

# Padding & Strides

Why we need padding?

(Image)

7	2	3	3	8
4	5	3	8	4
3	3	2	8	4
2	8	7	2	7
5	4	4	5	4

(5x5)

(filter)

(3x3)

1	0	-1
1	0	-1
1	0	-1

=

(feature map)

6	-9	-8
-3	-2	-3
-3	0	-2

(3x3)

\*
 
$$\begin{aligned}
 &2 \times 1 + 5 \times 1 + 3 \times 1 + 3 \times 0 + 2 \times 0 + 3 \times 1 + 8 \times -1 + 8 \times -1 \\
 &= -9
 \end{aligned}$$

### 2 problem

1. Feature map (3x3) size is small as compare to Image after using filter. If we <sup>again</sup> use filter on feature map then size of feature map will be reduce as compare to previous feature map. (jisme convolutional layer (filter) apply karoge har layer ke bad uska size chhota hoga)

Insight → losing Data

2. Border pixel (green Area) → less part in convolution as compare to middle part (orange)

for eg:- pixel(0,0) → 7  
 ↳ be only 1 time in convolution part

pixel (3,3) → 2  
 ↳ be multiple time in convolution part

So, In feature map  $\rightarrow$  middle pixel  
 $\downarrow$   
 more importance  
 $\nwarrow$   
 border pixel  $\rightarrow$  less importance

These two problem solve padding.

What is padding?

In Convolution

Image

$n \times n$

$5 \times 5$

filter

$f \times f$

$3 \times 3$

feature map

$(n-f+1) (n-f+1)$

$(5-3+1) (5-3+1)$   
 $3 \times 3$

but we want  $n-f+1 = n \rightarrow$  so Image Size = feature map size

$\rightarrow$  Not change in filter

$\rightarrow$  change in Image size in padding

Add. column and Row

0	0	0	0	0	0	0
0						0
0						0
0						0
0						0
0						0
0	0	0	0	0	0	0

$\rightarrow$  Added column and Row  
 And this boundary is called  
 padding. Value of padding is 0.



After padding ↓

padding

0	0	0	0	0	0	0
0	60	113	56	139	85	0
0	73	121	54	84	128	0
0	131	99	70	129	127	0
0	80	57	115	69	134	0
0	104	126	123	95	130	0
0	0	0	0	0	0	0

