DER Models

Seohyun Jang

April 28, 2025

1 Without Storage

1.1 Disaggregation

$$\max \sum_{t \in T} \left(P_t^{DA} x_{it} + \mathbb{E} \left[P_t^{RT}(\xi) y_{it}^+(\xi) - P_t^{PN} y_{it}^-(\xi) \right] \right)$$
 (1a)

s.t.
$$R_{it}(\xi) - x_{it} = y_{it}^+(\xi) - y_{it}^-(\xi) \quad \forall t \in T$$
 (1b)

$$R_{it}(\xi) \geqslant y_{it}^+(\xi) \quad \forall t \in T$$
 (1c)

$$y_{it}^{+}(\xi) \leqslant M z_{it}(\xi), \quad y_{it}^{-}(\xi) \leqslant M (1 - z_{it}(\xi)) \quad \forall t \in T$$
 (1d)

$$x_{it}^{DA} \geqslant 0, y_{it}^{+}(\xi) \geqslant 0, y_{it}^{-}(\xi) \geqslant 0, z_{it}(\xi) \in \{0, 1\} \quad \forall t \in T$$

1.2 Aggregation

$$\max \sum_{t=T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right] \right)$$
 (2a)

s.t.
$$\sum_{i \in I} R_{it}(\xi) - \alpha_t = \beta_t^+(\xi) - \beta_t^-(\xi) \quad \forall t \in T$$
 (2b)

$$\sum_{i \in I} R_{it}(\xi) \geqslant \beta_t^+(\xi) \quad \forall t \in T$$
 (2c)

$$\beta_t^+(\xi) \leqslant M z_t(\xi), \quad \beta_t^-(\xi) \leqslant M(1 - z_t(\xi)) \quad \forall t \in T$$
(2d)

$$\alpha_t^{DA} \ge 0, \beta_t^+(\xi) \ge 0, \beta_t^-(\xi) \ge 0, z_t(\xi) \in \{0, 1\} \quad \forall t \in T$$
 (2e)

1.3 Settlement

$$\max \quad \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right] \right) \tag{3a}$$

s.t.
$$\sum_{i \in I} R_{it}(\xi) - \alpha_t^{DA} = \beta_t^+(\xi) - \beta_t^-(\xi) \quad \forall t \in T$$
 (3b)

$$\sum_{i \in I} R_{it}(\xi) \geqslant \beta_t^+(\xi) \quad \forall t \in T$$
 (3c)

$$\beta_t^+(\xi) \leqslant M z_t(\xi), \quad \beta_t^-(\xi) \leqslant M(1 - z_t(\xi)) \quad \forall t \in T$$
 (3d)

$$\alpha_t = \sum_{i \in I} x_{it}(\xi), \quad \beta_t^+(\xi) = \sum_{i \in I} e_{it}^+(\xi), \quad \beta_t^-(\xi) = \sum_{i \in I} e_{it}^-(\xi) \quad \forall t \in T$$
(3e)

$$R_{it}(\xi) - x_{it}(\xi) = y_{it}^{+}(\xi) - y_{it}^{-}(\xi) \quad \forall t \in T$$
 (3f)

$$R_{it}(\xi) \geqslant y_{it}^+(\xi) \quad \forall t \in T$$
 (3g)

$$y_{it}^{+}(\xi) \leqslant M z_{it}(\xi), \quad y_{it}^{-}(\xi) \leqslant M (1 - z_{it}(\xi)) \quad \forall t \in T$$
 (3h)

$$\sum_{j \in I, j \neq i} d_{ijt}(\xi) \leqslant y_{it}^{+}(\xi), \quad \sum_{j \in I, j \neq i} d_{jit}(\xi) \leqslant y_{it}^{-}(\xi) \quad \forall t \in T$$
(3i)

$$d_{iit}(\xi) = 0 \quad \forall t \in T \tag{3j}$$

$$e_{it}^+(\xi) = y_{it}^+(\xi) - \sum_{j \in I, j \neq i} d_{ijt}(\xi) \quad \forall t \in T$$

$$e_{it}^{-}(\xi) = y_{it}^{-}(\xi) - \sum_{j \in I, j \neq i} d_{jit}(\xi) \quad \forall t \in T$$
 (31)

