

## CS 155 Final

## Multiple Choice Questions

A True -

B B

C Left image:  $K_1$  Center:  $K_2$  Right:  $K_3$ 

D 2

E C

F True

G B

H True

I True

J False

K B

L False

M True

N False



## Naive Bayes

|   |       |          |                   |
|---|-------|----------|-------------------|
| 1 | Grade | Year     | $P(\text{Happy})$ |
|   | A     | Senior   | $\frac{2}{3}$     |
|   | A     | Freshman | 1                 |
|   | C     | Senior   | $\frac{1}{2}$     |
|   | C     | Freshman | 0                 |

2 1

3  $x = P(\text{grade, year} \rightarrow \text{happy})$   
prob = random()  
if prob  $\leq x$  then happy  
else not happy

## Data Transformations

1  $\bar{w} = Aw$

2  $\arg \min_w \frac{1}{2} \|Aw\|^2 + \sum_i (y_i - (Aw)^T(Ax_i))^2$

3 The transformation matrix is used.



## Latent Markov Embedding

- 1 The value of  $\|U(s') - V(s)\|_2^2$  is strictly  $\equiv \|X(s') - X(s)\|_2^2$  because the vectors  $U, V$ , and  $X$  are equal. This causes the  $R(s)$  for the dual-point model to never be less than that of the single point model.
- 2 The vectors  $U, V$ , and  $X$  are equivalent.

## Neural Net Backprop Gradient Derivation

$$1 \quad \frac{\partial}{\partial w_{ii}} L(y, f(x)) = \frac{\partial}{\partial w_{ii}} (y - f(x))^2 = -2(y - f(x)) \cdot \frac{\partial f(x)}{\partial w_{ii}} = -2(y - f(x)) \cdot \frac{\partial}{\partial w_{ii}} \sigma \left( \sum_{i=1}^2 u_i \left( \sigma \left( \sum_{j=1}^2 w_{ij} x_j \right) \right) \right)$$

$$2 \quad f(0.1, 0.5) = \sigma\left(\sum_{i=1}^2 v_i (\sigma(\sum_{j=1}^2 w_{ji} x_j))\right)$$

$\swarrow$

$$\begin{aligned} & 0.5 \cdot \sigma(0.25 \cdot 0.1 + 0.05 \cdot 0.5) = 0.2562 \\ & + \\ & -0.1 \cdot \sigma(0.1 \cdot 0.1 - 0.25 \cdot 0.5) = -0.0471 \\ & = \sigma(0.2091) = 0.5521 = f(x) \end{aligned}$$

Plugging in:  $-2(0.75 - 0.5521) \cdot 0.5521 \cdot (1 - 0.5521) = \boxed{-0.0979}$

- 3 The term  $\sigma(s)$  causes the vanishing gradient problem, and having more layers causes the weights to decrease, making us reach a gradient of zero more quickly.