

- ① Confidence Interval - Mean, Proportion
- ② Some other std. distributions
- ③ Hypothesis Testing & ANOVA

→ If X is a normal distribution with mean = 10, var = 25
then X^4 is ??

$$X \sim \text{Norm} \left(\underset{\mu}{5}, \underset{\sigma^2}{16} \right)$$

$$X - 5 \sim \text{Norm} \left(\underset{\mu}{0}, \underset{\sigma^2}{16} \right)$$

$$Z = \frac{X - 5}{4} \sim \text{Norm} \left(\underset{\mu}{0}, \underset{\sigma^2}{1} \right)$$

$$\text{Var} \left(\frac{X - 5}{4} \right) = \frac{1}{16} \cdot \text{Var}(X - 5)$$

$$\begin{aligned} X &\sim \text{Norm}(\mu, \sigma^2) \\ \frac{X - \mu}{\sigma} &\sim \text{Norm}(0, 1) \end{aligned}$$

$$\frac{X_1 + X_2}{2} \sim \text{Normal} \left(\mu, \frac{\sigma^2}{2} \right)$$

Assumption:

Population distribution is normal

$$X_1 \sim \text{Norm}(\mu, \sigma^2)$$

$$X_2 \sim \text{Norm}(\mu, \sigma^2)$$

$$H_0: w \leq 5 \quad (\underline{w = 5})$$

$$H_a: w > 5$$

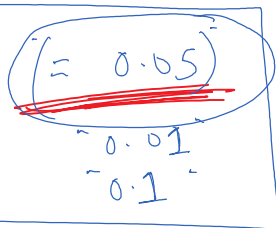
① Assume null hypothesis to be true.))

$$X_1, X_2, \dots, X_n \sim \text{Normal}(5, \sigma^2)$$

$$\bar{X} = \frac{X_1 + X_2 + X_3 + \dots + X_{50}}{50}$$

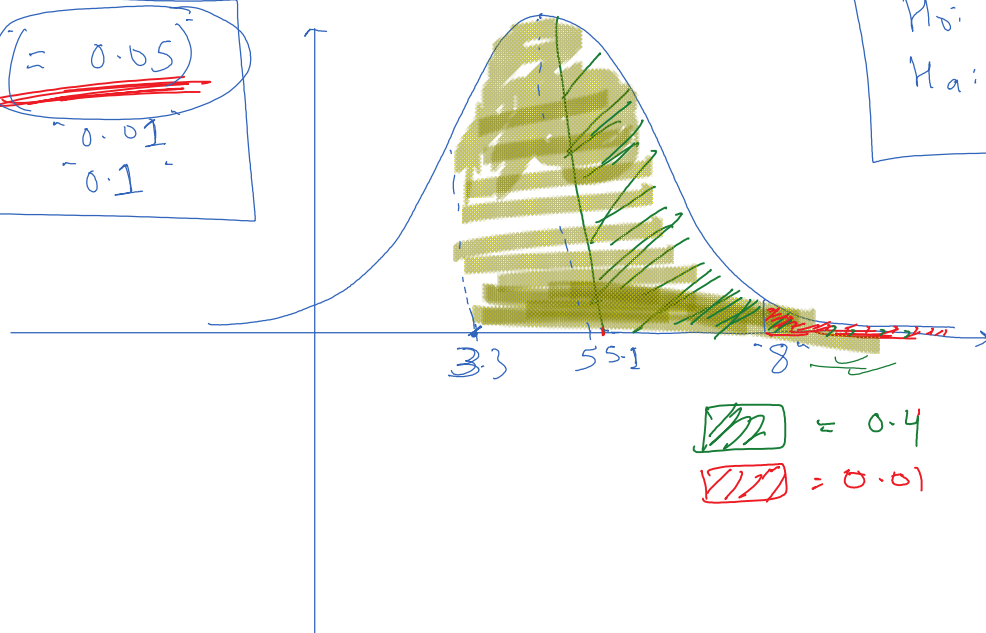
Normal(5, $\frac{\sigma^2}{n}$)

Type-1 error:



$H_0: w = 5$

$H_a: w > 5$



$\text{Green} = 0.4$

$\text{Red} = 0.01$