\*

0	-1	0
-1	5	-1
0	-1	0

=

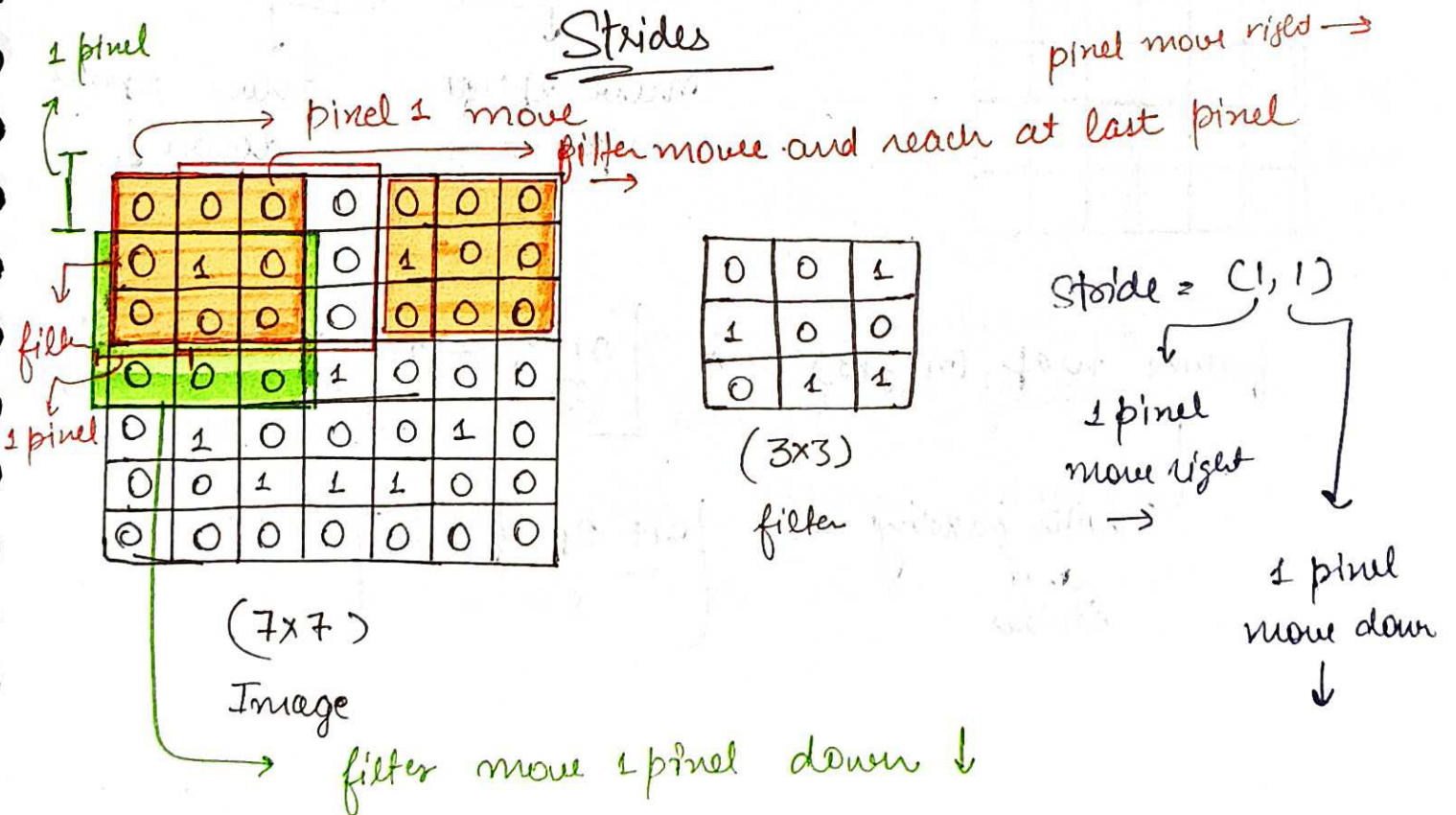
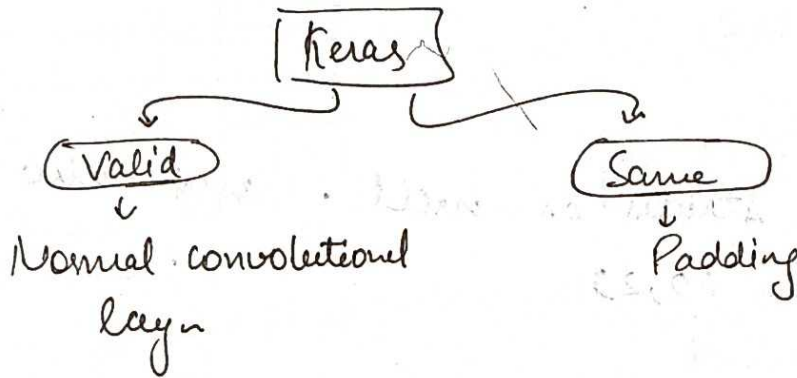
Kernel  
(3x3)


(5x5)  
feature map

Image (5x5)  
with padding (7x7)

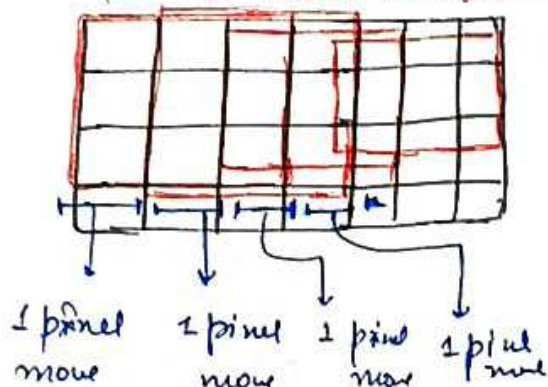
$$(n + 2p - b + 1)$$
$$5 + 2(1) - 3 + 1 = 5$$

