disc. Avg. ROIC 12 yrs.	Prob. ROIC < 0	Prob. ROIC between 0 & 250	Prob. ROIC between 250 & 500	Prob. ROIC > 500
C=0, M=0 ^{EV, *}	484,920	44,933	0.00	0.00	0.00	0.00	0.00
C=1, M=0 ^{EV}	1,190,743	366,304	370.61	0.00	12.00	74.31	13.69
C=2, M=0 ^{EV}	1,667,423	632,674	289.95	0.00	44.66	50.66	4.68

Cumulative profitability on the frontier - Medium Gin

Models	Disc. Avg. profit 12 yrs.	SD disc. profit 12 yrs.	Disc. Avg. ROIC 12 yrs.	Prob. ROIC < 0	Prob. ROIC between 0 & 250	Prob. ROIC between 250 & 500	Prob. ROIC > 500
C=0, M=0 ^{EV, *}	1,454,760	134,800	0.00	0.00	0.00	0.00	0.00
C=1, M=0 ^{EV}	1,914,656	377,991	595.93	0.00	0.00	24.13	75.87
C=2, M=0 ^{EV}	2,905,040	741,192	505.17	0.00	0.00	55.58	44.42
C=3, M=0 ^{EV}	3,816,778	1,098,925	472.15	0.00	0.00	63.99	36.01
C=4, M=0 ^{EV}	4,786,208	1,473,196	465.97	0.00	0.60	64.71	34.69
C=5, M=0 ^{EV}	5,534,335	1,813,371	446.31	0.00	2.28	66.99	30.73
C=6, M=0 ^{EV}	5,580,001	1,898,134	386.78	0.00	10.56	70.83	18.61

Extended analysis – small gin

Models ^a	Avg. ROIC	Prob. loss	Prob. ROIC > 100	Avg. profit	SD profit
C=0, M=0 ^{EV, *}	0.00	0.00	0.00	107,516	36,626
C=1, M=0 ^{EV}	82.17	0.29	17.26	264,011	284,846
C=2, M=0^{EV}	64.29	6.19	12.83	369,700	494,065
C=3, M=0	38.78	14.11	7.04	313,519	602,822
C=4, M=0	16.58	35.30	2.39	170,302	523,131
C=1, M=1	59.08	2.11	11.27	241,505	284,887
C=2, M=1	53.18	6.75	10.38	352,330	493,492
C=3, M=1	32.58	17.99	5.86	291,900	600,695
C=4, M=1	13.17	40.64	1.92	146,800	524,745
C=1, M=2	41.08	4.96	8.06	203,860	284,887
C=2, M=2	42.40	8.12	7.94	317,992	493,718
C=3, M=2	26.56	25.85	4.91	261,189	602,075
C=4, M=2	9.64	46.91	1.62	115,922	525,505

Extended analysis – small gin

Models	Disc. Avg. profit 12 yrs.	SD disc. profit 12 yrs.	Disc. Avg. ROIC 12 yrs.	Prob. ROIC < 0	Prob. ROIC between 0 & 250	Prob. ROIC between 250 & 500	Prob. ROIC > 500
C=0, M=0 ^{EV, *}	484,920	44,933	0.00	0.00	0.00	0.00	0.00
C=1, M=0 ^{EV}	1,190,743	366,304	370.61	0.00	12.00	74.31	13.69
C=2, M=0^{EV}	1,667,423	632,674	289.95	0.00	44.66	50.66	4.68
C=3, M=0	1,414,036	765,230	174.92	0.00	81.75	17.29	0.96
C=4, M=0	768,095	652,694	74.78	1.80	95.80	2.40	0.00
C=1, M=1	1,089,237	366,113	266.45	0.00	51.50	47.18	1.32
C=2, M=1	1,589,080	630,754	239.84	0.00	62.91	35.41	1.68
C=3, M=1	1,316,530	762,939	146.95	0.12	88.12	11.16	0.60
C=4, M=1	662,097	654,167	59.40	5.76	92.56	1.68	0.00
C=1, M=2	919,451	366,108	185.26	0.00	81.87	17.89	0.24
C=2, M=2	1,434,208	630,886	191.21	0.00	78.03	21.73	0.24
C=3, M=2	1,178,016	764,319	119.79	0.12	93.40	6.36	0.12
C=4, M=2	522,831	654,923	43.49	13.57	85.11	1.32	0.00

Extended analysis – small gin

Models	Avg. ROIC	Prob. loss	Prob. ROIC > 100	Avg. profit	SD profit
Panel A: Fixed cost for operator					
C=1, M=0	58.83	5.60	12.99	189,011	284,846
C=2, M=0	51.25	9.50	11.04	294,700	494,065
C=3, M=0	29.51	30.39	6.17	238,519	602,822
Panel B: Lower base electricity price					
C=1, M=0	82.15	0.33	17.26	263,953	284,886
C=2, M=0	64.10	6.22	12.78	368,639	494,156
C=3, M=0	38.52	14.55	7.00	311,370	603,181
Panel C: Lower marginal cost of ammonia plant					
C=1, M=1	58.85	2.14	11.25	240,563	284,880
C=2, M=1	53.00	6.78	10.36	351,135	493,410
C=3, M=1	32.47	18.15	5.86	290,932	600,545
Panel D: Lower conversion rate					
C=1, M=0	42.68	5.27	8.32	137,126	191,089
C=2, M=0	27.31	18.77	5.87	157,035	328,990
C=3, M=0	10.50	51.24	3.17	84,847	398,163
Panel E: Higher electricity prices					
C=1, M=0	94.91	0.02	21.54	304,938	313,079
C=2, M=0	76.25	5.71	15.89	438,519	543,966
C=3, M=0	47.98	9.44	9.08	387,918	665,178

