DER Models

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1 Without Storage

1.1 Disaggregation

$$\max \quad \sum_{t \in T} \left(P_t^{DA} x_{it} + \mathbb{E} \left[P_t^{RT}(\xi) y_{it}^+(\xi) - P_t^{PN} y_{it}^-(\xi) \right] \right)$$
 (1a)
$$\text{S.t.} \quad R_{it}(\xi) - x_{it} = y_{it}^+(\xi) - y_{it}^-(\xi) \quad \forall t \in T$$
 (1b)
$$R_{it}(\xi) \geqslant y_{it}^+(\xi) \quad \forall t \in T$$
 (1c)
$$y_{it}^+(\xi) \leqslant M z_{it}(\xi), \quad y_{it}^-(\xi) \leqslant M (1 - z_{it}(\xi)) \quad \forall t \in T$$
 (1d)
$$x_{it}^{DA} \geqslant 0, y_{it}^+(\xi) \geqslant 0, y_{it}^-(\xi) \geqslant 0, z_{it}(\xi) \in \{0, 1\} \quad \forall t \in T$$
 (1e)

(1a)

(3l)

Aggregation 1.2

$$\max \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right] \right)$$
s.t.
$$\sum_{i \in I} R_{it}(\xi) - \alpha_t = \beta_t^+(\xi) - \beta_t^-(\xi) \quad \forall t \in T$$

$$\sum_{i \in I} R_{it}(\xi) \geqslant \beta_t^+(\xi) \quad \forall t \in T$$

$$\beta_t^+(\xi) \leqslant M z_t(\xi), \quad \beta_t^-(\xi) \leqslant M (1 - z_t(\xi)) \quad \forall t \in T$$

$$\alpha_t^{DA} \geqslant 0, \beta_t^+(\xi) \geqslant 0, \beta_t^-(\xi) \geqslant 0, z_t(\xi) \in \{0, 1\} \quad \forall t \in T$$
(2c)

1.3 Settlement

$$\max \quad \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right] \right)$$
 (3a)
$$\text{S.t.} \quad \sum_{i \in I} R_{it}(\xi) - \alpha_t^{DA} = \beta_t^+(\xi) - \beta_t^-(\xi) \quad \forall t \in T$$
 (3b)
$$\sum_{i \in I} R_{it}(\xi) \geqslant \beta_t^+(\xi) \quad \forall t \in T$$
 (3c)
$$\beta_t^+(\xi) \leqslant M z_t(\xi), \quad \beta_t^-(\xi) \leqslant M (1 - z_t(\xi)) \quad \forall t \in T$$
 (3d)
$$\alpha_t = \sum_{i \in I} x_{it}(\xi), \quad \beta_t^+(\xi) = \sum_{i \in I} e_{it}^+(\xi), \quad \beta_t^-(\xi) = \sum_{i \in I} e_{it}^-(\xi) \quad \forall t \in T$$
 (3e)
$$R_{it}(\xi) - x_{it}(\xi) = y_{it}^+(\xi) - y_{it}^-(\xi) \quad \forall t \in T$$
 (3f)
$$R_{it}(\xi) \geqslant y_{it}^+(\xi) \quad \forall t \in T$$
 (3g)
$$y_{it}^+(\xi) \leqslant M z_{it}(\xi), \quad y_{it}^-(\xi) \leqslant M (1 - z_{it}(\xi)) \quad \forall t \in T$$
 (3h)
$$\sum_{j \in I, j \neq i} d_{ijt}(\xi) \leqslant y_{it}^+(\xi), \quad \sum_{j \in I, j \neq i} d_{jit}(\xi) \leqslant y_{it}^-(\xi) \quad \forall t \in T$$
 (3i)
$$e_{it}^+(\xi) = 0 \quad \forall t \in T$$
 (3j)
$$e_{it}^+(\xi) = y_{it}^+(\xi) - \sum_{j \in I, j \neq i} d_{ijt}(\xi) \quad \forall t \in T$$
 (3k)

 $e_{it}^-(\xi) = y_{it}^-(\xi) - \sum_{j \in I, j \neq i} d_{jit}(\xi) \quad \forall t \in T$

2 With Storage

2.1 Disaggregation

$$\max \quad \sum_{t \in T} \left(P_t^{DA} x_{it} + \mathbb{E} \left[P_t^{RT}(\xi) y_{it}^+(\xi) - P_t^{PN} y_{it}^-(\xi) \right] \right)$$
 (4a)
$$s.t. \quad R_{it}(\xi) - x_{it} = y_{it}^+(\xi) - y_{it}^-(\xi) + z_{it}^C(\xi) - z_{it}^D(\xi) \quad \forall i, t$$
 (4b)
$$R_{it}(\xi) \geqslant y_{it}^+(\xi) \quad \forall i, t$$
 (4c)
$$z_{i,t+1}(\xi) = z_{it}(\xi) + z_{it}^C(\xi) - z_{it}^D(\xi) \quad \forall i, t$$
 (4e)
$$z_{it}^D(\xi) \leqslant z_{it}(\xi) \quad \forall i, t$$
 (4f)
$$z_{it}^C(\xi) \leqslant K_i - z_{it}(\xi) \quad \forall i, t$$
 (4g)
$$y_{it}^+(\xi) \leqslant M_1 \rho_{it}(\xi), \quad y_{it}^-(\xi) \leqslant M_1 (1 - \rho_{it}(\xi)) \quad \forall i, t$$
 (4h)
$$y_{it}^-(\xi) \leqslant M_1 \delta_{it}(\xi), \quad z_{it}^D(\xi) \leqslant M_1 (1 - \delta_{it}(\xi)) \quad \forall i, t$$
 (4i)
$$z_{it}^C(\xi) \leqslant M_1 \zeta_{it}(\xi), \quad z_{it}^D(\xi) \leqslant M_1 (1 - \zeta_{it}(\xi)) \quad \forall i, t$$
 (4j)