2 With Storage

2.1 Disaggregation

$$\max \quad \sum_{t \in T} \left(P_t^{DA} x_{it} + \mathbb{E} \left[P_t^{RT}(\xi) y_{it}^+(\xi) - P_t^{PN} y_{it}^-(\xi) \right] \right)$$
 (4a)
$$\text{s.t.} \quad R_{it}(\xi) - x_{it} = y_{it}^+(\xi) - y_{it}^-(\xi) + z_{it}^C(\xi) - z_{it}^D(\xi) \quad \forall i, t$$
 (4b)
$$R_{it}(\xi) \geqslant y_{it}^+(\xi) \quad \forall i, t$$
 (4c)
$$z_{i,t+1}(\xi) = z_{it}(\xi) + z_{it}^C(\xi) - z_{it}^D(\xi) \quad \forall i, t$$
 (4d)
$$z_{it}^D(\xi) \leqslant z_{it}(\xi) \quad \forall i, t$$
 (4e)
$$z_{it}^C(\xi) \leqslant K_i - z_{it}(\xi) \quad \forall i, t$$
 (4f)
$$0 \leqslant z_{it}(\xi) \leqslant K_i \quad \forall i, t$$
 (4g)
$$y_{it}^+(\xi) \leqslant M_1 \rho_{it}(\xi), \quad y_{it}^-(\xi) \leqslant M_1 (1 - \rho_{it}(\xi)) \quad \forall i, t$$
 (4h)
$$y_{it}^-(\xi) \leqslant M_1 \delta_{it}(\xi), \quad z_{it}^C(\xi) \leqslant M_1 (1 - \delta_{it}(\xi)) \quad \forall i, t$$
 (4j)
$$z_{it}^C(\xi) \leqslant M_1 \zeta_{it}(\xi), \quad z_{it}^D(\xi) \leqslant M_1 (1 - \zeta_{it}(\xi)) \quad \forall i, t$$
 (4j)

2.2 Aggregation

$$\max \quad \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right) \right] \right) \tag{5a}$$

$$\text{s.t.} \quad \sum_{i \in I} R_{it}(\xi) - \alpha_t = \beta_t^+(\xi) - \beta_t^-(\xi) + \gamma_t^C(\xi) - \gamma_t^D(\xi) \quad \forall t \tag{5b}$$

$$\sum_{i \in I} R_{it}(\xi) \geqslant \beta_t^+(\xi) \quad \forall t \tag{5c}$$

$$\gamma_t^D(\xi) \leqslant \gamma_t(\xi) \quad \forall t \tag{5d}$$

$$\gamma_t^C(\xi) \leqslant \sum_{i \in I} K_i - \gamma_t(\xi) \quad \forall t \tag{5e}$$

$$0 \leqslant \gamma_t(\xi) \leqslant \sum_{i \in I} K_i \quad \forall t \tag{5f}$$

$$\gamma_{t+1}(\xi) = \gamma_t(\xi) + \gamma_t^C(\xi) - \gamma_t^D(\xi) \quad \forall t \tag{5g}$$

$$\beta_t^+(\xi) \leqslant M_2 \mu_t(\xi), \quad \beta_t^-(\xi) \leqslant M_2 (1 - \mu_t(\xi)) \quad \forall t \tag{5h}$$

$$\beta_t^-(\xi) \leqslant M_2 \eta_t(\xi), \quad \gamma_t^C(\xi) \leqslant M_2 (1 - \eta_t(\xi)) \quad \forall t \tag{5f}$$

(5j)

 $\gamma_t^C(\xi) \leqslant M_2 \lambda_t(\xi), \quad \gamma_t^D(\xi) \leqslant M_2 (1 - \lambda_t(\xi)) \quad \forall t$

2.3 Settlement

$$\begin{aligned} & \max & \sum_{t \in T} \left(P_t^{DA} \alpha_t + \mathbb{E} \left[P_t^{RT}(\xi) \beta_t^+(\xi) - P_t^{PN} \beta_t^-(\xi) \right) \right] \right) \\ & \text{s.t.} & R_{it}(\xi) - x_{it} = y_{it}^+(\xi) - y_{it}^-(\xi) + z_{it}^C(\xi) - z_{it}^D(\xi) & \forall i, t \\ & R_{it}(\xi) \geqslant y_{it}^+(\xi) & \forall i, t \\ & z_{it}^D(\xi) \leqslant z_{it}(\xi) & \forall i, t \\ & z_{it}^D(\xi) \leqslant z_{it}(\xi) & \forall i, t \\ & 0 \leqslant z_{it}(\xi) \leqslant K_i & \forall i, t \\ & 0 \leqslant z_{it}(\xi) \leqslant K_i & \forall i, t \\ & y_{it}^+(\xi) \leqslant M_1 \rho_{it}(\xi), & y_{it}^-(\xi) \leqslant M_1 (1 - \rho_{it}(\xi)) & \forall i, t \\ & y_{it}^-(\xi) \leqslant M_1 \delta_{it}(\xi), & z_{it}^D(\xi) \leqslant M_1 (1 - \delta_{it}(\xi)) & \forall i, t \\ & z_{it}^D(\xi) \leqslant M_1 \delta_{it}(\xi), & z_{it}^D(\xi) \leqslant M_1 (1 - \zeta_{it}(\xi)) & \forall i, t \\ & z_{it}^D(\xi) \leqslant M_1 \delta_{it}(\xi), & z_{it}^D(\xi) \leqslant M_1 (1 - \zeta_{it}(\xi)) & \forall i, t \\ & e_{it}^+(\xi) = y_{it}^+(\xi) - d_{it}^+(\xi) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & d_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^3(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & d_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^3(\xi)) \\ & e_{it}^D(\xi) \leqslant Z_{it}^D(\xi) - d_{it}^D(\xi) + d_{it}^D(\xi) \\ & d_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^4(\xi)) \\ & e_{it}^D(\xi) \leqslant z_{it}(\xi) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it}^D(\xi)) \\ & e_{it}^D(\xi) \leqslant M_1 \delta_{it}^D(\xi), & e_{it}^D(\xi) \leqslant M_1 (1 - q_{it$$