

$$\Rightarrow \vec{e}_\varphi: R(2\cos\theta\dot{\varphi}\dot{\theta} + \sin\theta\ddot{\theta}) = 0$$

$$\vec{e}_r: R(-\sin^2\theta\dot{\varphi}^2 - \dot{\theta}^2) = -\tilde{\lambda} - g\cos\theta \quad \checkmark$$

$$\vec{e}_\theta: R(\ddot{\theta} - \dot{\varphi}^2\cos\theta\sin\theta) = g\sin\theta$$

d) $\sum_{i=1}^N (\vec{F}_i^{\text{ext}} - m_i \ddot{\vec{r}}_i) \delta \vec{r}_i = 0$ 1 Teilchen $\Rightarrow (m\vec{g} - m\ddot{\vec{r}}) \delta \vec{r} = 0 \Rightarrow m\ddot{\vec{r}} = m\vec{g} = \begin{pmatrix} 0 \\ -mg \\ 0 \end{pmatrix}$

e) $\delta \vec{r} = \frac{\partial \vec{r}}{\partial \theta} \delta \theta + \frac{\partial \vec{r}}{\partial \varphi} \delta \varphi$

$$\vec{r} = a\vec{e}_x + b\vec{e}_y + c\vec{e}_z$$

$$= \begin{pmatrix} a \\ b \\ c \end{pmatrix}$$

$$\delta \vec{r} = \begin{pmatrix} \delta x \\ \delta y \\ \delta z \end{pmatrix}$$

$$\delta \vec{r} = \begin{pmatrix} 0 \delta \theta \\ R \sin\theta \delta \varphi \\ R \delta \theta \end{pmatrix}$$

$$\Rightarrow \delta \vec{r} = R\vec{e}_\theta \delta \theta + R\sin\theta \vec{e}_\varphi \delta \varphi \quad \checkmark$$

$$\Rightarrow (-mg(\cos\theta\vec{e}_r - \sin\theta\vec{e}_\theta) - m\ddot{\vec{r}}) (R(\vec{e}_\theta \delta \theta + \sin\theta\vec{e}_\varphi \delta \varphi)) = 0$$

$$\Rightarrow (mg\sin\theta R - mR(\ddot{\theta} - \dot{\varphi}^2\cos\theta\sin\theta))\delta\theta + -m\sin\theta R^2(2\cos\theta\dot{\varphi}\dot{\theta} + \sin\theta\ddot{\varphi})\delta\varphi = 0$$

$$\Rightarrow [g\sin\theta - R(\ddot{\theta} - \dot{\varphi}^2\cos\theta\sin\theta)]\delta\theta - \sin\theta R(2\cos\theta\dot{\varphi}\dot{\theta} + \sin\theta\ddot{\varphi})\delta\varphi = 0$$

$$\Rightarrow g\sin\theta - R(\ddot{\theta} - \dot{\varphi}^2\cos\theta\sin\theta) = 0$$

Top!

$$\wedge 2\cos\theta\dot{\varphi}\dot{\theta} + \sin\theta\ddot{\varphi} = 0 \quad \checkmark$$

Vorrechnen?