↓  
padding



$$\text{Strides} = (1, 1)$$

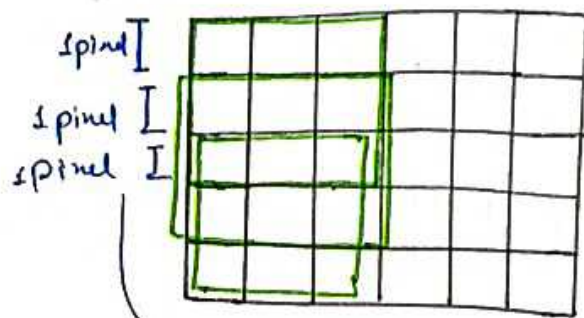
filter move right  $\rightarrow$   
 move to right side



$$\text{Strides} = (1, 1)$$

right  $\rightarrow$   
 total

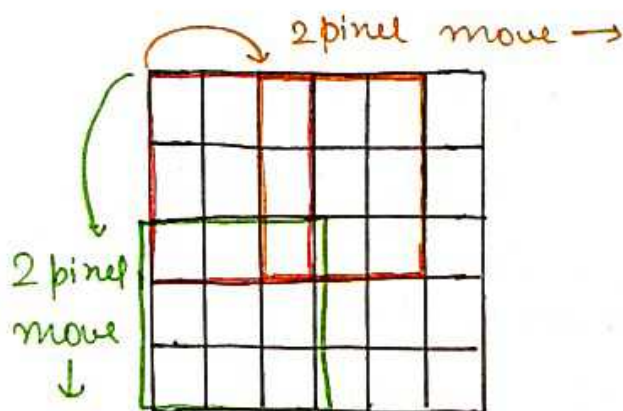
filter move down  $\downarrow$



$$\text{Strides} = (1, 1)$$

move down  $\downarrow$

We can change strides as well. and also  
 write  $\text{strides} = (2, 2)$



$$\text{Stride} = (2, 2)$$

move 2 pixels  
 right  $\rightarrow$

move 2 pixels  
 down  $\downarrow$

feature map  $(n-f+1) \rightarrow \left[ \frac{n-f}{s} + 1 \right]$   $\rightarrow$  with stride  
 $\rightarrow$  without padding

with padding  
 and  
 Strides  $\rightarrow \left[ \frac{n+2p-f}{s} + 1 \right]$



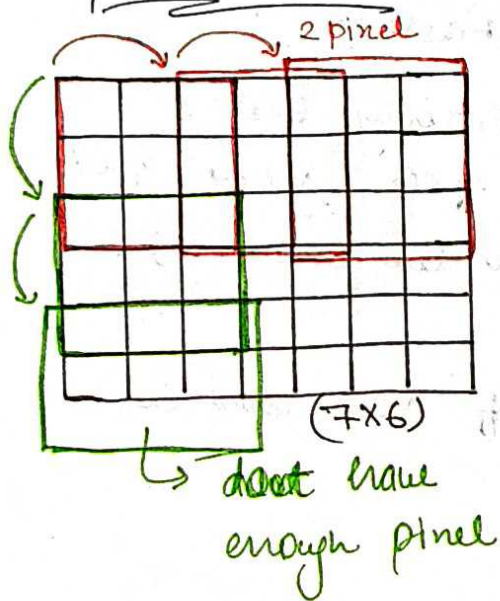
Stride value  $\uparrow \uparrow$  = feature map size  $\downarrow \downarrow$

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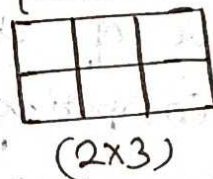
Which means information loss while using stride or more than 1 stride.

If stride value more than 1 is called strided convolution.

Special Case



let. stride = 2  $\rightarrow$  filter skip 2 pixel  
feature map



$\rightarrow$  because of don't have enough pixel

$$\left[ \frac{n-b}{s} + 1 \right] \quad \left[ \frac{n-f+1}{2} \right]$$

$$\frac{6-3}{2} + 1 = \frac{3}{2} + 1$$

floor rule  
= 1

2

$$(2 \times 3)$$

$$\frac{7-3}{2} + 1 = 2 + 1$$

= 3

Why strides are required?