2.2 Aggregation

$$\max \quad \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right) \right] \right)$$
 (5a)
$$s.t. \quad \sum_{i \in I} R_{it}(\xi) - \alpha_t = \beta_t^+(\xi) - \beta_t^-(\xi) + \gamma_t^C(\xi) - \gamma_t^D(\xi) \quad \forall t$$
 (5b)
$$\sum_{i \in I} R_{it}(\xi) \geqslant \beta_t^+(\xi) \quad \forall t$$
 (5c)
$$\gamma_t^D(\xi) \leqslant \gamma_t(\xi) \quad \forall t$$
 (5d)
$$\gamma_t^C(\xi) \leqslant \sum_{i \in I} K_i - \gamma_t(\xi) \quad \forall t$$
 (5e)
$$0 \leqslant \gamma_t(\xi) \leqslant \sum_{i \in I} K_i \quad \forall t$$
 (5f)
$$\gamma_{t+1}(\xi) = \gamma_t(\xi) + \gamma_t^C(\xi) - \gamma_t^D(\xi) \quad \forall t$$
 (5g)
$$\beta_t^+(\xi) \leqslant M_2 \mu_t(\xi), \quad \beta_t^-(\xi) \leqslant M_2 (1 - \mu_t(\xi)) \quad \forall t$$
 (5h)
$$\beta_t^-(\xi) \leqslant M_2 \eta_t(\xi), \quad \gamma_t^C(\xi) \leqslant M_2 (1 - \eta_t(\xi)) \quad \forall t$$
 (5i)

(5i)

 $\gamma_t^C(\xi) \leqslant M_2 \lambda_t(\xi), \quad \gamma_t^D(\xi) \leqslant M_2 (1 - \lambda_t(\xi)) \quad \forall t$

$$\begin{aligned} &\max \quad \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right) \right] \right) \\ &\text{s.t.} \quad R_{tt}(\xi) - x_{it} = y_{tt}^+(\xi) - y_{it}^-(\xi) + z_{tt}^C(\xi) - z_{it}^D(\xi) \quad \forall i, t \\ &R_{tt}(\xi) \geqslant y_{it}^+(\xi) \quad \forall i, t \\ &z_{it}^D(\xi) \leqslant z_{it}(\xi) \forall i, t \\ &z_{it}^D(\xi) \leqslant x_{it}(\xi) \quad \forall i, t \\ &0 \leqslant z_{it}(\xi) \leqslant K_i - z_{it}(\xi) \quad \forall i, t \\ &0 \leqslant z_{it}(\xi) \leqslant K_i - z_{it}(\xi) \quad \forall i, t \\ &y_{it}^-(\xi) \leqslant M_1 \delta_{it}(\xi), \quad y_{it}^-(\xi) \leqslant M_1(1 - \rho_{it}(\xi)) \quad \forall i, t \\ &y_{it}^-(\xi) \leqslant M_1 \delta_{it}(\xi), \quad z_{it}^D(\xi) \leqslant M_1(1 - \delta_{it}(\xi)) \quad \forall i, t \\ &z_{it}^D(\xi) \leqslant M_1 \delta_{it}(\xi), \quad z_{it}^D(\xi) \leqslant M_1(1 - \delta_{it}(\xi)) \quad \forall i, t \\ &z_{it}^D(\xi) \leqslant M_1 \delta_{it}(\xi), \quad z_{it}^D(\xi) \leqslant M_1(1 - \delta_{it}(\xi)) \quad \forall i, t \\ &e_{it}^+(\xi) = y_{it}^+(\xi) - d_{it}^+(\xi) \\ &e_{it}^D(\xi) = z_{it}^D(\xi) - d_{it}^D(\xi) \quad d_{it}^D(\xi) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad d_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad d_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad d_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad e_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant \gamma_i(\xi), \quad \forall t \\ &e_{it}^D(\xi) \leqslant \gamma_i(\xi), \quad \forall t \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad \gamma_i^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) \\ &e_{it}^D(\xi) \leqslant M_1 q_{it}^D(\xi), \quad \gamma_i^D(\xi) \leqslant M_2(1 - \mu_1(\xi)) \quad \forall t \\ &e_{it}^D(\xi) \leqslant M_2 \mu_1(\xi), \quad \gamma_i^D(\xi) \leqslant M_2(1 - \mu_1(\xi)) \quad \forall t \\ &e_{it}^D(\xi) \leqslant M_2 \mu_1(\xi), \quad \gamma_i^D(\xi) \leqslant M_2(1 - \mu_1(\xi)) \quad \forall t \\ &e_{it}^D(\xi) \leqslant M_2 \mu_1(\xi), \quad \gamma_i^D(\xi) \leqslant M_2(1 - \mu_1(\xi)) \quad \forall t \\ &e_{it}^D(\xi) \leqslant M_2 \mu_1(\xi), \quad \gamma_i^D(\xi) \leqslant M_2(1 - \mu_1(\xi)) \quad \forall t \\ &e_{it}^D(\xi) \leqslant M_2 \mu_1(\xi), \quad \delta_{it}^D(\xi) \leqslant M_1(1 - q_{it}^D(\xi)) - \epsilon \\ &e_{it}^D(\xi) \leqslant M_1($$