Extended analysis – medium gin

Models	Avg. ROIC	Prob. loss	Prob. ROIC > 100	Avg. profit	SD profit
C=0, M=0 ^{EV, *}	0.00	0.00	0.00	322,549	109,878
C=1, M=0 ^{EV}	132.13	0.00	57.66	424,517	297,249
C=2, M=0 ^{EV}	112.01	0.00	31.23	644,104	577,942
C=3, M=0 ^{EV}	104.69	0.01	25.79	846,254	854,539
C=4, M=0 ^{EV}	103.31	1.04	25.02	1,061,195	1,140,497
C=5, M=0 ^{EV}	98.96	3.54	23.35	1,227,070	1,391,770
C=6, M=0^{EV}	85.76	5.10	19.02	1,237,195	1,482,193
C=7, M=0	73.02	6.08	14.92	1,197,302	1,592,251
C=1, M=1	98.46	0.00	28.51	402,514	296,984
C=2, M=1	95.59	0.00	22.01	633,336	577,545
C=3, M=1	93.74	0.03	21.02	839,793	854,580
C=4, M=1	94.73	1.60	21.71	1,055,860	1,139,546
C=5, M=1	91.96	4.20	20.85	1,220,799	1,392,416
C=6, M=1	80.17	5.46	16.98	1,226,806	1,479,441
C=7, M=1	68.61	6.26	13.53	1,185,122	1,592,734
C=1, M=2	73.52	0.01	14.00	364,869	296,984
C=2, M=2	79.99	0.00	16.39	599,940	577,435
C=3, M=2	82.86	0.18	17.36	814,788	854,714
C=4, M=2	86.17	2.58	18.70	1,035,895	1,139,982
C=5, M=2	85.08	4.61	18.36	1,203,895	1,393,265
C=6, M=2	74.79	5.75	15.37	1,209,904	1,479,485
C=7, M=2	64.36	6.31	12.47	1,167,982	1,593,145

Extended analysis – medium gin

Models	Disc. Avg. profit 12 yrs.	SD disc. profit 12 yrs.	Disc. Avg. ROIC 12 yrs.	Prob. ROIC < 0	Prob. ROIC between 0 & 250	Prob. ROIC between 250 & 500	Prob. ROIC > 500
C=0, M=0 ^{EV, *}	1,454,760	134,800	0.00	0.00	0.00	0.00	0.00
C=1, M=0 ^{EV}	1,914,656	377,991	595.93	0.00	0.00	24.13	75.87
C=2, M=0 ^{EV}	2,905,040	741,192	505.17	0.00	0.00	55.58	44.42
C=3, M=0 ^{EV}	3,816,778	1,098,925	472.15	0.00	0.00	63.99	36.01
C=4, M=0 ^{EV}	4,786,208	1,473,196	465.97	0.00	0.60	64.71	34.69
C=5, M=0 ^{EV}	5,534,335	1,813,371	446.31	0.00	2.28	66.99	30.73
C=6, M=0^{EV}	5,580,001	1,898,134	386.78	0.00	10.56	70.83	18.61
C=7, M=0	5,400,078	2,041,002	329.32	0.00	29.05	60.62	10.32
C=1, M=1	1,815,420	377,379	444.10	0.00	0.00	75.51	24.49
C=2, M=1	2,856,472	740,221	431.12	0.00	0.00	76.59	23.41
C=3, M=1	3,787,636	1,098,489	422.79	0.00	1.08	75.27	23.65
C=4, M=1	4,762,144	1,474,845	427.23	0.00	2.40	72.03	25.57
C=5, M=1	5,506,050	1,814,758	414.77	0.00	5.64	70.95	23.41
C=6, M=1	5,533,146	1,891,622	361.60	0.00	16.57	69.63	13.81
C=7, M=1	5,345,144	2,040,417	309.45	0.00	37.58	54.62	7.80
C=1, M=2	1,645,634	377,365	331.59	0.00	11.16	85.83	3.00
C=2, M=2	2,705,850	740,052	360.75	0.00	9.00	80.91	10.08
C=3, M=2	3,674,859	1,098,332	373.70	0.00	9.36	77.07	13.57
C=4, M=2	4,672,099	1,474,955	388.64	0.00	8.52	73.47	18.01
C=5, M=2	5,429,811	1,814,679	383.73	0.00	11.04	71.31	17.65
C=6, M=2	5,456,916	1,891,956	337.33	0.00	25.09	64.35	10.56
C=7, M=2	5,267,835	2,040,863	290.27	0.00	45.86	48.38	5.76