Reasons  $\rightarrow$

1. When you just want high level feature and not want low level feature.

low level feature means capture details of the image

$\rightarrow$  when stride value is small.

for example  $\rightarrow$  We are working on computer vision problem and I only want some important feature (Not in detail feature). So, I use higher value of stride.

If I want details feature of image then I use lower value of stride.

2. Computing Power  $\rightarrow$  Training Fast

Increase value of stride for Training Fast but now, Computing Machine specs very good. So, we can use default value (stride=1).

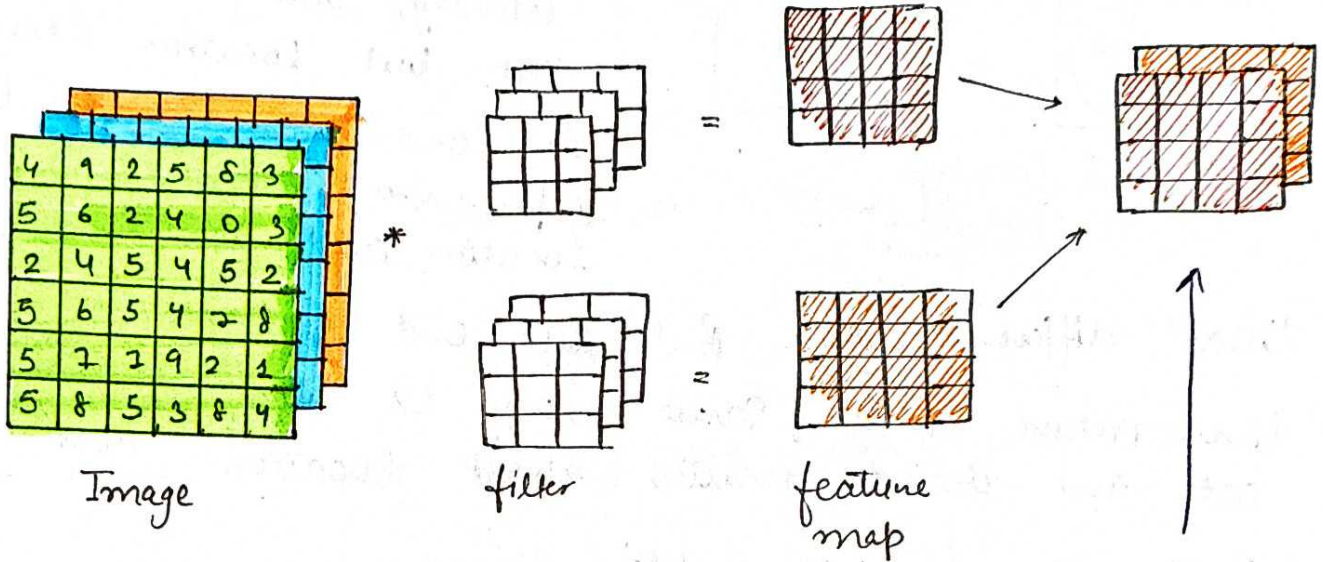
\* We can give different value of row and col  
stride = (2, 1)

# Pooling layer

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The problem with convolution

1. Memory Issue
2. Translation Variance



let

Image  
[228 x 228 x 3]

filter  
100

feature map

(226 x 226) x 100

Store in 32bit float storage

1 batch for 1 training ← 19MB ←

If batch = 100

↳ 1.59 GB → we can not store in storage

\* We need to reduce size of feature Map.

Possible solution

1. Increase the value of stride to reduce size of feature map.



2. Pooling solve  $\rightarrow$  Memory Issue  
 $\hookrightarrow$  Translation Variance

### Translation Variance

$\hookrightarrow$  dependent on location



location  
changed

Let say, both are same cat but location changed.  
 In convolution layer  $\rightarrow$  tied up with (dependent) on location and both image

treat different way. But our end goal is to both picture treat same way cz both are same cat and doesn't matter about location. And

Pooling solve this problem.

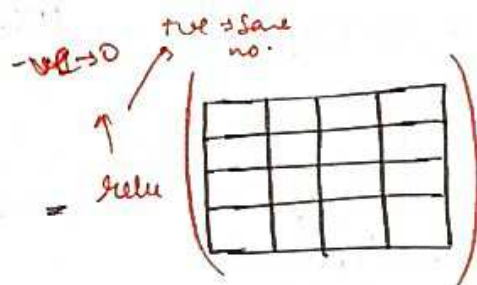
$\hookrightarrow$  down sample your feature map.

### Pooling

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
255	255	255	255	255	255
255	255	255	255	255	255
255	255	255	255	255	255

\*

1	1	1
0	0	0
1	1	1



apply "relu" for non-linearity adding

After Non-linearity  $\rightarrow$  apply pooling  $\rightarrow$  famous (Max pooling method)

Max pooling

Aug pooling

Min pooling

Global pooling

L2 pooling



Let assume this feature map

3	1	1	3
2	5	0	2
1	4	2	1
4	7	2	4

Size of pooling  $\rightarrow (2,2)$

Stride  $\rightarrow 2$

type  $\rightarrow$  Max

$\rightarrow$  Take first  $(2,2)$  box  $\rightarrow$  Max Number = 5

$\hookrightarrow$  Orange box

$\rightarrow$  Stride = 2  $\rightarrow$  Skip 2 pixel  $\rightarrow$  reach box  $\rightarrow$  Max no. = 3  
 $\hookrightarrow$  white box

$\rightarrow$  Move down  $\rightarrow$  skip 2 pixel  $\rightarrow$  reach blue box  $\rightarrow$  Max no. = 7

$\rightarrow$  Move right  $\rightarrow$  skip 2 pixel  $\rightarrow$  reach Green box  $\rightarrow$  Max no. = 4

5	3
7	4

$(2 \times 2) \hookrightarrow$  feature map (size reduce)

Pooling  $\rightarrow$  low level details  $\rightarrow$  eliminate  
Max  $\hookrightarrow$  higher level details  $\rightarrow$  Take

Pooling  $\rightarrow$  Min pooling  $\rightarrow$  extract min no.

$\hookrightarrow$  Avg pooling  $\rightarrow$  extract Avg of first box  
(4 pixel No.)

$\hookrightarrow$  L2 pooling  $\rightarrow$  extract L2 Norm

for Demo and Visualization visit

deep lizard - Maxpool demo

## Pooling on Volumes

4	9	2	5	8	3
5	6	2	4	0	3
2	4	5	4	5	2
5	6	5	4	7	8
5	7	7	9	2	1
5	8	5	3	8	4

\*

Filter 1

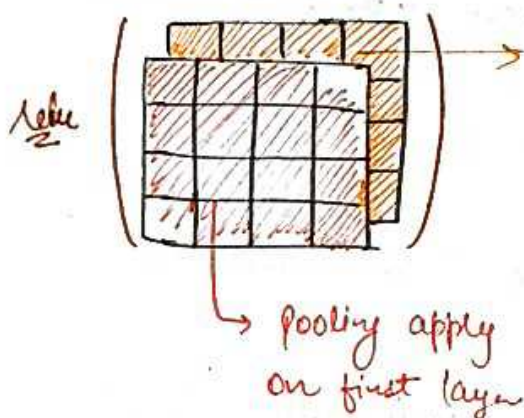
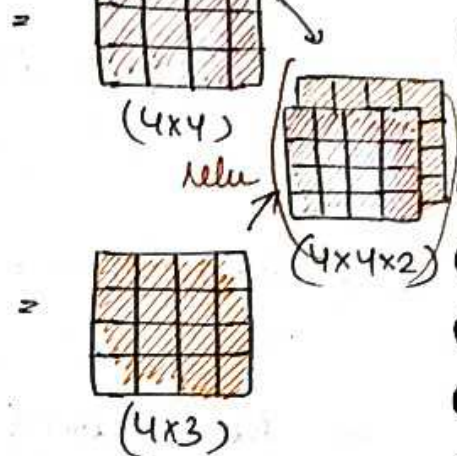
1	0	-1
1	0	-1
1	0	-1

(3x3x3)

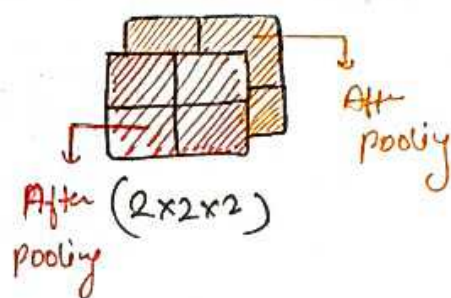
Filter 2

0	0	0
1	1	1
-1	-1	-1

(3x3x3)

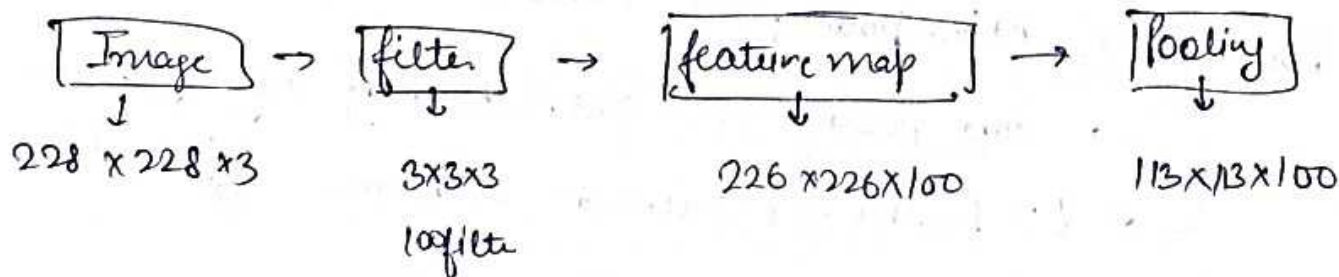


pooling apply on second layer



## Advantage of Pooling

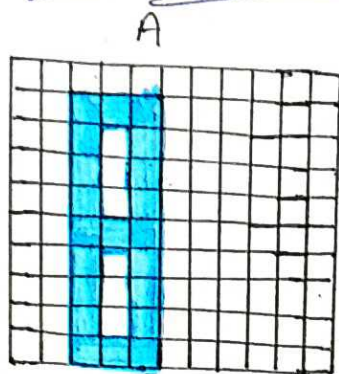
1. Reduced Size



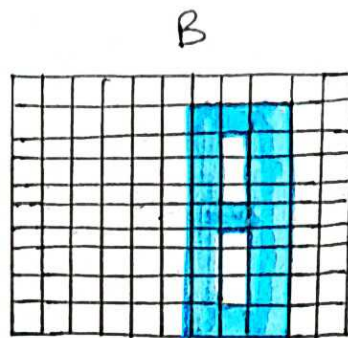


## 2. Translation Invariance

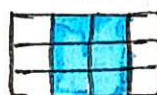
(89)



⇓  
Max Pool 2D

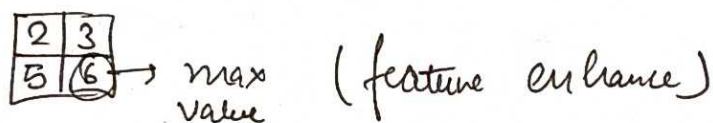


⇓  
Max Pool 2D



## 3. Enhanced Features (only in case of Max pooling)

Enhance edges of the ~~feature~~ Image



4. There's no need of training  
Cause pooling → just aggregate the number or  
finding max number from feature map.

### Types of Pooling

1. Max pooling

2. Avg Pooling

3. Global pooling

a) Global Max

b) Global Avg Pooling

2	1	1	3
2	5	0	2
1	4	2	1
4	7	2	4

→ Find max of feature map → 7 (Global Max)

7

→ Find Avg of feature map

### Disadvantage

Image Segmentation → require location  
So, Pooling not need in Image Segmentation